Review Article

Zero Spatial Frequency Limit: Method to Characterize Photopolymers as Optical Recording Material

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1. Introduction

Photopolymers are useful for different applications due to the refractive index variations and relief profiles generated [1–8]. There are many types of photopolymers that may be differentiated by the type of binder, since this component determines to a great extent the choice of monomer, dye, and initiator used in the photopolymer. Normally, these materials are used in holographic applications, where high values of spatial frequencies are recorded. In these range of frequencies many processes are involved in the hologram formation, such as species diffusion, nonlocal polymerization (due to the finite size of polymer chains), shrinkage or swelling (volume changes), and others [9–13]. Therefore, analyzing the behaviour of a photopolymer as an optical storage medium is a complicate task. In this sense, the variations in the estimation of the monomer diffusion affect significantly the values obtained for other material parameters, making difficult to calculate them separately. In particular, it is interesting to analyze the material behavior at very low spatial frequencies, since at these frequencies monomer diffusion does not play an important role [14] and even disappears at the zero spatial frequency limit [15–17].

Zero spatial frequency limit analysis is a method is based on an interferometer that has been successfully applied in the phase-shift versus applied voltage characterization of liquid-crystal displays (LCDs) [18]. In the limit of zero frequency recording, that is, uniform exposure of the photosensitive layer, no diffusion processes are produced [15–17] and we can determined directly many parameters (as opposed to holographic characterization, the data obtained in this case are directly related to the physical properties of the material without the need of nonlinear fitting of multiparametric models) and these values can be used in diffusion models to predict the exact holographic material behavior [12, 13]. The measuring of refractive index variation and the changes in the thickness, in noncover-plated samples only (where the light is reflected directly from the material), can be directly observed in real time. Some other parameters that can be measured are polymerization rate, polymer refractive index...
2. Materials and Experimental Setup

The zero spatial frequency method (Figures 1(a) and 1(b)) is based on an interferometer that has been successfully applied in the phase-shift versus applied voltage characterization of liquid-crystal displays (LCDs) [18]. It shows good precision, and, due to its quasi-common-path architecture, is a robust setup, less sensitive to changing environmental conditions, and simpler to construct than Mach-Zehnder type interferometers. The setup has two arms with an angular separation of 14°, one to expose the recording material, whereas the second arm is the interferometer used to measure, in real time, the phase-shift. The recording material is perpendicularly oriented with respect to the interferometer axis in order to simplify the analysis of the interferometric results: at an oblique incidence we should take into account both the Fresnel coefficients at the interface and the increase of the two orders is more than 1 cm, so as to eliminate the interference pattern, since the photopolymer does not present any absorption at 633 nm. We introduce a grating of layers (drying process) and it has to react through diffusion in the polymerization sense of movement of the fringes (indicated by the arrow in the Figure 1) we can deduce if the exposed zone is shrinking or swelling with respect to the nonexposed one. In the case of the photopolymer studied in this paper we obtained that the exposed zone shrinks with respect to the nonexposed area.

The photopolymer has been studied for many groups in many different cases [19–23]. Nevertheless, AA has an undesirable feature, the toxicity of AA and its low environmental compatibility [24, 25]. Therefore, we have changed the AA by sodium acrylate, NaAO, in order to obtain a higher environmental compatibility. Then we present the study of the recovered material at the zero spatial frequency limit. The shrinkage of recovered materials cannot be measured which is an important drawback in the characterization of this material with zero spatial frequency recording. Finally, we present how the zero spatial frequency recording can be applied successfully also to H-PDLC materials.

In the second arm we use a He-Ne laser to generate the interferences pattern, since the photopolymer does not present any absorption at 633 nm. We introduce a grating with a spatial frequency of 4lines/mm to generate a series of diffracted orders; we block all the orders except +1 and −1. One of the two orders impinges on the exposed zone (illuminated by the Nd-YVO4 laser, 532 nm) and the other one impinges on the nonexposed zone. The distance between the two orders is more than 1 cm, so as to eliminate the influence of the monomer diffusion in the polymerization process. Afterwards the orders are brought to interfere and from the interference pattern we may obtain the evolution in the material due to polymerization (diffusion is not present).

