Research Article

Molecular Laser Spectroscopy as a Tool for Gas Analysis Applications

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We have used the traceable infrared laser spectrometric amount fraction measurement (TILSAM) method to perform absolute concentration measurements of molecular species using three laser spectroscopic techniques. We report results performed by tunable diode laser absorption spectroscopy (TDLAS), quantum cascade laser absorption spectroscopy (QCLAS), and cavity ring down spectroscopy (CRDS), all based on the TILSAM methodology. The measured results of the different spectroscopic techniques are in agreement with respective gravimetric values, showing that the TILSAM method is feasible with all different techniques. We emphasize the data quality objectives given by traceability issues and uncertainty analyses.

1. Introduction

Throughout the last years many molecular laser spectroscopic techniques have been used to qualifty and quantify different physical mechanisms taking place in atoms or molecules [1–7]. Molecular spectroscopy as performed by probing intra- and intermolecular vibrational transitions and further underlying rotational substructure has been used to study and illuminate bond structures and formation of atomic and molecular agglomerates and clusters [8, 9].

These techniques are applied due to the absorption, emission, or scattering of electromagnetic radiation by atoms or molecules. The choice of each of these physical phenomena, for example, absorption, for molecular species quantification or qualification, depends on the intended application. Absorption spectroscopy, for instance, is employed to identify and quantify molecular species in gas analysis applications such as remote sensing, atmospheric monitoring, vehicle exhaust emissions, or even exhaled breath gas tests [10–28].

In metrology, molecular absorption spectroscopy could be used to assign amount fractions (concentrations) to species in gas mixtures of known molecular constituents (Note, for a clarification of different terms in use see e.g.: http://goldbook.iupac.org/A00296.html). The determination of the amount fraction of a species without the use of calibrated reference gas mixtures, leads to the so-called “calibration-free” infrared spectrometry. Calibration-free means the amount of substance fraction of a species is measured in terms of the International System of Units (SI) derived unit mol·mol⁻¹ without referencing to a standard or a measurement expressed in the same unit [29]. The desire to derive amount fraction results by means of spectroscopy that are directly traceable to the SI triggered the idea of a traceable infrared laser spectrometric amount fraction measurement (TILSAM) method [29, 30].

In order to apply the TILSAM method, typically, a sufficiently resolved, spectrally isolated molecular rovibrational absorption line is preferable. Regarding the derivation of an amount fraction, the documentary description of TILSAM [29] describes the raw data processing, the modeling, the influence quantities, and so forth, based on tunable diode laser absorption spectroscopy (TDLAS). However,
other spectrometric techniques, such as quantum cascade laser absorption spectroscopy (QCLAS) or cavity ring-down spectroscopy (CRDS), can also be used to perform absolute amount fraction measurements based on \textit{TILSAM}. The \textit{TILSAM} method can be applied to perform laser spectrometric amount fraction measurements in metrological environments and in field applications \cite{31, 32}.

Figure 1 visualizes schematically the amount fraction determination due to the \textit{TILSAM} method. Summarized to four steps, there are just the measurement process, the line area derivation, the incorporation of the input quantities, and the computation of the model equation to subsequently achieve a traceable amount fraction result. The uncertainty of the resulting amount fraction has to be reported according to the ISO GUM \cite{33}. However, the determined amount fraction would be traceable if all input quantities were traceable to the SI units, which unfortunately, to the best of our knowledge, has been achieved very rarely. Although not new in its single steps, the \textit{TILSAM} method aims to represent and document a combination of steps necessary to apply IR spectrometry as an absolute method. There has been other groups and other termini dealing with this idea. From a metrology point of view, \textit{TILSAM} promotes these ideas on some standardized basis, providing some descriptive framework and being as flexible as possible to different experimental implementations. Referring to Figure 1 and depending on the spectrometric technique applied, the measurements yield spectral absorbances or absorption coefficients as is the case for TDLAS/QCLAS and CRDS, respectively. Then, line areas are determined either in units of \text{cm}^{-1} for TDLAS/QCLAS or \text{cm}^{-2} for CRDS by means of direct numerical integration or by means of fitting an appropriate line profile to the measured data. Crucial to \textit{TILSAM} is the subsequent incorporation of the input quantities because, here, traceability of all parameters would be desired to maintain the quality issue of traceability to the final amount fraction result.

