Research Article

Inefficient Vibrational Cooling of $C_{60}$ in a Supersonic Expansion

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High-resolution gas-phase infrared spectroscopy of buckminsterfullerene ($C_{60}$) was attempted near 8.5 μm using cavity ring-down spectroscopy. Solid $C_{60}$ was heated in a high-temperature (~950 K) oven and cooled using an argon supersonic expansion generated from a 12.7 mm × 150 μm slit. The expected S/N ratio is ~140 for vibrationally cold $C_{60}$, but no absorption signal has been observed, presumably due to a lack of vibrational cooling of $C_{60}$ in the expansion. Measurements of $D_2O$ at 875K are presented as a test of instrument alignment at high temperature and show that efficient rotational cooling of $D_2O$ occurs in the hot oven ($T_{rot} = 20$ K in the expansion), though vibrational cooling does not occur. The attempted $C_{60}$ spectroscopy is compared to previous work which showed efficient vibrational cooling of polycyclic aromatic hydrocarbons (PAHs). Possible alternative experiments for observing a cold, gas-phase spectrum of $C_{60}$ are also considered.

1. Introduction

Ever since its discovery in 1985 [1], buckminsterfullerene ($C_{60}$) has been the subject of an enormous body of research (the publication of its discovery has been cited more than 8100 times at the time of writing according to Web of Science). One particular area of interest is the astrochemistry of $C_{60}$. $C_{60}$ was long believed to be present in the interstellar medium (ISM) and has recently been detected via emission spectroscopy in the mid-infrared (mid-IR) [2–7]. Though $C_{60}$ has been detected in the ISM, the mechanism by which it is formed is still under debate [8]. Obtaining an astronomical absorption spectrum of $C_{60}$ would yield additional information about the abundance and temperature of $C_{60}$ in the ISM, which could provide useful information in determining the formation mechanism. Unfortunately, astronomical searches for absorption from cold gas-phase $C_{60}$ are hampered by the lack of a high-resolution gas-phase laboratory spectrum of any of the four infrared active vibrational bands of $C_{60}$.

A rotationally resolved spectrum of $C_{60}$ would also be of great fundamental interest. The acquisition of such a spectrum would be a significant milestone in the field of molecular spectroscopy, as $C_{60}$ would be the largest and most symmetric molecule to be observed with rotational resolution. In addition, due to boson exchange symmetry restrictions on the overall symmetry of the molecular wave function there are many rotational levels in the ground and vibrationally excited state that are rigorously forbidden to exist [9, 10]. Such missing levels will manifest as “gaps” in the normal progression of rovibrational lines.

Despite great interest in a high-resolution spectrum of $C_{60}$, a rotationally resolved, gas-phase absorption spectrum of $C_{60}$ has not yet been observed. There are several obstacles which must be overcome to record such a spectrum. First, it is difficult to generate a gas-phase sample of $C_{60}$. $C_{60}$ has negligible vapor pressure at room temperature and must be heated to temperatures in excess of 875 K to reach a vapor pressure on the order of 10–100 mTorr [15]. Second, $C_{60}$ has 174 vibrational modes, which leads to a large vibrational partition function at even modest temperatures (see Figure 1). Cooling the vibrational degrees of freedom will be critical for observing a fundamental vibrational band. Finally, it is necessary to have a sensitive, high-resolution spectrometer in the mid-IR to observe the relatively small amount of gas-phase sample.
We have developed an experiment which attempts to address these obstacles. We have built a high-temperature oven source which has been used to generate \( \text{C}_{60} \) vapor. To attempt to relax the vibrational degrees of freedom, the hot \( \text{C}_{60} \) vapor has been cooled using a supersonic expansion. The supersonic jet is then probed using continuous wave cavity ring-down spectroscopy (cw-CRDS) [18]. We have attempted to observe the 8.5 \( \mu \text{m} \) band due to the availability of quantum cascade laser (QCL) sources at this wavelength and also because this band coincides with an atmospheric window, permitting ground-based astronomical observations. The cavity ring-down spectrometer has already been tested by carrying out high-resolution spectroscopy of methylene bromide [19] and pyrene [13]. Despite multiple spectral searches under a variety of expansion source conditions, no absorption signals from \( \text{C}_{60} \) have yet been detected.

Previous work has shown effective vibrational cooling of large molecules, such as polycyclic aromatic hydrocarbons (PAHs), in supersonic expansions [13, 14, 20]. In contrast to this previous work, our lack of signal indicates that the vibrational degrees of freedom are not effectively cooled in \( \text{C}_{60} \). We will discuss the details of our experiment and also briefly discuss measurements of \( \text{D}_2\text{O} \) made in the heated oven, which show good rotational cooling, but no vibrational cooling. We will also compare our current experiment to the previous work showing good vibrational cooling of other large molecules. Finally, we will present possible alternative experiments which may allow observation of a high-resolution absorption spectrum of \( \text{C}_{60} \).

