Thermal Conductivity of Uranium Nitride and Carbide

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We investigate the electronic thermal conductivity of alternative fuels like uranium nitride and uranium carbide. We evaluate the electronic contribution to the thermal conductivity, by combining first-principles quantum-mechanical calculations with semiclassical correlations. The electronic structure of UN and UC was calculated using Quantum Espresso code. The spin polarized calculations were performed for a ferromagnetic and antiferromagnetic ordering of magnetic moments on uranium lattice and magnetic moment in UC was lower than in UN due to stronger hybridization between 2p electrons of carbon and 5f electrons of uranium. The nonmagnetic electronic structure calculations were used as an input to BolzTrap code that was used to evaluate the electronic thermal conductivity. It is predicted that the thermal conductivity should increase with the temperature increase, but to get a quantitative agreement with the experiment at higher temperatures the interaction of electrons with phonons (and electron-electron scattering) needs to be included.

1. Introduction

The recent tragic accident in Fukushima clearly illustrates the risks associated with the present design of reactors based on uranium dioxide (UO₂) fuel and justifies research towards a safer fuel. Pioro et al. [1] demonstrate that the traditional urania fuel is not suitable for some designs of new generation reactors due to its low thermal conductivity (e.g., the estimated fuel centerline temperature for super critical water reactor (SCWR) surpasses the industry accepted limit of 1850 °C (2123 K). Uranium nitride (UN) and uranium carbide (UC) have been proposed as possible safer fuels. UC and UN are advanced types of nuclear fuel since they have not only higher thermal conductivity but also lower linear expansion coefficients and are more compatible with fuel cladding materials [2].

The thermal conductivity of UN is compared with UO₂ in [3]. The researchers show that in contrast to a typical ceramic (e.g., UO₂) the thermal conductivity of UN increases with temperature due to a large electronic transport. Additionally, UN melting temperature increases with pressure, which prevents dissociation of nitrogen gas and can be as high as 3035 K at 1 atm [3].

UC also has an advantage over UO₂ as a fuel for fast reactors due to about 2.6 times higher thermal conductivity [2, 3]. The melting temperature of UC is slightly lower (~2623 K [4], 2638 (165) K–2780 (25) K [2]) but still well above 2000 K.

We present here preliminary studies of the thermal conductivity of these advanced types of nuclear fuel.

2. Electronic Structure

To evaluate the electronic structure of UN and UC, we use Quantum Espresso (QE) code [5] (see Appendix) as there is already an interface provided between QE and Boltzmann Transport Properties (BoltzTraP) code [6] that will be used here to evaluate electronic transport.

The electronic structure of UC and UN has been studied before (see, e.g., [7, 8]) and researchers note that neither local density approximation (LDA) nor LDA with Hubbard U corrections is able to adequately describe its electronic structure around Fermi energy that is dominated by strongly correlated 5f electrons of uranium with antiferromagnetic ordering. However, in spite of the noted deficiencies, many
properties can be evaluated in agreement with the experiment, for example, phonon dispersion [8].

2.1. Uranium Nitride. Similar to urania, UN has a cubic structure ($Fm\bar{3}m$ symmetry). At low temperatures (below Néel temperature $T_N = 53$ K [9]) it shows ferromagnetic (001) planes coupled antiferromagnetically (type-I structure) [9]. We have discussed previously [10] that the calculated lattice constants for ferromagnetic urania agree very well with the experiment while for antiferromagnetic ordering very close values of the lattice constants were found but with unphysical, slightly tetragonal distortion. It is much easier to optimize the geometry of ferromagnetic UN due to a smaller size of the primitive unit cell. Using Quantum Espresso code [5] and generalized gradient approximation PBE (Perdew, Burke, and Ernzerhof) functional [11], we have found the equilibrium lattice constant for ferromagnetic UN to be 5.24 Å, which is larger than the experimental value of 4.89 Å [9] since PBE overestimates values of lattice constants.

The used norm conserved potentials provided with Quantum Espresso code (pbe-mt.fhi.UPF) may also lead to a larger lattice constant. 300 Ry cut-off energy and $16 \times 16 \times 16$ $k$ points mesh in the Brillouin zone were applied. Our tests show that changing cut-off energy up to 75 Ry and changing grid up to $10 \times 10 \times 10$ have not affected the lattice constant.