Among the most indispensable input quantities, there is the molecular line strength of the probed transition. Line strength values could be taken from data bases like HITRAN \cite{34} and GEISA \cite{35}. These data bases provide valuable information. Among them, there are some lines with incredibly small reported uncertainties, that is, “error codes” \cite{34}, based on very sophisticated measurements. However, there are a larger number of lines as well, where the uncertainties, for example, those of \textit{S} are somewhat larger and more imprecise; uncertainty budgets in accordance with the ISO GUM \cite{33} are generally not provided. This last point prevents any spectrometrically measured amount fraction based on HITRAN or GEISA from being traceable. As a consequence, a couple of studies have been undertaken to report line strength values and associated GUM compliant uncertainty figures \cite{36, 37}. Recently in the EMRP call 2010 \cite{38}, there was a proposal to establish a new reference line data measurement program. The lack of reference data that are more precise than those typically provided by HITRAN and GEISA and which are equipped with quality flags in terms of GUM-compliant uncertainties had also been reported earlier \cite{39}. As reported in \cite{39}, for instance, the accurate determination of the uncertainties of the spectrometric data is often suspect or even completely absent, suggesting the need for a precise quantification of the uncertainties associated with the reported spectrometric parameters in \cite{34}. Despite all above, it should be noted here, that HITRAN, GEISA, and other line parameter sources provide absolutely valuable information to any spectroscopist, no matter whether in academic research environments or metrology community. The present work itself takes advantage of the use of HITRAN’s beneficitals, that is, from line strength data on CO and CO$_2$ that are reliable within their specified error ranges.

Nevertheless, absolute amount fraction measurements sometimes meet other specific challenges depending on which spectrometric technique is used. For instance, in intra-pulse mode QCLAS, an effect reported by \cite{1} known as rapid passage is observed in the measured absorption signals of molecular species at low pressure. Rapid passage occurs when the laser frequency sweep through an absorption line is faster than the collisionally induced relaxation \cite{1}. This results in an asymmetric or even inverted or oscillating absorption signal. Such molecular effects have to be investigated and considered for any absolute amount fraction measurement.

Also the temperature dependence of the line strength has to be considered. By convention in spectroscopy, line strength figures are reported at some conventional temperature as, for example, that of HITRAN as 296 K, $S_0$. Because of that, for measurements performed at any other temperature $T$, the line strength has to be transformed to $S_T$, for example, applying a certain model that explicitly describes the temperature dependence of $S$. \textit{TILSAM}, of course, does not require any specific model. However, we need to emphasize the importance of matching the line strength $S_0$ to the actual temperature $T$ by means of any appropriate model, for example, as being used in standard analysis.

Additionally there are isotopic abundance issues hidden in the line strength figure that have to be taken into account. Line strength values are typically reported for a certain abundance of the probed isotopologue. However, for a given mixture, generally the abundance of the probed isotopologue may differ from this norm abundance. Therefore, in principle, one would have to correct the line strength figure by substituting $S = S_T \cdot r_{iso}$, where $r_{iso}$ is the

\[ \text{Spectral absorbance: Measurement} \quad A(\tilde{\nu}) = -\ln(\phi_t/\phi_0) \]

\[ \text{Absorbance area: Derivation} \quad A_{\text{line}} = \int A(\tilde{\nu})d\tilde{\nu} \]

\[ \text{Input quantities} \quad L, S, T, p_{\text{total}} \]

\[ \text{Traceable amount fraction: Calculation} \quad x_i = A_{\text{line}} - k_B \cdot T/(L \cdot S \cdot p_{\text{total}}) \]

\textbf{Figure 1: Process of the amount fraction determination according to \textit{TILSAM} \cite{21}, schematic view for TDLAS/QCLAS.}
isotopic composition factor, given for example, as
\[ r_{\text{iso}} = \frac{x_{12C^{16}O}}{x_{12C^{16}O^{18}HIT}} \]
for a probed \(^{12}\text{C}^{16}\text{O}\) excitation, where \(x_{12C^{16}O}\) and \(x_{12C^{16}O^{18}HIT}\) are the abundances of \(^{12}\text{C}^{16}\text{O}\) in the sample and the conventional value given by HITRAN, respectively.

There has been a wide range of studies to measure trace species using laser spectroscopic techniques such as TDLAS, QCLAS, and CRDS [16, 26, 40–45]. However, with the most prominent exception of DOAS [46], most of them to the best of our knowledge were not referring to any documented standardized method for the spectroscopic measurements. The method of TILSAM, aiming at results that are directly traceable to the SI and which were recently made available online [29], should be viewed as an attempt to make a first step towards standardization for gas analysis applications by means of laser spectroscopy.

In this paper, we focus on the use of the TILSAM method to perform absolute concentration measurements of molecular species using different laser spectroscopic techniques. We emphasize data quality objectives expressed by means of traceability and uncertainty issues. In Section 2, we report CO\(_2\) amount fraction results performed by TDLAS based on the TILSAM method. In Section 3, similar results for CO performed with a quantum cascade laser operated in the near infrared (NIR) combination band around 2 \(\mu\m\) are reported, and Section 4 focuses on the application of the TILSAM method to CRDS.