In Figure 1(a), once the two orders have propagated throughout the photopolymer, a lens is used to make them interfere. A microscope objective is used to amplify the interference pattern onto a CCD camera. This pattern is captured in real time as a function of exposure at specific time intervals, then it is digitized and transferred to a personal computer [15]. We note that there may appear reflection gratings generated by Fresnel boundary reflections. However the recording of these undesired reflection gratings probably is highly attenuated due to the following reasons: the last boundary reflection between glass and air is weak and in addition, due to the nonlocal effect, the size of polymer chains prevents the recording of these high spatial frequencies.

In Figure 1(b) once the two orders are reflected by the photopolymer, we place a lens to make them interfere. A microscope objective is used to amplify the interference pattern onto a CCD camera. This pattern is captured at specific exposure time intervals, then it is digitized and transferred to a personal computer. The reflections from the back surface are eliminated using a black film on the back surface [16].

Once the interference pattern has been stored, we can measure the shift with respect to the initial pattern obtained for the unexposed layer. To increase the accuracy in this calculation, we cross-correlate the different interference patterns with the initial one. The cross-correlation produces a clear peak [15–17]. The location of this peak for each correlated interference pattern with respect to the center of the image is equal to the shift in the fringe pattern. A full fringe shift is equal to a $2\pi$ radians variation in the phase shift. In this experiment, as we are using a reflection interferometer, the phase shift is directly related to the thickness variation of the material [16]. Depending on the sense of movement of the fringes (indicated by the arrow in the Figure 1) we can deduce if the exposed zone is shrinking or swelling with respect to the nonexposed one. In the case of the photopolymer studied in this paper we obtained that the exposed zone shrinks with respect to the nonexposed area.

When PVA is used as a binder the monomer must be water soluble, it must not evaporate during the preparation of layers (drying process) and it has to react through...
a radical chain mechanism. As mentioned above the toxicity of sodium acrylate (NaAO) is lower than that of AA [17]. Moreover, different triethanolamine (TEA) concentrations are normally used to obtain different material properties (TEA is a liquid at ambient temperature and plays an important role in the monomer and polymer diffusion during the polymerization process too).

The less toxic component of PVA/AA standard photopolymer is the dye, yellowish Eosin (YE), nevertheless to obtain a real environmental compatibility we have tested a less toxic dye [23, 24]. In the new photopolymer we use the sodium salt 5'-riboflavin monophosphate (PRF) as dye, bearing in mind that this substance is water soluble and exists in the environment, so it is not likely to cause environmental problems.

The solutions, whose compositions can be seen in Table 1, with water as solvent, and PVA as binder (Mw = 130000 a.m.u., hydrolysis degree = 87.7%) are deposited, using the force of gravity over a glass. The glass surface measures 30 × 40 cm² and left inside a dark chamber where humidity and temperature are controlled (relative humidity = 40–45%, T = 21–23°C) [17]. When large part of the water has evaporated (about 48 hours), the layer has enough mechanical resistance and it can be cut without deformation. As crosslinker we have used N, N’-methylene-bis-acrylamide (BMA) to study the mixture with NaAO. The presence of BMA in the formulation of biophotopol [25] is optional and not essential to the main features of the photopolymer. Furthermore, the toxicity of BMA is clearly lower than AA. In this work we have characterized five new compositions. We have tested photopolymers with different TEA concentrations, with different concentrations of BMA, and different dyes. Composition A is directly derived from the previous works where biophotopol composition is optimized to achieve thick layers (around 1 mm thick). Since we have found weak modulation of layer type A, we have introduced BMA as crosslinker in compositions B and C. To increase the differences between exposed and nonexposed zones we have also introduced more NaAO in compositions B and D. To substitute YE we have presented composition E. The standard compositions used in previous works are compositions F and G (PVA/AA-based materials without and with crosslinker). The thickness of the samples is around (100 μm) and the intensity at 532 nm used is 1 mW/cm².