\section*{2. Materials and Methods}

\subsection*{2.1. QCL-Based Cavity Ring-Down Spectrometer}

Our high-resolution mid-IR spectrometer has been described in detail previously [18, 19], so here we present only a brief overview of the instrument. Mid-IR light near 8.5 \( \mu \text{m} \) is generated using a QCL supplied by collaborators in the Gmachl group at Princeton. The frequency of the emitted light can be tuned from \( \sim 1180 \) to \( 1200 \text{ cm}^{-1} \) by changing the temperature of the laser and the current applied to the QCL. Light from the QCL is sent through an optical isolator to an optical cavity where we perform cw-CRDS to record the infrared absorption spectrum of our sample. To calibrate our spectra we utilize an absorption cell filled with \( \text{SO}_2 \) to provide absolute frequency calibration and a mid-IR wavemeter for relative frequency calibration.

\subsection*{2.2. Vaporization Source and Expansion Seeding}

We have constructed a high-temperature oven which we used to produce gas-phase \( \text{C}_{60} \). The oven is described in detail in our previous work on pyrene [13]. The oven is made from stainless steel with attached strip heaters to provide heating and is capable of operating under vacuum at temperatures up to 975 K for many hours. To produce gas-phase \( \text{C}_{60} \) for spectroscopy, solid \( \text{C}_{60} \) (MER Corporation, 99+ % purity) was loaded into the oven, which was then placed in a vacuum chamber and surrounded by an aluminum heat shield. The oven was heated by applying current to the strip heaters using variable transformers, which gave us coarse control over the temperature of the oven. The oven temperature was monitored using a thermocouple inserted into the interior of the oven. Once we had achieved the desired temperature (\( \sim 950 \text{ K} \)) a stream of \( \text{Ar} \) gas was passed through the oven and generated a continuous supersonic expansion of the \( \text{Ar}/\text{C}_{60} \) mixture through a 12.7 \text{ mm} \times 150 \mu \text{m} \) slit; the expansion was then probed with our spectrometer. Effective vaporization of \( \text{C}_{60} \) in the oven was verified by measuring the mass of \( \text{C}_{60} \) in the oven following a set of scans, and also by deposition of \( \text{C}_{60} \) on the walls of our vacuum chamber. The alignment between the supersonic expansion from the vaporization source and the optical cavity was verified in separate experiments through spectroscopy of \( \text{D}_2\text{O} \). In these experiments, trace \( \text{D}_2\text{O} \) (Cambridge Isotope Laboratories, 99.99% D) was seeded into the \( \text{Ar} \) flow and was passed through the vaporization source as it was being operated at temperatures similar to those used when vaporizing solid \( \text{C}_{60} \).

\subsection*{2.3. Signal-to-Noise Estimation for \( \text{C}_{60} \)}

Knowledge of where to scan in frequency space to detect the first signal from the 8.5 \( \mu \text{m} \) vibrational band of \( \text{C}_{60} \) is critical. Restricting the search window allowed us to focus on varying experimental parameters instead of trying to cover a large spectral region. The only gas-phase measurements come from observations of infrared emission at \( \sim 1000 \text{ K} \) [21, 22]. The estimated band center position was 1169.1 \text{ cm}^{-1} [21], but this estimate is likely red-shifted due to the contribution from hot bands, whose emission frequencies are shifted due to vibrational anharmonicity. Low-temperature (15 K) measurements of \( \text{C}_{60} \) films assign the center position to 1183.7 \text{ cm}^{-1} [23], while \( \text{Ar} \) matrix spectroscopy yields 1184.8 \text{ cm}^{-1} [24]. Measurements in para-\( \text{H}_2 \) (p-\( \text{H}_2 \)), considered the least perturbing matrix host, place the center position of the vibrational band at 1184.7 \text{ cm}^{-1} [10]. Because the frequency shift between \( \text{Ar} \) and p-\( \text{H}_2 \) matrix hosts for a spectral feature is generally comparable to the frequency shift between gas-phase and p-\( \text{H}_2 \), we feel confident
that the peak of the 8.5 μm absorption band should be near the p-H₂ matrix value of 1184.7 cm⁻¹.

We have simulated the 8.5 μm C₆₀ vibrational band at high resolution, following the approach of Sogoshi et al. [10]. As noted by Sogoshi et al., the appearance of the spectrum will be dependent on the change of the rotational constant from the ground to the excited vibrational state as well as the Coriolis coupling constant ξ. If the change in rotational constant is small, there will be a prominent Q-branch. If the change is large (on the order of 1%), there could be a prominent R-branch head. Because we do not know if either of these cases will happen in the actual experimental spectrum, we base our signal-to-noise (S/N) estimates on observing a single rovibrational transition. To estimate our expected signal, we use a theoretical value for the band strength of the 8.5 μm band [25] of 25 km/mol. Our estimates assume a vibrational temperature of 0 K. We will discuss the importance of vibrational excitation in Section 3.3.

Estimating the expected S/N for C₆₀ absorption using our experimental apparatus parallels calculations that we carried out to estimate vibrational cooling of pyrene in a previous publication [13]. We begin with the following formula for estimating the S/N for a single rovibrational transition:

\[
\frac{S}{N} = \frac{n_z f S L_{\text{jet}}}{\Delta \nu (\sigma_{\text{NEA}})}.
\]

In this equation, \(n_z\) is the number density of \(^{12}\)C₆₀ in units of cm⁻³ at a distance \(z\) from the slit, \(f\) is the ratio of the line intensity for a single transition (factoring in Boltzmann statistics) divided by the sum of all the line intensities, \(S\) is the calculated band strength in cm/molecule, \(L_{\text{jet}}\) is the length of the expansion in cm, \(\Delta \nu\) is the linewidth of the transition in cm⁻¹, and \(\sigma_{\text{NEA}}\) represents the noise equivalent fractional absorption of the spectrometer. By evaluating each of these parameters for our instrument and this band of C₆₀, we can calculate an expected S/N for our experiment.