2. Tunable Diode Laser Absorption Spectroscopy (TDLAS)

In this section, we report spectrometric CO\(_2\) amount fraction measurements using TDLAS according to the TILSAM protocol [29]. The experimental setup is depicted in Figure 2. The probed transition is the \(^{12}\text{C}^{16}\text{O}-\text{R}(12)\) line at 4987.31 \(\text{cm}^{-1}\) in the near infrared (NIR) combination band around 2 \(\mu\m\).

In absorption spectroscopy, the interaction of the gas species molecules at density \(n\) and the sensing radiation at wave number \(\tilde{\nu}\) is modeled by the Beer-Lambert law

\[ \Phi(\tilde{\nu}, L) = \Phi_0 \cdot \exp \{-S_T \cdot r_{\text{iso}} \cdot g(\tilde{\nu} - \tilde{\nu}_0) \cdot L \cdot n\} \]  

with \(\Phi_0\) and being the incident and transmitted radiant powers, respectively, of which the SI unit is W. The absorption is governed by the molecular transition line strength \(S_T\) at gas temperature \(T\), which is in principle to be matched to the actual present isotopologue abundance by means of \(r_{\text{iso}} = x_{\text{iso}}/x_{\text{iso}^{18}HIT}\), the respective normalized absorption profile \(g\) centered at \(\tilde{\nu}_0\), and the absorption path length \(L\). The line strength

\[ S_T = S_0 \left( \frac{Q_{\nu_0}}{Q_T} \right) \exp \left\{ -h \frac{E}{k_B \left( \frac{1}{T} - \frac{1}{T_0} \right)} \right\} \times \frac{1 - \exp \left\{ -h \frac{\tilde{\nu}_0}{k_B \left( \frac{1}{T_0} \right)} \right\}}{1 - \exp \left\{ -h \left( \frac{\tilde{\nu}_0}{k_B T_0} \right) \right\}} \]  

is specific for the probed molecular transition. \(S_0\) is the line strength at \(T_0 = 296\ \text{K}\), and \(Q_{\nu_0}\) and \(Q_T\) are the total internal partition functions of the molecule at temperature \(T_0\) and \(T\), respectively. The quantities, \(c\), \(h\), and \(k_B\), are the speed of light, the Planck and Boltzmann constants, respectively. \(E\) is the ground state energy of the probed transition, and \(\tilde{\nu}_0\) is its center wave number. For this work, we utilized the following expression for the line strength:

\[ S_T = S_0 \left( \frac{T_0}{T} \right)^j \cdot \exp \left\{ -h \frac{E}{k_B \left( \frac{1}{T} - \frac{1}{T_0} \right)} \right\} \times \frac{1 - \exp \left\{ -h \left( \frac{\tilde{\nu}_0}{k_B T_0} \right) \right\}}{1 - \exp \left\{ -h \left( \frac{\tilde{\nu}_0}{k_B T_0} \right) \right\}} \]  

Equation (3) is an approximation of (2) with the quantity \((Q_{\nu_0}/Q_T)\) replaced by \((T_0/T)^j\), where \(j\) depends on the molecular structure of the species and the transition being probed.

Relying on the ideal gas law, the molecular density \(n\) of the absorbing species can be expressed in terms of its partial pressure \(p_{\text{partial}}\) of the absorbing molecules and the gas temperature. The partial pressure can be related to the total pressure \(p_{\text{total}}\) using the amount-of-substance fraction of the absorbing species, \(x_{\text{species}} = p_{\text{partial}}/p_{\text{total}}\). Measuring \(\Phi\) and \(\Phi_0\) and probing a certain molecular transition for a known path length and measuring \(p_{\text{total}}\) and \(T\), leads to the amount fraction of the species

\[ x_{\text{species}} = -\ln \left( \frac{\Phi(\tilde{\nu})}{\Phi_0(\tilde{\nu})} \right) S_T \cdot r_{\text{iso}} \cdot g(\tilde{\nu} - \tilde{\nu}_0) \cdot L \cdot p_{\text{total}}. \]  

Introducing the spectral absorbance \(A(\tilde{\nu}) = -\ln(\Phi(\tilde{\nu})/\Phi_0(\tilde{\nu}))\), which in cases can also be called extinction, and making use of the normalization of \(g\), (see, e.g., http://goldbook.iupac.org/A00028.html) (4) may also be written in its integral form

\[ x_{\text{species}} = \frac{k_B \cdot T}{S_T \cdot r_{\text{iso}} \cdot L \cdot p_{\text{total}}} \int_{-\infty}^{\infty} A(\tilde{\nu})d\tilde{\nu}, \]  

where \(A_{\text{line}}\) is the line area obtained by integration of the measured absorbance data over wave number. Direct absorption spectroscopy is described by the Beer-Lambert law, as expressed in (1). Using (5) to determine the amount fraction in a given gas mixture would deliver results that are SI traceable if all input quantities were SI traceable. An uncertainty budget for the measurement according to the ISO Guide to the expression of uncertainty in measurement (GUM) [33] can be evaluated with (5) as the model function.

