We consider the parameter estimation in two seemingly unrelated regression systems. To overcome the multicollinearity, we propose a Liu-type estimator in seemingly unrelated regression systems. The superiority of the new estimator over the classic estimator in the mean square error is discussed and we also discuss the admissibility of the Liu-type estimator.

1. Introduction

Consider the following two seemingly unrelated regressions (SUR):

\[
\begin{align*}
Y_1 &= X_1 \beta_1 + \epsilon_1, \\
Y_2 &= X_2 \beta_2 + \epsilon_2,
\end{align*}
\]

where \(Y_i\) (\(i = 1, 2\)) are \(n \times 1\) vectors of observations, \(X_i\) (\(i = 1, 2\)) are \(n \times p\) matrices with full column rank, \(\beta_i\) (\(i = 1, 2\)) are \(p \times 1\) vectors of unknown regression parameters, \(\epsilon_i\) (\(i = 1, 2\)) are \(n \times 1\) vectors of error variables, and

\[
E(\epsilon_i) = 0, \quad \text{Cov}(\epsilon_i, \epsilon_j) = \sigma_{ij} I_n, \quad i, j = 1, 2,
\]

where \(V = (\sigma_{ij})\) is a \(2 \times 2\) positive definite matrix. This system has been used in many fields, such as social biological sciences and econometrics. Zellner [1, 2] firstly defined this system and later it was discussed by many researchers, such as Wang et al. [3], Roozbeh et al. [4], and Singh et al. [5].

For system (1), when \(\sigma_{12} = 0\), we can get the estimator of \(\beta\) as follows:

\[
\hat{\beta} = \begin{pmatrix} \hat{\beta}_1 \\ \hat{\beta}_2 \end{pmatrix} = \begin{pmatrix} (X_1'X_1)^{-1}X_1'Y_1 \\ (X_2'X_2)^{-1}X_2'Y_2 \end{pmatrix}.
\]

When the error vector is related, the estimator \(\hat{\beta}\) may not fully use the information of the parameter. How to use the information to improve the \(\hat{\beta}\) is a problem. Revankar [6] and Srivastava and Giles [7] have discussed this problem. Wang [8] uses the covariance-improve method to estimate the parameter in two seemingly unrelated regressions. With the prior information, Wang [8] proposes the covariance-improve estimator of \(\beta_1\) and \(\beta_2\):

\[
\tilde{\beta}_1 = (X_1'X_1)^{-1}X_1'Y_1 - \frac{\sigma_{12}}{\sigma_{22}} (X_1'X_1)^{-1}X_1'N_2Y_2,
\]

\[
\tilde{\beta}_2 = (X_2'X_2)^{-1}X_2'Y_2 - \frac{\sigma_{12}}{\sigma_{11}} (X_2'X_2)^{-1}X_2'N_1Y_1,
\]

where \(N_i = I - P_i\), \(P_j = X_j'X_j'^{-1}X_j'\), \(j = 1, 2\).

When the design matrix \(X_i\) is ill-conditioned, the estimator \(\tilde{\beta}_i\), \(i = 1, 2\) is no longer a good estimator. Many researchers have discussed this problem. One method to overcome this problem is to consider biased estimator, such as Liu and Wang [9] introduce the ridge estimator, Liu [10] proposes the principal regression component estimator, Qiu [11] proposes the classic \(c - k\) type estimator, and Roozbeh et al. [12] introduce the ridge estimator.

In this paper, we propose a Liu-type estimator to overcome the multicollinearity in the two seemingly unrelated regressions. Then we discuss the superiority of the Liu-type
estimator over the covariance-improve estimator in the mean square error criterion, and we also discuss the selection of the parameter in the proposed estimator. Since the estimator of \( \hat{\beta}_2 \) is similar to the estimator of \( \hat{\beta}_1 \), so in this paper, we only discuss the estimator of \( \hat{\beta}_1 \).

The rest of the paper is organized as follows. The Liu-type estimator is given in Section 2 and the properties of the new estimator under the mean square error criterion are discussed in Section 3. The admissibility of the proposed estimator is studied in Section 4 and some conclusion remarks are given in Section 5.

2. The Proposed Estimator

In this section, we use the prior information to obtain the Liu-type estimator. Firstly, we give a lemma.

