Review Article

Kilonova/Macronova Emission from Compact Binary Mergers

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1. Introduction

Mergers of compact stars, that is, neutron star (NS) and black hole (BH), are promising candidates for direct detection of gravitational waves (GWs). On 2015 September 14, Advanced LIGO [1] has detected the first ever direct GW signals from a BH-BH merger (GW150914) [2]. This discovery marked the dawn of GW astronomy.

NS-NS mergers and BH-NS mergers are also important and leading candidates for the GW detection. They are also thought to be progenitors of short-hard gamma-ray bursts (GRBs [3–5]; see also [6, 7] for reviews). When the designed sensitivity is realized, Advanced LIGO [1], Advanced Virgo [8], and KAGRA [9] can detect the GWs from these events up to ∼200 Mpc (for NS-NS mergers) and ∼800 Mpc (for BH-NS mergers). Although the event rates are still uncertain, more than one GW event per year is expected [10].

Since localization only by the GW detectors is not accurate, for example, more than a few 10 deg² [11–14], identification of electromagnetic (EM) counterparts is essentially important to study the astrophysical nature of the GW sources. In the early observing runs of Advanced LIGO and Virgo, the localization accuracy can be >100 deg² [15–17]. In fact, the localization for GW150914 was about 600 deg² (90% probability) [18].

To identify the GW source from such a large localization area, intensive transient surveys should be performed (see, e.g., [19–24] for the case of GW150914). NS-NS mergers and BH-NS mergers are expected to emit EM emission in various forms. One of the most robust candidates is a short GRB. However, the GRB may elude our detection due to the strong relativistic beaming. Other possible EM signals include synchrotron radio emission by the interaction between the ejected material and interstellar gas [25–27] or X-ray emission from a central engine [28–31].

Among variety of emission mechanisms, optical and infrared (IR) emission powered by radioactive decay of r-process nuclei [32–37] is of great interest. This emission is called “kilonova” [34] or “macronova” [33] (we use the term of kilonova in this paper). Kilonova emission is thought to be promising: by advancement of numerical simulations, in particular numerical relativity [38–41], it has been proved that a part of the NS material is surely ejected from NS-NS and BH-NS mergers (e.g., [36, 42–49]). In the ejected
material, r-process nucleosynthesis undoubtedly takes place (e.g., [35, 36, 49–56]). Therefore the emission powered by r-process nuclei is a natural outcome from these merger events.

Observations of kilonova will also have important implications for the origin of r-process elements in the Universe. The event rate of NS-NS mergers and BH-NS mergers will be measured by the detection of GWs. In addition, as described in this paper, the brightness of kilonova reflects the amount of the ejected r-process elements. Therefore, by combination of GW observations and EM observations, that is, "multi-messenger" observations, we can measure the production rate of r-process elements by NS-NS and BH-NS mergers, which is essential to understand the origin of r-process elements. In fact, importance of compact binary mergers in chemical evolution has been extensively studied in recent years [72–82].

This paper reviews kilonova emission from compact binary mergers. The primal aim of this paper is providing a guide for optical and infrared follow-up observations for GW sources. For the physical processes of compact binary mergers and various EM emission mechanisms, see recent reviews by Rosswog [83] and Fernández and Metzger [84]. First, we give overview of kilonova emission and describe the expected properties of the emission in Section 2. Then, we compare kilonova models with currently available observations in Section 3. Based on the current theoretical and observational understanding, we discuss prospects for EM follow-up observations of GW sources in Section 4. Finally, we give summary in Section 5. In this paper, the magnitudes are given in the AB magnitude unless otherwise specified.

2. Kilonova Emission

2.1. Overview. The idea of kilonova emission was first introduced by Li and Paczynski [32]. The emission mechanism is similar to that of Type Ia supernova (SN). The main differences are the following: (1) a typical ejecta mass from compact binary mergers is only an order of 0.01M⊙ (1.4M⊙ for Type Ia SN), (2) a typical expansion velocity is as high as v ∼ 0.1–0.2c = 30,000–60,000 km s⁻¹ (≈10,000 km s⁻¹ for Type Ia SN), and (3) the heating source is decay energy of radioactive r-process nuclei (56Ni for Type Ia SN).

Suppose spherical, homogeneous, and homologously expanding ejecta with a radioactive energy deposition. A typical optical depth in the ejecta is τ = κρR, where κ is the mass absorption coefficient or "opacity" (cm²·g⁻¹), ρ is the density, and R is the radius of the ejecta. Then, the diffusion timescale in the ejecta is

\[ t_{\text{diff}} = \frac{R}{c} \tau = \frac{3\kappa M_{ej}}{4\pi c v' t}, \tag{1} \]

by adopting \( M_{ej} = \frac{(4\pi/3)\rho R^3} \) (homogeneous ejecta) and \( R = vt \) (homologous expansion).