![Figure 1: Experimental setup for zero spatial frequency analysis. P is polarizer, WP is wave plate, MO is microscope objective. (a) Transmission analysis. (b) Reflection analysis.](image-url)
In these materials the absence of cover plate will lead to two types of cross membrane diffusion taking place: oxygen across the boundary [26] and water in and/or out (due to heating or absorption).

The H-PDLC photopolymer is composed of dipentaerythritol penta/hexa-acrylate (DPHPA) as monomer and binder, N-vinylpyrrolidone (NVP) as crosslinker, ethyl eosin (YEt) as dye, and N-methyl diethanolamine (NMDETA) as radical generator. These components were mixed under red light where the material is not sensitive and under a temperature of 40°C to solve properly all the components, specially the crystal liquid molecules (LC BL087 provided by Merck). The solution (100 mL) was sonicated in an ultrasonic bath, heated, mixed with a magnetic mixer, and deposited between two glass plates each 2 mm thick. The H-PDLCs layers have thickness around 12 μm in order to apply the electric field and to align the crystal liquid molecules, thus obtain the switchable holographic gratings. In the samples analyzed in this work we have used spacing of 106 μm to increase the phase shift and see properly the different behaviours reducing the error in our calculations [15]. We focus our attention on the characterization of the chemical composition; we do not make switchable gratings. In Table 2 we described the composition of different layers analyzed at zero spatial frequencies. These compositions are designed to keep the liquid volume constant. In the five compositions we analyzed the influence of the liquid crystal in the polymerization process.

In order to calculate an approximate value for the refractive index, we will assume that when exposition has finished, all the monomer has been polymerized. In this sense, it is important to obtain a precise estimation of the initial volume fraction of the monomer present in the layer [13, 27, 28]. This volume fraction it is more complicate to calculate in noncover-plated PVA materials, because PVA water absorption from the environment depends on the humidity. The water presence can be estimated if we measure the quantity of water evaporated during the drying process. It is interesting to note that after the drying process only very small portion of the initial water remains inside the layer. In our case, 48 hours after the layer deposition, the initial monomer volume fraction reaches the values presented in Table 3.

Once we have introduced the volume fractions, it is easy obtain the volume fraction for each component, \( \phi(i) \). Using the values of the refractive index, \( n_i \), of each compound together with the Lorentz-Lorenz equation [27, 28], the refractive index of the layer before recording can be calculated, \( n_0 \):

\[
\frac{n_0^2 - 1}{n_0^2 + 2} = \sum_{i=1}^{k} \phi(i) \left(\frac{n_i^2 - 1}{n_i^2 + 2}\right).
\]

These values were checked using Abbe refractometer (Model AYA-15) measurements and are presented in Table 4. As can be deduced from Table 4, in compositions C1 and C2 the liquid crystal volume fraction is higher than 20%. That can avoid huge variations in the refractive index at zero spatial frequency recording. \( n_0 \) is the average refractive index of the layer before the exposure. For zero spatial frequency analysis applied to H-PDLC, liquid crystal plays a similar role than binder in PVA materials; therefore, it does not participate in the chemical reactions.

### 3. Theoretical Treatment of Experimental Data

The phase shift in the reflection measurements, \( \Delta \Phi_{\text{Shr}} \), is directly related to thickness variation during exposition at the zero spatial frequency limit. In this case, the thickness variations of the material (\( \Delta d \)) can be expressed as follows:

\[
\Delta d = \frac{\Delta \Phi_{\text{Shr}} \lambda \cos \alpha}{4\pi},
\]
Table 4: Initial volume fractions and refractive indices, $n$.