By Lemma 1, when \( V \) is known, we establish a new estimator for \( \hat{\beta}_1 \):

\[
\tilde{\beta}_1(k, d) = \tilde{\beta}_1(k, d) - \frac{\sigma_{12}}{\sigma_{22}}(X'_1X_1 + kI)^{-1}X'_1Y_2
\]

\[
\times (X'_1X_1 + dI)(X'_1X_1)^{-1}X'_1Z_2(Z'_2Z_2)^{-1}X'_2Y_2
\]

\[
= (X'_1X_1 + kI)^{-1}X'_1X_1 + dI)(X'_1X_1)^{-1}X'_1Y_1
\]

\[
- \frac{\sigma_{12}}{\sigma_{22}}(X'_1X_1 + kI)^{-1}(X'_1X_1 + dI)
\]

\[
\times (X'_1X_1)^{-1}X'_1N_2Y_2,
\]

(8)

where \( \tilde{\beta}_1(k, d) = (X'_1X_1 + kI)^{-1}(X'_1X_1 + dI)X'_1Y_1 \) is the estimator for the single model in (1), \( k > 0, 0 < d < 1, d < k, N_2 = I - P_2, \) and \( P_2 = X_2(X'_2X_2)^{-1}X_2 \). We call this estimator as Liu-type estimator in SUR model. By the definition of the Liu-type estimator, it is easy to know that it is a general estimator which includes the covariance-improve estimator proposed by Wang [8] and the ridge estimator proposed by Liu [10] as special cases.

(1) When \( d = 0 \), then

\[
\tilde{\beta}_1(k, d) = \tilde{\beta}_1 = (X'_1X_1)^{-1}X'_1Y_1 - \frac{\sigma_{12}}{\sigma_{22}}(X'_1X_1)^{-1}X'_1N_2Y_2.
\]

(9)

(2) When \( d = 1 \), then

\[
\tilde{\beta}_1(k, d) = \tilde{\beta}_1(k)
\]

\[
= (X'_1X_1 + kI)^{-1}X'_1Y_1
\]

\[
- \frac{\sigma_{12}}{\sigma_{22}}(X'_1X_1 + kI)^{-1}X'_1N_2Y_2.
\]

(10)

Lemma 1 (see [10]). Let \( \hat{\theta} \) be an estimator of \( \theta \), \( \hat{\theta} \) the prior information with \( E(\hat{\theta}) = 0 \), and

\[
\text{Cov}(\hat{\theta}) = \begin{pmatrix}
V_{11} & V_{12} \\
V_{12} & V_{22}
\end{pmatrix}.
\]

(5)

Then in the estimator \( \Lambda = \{\theta^*(X) = \hat{\theta} + X\hat{\theta}\} \), the estimator \( \theta^* = \hat{\theta} - V_{12}V_{22}^{-1}\hat{\theta} \) has minimum mean square error and

\[
\text{MSE}(\theta^*) = \text{MSE}(\hat{\theta}) - \text{tr}(V_{12}V_{22}^{-1}V_{12}).
\]

(6)

Now we establish the Liu-type estimator in SUR model. Set \( Z_2 \) satisfy \( X'_1Z_2 = 0 \) and \( X_2 \) has the max column full rank; then \( E(Z'_2Y_2) = 0 \) and

3. MSE: The Superiority of the New Estimator over the Covariance-Improve Estimator

In this section, we discuss the statistical properties of the new estimator \( \tilde{\beta}(k, d) \). Firstly, we give the definition of the mean square error (MSE).

Let \( b^* \) be an estimator of \( \beta \); the MSE of \( b^* \) is defined as

\[
\text{MSE}(b^*, \beta) = E[(b^* - \beta)^T(b^* - \beta)]
\]

\[
= \text{tr}(\text{Cov}(b^*)) + (\text{bias}(b^*))^T(\text{bias}(b^*)),
\]

(11)

where \( \text{bias}(b^*) = E(b^*) - \beta \).

In the following theorem, we give the superior properties of the new estimator over the covariance-improve estimator in the mean square error.