For the following quantitative determinations, the isotopic composition factor \(r_{\text{iso}}\) was always set to unity. This is due to the lack of a priori information on the actual isotopologue abundance present in the sample. However, this lack of information was to be transferred into to the uncertainty associated with the \(r_{\text{iso}} = 1\) [47].

2.1. Quantitative Amount Fraction Determination by TDLAS.

A distributed feedback (DFB) tunable diode laser (TDL) emitting at 2 \(\mu\m\) was used to probe the desired CO\(_2\) transition at 4987.31 \(\text{cm}^{-1}\). A triangular-shaped laser current
Figure 2: Schematic diagram of the setup used for species quantification in a two-channel regime. The multipass White-type absorption cell has a path length of $L = 21$ m. OAP: off-axis parabolic mirror, BS: beam splitter, M: mirror, Det: detector, PG: pressure gauge, and L: lens.

Figure 3: (a) Data from the reference channel, without CO$_2$ absorption (dashed line) and the sample channel (full line) featuring CO$_2$ absorption, respectively. (b) Etalon transmission signal seen by detector 1 with the etalon ($\text{FSR}_\nu \approx 0.05$ cm$^{-1}$) placed in the reference beam path. (c) and (d) Data transferred to the wave number domain. (c) Etalon transmittance curve. (d) Data of the lower panel of (a), converted to absorbance values (solid dots). A Voigt profile has been fitted to the data (full line) representing the CO$_2$-R(12) line at 4987.31 cm$^{-1}$. (e) The residuals from the fitted line in (d). (f) Generalized linear regression of $A_{\text{line}}$ versus $\Gamma$.

Modulation was applied to sweep the diode laser wavelength across the R(12) line. After collimation, the TDL beam was split into a reference beam and a second sample beam transmitted through a 21 m multipass absorption cell. The reference beam was used for intensity normalization and for fixing the wavelength axis by means of a removable etalon. Both channels were terminated into extended indium-gallium-arsenide (XInGaAs) photo detectors. An A/D converter (ADLink-DG-9114) was used to digitize the electrical signals at 10 kS/s.

A reference gas mixture of carbon dioxide in nitrogen, gravimetrically prepared with a nominal level of 11 mmol·mol$^{-1}$ CO$_2$, was filled into the gas cell for analysis. Quantitative measurements were performed based on the TILSAM method [29] with $p_{\text{total}}$ preset in the range of 10 to 43 hPa with the help of a gas sampling system equipped with a turbomolecular vacuum pump.

Figure 3(a) depicts the detector signals, representing a simultaneous two-channel measurement scheme. Data has been measured in the time domain in units of sample points (SPs). Figure 3(b) shows the signal of detector 1 when a Fabry Perot etalon with a free spectral range (FSR) of about 0.05 cm$^{-1}$ is placed in the beam path. Figure 3(d) depicts the absorbance realized by means of the detector signals from the two channels. The residuals from the fitted R(12) line of CO$_2$ are shown in Figure 3(e). The wave number axis was accomplished by means of the sweep rate, $r_{\text{sweep}} = \text{FSR}/\text{FSR}_\text{SP}$. FSR$\nu$ is the free spectral range of the etalon in wave numbers, and FSR$\text{SP}$ is the experimental fringe separation measured in the time domain (SP) visible in
Figure 3(b). The sweep rate evaluated at the absorption peak position was used to realize the wave number axis.

In Figure 3(e) a plot of the derived line area $A_{\text{line}}$ as a function of the experimental parameter $\Gamma = S_T \cdot L \cdot p_{\text{total}}/(k_B \cdot T)$ is shown. A variation in $\Gamma$ is mostly related to a variation of the total gas pressure. From (5), the CO$_2$ amount fraction ($x_{\text{CO}_2}$) can be identified as the slope of a generalized linear regression (GLR) of values of $A_{\text{line}}$ as a function of $\Gamma$. A GLR is recommended by ISO 6143 [48] for purposes like that to account for uncertainties of both, the $y$- and the $x$-axis data. As also mentioned in ISO 6143, we applied the B_LEAST software to perform the GLR. B_LEAST is a software developed by Bundesanstalt für Materialprüfung (BAM), which fits model functions, here that is, a linear function, to experimental data by means of a generalised least square fit. The experimental data to be fitted must contain uncertainties in the $x$- and $y$-axis. The uncertainties of both axes data are taken into account for the GLR by B_Least. The uncertainty of the line area in Figure 3(e) (vertical bars smaller than symbol size) is due to the uncertainty of the sweep rate $t_{\text{sweep}}$ and that of the fitted line area [49]. The uncertainty of $\Gamma$ is calculated from the uncertainties of the parameters, $S_T$, $L$, $p_{\text{total}}$, $k_B$, and $T$. The line strength used for these measurements was taken from [36] as $1.255 \cdot 10^{-21} \text{cm}^{-1}$(molecule cm$^{-2}$) with an expanded uncertainty of $±1.0\%$ relative. The CO$_2$ amount fraction resulting from the data in Figure 3(e) was evaluated to be $(11.43 \pm 0.23) \text{ mmol-mol}^{-1}$. The uncertainty figure ($±2.0\%$, relative) is expressed as an expanded uncertainty. The deviation of the spectrometric $x_{\text{CO}_2}$ result from its gravimetric reference value of $(11.38 \pm 0.16) \text{ mmol-mol}^{-1}$ is $0.4\%$ relative, which is well covered by the uncertainty of $2.0\%$.