Next we performed a band structure calculation for antiferromagnetic and nonmagnetic UN using conventional unit cells (with 5.24 Å lattice constant) and no symmetry. We used 150 Ry cut-off energy and the Monkhorst-Pack [12] $16 \times 16 \times 16$ grid to calculate the electron band structure suitable as an input to BoltzTraP (BoltzmannTransportProperties) code [6]. This code uses smoothed Fourier interpolation of the electron band structure, which is used to calculate the electron density of states and semiclassical transport coefficients [6]. In Figure 1 the derived electron densities of states (black, solid lines) and their integrals over energy (dashed red lines) are shown for antiferromagnetic (a) and nonmagnetic (b) UN, respectively. These electron densities of state compare well with the one calculated by QE code (Figure 5) presented.
in Appendix. In the nonmagnetic calculations one broad peak originating from 5f electrons is visible (b) near the Fermi energy, which splits into two peaks (as discussed in Appendix) for antiferromagnetic ordering (a).

2.2. Uranium Carbide. Next, we performed electronic structure calculations for UC using QE code as described in detail for UN. The same setup of parameters was used. UC has the same crystal structure as UN and we found, similar to UN, the equilibrium lattice constant of 5.26 Å to be larger than the experimental one of 4.958 Å [13]. We also used here norm conserved potentials (pbe-mt.fhi.UPF) provided with Quantum Espresso code. In Figure 2, the electron densities of states of UC used in BolzTrap code are shown and they compare well with the original densities (Figure 6) obtained by QE code. Similar to UN we see the 5f electrons of uranium around Fermi energy although the energy of 2p electrons of carbon is about 0.1 Ry higher than the respective energy of 2p electrons of nitrogen in UN (Figure 1).

3. Thermal Conductivity

The origin of the high thermal conductivity of UC and UN has been investigated previously. The review [14] of experimental data indicates that the thermal conductivity of UC above 1000°C (1273 K) is 100% electronic. In [3], the authors state that at temperatures ranging between 300 K and 2000 K, energy transport of UN is controlled by lattice vibrations (phonons) while at higher temperatures there is significant contribution from conductive electrons. This is in contrast to the other analysis [7, 8] indicating a large electronic contribution to transport above 1000 K and below. Yin et al. have evaluated [8] that the phonon contribution to the thermal conductivity of UN at 1000 K is only 4.4 W m⁻¹ K⁻¹ and in UC 2.7 W m⁻¹ K⁻¹ versus the electronic contributions of 12.1 W m⁻¹ K⁻¹ and 16 W m⁻¹ K⁻¹, respectively. Researchers have found the electronic contribution to thermal conductivity comparable to phonon transport in UN even below room temperature [7], as we discuss below.

In this work we evaluate only the electronic contribution to the thermal conductivity of UN and UC. The electronic structures of nonmagnetic UN and UC, presented in Section 2, are used in the calculations performed using BolzTrap code for the temperatures between 50 K and melting point.

Figure 3: The calculations for thermal conductivity of electronic origin in UN as a function of temperature are shown for nonmagnetic UN with (short, black, dashed line) and without (black solid line) correction for nonresidual resistivity. The previously estimated phonon contribution to the thermal conductivity at 1000 K [8] is indicated by a pink diamond and at lower temperatures by a pink dashed line [7] and the electron contribution at 1000 K [8] is indicated by a green square. The dotted line indicates the phonon contribution evaluated by the linear interpolation between the estimates from [7, 8]. The electronic contribution, calculated from the experimental resistivity [7], is shown by blue triangles. The measured total thermal conductivity is indicated by the long, red, dashed line [3] and black spheres [16].

Figure 4: The calculations for thermal conductivity of electronic origin in UC as a function of temperature are shown for nonmagnetic UC with (short, black, dashed line) and without (black solid line) correction for nonresidual resistivity. The recommended experimental data for the total thermal conductivity (red squares) and the electronic contribution (blue triangles) to the thermal conductivity [14] are shown. The electron and phonon contributions to the thermal conductivity at 1000 K, evaluated in [8], are indicated by a green square and a pink diamond, respectively.
Figure 5: The calculated by QE code the total electron density of states of UN for: (a) ferromagnetic (black, solid line for majority and dashed for minority spins), (b) antiferromagnetic ordering (note identical total majority and minority spin density) and (c) nonmagnetic UN (sum of the density of states of spin up and down electrons plotted by solid line) and conventional unit cell. The densities of states of $5f$ electrons of uranium are shown by red solid line and blue dashed line for majority and minority spin on Figures 5(a) and 5(b) and its sum on Figure 5(c).

