Research Article

Reality or Locality? Proposed Test to Decide How Nature Breaks Bell’s Inequality

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Bell’s theorem, and its experimental tests, has shown that the two premises for Bell’s inequality—locality and objective reality—cannot both hold in nature, as Bell’s inequality is broken. A simple test is proposed, which for the first time may decide which alternative nature actually prefers on the fundamental, quantum level. If each microscopic event is truly random (e.g., as assumed in orthodox quantum mechanics) objective reality is not valid whereas if each event is described by an unknown but deterministic mechanism (“hidden variables”) locality is not valid. This may be analyzed and decided by the well-known reconstruction method of Ruelle and Takens; in the former case no structure should be discerned, in the latter a reconstructed structure should be visible. This could in principle be tested by comparing individual “hits” in a double-slit experiment, but in practice a single fluorescent atom, and its (seemingly random) temporal switching between active/inactive states would possibly be better/more practical, easier to set up, observe, and analyze. However, only imagination limits the list of possible experimental setups.

Through Bell’s theorem [1, 2], which put the (in)famous Einstein-Podolsky-Rosen [3] argument on a solid and testable footing, and experimental tests thereof [4–8] it has been proven beyond reasonable doubt that no “locally realistic” fundamental model of the world can be correct. That is, a “sensible” worldview, such as that proposed in [3], is unfortunately untenable.

So either the objective reality-condition (that things exist in definite states whether we look or not) must be broken, for example, as in orthodox quantum mechanics, or the locality-condition (that events arbitrarily far away cannot affect what happens here and now—relativistic separability and causality) must be broken, for example, as in nonlocal hidden variable theories. The variables are called “hidden” because their existence is only conjectured and beyond our (present) control, but meant to complete quantum mechanics into a uniform description of micro and macro (Bell himself was heavily biased towards a hidden variable resolution of the problem [9]). The first detailed such theory, perfectly deterministic and compatible with all known experimental data, was [10]. Notice, however, that we are not necessarily considering any specific existing hidden variable theory, but an “ultimate” hidden variable theory that in principle decides everything deterministically. In contrast in the orthodox approach to quantum mechanics the quantum particles in effect behave as particles when observed and as waves when not observed—thereby, and at the most fundamental level, introducing the ill-defined act of observation (“measurement problem,” “collapse of the wave function,” and Bohr’s “irreversible act of measurement”), whereas particles in hidden variable theories always behave as particles but are being “pushed around” by the underlying (hidden) dynamics. In such deterministic systems the present state completely and uniquely determines the future, but as is well-known chaotic systems can “impersonate” randomness due to their extreme sensitivity to initial conditions; in a nutshell chaos is about order and disorder in deterministic systems that are nonlinear.

So far, it has not been possible to distinguish between the locality versus reality alternatives, and the choice has been mainly one of personal taste.

However, as hidden variable theories are deterministic (quantum particles behaving as realistic classical particles all the time, encoding Einstein’s “elements of physical reality” [3]) and orthodox quantum mechanics fundamentally probabilistic (each individual event/measurement assumed
to be completely random), it should be possible to experimentally test the distinction between them.

An experiment to test this possibility could be devised in analogy to the confirmation of deterministic chaos in a dripping water faucet [11, 12]. It is of course well-known that deterministic chaos requires nonlinear systems whereas the Schrödinger equation is linear. However, most hidden variable theories like the original by Bohm [10] are manifestly nonlinear (As an aside, if hidden variables is the correct way to explain the violation of Bell’s inequality this could make true quantum chaos possible, as opposed to the usual notion of “quantum chaos” which is concerned with quantum signatures of corresponding systems known to be chaotic in the classical case, as the linear structure of the Schrödinger equation alone does not support true chaos).

If we, for example, replace the dripping faucet with a double-slit experiment (According to R. P. Feynman the double-slit experiment “...has in it the heart of quantum mechanics. In reality, it contains the only mystery.”, The Feynman Lectures on Physics, Vol.III, p. 1-1) with individual quantum entities (electrons, neutrons, photons, etc.), the effectively one-dimensional position \( q_i \) of the successive “hits” on the detector screen, in effect defining a discrete time series, can be used to try to reconstruct a chaotic attractor, in case the underlying theory is dissipative, or a deterministic structure in phase space, in case it is nondissipative (Hamiltonian), by applying a method [14, 15] of converting a single data series into a phase space portrait via “delay coordinate embedding.” This can be accomplished, assuming a suitably low-dimensional attractor/structure, by defining the coordinates as follows:

\[
x = q_i, \quad y = q_{i+1}, \quad z = q_{i+2}. \tag{1}
\]

A given \( i \) then gives a point, \((x, y, z)\), in phase space.

To give an elementary example, the seemingly random data in Figure 1 is really due to the deceptively simple, but actually incredibly rich, “logistic mapping,”

\[
x_{n+1} = k x_n (1 - x_n), \tag{2}
\]

in its highly chaotic regime with \( k = 4 \) [13].

The reconstructed attractor, using the method described above, is seen in Figure 2 (2D) and in Figure 3 (3D).

We do not, however, expect that an eventual attractor/structure in real quantum mechanical data will be so simple and low dimensional, even though the logistic mapping has been shown to be in qualitative \textit{and} quantitative agreement with numerous real-life systems in all branches of science, see, for example, [16] for some early examples. This would be very surprising if not for the remarkable fact that there exists a “universality” in this kind of chaos [17].