3. Quantum Cascade Laser Absorption Spectroscopy (QCLAS)

In this section we report results on the spectroscopy of carbon monoxide (CO) by means of pulsed quantum cascade laser spectroscopy. A detailed discussion of our pulsed QCL spectroscopy can be found in [31]. The light source is a quantum cascade laser (QCL) emitting around $4.6 \mu\text{m}$, where the fundamental band of CO is located. The experimental setup is the same as shown in Figure 2, except that the DFB diode laser discussed in Section 2 was replaced by the QCL. Compared to the measurements published in [31], for the present work, the 21 m multipass cell was used. The probed transition is the CO-P(1) line at 2139.43 cm$^{-1}$. The two channels in Figure 2 were terminated into TE-cooled HgCdZnTe detectors (Vigo PDI-2TE-10.6), and the electrical signals were digitized at 5 GS/s by an 8-bit A/D converter (CompuScope 85 G).

The formalism of quantum cascade laser absorption spectroscopy (QCLAS) based on the Beer-Lambert law is the same as that of TDLAS discussed in Section 2. All QCL data shown in the present work were corrected for the detector nonlinearities as pointed out in [31].

For the spectrometric QCL measurements of CO, a gravimetrically prepared multicomponent gas mixture of CO, CO$_2$, and O$_2$ in N$_2$ with a nominal value of $100 \mu\text{mol} \cdot \text{mol}^{-1}$ CO was filled into the 21 m gas cell for analysis.

Figure 4 shows typical data of the QCLAS similar to that in Figure 3. Although QCLAS is not covered by its documentary description, the spectrometric measurements were performed according to the TILSAM method [29] with the total gas pressure $p_{\text{total}}$ in the range of 100 to 300 hPa. Two methods for operating pulsed QCLs are known, the inter-pulse [50, 51] and the intrapulse mode [52, 53]. A comparison of these two modes is published in [43, 54]. For few years, also room temperature QCLs in continuous wave (cw) mode of operation have been used to perform laser spectroscopic measurements [55–57]. However, for the present work, our QCL was operated in the intrapulse mode.

The wave number axes in Figures 4(c) and 4(d) were realized in a similar manner as those in Section 2. The CO amount fraction retrieved from the generalized linear regression performed by B_LEAST as shown in Figure 4(c) was evaluated to be $87.3 \mu\text{mol} \cdot \text{mol}^{-1}$. The estimated uncertainty of this CO amount fraction result reads $±4.6 \mu\text{mol} \cdot \text{mol}^{-1}$ (5.2% relative). This uncertainty figure is comparably larger than that of the TDLAS result because of the uncertainty contribution originating from the line strength. The line strength of the P(1) line of CO at 2139.4261 cm$^{-1}$ was taken from HITRAN [34]. Its uncertainty is in the 2 to 5 percentage range as specified by HITRAN. For this work we used the lower level of 2% for the uncertainty evaluation, since the P(1) line is one of the most intense lines in this branch. However, as seen here, there is quite some room to improve the uncertainty figure of the spectrometric CO amount fraction to a significantly lower number, addressing the line strength contribution by first priority. The nominal CO amount fraction of the measured sample is specified as $100 \mu\text{mol} \cdot \text{mol}^{-1}$. A possible discrepancy between the spectrometrically derived amount fraction of $(87.3 \pm 4.6) \mu\text{mol} \cdot \text{mol}^{-1}$ and that of the nominal value could not be exactly quantified and further evaluated at the time this paper was prepared, because the sample was taken from an ongoing comparison for which exact reference values were not yet available. These QCL results were presented here, to demonstrate the application of the TILSAM method to intrapulse QCL spectrometry.

Line strength figures taken from HITRAN are not GUM compliant, that is, neither $S_T \approx 296 \text{ K}$ nor $S_T$, as discussed in Section 1. As a consequence, our spectrometrically measured CO amount fraction result is not yet traceable.

QCLAS faces a couple of challenges performing amount fraction measurements in the mid infrared. Effects such as rapid passage [1] as introduced in Section 1 and some possible nonlinearity of detectors are of concern [58]. The latter was accounted for in the presented amount fraction results by applying an appropriate correction [31]. Rapid passage occurs when the laser frequency sweep through an absorption line is faster than the collisionally induced relaxation, resulting in an asymmetric or even inverted absorption signal [1].