Theorem 2. For the SUR model (1), when \( V \) is known,

(a) when \( 0 < d < 1 \) fixed,

(1) if \( \sigma_{12}(1/\lambda_1 - \rho_{12}^2(a_{ij}/\lambda_1^2)) - \alpha_2^2 \geq 0 \), then

MSE(\( \tilde{\beta}_1 \)) \geq MSE(\( \hat{\beta}_1(\hat{d}) \));

(2) if \( \sigma_{12}(1/\lambda_1 - \rho_{12}^2(a_{ij}/\lambda_1^2)) - \alpha_2^2 < 0 \), when \( 0 < k < \sigma_{12}(1/\lambda_1 - \rho_{12}^2(a_{ij}/\lambda_1^2)) \), then

MSE(\( \tilde{\beta}_1 \)) \geq MSE(\( \hat{\beta}_1(k, d) \)).

(b) when \( k > 0 \) fixed,

(1) if \( \sigma_{12}(2\lambda_1 + k)(1/\lambda_1 + \rho_{12}^2(a_{ij}/\lambda_1^2)) \geq k\alpha_2^2 \), then

MSE(\( \tilde{\beta}_1 \)) \geq MSE(\( \hat{\beta}_1(k, d) \)).


In order to compare $\tilde{\beta}_1(k, d)$ and $\bar{\beta}_1$, we consider the following difference:

\[ \text{MSE}(\tilde{\beta}_1) - \text{MSE}(\bar{\beta}_1(k, d)) \]

\[ = \sigma_{11} \sum_{i=1}^{p_1} \left( \frac{1}{\lambda_i} - \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) - \sigma_{11} \sum_{i=1}^{p_1} \frac{(\lambda_i + d)^2}{\lambda_i} \left( \frac{1}{\lambda_i} - \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) \]

\[ - (k - d)^2 \sum_{i=1}^{p_1} \frac{\alpha_i^2}{(\lambda_i + k)^2} \]

\[ = \sum_{i=1}^{p_1} \frac{(k - d)}{(\lambda_i + k)^2} \left[ (2\lambda_i + k + d) \left( \frac{1}{\lambda_i} - \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) - (k - d) \alpha_i^2 \right]. \]

When $0 < d < 1$ fixed, then we write (17) as follows:

\[ \text{MSE}(\tilde{\beta}_1) - \text{MSE}(\bar{\beta}_1(k, d)) \]

\[ = \sum_{i=1}^{p_1} \frac{(k - d)}{(\lambda_i + k)^2} \left[ \left( \sigma_{11} (2\lambda_i + d) \left( \frac{1}{\lambda_i} + \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) + d \alpha_i^2 \right) \right] \]

\[ + k \left[ \sigma_{11} \left( \frac{1}{\lambda_i} - \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) - \alpha_i^2 \right]. \]

1. If $\sigma_{11} \left( 2\lambda_i + d \right) \left( \frac{1}{\lambda_i} + \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) + d \alpha_i^2 \geq 0$, then $\text{MSE}(\tilde{\beta}_1) \geq \text{MSE}(\bar{\beta}_1(k, d))$;

2. If $\sigma_{11} \left( 2\lambda_i + d \right) \left( \frac{1}{\lambda_i} + \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) + d \alpha_i^2 < 0$, when $0 < k < (\sigma_{11} (2\lambda_i + d) (1/\lambda_i + \rho_{12}^2 (a_{ii}/\lambda_i^2))) / (\alpha_i^2 - \sigma_{11} (2\lambda_i + d) (1/\lambda_i + \rho_{12}^2 (a_{ii}/\lambda_i^2)))$, then $\text{MSE}(\tilde{\beta}_1) \geq \text{MSE}(\bar{\beta}_1(k, d))$.

When $k > 0$ fixed, then we write (17) as follows:

\[ \text{MSE}(\tilde{\beta}_1) - \text{MSE}(\bar{\beta}_1(k, d)) \]

\[ = \sum_{i=1}^{p_1} \left[ \left( 2\lambda_i + k \right) \left( \frac{1}{\lambda_i} + \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) - k \alpha_i^2 \right] \]

\[ + d \left[ \sigma_{11} \left( \frac{1}{\lambda_i} - \rho_{12}^2 \frac{a_{ii}}{\lambda_i^2} \right) + \alpha_i^2 \right]. \]

So if

1. $\sigma_{11} (2\lambda_i + k) (1/\lambda_i + \rho_{12}^2 (a_{ii}/\lambda_i^2)) \geq k \alpha_i^2$, then $\text{MSE}(\tilde{\beta}_1) \geq \text{MSE}(\bar{\beta}_1(k, d))$;