To estimate the number density, we use the rate of mass loss from the oven per unit time, combined with the velocity of molecules in the expansion. We account for the fact that not all of the molecules in the expansion will overlap with the TEM₉₀ mode of the cavity and be probed by our spectrometer and that only 51.5% of the sample is \(^{12}\)C₆₀. If we use our work with pyrene, we have determined that only ~20% of the molecules in the expansion overlap with the TEM₉₀ mode of the ring-down cavity [13]. Because there is little expansion along the axis of the slit, we assume that \(L_{\text{jet}}\) equals the length of the slit (12.7 mm) and can find the number density of molecules probed by our spectrometer:

\[
N_{\text{probed}} = \frac{0.20 \times 0.515 \times N_{\text{C}_{60}}}{2\omega_0 \times L_{\text{slit}} \times v_{\text{max}}},
\]

where \(N_{\text{C}_{60}}\) is the rate of molecules lost from the oven per second, \(\omega_0\) is the beam waist of the TEM₉₀ mode, \(L_{\text{slit}}\) is the length of the slit, and \(v_{\text{max}}\) is the flow velocity of molecules in the expansion (for further details on the derivation of this expression, we refer readers to the supporting information for [13]). We estimate \(N_{\text{C}_{60}}\) by measuring the amount of C₆₀ before and after heating the sample and recording the length of time for which the expansion was on. \(\omega_0\) can be calculated from the radius of curvature of our ring-down mirrors, the length of the cavity, and the wavelength of light in the cavity [26]. For our setup, \(\omega_0\) is equal to 1.1 mm. \(v_{\text{max}}\) for the expansion can be found from the temperature and mass of carrier gas atoms in the expansion [27].

We can now use (1) to calculate our expected S/N for the slit expansion, using a 0.0004 cm⁻¹ (12 MHz) linewidth, which we have observed in slit expansions of methylene bromide and pyrene [13, 19]. Figure 2 displays the estimated S/N for the entire vibrational band for the measured mass loss at 955 K (2 g/hr) with the slit 6 mm from the cavity axis. The largest estimated S/N for a single rovibrational transition is ~130 (for the P(60), Q(60), and R(60) lines).

3. Results and Discussion

3.1. Search for the C₆₀ Spectrum. Our attempts to observe C₆₀ are summarized in Table I. We also attempted 6 spectroscopic searches for C₆₀ using a smaller oven with both a slit and pinhole expansion, which are discussed in detail in [28], but the work presented here represents our best attempts with a high calculated S/N and complete frequency coverage of where the band is expected to be. We decided to use a slit expansion because of the narrower linewidth of transitions and the greater vibrational cooling due to the larger number of collisions that occur in a slit expansion. Our attempts were performed at three different backing pressures and all three attempts covered the entire frequency region between 1184 and 1186 cm⁻¹ where we expect to observe the C₆₀ vibrational band. In all attempts a S/N > 70 was anticipated; however, we saw no evidence of absorption due to C₆₀ in any of these.
TABLE I: Summary of attempted absorption spectroscopy of C_{60}. The measured mass loss rate for each attempt was used to calculate S/N. The mass loss rates were 2.0 g/hr for attempts 1 and 2 and 0.7 g/hr for attempt 3. For all attempts, the supersonic expansion was probed 6 mm downstream from the exit of the slit.

<table>
<thead>
<tr>
<th>Attempt</th>
<th>T_{0} (K)</th>
<th>P_{0} (torr)</th>
<th>NEA (ppm)^{a}</th>
<th>Estimated S/N^b</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>955</td>
<td>150</td>
<td>1.0</td>
<td>130</td>
</tr>
<tr>
<td>2</td>
<td>955</td>
<td>500</td>
<td>0.9</td>
<td>140</td>
</tr>
<tr>
<td>3</td>
<td>965</td>
<td>1900</td>
<td>0.6</td>
<td>74</td>
</tr>
</tbody>
</table>

^aNEA: noise equivalent absorption.

^bThese values represent the largest S/N value for a single rovibrational transition at T_{rot} = 20 K and T_{vib} = 0 K following the analysis presented in Section 2.3.

As can be seen in Table I, the mass loss rate for our attempts decreased from attempts 1 and 2 to attempt 3, even though all three attempts were performed at approximately the same oven temperature. The same sample was used for attempt 3 after it had been used for attempts 1 and 2, and the reduced mass loss rate for attempt 3 is indicative of sample decomposition. We also observed that after attempt 3, our sample was no longer soluble in toluene and had become conductive, even though pure C_{60} is an insulator. Further characterization by CHN analysis revealed that the recovered sample was ~89% carbon by weight, with the elemental composition of the remaining mass as yet unknown. This implies that the actual mass of C_{60} lost over the course of attempts 1, 2, and 3 was higher than reported, but without elemental analysis between attempts we cannot say when this C_{60} mass loss occurred. Because of the decomposition of our sample, the reported S/N ratios in Table I represent average values for the expected S/N over the course of a scan, as the mass loss rate was decreasing as we were scanning our spectrometer.