Rapid passage imprints can be present in QCLAS signals typically at low pressures [59]. Figure 5 displays results of a separate measurement at 5.1 hPa total gas pressure,
performed with a gravimetrically prepared gas mixture with a nominal CO amount fraction of 1000 μmol·mol⁻¹, where rapid passage signals were observed. While increasing the pressure to 66.5 hPa, this effect was removed as visible in the inset of Figure 5. This is caused by the addition of collision partners to the absorbing medium, thus increasing the relaxation rate of the excited state molecules. Evidently, for any absolute amount fraction measurements, it is necessary to correct for such rapid passage effects or simply to eliminate them.

4. Cavity Ring-Down Spectroscopy (CRDS)

In this section, we report CO₂ amount fraction measurements performed by CRDS referring to the TILSAM method. Different implementations of CRDS and related cavity-enhanced spectroscopy (CES) techniques can be found in [60, 61] as well as their underlying theory. A schematic diagram of the experimental setup is shown in Figure 6. The laser source is a DFB diode laser operating around 1.6 μm. We probed the CO₂-R(20) transition line at 6242.67 cm⁻¹.

In CRDS the absorption coefficient of a gas sample is measured by monitoring the temporal evolution of the intensity of light trapped inside an optical cavity consisting of highly reflective mirrors. The light is reflected typically thousands of times back and forth by the mirrors. After decoupling the incoming light beam from the cavity, the buildup of light intensity inside the cavity is stopped and the intensity will decay exponentially because of various linear loss mechanisms that are present (transmission of the mirrors, absorption by the gas sample, absorption by the mirrors, diffractive losses, and scattering). The time constant of the intensity decay is called ring-down time and is denoted by the symbol τ. A fast photodetector monitors the intensity of the escaping light which is proportional to the intensity of light still inside the cavity. The detected signal, therefore, also exhibits an exponential decay function from which the ring-down time is obtained.

Light intensity leaking out of the cavity is given by

\[ I(\tilde{\nu}) = I_0 \cdot \exp\left(-\frac{t}{\tau(\tilde{\nu})}\right), \quad (6) \]

where \( I_0 \) is the intensity of the light inside the cavity right after decoupling the incoming light from the cavity. If one

![Figure 4: Intrapulse chirp spectroscopy. (a) Data from the reference channel, without CO absorption (dashed line) and the sample channel (full line) featuring CO absorption, respectively. (b) Etalon transmission signal seen by detector 1 with the etalon (FSR = 0.05 cm⁻¹) placed in the reference beam path. (c) and (d) Data transferred to the wave number domain. (c) Etalon transmittance curve. (d) Data of A line versus Γ.

![Figure 5: Rapid passage (RP) signal observed at 5.1 hPa. Inset: pressure increased to 66.5 hPa, thus depleting the RP structure, that is, no RP signal observable anymore.](Image)
assumes that the cell is filled homogeneously with the gas sample over its entire length, then the ring-down time is given by

$$\tau(\tilde{\nu}) = \frac{L}{c\left[|\ln R_{\text{eff}}(\tilde{\nu})| + k(\tilde{\nu}) \cdot L\right]}, \quad (7)$$

where $L$ is the mirror separation and $R_{\text{eff}}$ being the effective reflectivity of the mirrors including all other loss mechanisms except that of sample absorption. Note that as $R_{\text{eff}} \approx 1$, the term $|\ln R_{\text{eff}}|$ is frequently replaced by $(1 - R_{\text{eff}})$. The quantity $k = S_T \cdot g \cdot n$ is called the absorption coefficient. $S_T$ is the line strength at temperature $T$, $g$ the normalized line profile function, and $n$ the molecular density of the absorbing species, and that might be expressed as $n = x_{\text{species}} \cdot p/(k_B \cdot T)$ as described in Section 2. Thus, the ring-down time reads as

$$\tau(\tilde{\nu}) = \frac{L}{c\left[|\ln R_{\text{eff}}(\tilde{\nu})| + S_T \cdot r_{\text{iso}} \cdot g(\tilde{\nu} - \tilde{\nu}_0) \cdot x_{\text{species}} \cdot (p_{\text{total}}/k_B \cdot T) \cdot L\right]}, \quad (8)$$

where $x_{\text{species}}$ is the amount of the substance fraction, $p_{\text{total}}$ the total gas pressure, $k_B$ the Boltzmann constant, and $T$ the gas temperature. The decay time obtained by measuring a nonabsorbing gas sample or vacuum is called $\tau_0$ and is given by

$$\tau_0(\tilde{\nu}) = \frac{L}{c|\ln R_{\text{eff}}(\tilde{\nu})|}. \quad (9)$$