3.1. Uranium Nitride. In BoltzTraP code it is assumed that the electron relaxation time is isotropic and constant, which is true at lower temperatures where residual resistivity is dominant. We evaluated the relaxation time ($\tau = 4.98 \times 10^{-15}$ s) using the electronic conductivity, $\sigma/\tau$ equal to $1.18875 \times 10^{20}$ $\Omega^{-1}$ $m^{-1}$ $s^{-1}$ calculated by BoltzTraP (for nonmagnetic UN) at 300 K, and the measured resistivity at the same temperature $16.9 \times 10^{-7}$ $\Omega m$ [7]. However, since the non-residual resistivity, neglected in BoltzTraP, increases linearly with temperature, it becomes important at high temperatures. Interestingly, the previous analysis [8] indicates that in UN approximately 80% of $\rho(T)$ originates from electron-electron scattering, in contrast to UC where electron-phonon scattering dominates. We evaluated this contribution for UN from the experimental resistivity slope between 300 K and 1100 K [15]. We found it to be equal to $\Delta_{\rho} = 0.4789 \times 10^{-9}$ $(T(K) - 300 K)$ $\Omega m$. In Figure 3 we present the calculated electronic contributions to the thermal conductivity ($\kappa_e$) of nonmagnetic UN using constant relaxation time, as derived above (black, solid line), and the results with $\Delta_{\rho}$ correction (short, dashed, black line). The electronic contribution to the thermal conductivities was calculated via Wiedemann-Franz law from the electronic conductivities ($\sigma$) calculated by BoltzTraP code as follows:

$$\kappa_e = \frac{\pi}{3} \left( \frac{k_B}{e} \right)^2 \sigma T,$$

where $k_B$ is Boltzmann constant, $e$ is electron charge, and $T$ is the temperature in K.

The previously estimated electronic thermal conductivity at low temperatures [7], shown by blue triangles in Figure 3, is in very good agreement with the values calculated here for nonmagnetic UN and is above Néel temperature (51 K). The phonons’ contribution to the thermal conductivity (indicated by dashed and dotted pink lines) decreases with temperature [7] and therefore around 1500 K of our estimate of the electronic contribution to the thermal conductivity of nonmagnetic UN (black solid line) agrees well with the measured
The calculated by QE code the total electron density of states of UC for: (a) ferromagnetic (black, solid line for majority and dashed for minority spins), (b) antiferromagnetic ordering (note identical total majority and minority spin density) and (c) nonmagnetic UC (sum of the density of states of spin up and down electrons plotted by solid line) and conventional unit cell. The densities of states of 5f electrons of uranium are shown by red solid line and blue dashed line for majority and minority spin on Figures 6(a) and 6(b) and its sum on Figure 6(c).

There is, however, disagreement between experimental data for resistivity (e.g., at 300 K resistivity: $16.9 \times 10^{-7} \Omega m$ [7] versus $14.8 \times 10^{-7} \Omega m$ [15]) and thermal conductivity, as shown in Figure 3 (e.g., around 1500 K, conductivity: $22 \text{ W m}^{-1} \text{K}^{-1}$ [16] versus $26 \text{ W m}^{-1} \text{K}^{-1}$ [3]). The band structure of uranium 5f electrons is also not very well represented within DFT, as discussed before [8]. However, our calculations reproduce very well the trend in the thermal conductivity of UN to increase with temperature.

3.2. Uranium Carbide. The relaxation time of UC ($\tau = 5.79 \times 10^{-15}$ s) was evaluated using the experimental value of resistivity $13.4 \times 10^{-7} \Omega m$ [14] at 1000 K and the electronic conductivity, $\sigma/\tau$ equal to $1.2886 \times 10^{20} \Omega^{-1} \text{m}^{-1} \text{s}^{-1}$, calculated by BoltzTraP (for nonmagnetic UC) at the same temperature. As with UN, we evaluated the nonresidual contribution to the resistivity of UC from the experimental resistivity slope between 298 K and 1773 K [14]. We used this correction above 1000 K and found the slope two times steeper than in UN and the correction equal to $\Delta \rho = 0.1079 \times 10^{-8}(T(\text{K}) - 1000) \Omega m$.

In Figure 4, we show by solid line the electronic contribution to the thermal conductivities calculated via Wiedemann-Franz law (I) from the electronic conductivities as a function of temperature. The electronic conductivities were derived using BoltzTraP. The relaxation time evaluated above was used. The recommended experimental data for both the total thermal conductivity (red squares) and the electronic contribution (blue triangles) to the thermal conductivity...
show very little variation with temperature, which is in disagreement with the calculation.

However, when the correction for electron-phonon interaction is taken into account (broken, black line) above 1000 K, a very good agreement with experiment is obtained. The previously [8] calculated electron and phonon contributions to the thermal conductivity of UC at 1000 K is indicated by green square and pink diamond, respectively, and predict slightly lower the total thermal conductivity of UC (18.7 W m\(^{-1}\) K\(^{-1}\)) than experiment (21.3 W m\(^{-1}\) K\(^{-1}\)) [14]. The estimated in [8] electron contribution to the thermal conductivity: 16 W m\(^{-1}\) K\(^{-1}\) is also lower than calculated here: \(\kappa_e = 18.2\) W m\(^{-1}\) K\(^{-1}\). Our analysis confirms that in evaluation of the thermal conductivity of UC, the effect of phonons needs to be taken into account.