The observed reduction in the mass loss of C_{60} from the source is consistent with prior reports in the literature. In a previous study on the thermal decomposition of C_{60}, Sundar et al. observed that C_{60} held at 975 K for an extended period of time (24 h) decomposed to amorphous carbon [29]. Other publications have also observed a similar reduction in vapor pressure over time when measuring the vapor pressure of C_{60} at elevated temperatures [15, 30, 31]. This effect has been attributed to residual solvent impurities of benzene, toluene, or hexane resulting from the HPLC separation of the raw fullerene sample produced by the carbon arc method [32]. Heating the impure sample above 750 K then results in a chemical transformation of C_{60} to a different substance, such as amorphous carbon, with a reduced vapor pressure.

3.2. High Temperature Measurements of D_{2}O. Because of the high temperatures involved in producing gas-phase C_{60}, we were concerned that the alignment of our optical cavity with our oven might be affected by thermal expansion or other heating effects. To eliminate this possibility, we observed absorption spectra of D_{2}O in expansions from our oven at similar temperatures as our C_{60} searches. There are many lines of the bending mode as well as a hot band within the spectral coverage of our spectrometer, which also allowed us to monitor the rotational and vibrational temperature of D_{2}O molecules in the high temperature supersonic expansion.

We introduced a small amount of D_{2}O into an Ar slit expansion and observed low-lying states which were populated in the expansion. We observed the 1_{11} ← 0_{00} transition of the (010) ← (000) band of D_{2}O at 1199.79 cm\(^{-1}\) with the oven at 875 K to determine if alignment effects could be responsible for failure to observe C_{60}. We were easily able to observe the line in the expansion, and placing the oven vertically only caused a slight change in the intensity of the line, consistent with the molecular distribution we measured with pyrene. This indicates that the extreme temperatures of our oven are not affecting the alignment of our ring-down cavity and preventing the observation of a C_{60} absorption signal.

Measuring several transitions of D_{2}O in the expansion from the hot oven permitted calculation of both the rotational and vibrational temperatures for D_{2}O. Table 2 presents a list of the transitions that we measured in the (010) ← (000) and (020) ← (010) vibrational bands of D_{2}O. Each line was measured 5 times and the average intensity for each line was used for all temperature calculations. Figure 4 shows a Boltzmann plot for both the fundamental and hot band transitions, showing that the rotational temperature of the D_{2}O molecules is ~20 K in both the ground and excited vibrational states. From this we see that even though the expansion originated in an oven at 875 K, the rotational degrees of freedom are cooled efficiently. On the other hand, the strength of the hot band lines is consistent with a vibrational temperature >1000 K. The hot vibrational temperature for D_{2}O is not surprising,
Table 2: List of observed D_{2}O transitions. Rotational levels are denoted in the usual way \( J_{K_{a},K_{c}} \). The listed frequencies are from \([11, 12]\).

<table>
<thead>
<tr>
<th>Vibrational band</th>
<th>Transition</th>
<th>Frequency (cm(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>(010) ← (000)</td>
<td>1_{11} ← 0_{00}</td>
<td>1199.793</td>
</tr>
<tr>
<td></td>
<td>2_{02} ← 1_{11}</td>
<td>1194.038</td>
</tr>
<tr>
<td></td>
<td>2_{11} ← 2_{02}</td>
<td>1193.255</td>
</tr>
<tr>
<td></td>
<td>3_{12} ← 3_{03}</td>
<td>1198.536</td>
</tr>
<tr>
<td>(020) ← (010)</td>
<td>1_{11} ← 0_{00}</td>
<td>1181.311</td>
</tr>
<tr>
<td></td>
<td>3_{13} ← 2_{02}</td>
<td>1199.154</td>
</tr>
<tr>
<td></td>
<td>2_{20} ← 2_{11}</td>
<td>1192.497</td>
</tr>
<tr>
<td></td>
<td>2_{21} ← 2_{12}</td>
<td>1199.690</td>
</tr>
<tr>
<td></td>
<td>4_{44} ← 3_{13}</td>
<td>1198.379</td>
</tr>
</tbody>
</table>

considering that the lowest energy vibration in the molecule lies at \(-1178 \text{ cm}^{-1}\). Even at an oven temperature of 875 K, this is almost twice the value of \( k_{B}T \) (608 cm\(^{-1}\) at 875 K), and vibrational modes with energies significantly higher than \( k_{B}T \) do not effectively relax to the ground vibrational state in a supersonic expansion \([33]\).

3.3. Vibrational Partition Function and Importance of Vibrational Cooling. From the material presented in Section 2.3 describing the method of calculating the experimental \( S/N \), we can see that if the \( C_{60} \) molecules are cooled vibrationally in the supersonic expansion, we would anticipate observing an absorption signal even if there is not a strong \( R \)-branch head or \( Q \)-branch. Therefore, the most likely explanation for our lack of observed signal is that we are not achieving sufficient vibrational cooling of \( C_{60} \). For us to observe absorption from the \( C_{60} \) molecules, they must be in the ground vibrational state. The fraction of molecules in the ground vibrational state (assuming a Boltzmann distribution) is given by the expression

\[
 f_{0} = \frac{e^{-E_{0}/(k_{B}T_{\text{vib}})}}{Q_{\text{vib}}},
\]  