2. $\sigma_{11} (2\lambda_i + k) (1/\lambda_i + \rho_{12}^2 (a_{ii}/\lambda_i^2)) < k \alpha_i^2$, when $\left( k \alpha_i^2 - \sigma_{11} (2\lambda_i + k) (1/\lambda_i + \rho_{12}^2 (a_{ii}/\lambda_i^2)) \right) / (\sigma_{11} (2\lambda_i + k) (1/\lambda_i + \rho_{12}^2 (a_{ii}/\lambda_i^2))) \leq d < 1$, then $\text{MSE}(\tilde{\beta}_1) \geq \text{MSE}(\bar{\beta}_1(k, d))$.

\[ \square \]
4. The Admissible of the New Estimator $\tilde{\beta}_1(k,d)$

As we all know, the admissible of an estimator is an important problem in SUR model. In this section, we discuss the admissible of the new estimator $\tilde{\beta}_1(k,d)$. Firstly, we give the definition of the admissible.

**Definition 3.** Let $\tilde{\theta}_1$ and $\tilde{\theta}_2$ be two estimators of $\theta$, for arbitrarily risk loss function $R(\cdot, \cdot)$, (1) $R(\tilde{\theta}_1, \theta) \leq R(\tilde{\theta}_2, \theta)$ for arbitrarily $\theta$. (2) There at least exist a $\tilde{\theta}_2$ such that the inequality is satisfied. Then we see that $\tilde{\theta}_1$ is uniformly better than $\tilde{\theta}_2$ for risk loss function $R(\cdot, \cdot)$. If, in some class estimators, there is not exist an estimator that is uniformly better than $\tilde{\theta}$, we can say that $\tilde{\theta}$ is admissible estimator of $\theta$ for risk loss function $R(\cdot, \cdot)$ in that class estimators.

**Lemma 4** (see [13]). For linear model

$$y = X\beta + \varepsilon, \quad E(\varepsilon) = 0, \quad \text{Cov}(\varepsilon) = \sigma^2 \Sigma,$$

(20)

where $\Sigma > 0$ is a known matrix and $X$ is full column rank. Let $T = X'\Sigma^{-1}X$, $\beta^* (\Sigma) = T^{-1}X'\Sigma^{-1}y$; then in the linear estimators of $S\beta$, $L\beta^* (\Sigma)$ is admissible estimator of $S\beta$ if and only if

$$LT^{-1}L' \leq LT^{-1}S'.\quad (21)$$

Now we discuss the admissibility of the new estimator. In this section we consider the quadratic loss (mean square error).

**Theorem 5.** For the SUR model (I), when $V$ is know, if $X_1'X_2 = 0$, then $\tilde{\beta}_1(k,d)$ is admissible estimator of $\tilde{\beta}_1$ in the class of linear estimators $\Phi$.

**Proof.** If $X_1'X_2 = 0$, then

$$\tilde{\beta}_1(k,d) = (X_1'X_1 + kl)^{-1}(X_1'X_1 + dI)(X_1'X_1)^{-1}X_1'Y_1$$

$$-\frac{\sigma_1^2}{\sigma_2^2}(X_1'X_1 + kl)^{-1}$$

$$\times (X_1'X_1 + dI)(X_1'X_1)^{-1}X_1'Y_2.$$

(22)

For SUR model (I), let $Y = (Y_1', Y_2')', X = \text{diag}(X_1, X_2), \beta = (\beta_1', \beta_2')$, and $\varepsilon = (\varepsilon_1', \varepsilon_2')$. Then (I) can be written as

$$Y = X\beta + \varepsilon, \quad E(\varepsilon) = 0, \quad \text{Cov}(\varepsilon) = V,$$

(23)

where

$$V = \begin{pmatrix} \sigma_{11}I & \sigma_{12}^2 \\ \sigma_{21}^2 & \sigma_{22}I \end{pmatrix}, \quad \beta^* (V) = (\beta_1^* (V), \beta_2^* (V)),$$

(24)

and (24) satisfies the following equation:

$$X'V^{-1}X\beta^* = X'V^{-1}Y.$$

(25)

Note that

$$V^{-1} = \begin{pmatrix} \sigma_{11}I & -\sigma_{12} \\ -\sigma_{21} & \sigma_{22}I \end{pmatrix}.$$