<table>
<thead>
<tr>
<th>Compound</th>
<th>C1</th>
<th>C2</th>
<th>C3</th>
<th>C4</th>
<th>C5</th>
<th>$n$</th>
</tr>
</thead>
<tbody>
<tr>
<td>DPHPA</td>
<td>0.5241</td>
<td>0.5649</td>
<td>0.6061</td>
<td>0.6899</td>
<td>0.7758</td>
<td>1.4900</td>
</tr>
<tr>
<td>NMDETA</td>
<td>0.1729</td>
<td>0.1739</td>
<td>0.1750</td>
<td>0.1771</td>
<td>0.1792</td>
<td>1.4694</td>
</tr>
<tr>
<td>NVP</td>
<td>0.0433</td>
<td>0.0435</td>
<td>0.0437</td>
<td>0.0443</td>
<td>0.0448</td>
<td>1.5110</td>
</tr>
<tr>
<td>YE</td>
<td>0.0002</td>
<td>0.0002</td>
<td>0.0002</td>
<td>0.0002</td>
<td>0.0002</td>
<td>1.7700</td>
</tr>
<tr>
<td>LC BL087</td>
<td>0.2594</td>
<td>0.2175</td>
<td>0.1750</td>
<td>0.0885</td>
<td>0.0885</td>
<td>1.5460</td>
</tr>
</tbody>
</table>

where $\lambda$ is the wavelength, 633 nm in our case, and $\alpha$ is the angle inside the material. At zero spatial frequency limit, when diffusion does not take place, the decreasing of the monomer concentration $\phi^{(m)}$, depends on the recording intensity, $I$, the dependency of the polymerization on intensity, $\gamma$, the initial monomer concentration, and the polymerization reaction constant, $K_R$ [12]:

$$\phi^{(m)}(t) = \phi^{(m)}_0 e^{-I^\gamma K_R t}, \quad (3)$$

where $\phi^{(m)}_0$ is the initial monomer concentration in volume fraction.

The model used in this paper is simple and based on the classical model proposed by Zhao and Moroulis [12]. The aim of the paper is to propose and demonstrate a simple diffractive and interferometric method to calculate the first approximation of the polymerization rate and monomer diffusion. It is important to note that the gradient of monomer concentration in depth due to the dye absorption analyzed in previous works [29, 30] has been disregarded in this first approximation to the problem. In this sense it is important to mention the contributions of Sheridan et al. to clarify all the parameters involved in the polymerization process such as the influence of oxygen inhibiting [26], the effects of the dye kinetics, and polymer chain initiation, propagation, and termination [31–33] that can be studied using real zero analysis in future works. In any case the parameters obtained using the presented methodology produce good results when introduced in simple models as it is shown in references [34, 35]. Following the same steps presented in [15–17] we can obtain the polymerization rate as a function of the experimental values of the phase shift during recording, $PS$, and the phase of saturation, $PS_{\infty}$:

$$\ln\left(1 - \frac{PS(t)}{PS_{\infty}}\right) = -I^\gamma K_R t = -F_R t. \quad (4)$$

Parameter, $\gamma$ (which governs the relation between recording intensity and polymerization rate, see (3)), can be associated to the viscosity of photopolymer system. In this sense values of $\gamma$ around 0.5 are associated to high fluid systems and for very dry systems values are near to 1 [12, 17]. To calculate this parameter the material can be exposed with some different intensities.

Furthermore, if the quantities of different compounds are known, it is possible to obtain the polymer refractive index using Lorentz-Lorenz equation [28]. To make the calculus more accurate it is possible to measure the exact concentration of each component at the end of zero spatial frequency recording by additional methods. In any case, interesting information can be extracted solving the following equation for some particular cases:

$$\frac{n_p^2 - 1}{n_p^2 + 2} = \frac{1}{\phi^{(P)}} \left[\frac{n_i^2 - 1}{n_i^2 + 2} - \sum \frac{n_{fi}^2 - 1}{n_{fi}^2 + 2} \phi^{(i)}\right], \quad (5)$$