(3)

where \( E_{0} \) is the energy of the ground vibrational state, \( T_{\text{vib}} \) is the vibrational temperature, and \( Q_{\text{vib}} \) is the vibrational partition function. If we express the vibrational energies relative to \( E_{0} = 0 \), (3) simply becomes the inverse of the partition function. Because \( C_{60} \) has 174 vibrational degrees of freedom, its vibrational partition function increases rapidly with increasing temperature (see Figure 1), meaning that very few molecules occupy the ground vibrational state at high temperatures. Even at a vibrational temperature as low as 190 K, only 1 in 10 \( C_{60} \) molecules will be in the ground vibrational state, leading to an order of magnitude decrease for an absorption signal. If we assume that the lack of vibrational cooling is the primary cause preventing us from observing \( C_{60} \), we can calculate a lower limit for \( T_{\text{vib}} \) in the expansion using our expected \( S/N \) and (3). Our expected signal is proportional to \( f_{0} \), so if our expected \( S/N \) is 140 (as in attempt 2 in Table 1), \( f_{0} \) must be decreased by at least a factor of 140 for us not to observe the signal. This means that \( Q_{\text{vib}} \) must be at least 140, which would correspond to \( T_{\text{vib}} = 250 \text{ K} \). It should be noted that this lower limit of 250 K assumes a Boltzmann distribution for the vibrational levels, which is likely not the case in a supersonic expansion.

Previous studies have shown that large molecules (specifically PAHs) can be effectively cooled in supersonic expansions \([14]\). Our own recent measurements of pyrene using the experimental setup described in this paper indicated that pyrene was cooled to \( T_{\text{vib}} = 23–111 \text{ K} \) \([13]\). It is useful to compare these previous studies with our current attempted spectroscopy to ascertain why we were unable to observe \( C_{60} \) absorption in our expansion.

Vibrational cooling of large molecules seeded in a supersonic expansion of a monatomic carrier gas proceeds by transferring vibrational energy from the large molecule to translational energy in the expansion by collisions with the carrier gas (V-T transfer). Because of this, the number of collisions that a molecule experiences in the supersonic expansion will have a significant effect on the amount of vibrational cooling that is possible in the expansion. We have estimated the number of two-body hard sphere collisions which occur in our attempted \( C_{60} \) spectroscopy and previous work on PAHs by our group \([13]\) and Amirav et al. \([14]\). The estimated number of collisions for our work and the work of Amirav et al. \([14]\) is found in Table 3. The details of our calculations are outlined in the following paragraphs.

The first step in estimating the number of collisions in a supersonic expansion is to describe the temperature, density, and velocity of molecules in the expansion. These properties...
Table 3: Estimated number of two body hard sphere collisions experienced by large molecules seeded in an argon supersonic expansion. The first three entries in the table are from the attempted C$_{60}$ spectroscopy reported in this work. The pyrene entry is from our previous work observing pyrene in the same experimental setup which we used to attempt C$_{60}$ spectroscopy [13]. The remaining entries are from laser induced fluorescence spectroscopy of the listed PAHs performed by Amirav et al. [14]. The listed pressures for the PAHs were sufficient to produce vibrationally cold molecules (T$_{PAH}$ ≲ 100 K). The C$_{60}$ and pyrene expansions used a 12.7 mm × 150 μm slit. For the work of Amirav et al. [14] all expansions used a 12.7mm diameter pinhole. Further details on how the number of collisions was calculated can be found in the article text.

<table>
<thead>
<tr>
<th>Molecule</th>
<th>$T_0$ (K)</th>
<th>$P_0$ (torr)</th>
<th>Nozzle type</th>
<th>Number of collisions</th>
</tr>
</thead>
<tbody>
<tr>
<td>C$_{60}$ (att. 1)</td>
<td>955</td>
<td>150</td>
<td>Slit</td>
<td>320</td>
</tr>
<tr>
<td>C$_{60}$ (att. 2)</td>
<td>955</td>
<td>500</td>
<td>Slit</td>
<td>1100</td>
</tr>
<tr>
<td>C$_{60}$ (att. 3)</td>
<td>965</td>
<td>1900</td>
<td>Slit</td>
<td>4000</td>
</tr>
<tr>
<td>Pyrene</td>
<td>430</td>
<td>150</td>
<td>Slit</td>
<td>560</td>
</tr>
<tr>
<td>Anthracene</td>
<td>410</td>
<td>270</td>
<td>Pinhole</td>
<td>600</td>
</tr>
<tr>
<td>Tetracene</td>
<td>485</td>
<td>175</td>
<td>Pinhole</td>
<td>360</td>
</tr>
<tr>
<td>Pentacene</td>
<td>550</td>
<td>250</td>
<td>Pinhole</td>
<td>500</td>
</tr>
<tr>
<td>Ovalene</td>
<td>630</td>
<td>300</td>
<td>Pinhole</td>
<td>620</td>
</tr>
</tbody>
</table>

Table 4: Hard sphere radii used to compute the mean free path of molecules in the supersonic expansion.