When the dynamical timescale of the ejecta (\( t_{\text{dyn}} = R/v = t \)) becomes comparable to the diffusion timescale, photons can escape from the ejecta effectively [85]. From the condition of \( t_{\text{diff}} = t_{\text{dyn}} \), the characteristic timescale of the emission can be written as follows:

\[ t_{\text{peak}} = \left( \frac{3\kappa M_{ej}}{4\pi cv} \right)^{1/2} = 8.4 \text{ days} \times \left( \frac{M_{ej}}{0.01 M_{\odot}} \right)^{1/2} \times \left( \frac{v}{0.1c} \right)^{-1/2} \left( \frac{\kappa}{10 \text{ cm}^2 \text{ g}^{-1}} \right)^{1/2}. \tag{2} \]

The radioactive decay energy of mixture of r-process nuclei is known to have a power-law dependence \( \dot{q}(t) = 2 \times 10^{10} \text{ erg s}^{-1} \text{ g}^{-1} (t/1 \text{ day})^{-1.3} \) [34, 35, 54, 86–88]. By introducing a fraction of energy deposition (\( \epsilon_{\text{dep}} \)), the total energy deposition rate (or the deposition luminosity) is \( L_{\text{dep}} = \epsilon_{\text{dep}} M_{ej} \dot{q}(t) \). A majority (~90%) of decay energy is released by β decay while the other 10% is released by fission [34]. For the β decay, about 25%, 25%, and 50% of the energy are carried by neutrinos, electrons, and γ-rays, respectively. Among these, almost all the energy carried by electrons is deposited, and a fraction of the γ-ray energy is also deposited to the ejecta. Thus, the fraction \( \epsilon_{\text{dep}} \) is about 0.5 (see [89] for more details). The dashed line in Figure 1 shows the deposition luminosity \( L_{\text{dep}} \) for \( \epsilon_{\text{dep}} = 0.5 \) and \( M_{ej} = 0.01M_{\odot} \).

![Figure 1: Bolometric light curves of a NS-NS merger model (red, \( M_{ej} = 0.01M_{\odot} \) [57, 58]) and a wind model (green, \( M_{ej} = 0.01M_{\odot} \)) compared with a light curve of Type Ia SN model (gray, \( M_{ej} = 1.4M_{\odot} \)). The black dashed line shows the deposition luminosity by radioactive decay of r-process nuclei (\( \epsilon_{\text{dep}} = 0.5 \) and \( M_{ej} = 0.01M_{\odot} \)).](image-url)
Since the peak luminosity is approximated by the deposition luminosity at \( t_{\text{peak}} \) (so-called Arnett’s law [85]), the peak luminosity of kilonova can be written as follows:

\[
L_{\text{peak}} = L_{\text{dep}}\left(t_{\text{peak}}\right) = \varepsilon_{\text{dep}} M_{\text{ej}} \dot{q}(t_{\text{peak}})^{1/2} \left( \frac{M_{\text{ej}}}{0.01 M_\odot} \right)^{0.35} \times \left( \frac{\nu}{0.1 \text{c}} \right)^{0.65} \left( \frac{\kappa}{10 \text{ cm}^2 \text{ g}^{-1}} \right)^{-0.65}.
\]

An important factor in this analysis is the opacity in the ejected material from compact binary mergers. Previously, the opacity had been assumed to be similar to that of Type Ia SN, that is, \( \kappa \sim 0.1 \text{ cm}^2 \text{ g}^{-1} \) (bound-bound opacity of iron-peak elements). However, recent studies [57, 90, 91] show that the opacity in the \( r \)-process element-rich ejecta is as high as \( \kappa \sim 10 \text{ cm}^2 \text{ g}^{-1} \) (bound-bound opacity of lanthanide elements). This finding largely revised our understanding of the emission properties of kilonova. As evident from (2) and (3), a higher opacity by a factor of 100 leads to a longer timescale by a factor of \(-10\) and a lower luminosity by a factor of \(-20\).

2.2. NS-NS Mergers. When two NSs merge with each other, a small part of the NSs is tidally disrupted and ejected to the interstellar medium (e.g., [36, 42]). This ejecta component is mainly distributed in the orbital plane of the NSs. In addition to this, the collision drives a strong shock, and shock-heated material is also ejected in a nearly spherical manner (e.g., [48, 92]). As a result, NS-NS mergers have quasi-spherical ejecta. The mass of the ejecta depends on the mass ratio and the eccentricity of the orbit of the binary, as well as the radius of the NS or equation of state (EOS) (e.g., [48, 92–96]): a more uneven mass ratio and more eccentric orbit lead to a larger amount of tidally disrupted ejecta and a smaller NS radius leads to a larger amount of shock-driven ejecta.

The red line in Figure 1 shows the expected luminosity of a NS-NS merger model (APR4-1215 from Hotokezaka et al. [48]). This model adopts a “soft” EOS APR4 [97], which gives the radius of 11.1 km for a 1.35\( M_\odot \) NS. The gravitational masses of two NSs are 1.2\( M_\odot \) + 1.5\( M_\odot \) and the ejecta mass is 0.01\( M_\odot \). The light curve does not have a clear peak since the energy deposited in the outer layer can escape earlier. Since photons kept in the ejecta by the earlier stage effectively escape from the ejecta at the characteristic timescale (2), the luminosity exceeds the energy deposition rate at \(-5\)–\(8\) days after the merger.