In a sense, the logistic mapping is just like a model for observing “random” hits on an effectively 1D-detector screen of unit length (arbitrarily defined), just like in the double-slit experiment. The detector in effect defines a natural Poincaré section—a discrete “stroboscope” mapping.
When no dynamical relation between the data points \((q_i)\) exists, no structure is obtained by the reconstruction mechanism, (1). This would be the case for “orthodox” quantum mechanics where each individual hit/result/event is assumed to be completely random. The world could then not be objectively real, but could be local.

of the unit interval onto itself—of the underlying continuous dynamics described by differential equations. If there is a deterministic mechanism underlying the “random” hits on the screen, creating the known statistical distribution after many hits, it should then show up as a structure in reconstructed phase space.

In principle, to capture all emitted quantum particles, the ideal would be to have a perfectly efficient \(4\pi\)-detector, faithfully recording each individual quantum particle on its “latitude and longitude.” A 2D-iterated mapping, of the classic predator-prey kind, would then be a model for the successive hits, the simplest one using “nonoverlapping generations,” where each hit is described by two coordinates (originally the populations of predator and prey species) and is determined by the previous hit through a mapping of the form

\[
x_{n+1} = f(x_n, y_n), \quad y_{n+1} = g(x_n, y_n). \quad (3)
\]

One such model, the Hénon mapping [18]

\[
x_{n+1} = y_n + 1 - ax_n^2, \quad y_{n+1} = bx_n, \quad (4)
\]
gives the famous Hénon-attractor. For the canonical values \(a = 1.4\) and \(b = 0.3\) the Hénon map is chaotic; each individual hit appears random, but a clear structure builds up over time, analogous to hits in the double-slit experiment. In the former case the structure is fractal [19] whereas in the latter case it may or may not be.

However, one could argue that any eventual hidden variables must “know” that we have restricted the “landing platform” for the quantum particle to an effectively 1D strip, so that additional spatial variables are superfluous. The hidden variables must also keep track of if one or both slits are open and relay that information nonlocally (faster than the speed of light) to the detector screen, as in [10], to comply with the violation of Bell’s inequality.

As modern technology has made it possible to trap and observe individual quantum objects, such as atoms, it might be better and easier to exploit this fact than trying to use the mythical double-slit. Measurements of “quantum jumps” in single atoms [23, 24], and the resulting fluctuation of their fluorescent on/off states, may make an ideal testing ground where recorded data should already be present (the time series underlying Figure 2 in both articles [23, 24] could in principle be directly inserted into (1) above), but only imagination limits the list of possible experimental setups.

If the seemingly random florescence gives rise to a distinct structure in phase space, with noninteger fractal dimension, onto which the phase space points are concentrated, it would be a clear indication that it is actually the consequence of dynamical deterministic chaos (i.e., hidden variables), in direct analogy to how [11, 12] revealed deterministic chaos in the dynamics of the dripping water faucet (Figure 6). For examples of qualitatively typical chaotic attractors/structures see, for example, the figures in [11, 12] or the famous examples presented in the figures in this article.
Figure 6: “The Lorenz map”—when successive, erratically fluctuating, amplitude maxima were plotted for the Lorenz attractor (previous figure) using a technique analogous to the one described in this article, the surprising result was this nearly one-dimensional attractor; hidden order in chaos [20], and a concrete simple example of the relation between continuous dynamics and discrete mappings.

(accompanied by their respective physical implications to the problem at hand in the figure captions to Figures 5 and 7). However, the exact shape, dimension, and complexity will be governed by the (unknown) detailed underlying dynamics. The rest of the analysis carries through just like in [11, 12].

In fact, in the present case it is in principle even easier to obtain a conclusive result as any observed structure indicates a deviation from the usual assumption of total randomness of quantum mechanics—where it is normally assumed that, for example, the hit of an individual particle is a completely independent and truly random process—even if one has collected one million successive data points the next one, according to orthodox quantum mechanics, will be a complete surprise and impossible to predict even in principle, see Figure 4.

So, in a perfect world it should be easy to potentially disprove orthodox quantum mechanics. A practical problem is of course that there exist no perfect particle detectors, which results in missing part of the series and also in the introduction of noise in the data. The more of the series one misses, the harder it becomes to reconstruct an (eventual) attractor/structure. This may, as stated above, be circumvented by observing, for example, single atoms exhibiting quantum jumps as this “...can be detected with unity quantum efficiency” [23].

If, however, no attractor/structure is found in the experimental data, that is, if the points are scattered randomly in phase space, as in Figure 4, where every \( q_i \) has been generated at random, then quantum mechanical “measurements” (e.g., hits on detector screen, timing between on/off states, etc.) probably cannot be described by deterministic equations, and some truly stochastic effect(s) must instead be at work, for example, as assumed in orthodox quantum mechanics.

Hence, it should be possible to test, and potentially falsify: either the hypothesis that quantum randomness is due to underlying deterministic dynamics-hidden variables (in which case the “randomness” actually would merely be apparent, not fundamental)—without having to know and penetrate the details of the underlying equations, or the standard fundamentally probabilistic interpretation/postulate of Born as used in orthodox quantum mechanics, and hence answer if nature prefers to break locality or objective reality on her fundamental level. In case of the former, it would indicate an unexpected and deep hidden connection between the three great revolutions of 20th-century science; relativity, quantum mechanics, and chaos theory, and perhaps even point the way towards a unified complex nonlinear systems theory of the future.

References


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