where $n_i$ is the final refractive index of the layer, $n_p$ is the refractive index of the polymer formed during exposition, $n_i$ is the refractive index of chemical compound $i$, and $\phi^{(i)}$ is the final volume fraction for compound $i$. In the cases analyzed in this work, due to the high value of dye concentration, the samples show high absorption (the initial transmittances are around 1%). In addition, at the end of exposing process we detected a weak presence of dye. Thus we assume that in the exposed zones all the components, except the binder (in the case of PVA/AA and PVA/NaAO) or liquid crystal (in PEA photopolymer), are polymerized. In this sense, radical polymerization models could be used to know the exact concentration of monomer and dye after illumination [31–33]. With this assumption (5) can be reduced to:

$$\frac{n_p^2 - 1}{n_p^2 + 2} = \frac{1}{\phi^{(P)}} \left[\frac{n_i^2 - 1}{n_i^2 + 2} - \frac{n_{Cfi}^2 - 1}{n_{Cfi}^2 + 2} \phi^{(C)}\right], \quad (6)$$

where $n_C$ and $\phi^{(C)}$ are the refractive index and volume fraction of the constant component, binder in PVA materials, and liquid crystal in H-DPLC.

4. Results and Discussion

In this section we present the experimental data obtained for different material compositions and different thicknesses using both experimental setups for PVA photopolymers and only transmission analysis for H-DPLC.

4.1. PVA Photopolymers. In transmission analysis we can observe the effects of the refractive index changes and thickness variation during polymerization. The results for the new five compositions are presented in Figure 2. As can be seen the changes in the phase between exposed and nonexposed zones for compositions A and E are very weak (around 60°), therefore the refractive index variation and polymerization rate are small. It is important to note that the absorption of PRF is clearly lower than YE.

As the velocity of the reaction is very slow, after 1000 s the material continues changing in compositions A, E, and D (compositions without crosslinker). Compositions B and C (compositions with crosslinker) present very similar behavior in transmission analysis. In these compositions after 400 s the reaction stops and the layers are in saturation state (where the phase shift does not change with the illumination). Using composition G (AA+BMA) the highest values of phase shift are obtained due to presence of the crosslinker.

In Figure 3, we have presented the results obtained in reflection analysis for NaAO-based compositions (A, B, C, D, and E). We can observe that the maximum shrinkage is around 3% for compositions B, C, and D. This shrinkage is
large enough to store reflection diffractive elements using the relief variations [35]. On the other hand to use these materials as holographic memories the shrinkage should be reduced. As can be deduced from this and last figures compositions B, C, and D present similar behavior. The composition E, with PRF as a dye, the shrinkage is around 0.25 μm, nevertheless we cannot extract any significant information because the dye crystallizes during exposition.

In Figure 4 we depicted the results for some compositions obtained by the fitting based on (4). The results show us different values of $F_R$ for each composition and in Table 5.

**Table 5: Initial volume fractions and refractive indexes, $n$.**

<table>
<thead>
<tr>
<th>Composition type</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>F</th>
<th>G</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_R \times 10^{-3}$ (s$^{-1}$)</td>
<td>3.2</td>
<td>3.6</td>
<td>4.1</td>
<td>3.3</td>
<td>5.8</td>
<td>7.0</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.999</td>
<td>0.993</td>
<td>0.992</td>
<td>0.994</td>
<td>0.997</td>
<td>0.994</td>
</tr>
</tbody>
</table>

The correlation value of the fittings, $R^2$, indicates the good agreement between theory and experiments. In addition the compositions A and D present similar values of $F_R$ because the only variation is the monomer concentration. For composition G (AA+BMA) we measured the highest values of phase shift are obtained due to presence of the crosslinker. Maybe for holographic recording there are some small changes in $F_R$ values, because the experimental conditions present some differences such as the moving of monomers. Nevertheless we believe that using real zero spatial frequency a good estimation of the order of magnitude of $F_R$ can be obtain. The validity of these values has been confirmed in recent papers [35], where the values of zero spatial frequency were used to predict the formation of relief optical elements on the photopolymer surface.