<table>
<thead>
<tr>
<th>Species</th>
<th>Radius (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ar</td>
<td>1.88</td>
</tr>
<tr>
<td>C$_{60}$</td>
<td>5.0</td>
</tr>
<tr>
<td>Pyrene</td>
<td>4.0</td>
</tr>
<tr>
<td>Anthracene</td>
<td>3.8</td>
</tr>
<tr>
<td>Tetracene</td>
<td>4.2</td>
</tr>
<tr>
<td>Pentacene</td>
<td>4.6</td>
</tr>
<tr>
<td>Ovalene</td>
<td>5.1</td>
</tr>
</tbody>
</table>

are given by the following equations for the centerline of the expansion, which are reproduced from [34]

$$T(z) = T_0 \left(1 + \frac{y_1 - \frac{1}{2} M^2}{M^2} \right)^{-1},$$

$$n(z) = n_0 \left(1 + \frac{y_1 - \frac{1}{2} M^2}{M^2} \right)^{-1/(y_1 - 1)},$$

$$s(z) = \sqrt{\frac{8 k_B T(z)}{\pi \mu}},$$

In these equations, $s(z)$ represents the distance from the nozzle along the centerline of the expansion, $T_0$ and $n_0$ are the temperature and number density of the gas prior to the expansion, $y$ is the heat capacity ratio (which is 5/3 for the argon expansion we consider here), $M$ is the Mach number of the expansion, and $m$ is the mass of the gas. Because the large molecule is only a minor constituent of the gas being expanded, we assume that the properties of the expansion can be approximated as that of a pure argon expansion. To use these equations, we also need to know the value of $M$ as a function of $z$; equations to do so for both slit and pinhole expansion sources are provided in [34].

The next step in calculating the number of collisions is to calculate the mean free path of the large molecules in the expansion. To do so, we use a hard sphere model, which gives the usual equation:

$$\lambda(z) = \frac{1}{\sqrt{2\pi(r_{large} + r_{Ar})^2 n(z)}},$$

where $\lambda(z)$ is the mean free path as a function of distance from the expansion nozzle and $r_{large}$ and $r_{Ar}$ are the hard sphere radii for the large molecule and argon atoms, respectively. Because C$_{60}$ is roughly a sphere, we can simply use the van der Waals radius of C$_{60}$ for $r_{large}$ in this equation, but the PAHs studied by us and Amirav et al. are far from spherical.

To get a rough approximation of a hard sphere radius for these species, we used values for the minimum and maximum projected cross-sections of the molecules as given in the chemicalize.org database from ChemAxon [35]. To obtain a hard sphere radius, we averaged the minimum and maximum projected cross-sections for the PAHs and then calculated an effective radius based on the average cross section of the molecule. While this is certainly not exact, it should give a rough estimate of the relative size of the PAHs for computing the mean free path and seems to give reasonable results. The hard sphere radii which we used to compute the mean free path are listed in Table 4.

We can then calculate the average frequency of two-body collisions of the large molecule with Ar atoms in the expansion by dividing the average speed of the molecules by the mean free path. We assume that the translational temperature of the large molecules is thermalized with the translational temperature of the Ar atoms and calculate the average speed according to

$$(6)$$

where $\mu$ is the reduced mass of the Ar and large molecule. Using the above equations, we can calculate the collision frequency at any point $z$ along the centerline of the expansion. We calculated the collision frequency in steps of 1.5 μm from $z = 0$ to 6 mm along the expansion for all of the molecules and conditions listed in Table 3. We then calculated the number of collisions at each point by calculating the velocity of the expansion to determine how long the molecules were within each 1.5 μm section and then multiplying that time by the collision frequency. We then added together the number of collisions calculated for each of these 1.5 μm sections from $z = 0$ to 6 mm to give the total number collisions listed in Table 3. We use a maximum of 6 mm because that is where the expansion was probed in our work and in the work of Amirav et al. [14].

From Table 3, we can see that the PAHs were vibrationally cooled after undergoing an average of 360–620 collisions with Ar. In our attempted C$_{60}$ spectroscopy, the C$_{60}$ molecules underwent an average of 320, 1100, and 4000 collisions with...
Table 5: Vibrational partition function, average vibrational energy (above zero-point energy) in cm$^{-1}$, frequency of the lowest energy vibrational mode, and energy to collision ratio for the molecules listed in Table 2 at the temperatures listed in that table. The calculated values for our D$_2$O measurements from Section 3.2 are also included for comparison.

<table>
<thead>
<tr>
<th>Molecule</th>
<th>$Q_{\text{vib}}$</th>
<th>$E_{\text{vib}}$ (cm$^{-1}$)</th>
<th>$\nu_{\text{min}}$ (cm$^{-1}$)</th>
<th>$E_{\text{vib}}$/collisions</th>
</tr>
</thead>
<tbody>
<tr>
<td>C$_{60}$ (att. 1)</td>
<td>$1.3 \times 10^{28}$</td>
<td>56000</td>
<td>267</td>
<td>174</td>
</tr>
<tr>
<td>C$_{60}$ (att. 2)</td>
<td>$1.3 \times 10^{28}$</td>
<td>56000</td>
<td>267</td>
<td>50</td>
</tr>
<tr>
<td>C$_{60}$ (att. 3)</td>
<td>$3.0 \times 10^{28}$</td>
<td>57000</td>
<td>267</td>
<td>14</td>
</tr>
<tr>
<td>Pyrene</td>
<td>$4.0 \times 10^3$</td>
<td>4000</td>
<td>99</td>
<td>7</td>
</tr>
<tr>
<td>Anthracene</td>
<td>$1.5 \times 10^3$</td>
<td>3200</td>
<td>91</td>
<td>5</td>
</tr>
<tr>
<td>Tetracene</td>
<td>$1.0 \times 10^6$</td>
<td>6400</td>
<td>56</td>
<td>18</td>
</tr>
<tr>
<td>Pentacene</td>
<td>$2.5 \times 10^6$</td>
<td>10000</td>
<td>38</td>
<td>21</td>
</tr>
<tr>
<td>Ovalene</td>
<td>$8.6 \times 10^{13}$</td>
<td>18000</td>
<td>61</td>
<td>29</td>
</tr>
<tr>
<td>D$_2$O</td>
<td>1.20</td>
<td>260</td>
<td>1178</td>
<td>0.8</td>
</tr>
</tbody>
</table>