Then (25) can be written as follows:

$$\begin{pmatrix} \sigma_{22}X_1'X_1 & -\sigma_{21}X_1'X_2 \\ -\sigma_{12}X_1'X_2 & \sigma_{11}X_1'X_2 \end{pmatrix} \begin{pmatrix} X_1'Y_1 \\ X_2'Y_2 \end{pmatrix} = \begin{pmatrix} \sigma_{22}X_1'X_1 & -\sigma_{21}X_1'X_2 \\ -\sigma_{12}X_1'X_2 & \sigma_{11}X_1'X_2 \end{pmatrix} \begin{pmatrix} Y_1 \\ Y_2 \end{pmatrix}.$$

(27)

When $X_1'X_2 = 0$, (25) can be written as follows:

$$\begin{pmatrix} \sigma_{22}X_1'X_1 & 0 \\ 0 & \sigma_{11}X_1'X_2 \end{pmatrix} \begin{pmatrix} \beta_1^* (V) \\ \beta_2^* (V) \end{pmatrix} = \begin{pmatrix} \sigma_{22}X_1'X_1 & -\sigma_{21}X_1'X_2 \\ -\sigma_{12}X_1'X_2 & \sigma_{11}X_1'X_2 \end{pmatrix} \begin{pmatrix} Y_1 \\ Y_2 \end{pmatrix}.$$

(28)

Then by (28), we may get

$$X_1'X_1\beta_1^* (V) = X_1'Y_1 - \frac{\sigma_{12}}{\sigma_{22}}X_1'Y_2,$$

(29)

multiplication $(X_1'X_1 + kl)^{-1}(X_1'X_1 + dI)(X_1'X_1)^{-1}$ in (28); we have

$$X_1'X_1 + kl)^{-1}(X_1'X_1 + dI)\beta_1^* (V) = \tilde{\beta}_1 (k,d).$$

(30)

Then

$$\tilde{\beta}_1 (k,d) = (X_1'X_1 + kl)^{-1}(X_1'X_1 + dI)(I, 0)\beta_1^* (V).$$

(31)

Let $L = (X_1'X_1 + kl)^{-1}(X_1'X_1 + dI)(I, 0)$ and $S = (I, 0)$; by Lemma 4, if we want to prove that $\tilde{\beta}_1 (k,d)$ is admissible estimator of $\tilde{\beta}_1$, we only need to prove $LT^{-1}L' \leq LT^{-1}S'$. Since $X_1'X_2 = 0$, we may conclude that

$$T = X'V^{-1}X = \begin{pmatrix} \sigma_{11}I & -\sigma_{12} \\ -\sigma_{21} & \sigma_{22}I \end{pmatrix} \begin{pmatrix} \sigma_{22}X_1'X_1 & 0 \\ 0 & \sigma_{11}X_1'X_2 \end{pmatrix}.$$

(32)
Then
\[ LT^{-1}L' = \left( \sigma_{11} \sigma_{22} - \sigma_{12}^2 \right) \left( X_1' X_1 + kI \right)^{-1} \]
\[ \times \left( X_1' X_1 + dI \right) \left( I, 0 \right) \left( \begin{array}{cc} \sigma_{22} X_1' X_1 & 0 \\ 0 & \sigma_{11} X_2' X_2 \end{array} \right)^{-1} \]
\[ \times \left( I, 0 \right) \left( X_1' X_1 + dI \right) \left( X_1' X_1 + kI \right)^{-1} \]
\[ = \frac{\sigma_{11} \sigma_{22} - \sigma_{12}^2}{\sigma_{22}} \left( X_1' X_1 + kI \right)^{-1} \left( X_1' X_1 + dI \right) \left( X_1' X_1 + kI \right)^{-1} \]
\[ \times \left( X_1' X_1 + dI \right) \left( X_1' X_1 \right)^{-1} \]
\[ LT^{-1}S' = \left( \sigma_{11} \sigma_{22} - \sigma_{12}^2 \right) \left( X_1' X_1 + kI \right)^{-1} \left( X_1' X_1 + dI \right) \left( I, 0 \right) \left( \begin{array}{cc} \sigma_{22} X_1' X_1 & 0 \\ 0 & \sigma_{11} X_2' X_2 \end{array} \right)^{-1} \]
\[ \times \left( X_1' X_1 + dI \right) \left( X_1' X_1 + kI \right)^{-1} \]
\[ = \frac{\sigma_{11} \sigma_{22} - \sigma_{12}^2}{\sigma_{22}} \left( X_1' X_1 + kI \right)^{-1} \left( X_1' X_1 + dI \right) \left( X_1' X_1 + kI \right)^{-1} \]
\[ \times \left( X_1' X_1 + dI \right) \left( X_1' X_1 \right)^{-1} \]
\[ \quad \quad \quad (33) \]

It is obvious that \( L'T^{-1}L' \leq L'T^{-1}S' \). The proof is completed.