To calculate the value of $y$ in PVA/NaAO materials we exposed the material to two different exposure intensities 0.5 and 1 mW/cm$^2$ for composition type A and we calculated the polymerization rate value in each experiment using (4). The comparative result between the two exposures intensities are presented in Figure 5. With these data it is easy to obtain the value of $y$. In our case the value obtained is 0.48. This value is in good agreement with the value of 0.5, usually assumed for photopolymers with low viscosity [12, 17]. It is important to note that for low values of the parameter $y$ the nonlinearity is increased.

It is obvious that the phase shift obtained depends directly of the photopolymer thickness. In [15] this method was applied to characterize layers thicker than 0.5 mm able to store high quantity of data pages [5]. Results provided by (6) are presented in Table 6 (we have omitted composition G due to its different behavior). These values for $n_p$ are important when they are compared with the monomers ones; that is,
the refractive index of acrylamide is clearly lower than the NaAO refractive index [17]. To determinate these values we have followed the steps indicated in [15–17]. Furthermore we want to remark that the main important point is to compare \( n_m \) with \( n_p \) and these parameters with the value of the refractive index of the binder, \( n_b \) (5). In this sense the importance of crosslinker to increase \( n_p \) has been demonstrated using the zero frequency technique. To obtain a better analysis of the data presented in Table 6 it is important to note that the refractive index of NaOA is 1.565 [17].

4.2. H-DPLC Photopolymers. In order to obtain information about the effect of incorporating CL in the photopolymerizable solution using real zero frequency recording, the phase shift between illuminated and nonilluminated zones for compositions C1, C2, C3, C4, and C5 is shown in Figure 6. As can be seen in this figure, the presence of CL molecules produces a decrease in phase shift. The values of \( n_p \) obtained for C5, C4, C3, and C5 (without LC) using (6) are 1.492, 1.492, 1.495, 1.496, and 1.496, respectively. Therefore we can conclude that incorporation of LC molecules results in only a small change in polymer refractive index. As zero spatial frequency recording prevents diffusion of liquid crystalline molecules into dark regions and of monomers to bright regions, the uniform concentration of LC throughout the whole layer makes it difficult for the refractive index to change.

Following the steps described previously and using (4), it is possible to obtain the polymerization rate for each composition. The values obtained are represented in Table 7. As can be seen in this figure the correlation parameter indicates that there is agreement between experimental data and theoretical behaviour. From the analysis of Table 7 the high values of the polymerization rates obtained can be deduced. These values are 10 times higher than the ones obtained for PVA materials analyzed in Table 5, due to the multifunctional monomer used in H-PDLC materials. To fit accurately the polymerization rate in these materials the temperature is a fundamental parameter. In general, in Table 7 we can detect a decrease in the polymerization when high values of LC concentration are included in the composition. The exception is the C3 with very low polymerization rate and correlation parameter. As can be seen the curve grows very quickly from 0 to 50 s and then the phase shifts increases slowly, as if the residual monomer polymerizes with difficulties, maybe produced by Trommsdorff effect [36] and the cooling of the layer.

5. Conclusions

Using zero frequency recording we characterized different types of photopolymers with and without liquid crystal molecules, cover plating, crosslinker, and so forth. Using this method we were able to analyze polymerization separately from the diffusion and thus discuss the influence of the different components such as liquid crystal molecules, crosslinker, and so forth on grating formation. We also presented some simply models using interferometric methods to fit the polymerization rate, the refractive index of polymers and the relation between exposure intensity on polymerization. We
have shown how this method can be used to obtain photopolymer layers with desired properties. Finally we think that this method can be applied to fit some of the multitude of parameters that take place in the light absorption in photopolymers materials. All these parameters should be taking into account in order to design holographic diffusion model to predict the behavior of these photopolymers. In our opinion the viability of these three types of photopolymers for diffractive and holographic application has been demonstrated.

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