Ar for attempts 1, 2, and 3 in Table 1, respectively. For attempts 1 and 2, the number of collisions is similar to the number of collisions for the PAH molecules, while the much higher backing pressure for attempt 3 increased the number of collisions by an order of magnitude compared to attempt 1. While the C$_{60}$ molecules underwent a similar number of collisions as the PAHs, or significantly more for attempt 3, we have seen that this was insufficient to produce vibrationally cold C$_{60}$, which would have been observable with our spectrometer. To try to understand why this might be the case, we can compare the vibrational properties of these molecules.

Theoretical harmonic vibrational frequencies for all of the PAHs listed in Table 3 can be found in the PAH IR Spectral Database [36], which come from the original data of Langhoff [37]. We have used these vibrational frequencies to calculate the vibrational partition functions of the PAHs and C$_{60}$ at high temperature before being cooled by supersonic expansion. Using the vibrational partition function, we can also calculate the amount of vibrational energy in an average molecule at high temperature. These values are presented in Table 5 for all of the molecules we have been considering. The first thing to notice is the incredibly large partition functions for these molecules at elevated temperatures, especially for C$_{60}$ and ovalene. According to (3), this means that on average only 1 in $10^{28}$ molecules of C$_{60}$ is in the ground vibrational state before the expansion. Table 5 also shows that these molecules have a large amount of vibrational energy (over 50000 cm$^{-1}$ for C$_{60}$) that must be transferred into the supersonic expansion to cool them vibrationally. For the PAHs, we have seen that it is possible to transfer this energy in the hundreds of collisions that occur in the expansion. We can divide the vibrational energies in Table 5 by the collision numbers in Table 3 to calculate an energy to collision ratio to get an idea of how much energy would need to be removed in an average collision to cool the molecule. This ratio is listed in the last column of Table 5. For the vibrationally cold PAH molecules, an average collision carried away 5–30 cm$^{-1}$ of energy. For our attempted C$_{60}$ spectroscopy, the energy to collision ratio is significantly higher than this for attempt 1, slightly higher for attempt 2, and right in the range of the PAHs for attempt 3.

Looking at these values, it is somewhat surprising that C$_{60}$ was not efficiently cooled using a supersonic expansion for attempts 2 and 3. Considering the previous work with PAHs, it appears that there should be enough collisions to carry away the vibrational energy for these attempts. One possible reason why C$_{60}$ was not efficiently cooled is that the lowest energy vibrational mode for C$_{60}$ is at 267 cm$^{-1}$, which is significantly higher than the lowest modes for the PAHs (see Table 5). To completely cool the molecule to the ground vibrational state, energy must be transferred from the lowest vibrational mode into translational energy. The efficiency of V-T transfer decreases as the energy gap increases, making it more difficult for modes with higher energy to be completely cooled. As an extreme example of this, we can consider the D$_2$O spectroscopy presented in Section 3.2. We have calculated the vibrational properties for D$_2$O following the same procedure as for C$_{60}$ and the PAHs, using vibrational frequencies from [38]. The results are listed in Table 5 and show that the amount of vibrational energy for a small molecule at high temperature is much lower than the large molecules we have been considering. At a temperature of 875 K and a backing pressure of ~300 torr, the average number of hard sphere collisions for a D$_2$O molecule in the expansion is 310 (using a hard sphere radius of 1.6 Å), which gives an energy to collision ratio of 0.8. Even though this ratio is significantly lower than for all of the PAHs, we observed substantial population in the (010) state, indicating no cooling of this vibrational mode. This lack of cooling is a direct consequence of the fact that the lowest energy mode lies so high in energy.

Another possibility is that the extremely large size of C$_{60}$ is causing a significant velocity slip effect to occur because of the large difference in mass between the C$_{60}$ molecules and the Ar carrier gas [14]. While this does not seem to be a problem for the previous work on ovalene, C$_{60}$ is about 2 times heavier than ovalene. This problem would be easily remedied by using a heavier carrier gas such as Kr or Xe, which would more closely match the mass of C$_{60}$. We did not try a heavier gas because of the increased cost of these gases compared to Ar, especially when used continuously, as in our experiment. For future attempts to observe C$_{60}$, it may be worth the extra expense to try the heavier rare gases to reduce the velocity slip effect.

Finally, it is worth noting that other molecules have been observed to have anomalously low cooling efficiency in supersonic expansions. In particular, Sulkes observed that benzene
displays a lack of collision-induced vibrational relaxation in He and Ar expansions, despite the fact that substituted benzene derivatives showed excellent cooling under similar conditions [39]. Sulkes attributed this to a lack of efficient cooling via orbiting resonances; it is conceivable that a similar effect is occurring with C\textsubscript{60}.