Theorem 6. For the SUR model (1), when \( V \) is known, if \( P_1 P_2 = P_2 P_1 \), then \( \tilde{\beta}(k, d) \) is an admissible estimator of \( \beta_1 \) in the class of linear estimators \( \Phi \).

Proof. For SUR model (1), when \( P_1 P_2 = P_2 P_1 \), by Lin [14], we obtain \( \tilde{\beta}_1 = \beta_1^*(V) \); thus we obtain
\[ \tilde{\beta}_1 (k, d) = \left( X_1' X_1 + kI \right)^{-1} \left( X_1' X_1 + dI \right) \tilde{\beta}_1 \]
\[ = \left( X_1' X_1 + kI \right)^{-1} \left( X_1' X_1 + dI \right) \beta_1^* (V) \]
\[ = \left( X_1' X_1 + kI \right)^{-1} \left( X_1' X_1 + dI \right) \left( I, 0 \right) \beta_1^* (V) \]
\[ = L \beta_1^* (V). \]

Similar to Theorem 5, we only need to prove \( LT^{-1}L' \leq LT^{-1}S' \); \( L \) and \( S \) are defined as Theorem 5:
\[ T = X' V^{-1} X = \left( \sigma_{11} \sigma_{22} - \sigma_{12}^2 \right)^{-1} \left( \sigma_{22} X_1' X_1 - \sigma_{21} X_1' X_2 \right. \left. \sigma_{21} X_1' X_2 - \sigma_{11} X_2' X_2 \right) \]
\[ \quad \quad \quad (35) \]

Denote \( T^{-1} = \left( T^{11} \quad T^{12} \quad T^{21} \quad T^{22} \right) \); by Rao et al. [15], we have
\[ T^{11} = \frac{\sigma_{11} \sigma_{22} - \sigma_{12}^2}{\sigma_{22}^2} \left[ I - \rho_2^2 \left( X_1' X_1 \right)^{-1} X_1' P_2 X_1 \right]^{-1} \]
\[ \times \left( X_1' X_1 \right)^{-1} \]
\[ \quad \quad \quad (36) \]

Then we have
\[ LT^{-1}L' = \left( X_1' X_1 + kI \right)^{-1} \left( X_1' X_1 + dI \right) T^{11} \]
\[ \times \left( X_1' X_1 + dI \right) \left( X_1' X_1 + kI \right)^{-1} \]
\[ = \frac{\sigma_{11} \sigma_{22} - \sigma_{12}^2}{\sigma_{22}^2} \left( X_1' X_1 + kI \right)^{-1} \left( X_1' X_1 + dI \right) \left( X_1' X_1 + kI \right)^{-1} \]
\[ \times \left[ I - \rho_2^2 \left( X_1' X_1 \right)^{-1} X_1' P_2 X_1 \right]^{-1} \left( X_1' X_1 \right)^{-1} \]
\[ \quad \quad \quad (37) \]

Obviously \( L'T^{-1}L' \leq L'T^{-1}S' \). The proof is completed.

5. Conclusion Remarks

In this paper we consider the parameter estimation in seemingly unrelated regression system. A Liu-type estimator is proposed to overcome the multicollinearity in seemingly unrelated regression system. The superiority of the new estimator has been also discussed and the admissibility of the new estimator is also discussed.

Conflict of Interests

The author declares that there is no conflict of interests regarding the publication of this paper.

Acknowledgments

The author is grateful to the editor and the anonymous referee for the valuable comments which improved the quality of the paper. This work was supported by the Scientific Research Foundation of Chongqing University of Arts and Sciences (Grant no. R2013SC12), Program for Innovation Team Building at Institutions of Higher Education in Chongqing (Grant no. KJTD201321), and the National Natural Science Foundation of China (nos. 11201505, 71271227).

References