The absorption coefficient $k(\tilde{\nu})$ is derived from the difference in the reciprocals of $\tau$ and $\tau_0$,

$$k(\tilde{\nu}) = \frac{1}{c} \left( \frac{1}{\tau(\tilde{\nu}) - \frac{1}{\tau_0(\tilde{\nu})}} \right), \quad (10)$$

By integrating both sides of (10) and rearranging them, the amount fraction of a given species can be calculated as

$$x_{\text{species}} = A_{\text{line}} \cdot \frac{k_B \cdot T}{S_T \cdot r_{\text{iso}} \cdot p_{\text{total}}}, \quad (11)$$

where $A_{\text{line}}$ is the line area calculated by integrating the absorption coefficient over wave number (note: in CRDS $A_{\text{line}}$ is given in units of cm$^{-2}$ as compared to that of TDLAS and QCLAS given in units of cm$^{-1}$). Equation (11) is essentially the same expression as (5), where instead the path length $L$ is included in the integral absorption coefficient $A_{\text{line}}$, allowing to obtain quantitative absorption measurements without measuring the path length. In CRDS the path length measurement is replaced by a time measurement. CRDS is restricted to the measurement of small absorptions. If absorption becomes much larger than empty cavity losses, virtually no intensity can build up in the cavity and the decay time will be correspondingly shorter. This would lead to an unreliable determination of the $\tau$ as the decay trace consists, then, of a very limited amount of data points (determined by the sampling rate of the data acquisition system).

### 4.1. Quantitative CO$_2$ Amount Fraction Detection by OF-CRDS

Details of the experimental setup of the optical feedback cavity-enhanced spectroscopy (OF-CES) are shown in Figure 6, and the theoretical background can be found in [62]. The spectrometer is capable of performing optical feedback absorption spectroscopy (OF-CEAS) and optical feedback cavity ring-down spectroscopy (OF-CRDS). Here, we focus on OF-CRDS or simply cavity ring down as discussed in the previous subsection. Details on how to benefit from the optical feedback performance and on the use of the different piezo-actuated mirrors displayed in Figure 6 will be addressed in an upcoming publication.

For quantitative detection of CO$_2$, the cavity was filled with a gravimetrically prepared gas mixture with a nominal...
value of 389 μmol·mol⁻¹. Carbon dioxide amount fractions were measured referring to the TILSAM method to demonstrate the feasibility of applying this method also to CRDS.

Figure 7(a) depicts typical raw data, each peak representing the built-up light intensity in a certain cavity mode. In Figure 7(b), the absorption coefficient, derived from the measured ring-down times, is plotted as a function of wave number. The residuals from the fitted CO₂-R(20) line are depicted in Figure 7(c). The wave number axis has been established by means of the known cavity FSR of 152 MHz between adjacent cavity modes displayed in (a) of Figure 7. From (11), the CO₂ amount fraction can be identified as the slope of a linear regression of $A_{\text{line}}$ (units: cm⁻²) versus the experimental parameter $\Omega$. The relative deviation of this spectrometric CO₂ amount fraction can be calculated from the line area $S_\text{T}$, $p_\text{total}$, $k_\text{B}$, and $T$. The line strength of the probed R(20) line of CO₂ was taken from HITRAN. Its uncertainty is specified as being 2 to 5%, relative.

The expanded uncertainties of the CO₂ amount fraction measured with TDLAS and CRDS were found to be ±2.0%, and 4.2%, respectively, whereas the QCLAS uncertainty analysis delivered ±5.2% for the CO quantification. The uncertainty figures of the QCLAS and CRDS quantification are comparable larger than that of the TDLAS result. This is because the uncertainties of the line strength values used to evaluate the QCLAS and CRDS amount fraction results were in the range 2 to 5% relative, as specified by HITRAN. The $S$ value and its relative expanded uncertainty of 1.0%, used to evaluate the CO₂ amount fraction TDLAS result, were taken from [36]. The standard uncertainties of the other input parameters, that is, $p_\text{total}$, $k_\text{B}$, $T$, and $L$, were all in the subpercentage range. Comparing the 5.2% uncertainty of the CO₂ amount fraction, for instance, to the 7.5%, requested by the data quality objectives set in EU directive 2000/69/EC [63] for CO field measurements, our presented results based on TILSAM would already be within this scope, although not yet validated for field measurements. However, one has to note that, if the line strength uncertainties used to derive QCLAS and CRDS amount fraction results presented in this paper were taken instead as the upper limit of 5%, the relative uncertainty of the spectrometric amount of substance fraction would have to be scaled accordingly larger. Since they are in accordance, our present results, however, do support the 2% level.