3.4. Alternative Methods for Producing Gas-Phase C\textsubscript{60}. It would be preferable to produce C\textsubscript{60} vapor at a much lower temperature than is possible in our oven. Doing so would significantly decrease the vibrational partition function and vibrational energy of the molecules prior to the supersonic expansion. For example, if C\textsubscript{60} vapor could be produced at a temperature similar to our pyrene work (430 K), then the vibrational partition function would be only $5 \times 10^{-7}$ and an average molecule would only have 11000 cm\textsuperscript{-1} of vibrational energy, which would be quite similar to the PAHs that were observed by Amirav et al. This should make it much easier to cool the C\textsubscript{60} molecules to the ground vibrational state.

We are aware of three possible methods for producing C\textsubscript{60} vapor at lower temperatures: supercritical fluid expansion, laser desorption, and collisional cooling in the gas-phase. In the supercritical fluid expansion method the C\textsubscript{60} sample would be dissolved in a supercritical fluid. It has been demonstrated that C\textsubscript{60} can be dissolved in supercritical toluene, or to a lesser extent in supercritical carbon dioxide containing toluene as a co-solvent [40, 41]. Assuming a 1:1 volume ratio of CO\textsubscript{2} to toluene, the critical temperature is $\sim$450 K. Decreasing the toluene content will lower the critical temperature, though this would be at the expense of solubility. It will be necessary to optimize the toluene content for our particular needs. We would likely employ an argon sheath-flow continuous expansion source, as in [42].

A laser desorption/supersonic expansion source has been successfully employed for resonant two-photon ionization measurements of C\textsubscript{60} [43, 44], but the vibrational temperature of the vapor produced was not directly observed. Likewise, while it has been shown that laser desorption can volatilize large molecules with pre-expansion vibrational temperatures below what one would expect for thermal vaporization [45, 46], the temperatures achievable are molecule- and surface-dependent and as yet unknown for C\textsubscript{60}. As such, the viability of a laser desorption source is difficult to assess without further experiments.

The final method to discuss for producing cold gas-phase C\textsubscript{60} relies upon the modified use of a gas-phase aggregation cluster source [47] to collisionally cool isolated C\textsubscript{60} molecules. In an aggregation source the hot vapor from the heated sample is entrained in a flow of noble gas that is cooled by collisions with the walls inside the source that are kept at 77 K using liquid nitrogen cooling [48, 49]. A collimated molecular beam of cold sample clusters is produced by passing the flow out of the source through a nozzle. While normally such sources are used to efficiently produce large clusters of molecules or atoms, it has been shown that cold isolated C\textsubscript{60} molecules can be produced by keeping the gas-phase number density of C\textsubscript{60} low through reduction of the temperature of the sample oven [47]. By operating the aggregation source in this way it was possible to collect two-photon resonant ionization spectra of C\textsubscript{60} with an estimated vibrational temperature <80 K [47].

Although we expect all of the proposed methods to be superior to our current oven in terms of vibrational temperature, we also expect them to produce significantly lower number densities of gas-phase C\textsubscript{60}. Based on reports of supercritical fluid extractions of C\textsubscript{60} [40, 41], we anticipate that the number density produced by a supercritical fluid expansion would be two orders of magnitude lower than that of our current oven. Studies where laser desorption [43, 44] or collisional cooling [47] was used do not report gas-phase C\textsubscript{60} number densities; however, the C\textsubscript{60} number densities generated using these methods will be considerably lower than the number density produced using a supercritical fluid. Assuming that C\textsubscript{60} can be efficiently cooled in a supercritical fluid expansion, we will need to implement high repetition rate CRDS [50] to account for the low C\textsubscript{60} number density. Depending on the repetition rate achieved, doing so would improve S/N by a factor of 10–20. If C\textsubscript{60} does not cool completely or the number density is lower than anticipated, noise-immune cavity-enhanced optical heterodyne molecular spectroscopy (NICE-OHMS) detection could be implemented instead, improving our signal-to-noise ratio by as much as three orders of magnitude [51]. This route would also significantly increase the technical complexity of our spectrometer.

4. Conclusions

Obtaining a high-resolution gas-phase spectrum of C\textsubscript{60} represents a significant challenge for molecular spectroscopy. We have attempted to obtain such a spectrum using a highly sensitive cw-CRDS spectrometer but were unable to detect any absorption signal from C\textsubscript{60}. We have shown that an absorption signal should be expected with our current experimental setup if we are able to vibrationally cool C\textsubscript{60}. Our lack of signal is most likely due to the fact that we must heat our sample to >950 K to obtain sufficient vapor pressure for spectroscopy, which leads to an incredibly large vibrational partition function because of the large size of C\textsubscript{60}. We have compared these results with previous work that has shown efficient vibrational cooling of large polycyclic aromatic hydrocarbons. To overcome this problem it will be necessary to produce gas-phase C\textsubscript{60} at much lower temperatures so that the vibrational degrees of freedom can be cooled. While there may exist alternative methods that are capable of generating a cold gas-phase sample, these methods will result in low number densities of C\textsubscript{60}. The low C\textsubscript{60} number density will require the use of more sensitive and complex absorption spectroscopy techniques than cw-CRDS to enable collection of a rotationally resolved spectrum.

Conflict of Interests

The authors have no direct financial relations with the commercial identities named in this work.
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