### 4. Summary

We demonstrate that, by combining first-principles quantum-mechanical calculations with classical correlations, it is possible to predict the thermal conductivity of UN and UC in qualitative agreement with experiment.

The electronic structure was calculated using Quantum Espresso code. BoltzTrap code was used to evaluate electronic conductivity for nonmagnetic UN and UC, which was used to estimate the electronic contribution to the thermal conductivities via Wiedemann-Franz law. The relaxation time was derived using the experimental values of resistivity.

The metallic fuels like UN and UC show high electronic contribution to thermal conductivity, which increases with temperature and therefore makes them more suitable as fuels for some new generation reactors, as, for example, SCWR and fast reactors.

### Appendix

In this section the electronic densities of states as calculated by QE code [5] are presented. Similar to our earlier work on uranium oxides [10, 17], spin polarized and nonspin polarized calculations were performed without spin orbital effect included. As described in Section 2 the ferromagnetic ordering on U lattice was assumed to evaluate the equilibrium lattice constants of UN and UC at 0 K, and therefore primitive unit cell could be used (with only two atoms) during geometry optimization calculations. In Figures 5 and 6, the calculated densities of states are shown using the respective equilibrium lattice constants: 5.24 Å (UN) and 5.26 Å (UC). The presented here densities of states were calculated using PBE functional [11]. We used 150 Ry cut-off energy and the dense Monkhorst-Pack [12] \(16 \times 16 \times 16\) grid for higher accuracy. Figures 5(a) and 5(b) and Figures 6(a) and 6(b) represent spin polarized calculation for ferromagnetic and antiferromagnetic ordering on U lattice, while Figures 5(c) and 6(c) are for nonmagnetic UN and UC, respectively.

The presented here on Figures 5 and 6 electron densities of states as obtained by QE code agree very well with that derived by BoltzTrap code and shown on Figures 1 and 2. In Figures 5 and 6 the calculations for ferromagnetic ordering are shown additionally. The minority spin density of states is represented by broken line, while majority electron spin density is shown by solid line.

The density of states per one U atom of spin-up and -down 5f electrons is indicated by red and blue lines and it can be easily confirmed that the broad peak around the Fermi energy of the total density of states (plotted for the conventional unit cell and containing four U atoms) originates from its majority spin electron density. The same is true for antiferromagnetic ordering (Figures 5(b) and 6(b)).

As discussed before for UO\(_2\) [10] there is a big similarity between antiferromagnetic and ferromagnetic densities of states of uranium compounds.

In Figures 5(c) and 6(c) the electron densities are shown for nonmagnetic UC and UN. It can be confirmed that there is only one broad peak near the Fermi energy that originates from 5f electrons of U atoms. The peak in the density of states at lower energy originates predominantly from 2p electrons of N and C atoms as indicated. However there is also smaller contribution from 5f and 6d electrons of U, which is larger for UC due to a stronger hybridization with 2p electrons of carbon.

Although only the non-spin-polarised calculations are used for thermal conductivity calculations (see Section 3) for completeness, we are presenting here also the details on the polarization calculated using QE code. Similar to our earlier work on UO\(_2\) [10], polarization on uranium atoms in UC and UN is evaluated in Table 1 and compared for ferromagnetic (FM) and antiferromagnetic ordering (AFM). The calculations for UC and UN were done using PBE functional [11] and QE code [5]. Löwdin [18] method was used to extract presented in Table 1 magnetic moments. Additionally for comparison we present the predicted local moments on uranium by CASTEP code using local spin density with Hubbard U correction [10] (3.5 eV for UO\(_2\) [10, 17] and 4.5 eV for UX compounds) and Mulliken [19] and Hirshfeld [20] analysis.

As discussed in [7] the distance U-U in UX compounds is large and therefore the calculated here local magnetic moments should be compared to the evaluated experimentally effective moment from susceptibility equal to \(\sim 2.66\mu_B\). This value compares well with the calculated values presented in Table 1 for UN and UC for both ferromagnetic (FM) and antiferromagnetic ordering (AFM). Both QE and CASTEP predict lower moment in UC that can be explained by

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discussed above stronger hybridization between 2p electrons of carbon and 5f electrons of uranium.

**Conflict of Interests**
The authors declare that there is no conflict of interests regarding the publication of this paper.

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