A linear model developed from (5) and (11) was used to evaluate the amount fractions of CO and CO₂ presented in this paper. The model does not predict any intercept. Therefore, as recommended in [29], the GLR was performed with a free intercept parameter. The resulting intercept parameters from the GLR are an additional measure of the quality of the measurements. The intercept parameter is either insignificant as predicted by the model or not. If the resulting intercept was significant, that is, its uncertainty is smaller than its numerical value, the model does not describe the experimental conditions appropriately. Hence,

**5. Discussions**

The resulting amount fractions derived by the different spectroscopic techniques are in good agreement with the respective reference values. The uncertainty evaluation is based on the method described by the ISO GUM [33].
the quality of the spectrometric amount fraction results presented here was judged by looking at the intercept parameters resulting from the respective generalized linear regressions. The intercept parameters of the TDLAS CO₂ amount fraction results calculated from the GLR were \((-5.8 \pm 5.8) \times 10^{-4} \text{ cm}^{-1}\) and that of the CRDS CO₂ amount fraction \((6.6 \pm 22.2) \times 10^{-11} \text{ cm}^{-2}\), being both insignificant. A final answer could not be given at this stage for the instead significant intercept parameter of the QCLAS CO amount fraction of \((-5.2 \pm 2.6) \times 10^{-3} \text{ cm}^{-1}\), since the measurements were performed on a sample from an ongoing comparison between different institutes, for which exact reference values are not yet known. With this result, there might be a further issue resulting from a “w” structure in the residuals in Figure 4(e). This typical residual structure indicates that collisional narrowing affects the data which cannot be modeled appropriately by a Voigt profile [64]. From the oscillatory nature of the residual “w” structure, it can be expected that the line area is less affected [64]. However, this proves already that by means of the TILSAM recommended data retrieval strategy, some data quality flags are provided which indicates some hidden problems with a used setup, as it is apparently now the case with our 21-m-path length QCL setup.

All the measurements presented in this paper are based on the TILSAM method as discussed earlier. The online-available TILSAM documentary description [29] details the spectrometric measurement process, the raw data processing, and the uncertainty assessment principles. Although the TILSAM protocol in its present form considers only TDLAS, other techniques such as QCLAS and CRDS could be addressed by this documentary framework in a future edition as shown in this paper, Sections 3 and 4. The TILSAM method has the potential of being used in the next generation of spectrometric reference methods in gas metrology. The method could also benefit other interesting fields of application, for example, breath gas analysis, as it is aimed at in an iMERA-plus project [65], or industrial process control [66]. The TILSAM method could also be used to trigger the development of similar documentary method descriptions for the measurement of molecular reference line data, such as, for example, those of line strengths, broadening coefficients, and temperature dependencies or those of molecular constants such as spin coupling constants, ground state energy, and rotational g factors, or simply to support the development of process analyzers.

Contrary to measurements often performed by calibrated spectrometric systems, where the aim might be to eliminate systematic errors and study the Allan variance to provide the rms noise and the drift as a function of measurement time, our measurements performed using the TILSAM method are based on first principle measurements rather than relying on a comparison, since calibrated systems face the challenges of recalibration especially when the analyte is changed. Therefore, the use of “absolute” methods for amount fraction measurements, such as the TILSAM method, could be more cost effective than calibrated methods. Further on, calibration requires the application of reference gas mixtures. Those have to be taken aboard the spectrometric instrument by means of suitable gas containers which is not always possible due to weight and size constraints premised by some applications.

However, for the time being, the TILSAM method suffers from the unavailability of traceable line strength values and from comparably large associated uncertainties. Therefore, the line strength \(S_T\) is the limiting factor. Traceable line strength figures are rather rare throughout the literature [39]. Nevertheless, in addition, also other quantities like the optical path length \(L\) could often provide challenges if traceability is requested, for example, if multipass absorptions cells were to be considered.

Regarding the line strength, currently, there are a few efforts being undertaken to improve the lack of traceable reference line data [36, 37, 65–67]. If line strength uncertainties used in this work were in the subpercentage range, then the relative uncertainty of the spectrometric amount of substance fraction would be rigorously smaller. Consequently, the applicability would be increased and the method more competitive to existing nonspectrometric techniques. In turn, with respect to the CO measurements reported above, there is still some way to go before the uncertainty figure assigned to the CO amount fraction would match, for example, that of the data quality objective established by the WMO to be 0.5% relative for the GAW programme [68]. Thus, with an uncertainty of the amount fraction result less than one percent, the spectrometric measurements based on TILSAM presented in this paper could be applicable to environmental measurements as well as to other interesting gas analysis applications.

6. Conclusions

We have demonstrated the feasibility of the TILSAM method using TDLAS, QCLAS, and CRDS to perform absolute amount of substance fraction measurements. The spectrometric amount fraction results agree with their respective gravimetric reference values where available. The uncertainties of CO and CO₂ amount fractions evaluated by TDLAS, QCLAS, and CRDS are ±2.0%, ±5.2%, and ±4.2%, respectively. We project that, with a reduced uncertainty of the line strength value, absolute spectrometric measurements based on TILSAM could be applied to multiple gas analysis applications.

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