Figure 2 shows multicolor light curves of the same NS-NS merger model (red line; see the right axis for the absolute magnitudes). As a result of the high opacity and the low temperature [90], the optical emission is greatly suppressed, resulting in an extremely “red” color of the emission. The red color is more clearly shown in Figure 3, where the spectral evolution of the NS-NS merger model is compared with the spectra of a Type Ia SN and a broad-line Type Ic SN. In fact, the peak of the spectrum is located at near-IR wavelengths [57, 90, 91].

Because of the extremely high expansion velocities, NS-NS mergers show feature-less spectra (Figure 3). This is a big contrast to the spectra of SNe (black and gray lines), where Doppler-shifted absorption lines of strong features can be identified. Even broad-line Type Ic SN 1998bw (associated with long-duration GRB 980425) showed some absorption features although many lines are blended. Since the high expansion velocity is a robust outcome of dynamical ejecta from compact binary mergers, the confirmation of the smooth spectrum will be a key to conclusively identify the GW sources.

The current wavelength-dependent radiative transfer simulations assume the uniform element abundances. However, recent numerical simulations with neutrino transport show that the element abundances in the ejecta becomes nonuniform [54, 92, 95, 96]. Because of the high temperature and neutrino absorption, the polar region can have higher electron fractions (\( Y_e \) or number of protons per nucleon), resulting in a wide distribution of \( Y_e \) in the ejecta. Interestingly the wide distribution of \( Y_e \) is preferable for reproducing the solar \( r \)-process abundance ratios [54, 56]. This effect can have a big impact on the kilonova emission: if the synthesis of lanthanide elements is suppressed in the polar direction, the opacity there can be smaller, and thus, the emission to the polar direction can be more luminous with an earlier peak.

2.3. BH-NS Mergers. Mergers of BH and NS are also important targets for GW detection (see [98] for a review). Although the event rate is rather uncertain [10], the number of events can be comparable to that of NS-NS mergers thanks to the stronger GW signals and thus larger horizon distances. BH-NS mergers in various conditions have been extensively studied by numerical simulations (e.g., [99–103]). In particular, for a low BH/NS mass ratio (or small BH mass) and a high BH spin, ejecta mass of BH-NS mergers can be larger than that of NS-NS mergers [59, 104–109]. Since the tidal disruption is the dominant mechanism of the mass ejection, a larger NS radius (or stiff EOS) gives a higher ejecta mass, which is opposite to the situation in NS-NS mergers, where shock-driven ejecta dominates.

Radiative transfer simulations in BH-NS merger ejecta show that kilonova emission from BH-NS mergers can be more luminous in optical wavelengths than that from NS-NS mergers [58]. The blue lines in Figure 2 show the light curve of a BH-NS merger model (APR4Q3a75 from Kyutoku et al. [59]), a merger of a 1.35\( M_\odot \) NS and 4.05\( M_\odot \) BH with a spin parameter of \( a = 0.75 \). The mass of the ejecta is \( M_{\text{ej}} = 0.01 M_\odot \). Since BH-NS merger ejecta are highly anisotropic and confined to a small solid angle, the temperature of the ejecta can be higher for a given mass of the ejecta, and thus, the emission tends to be bluer than in NS-NS mergers. Therefore, even if the bolometric luminosity is similar, the optical luminosity of BH-NS mergers can be higher than that of NS-NS mergers.

It is emphasized that the mass ejection from BH-NS mergers has a much larger diversity compared with NS-NS mergers, depending on the mass ratio, the BH spin, and its orientation. As a result, the expected brightness also has a
large diversity. See Kawaguchi et al. [110] for the expected kilonova brightness for a wide parameter space.

2.4. Wind Components. After the merger of two NSs, a hypermassive NS is formed at the center, and it subsequently collapses to a BH. During this process, accretion disk surrounding the central remnant is formed. A BH-accretion disk system is also formed in BH-NS mergers. From such accretion disk systems, an outflow or disk “wind” can be driven by neutrino heating, viscous heating, or nuclear recombination [56, 111–117]. A typical velocity of the wind is \( v = 10,000–20,000 \text{ km s}^{-1} \), slower than the precedent dynamical ejecta. Although the ejecta mass largely depends on the ejection mechanism, a typical mass is likely an order of \( M_{ej} = 0.01M_\odot \) or even larger.

This wind component is another important source of kilonova emission [112, 113, 118–120]. The emission properties depend on the element composition in the ejecta. In particular, if a high electron fraction (\( Y_e \gtrsim 0.25 \)) is realized by the neutrino emission from a long-lived hypermassive NS [118, 119] or shock heating in the outflow [115], synthesis of lanthanide elements can be suppressed in the wind. Then, the resulting emission can be bluer than the emission from the dynamical ejecta thanks to the lower opacity [57, 90]. This component can be called “blue kilonova” [84].

To demonstrate the effect of the low opacity, we show a simple wind model in Figures 1 and 2. In this model, we adopt a spherical ejecta of \( M_{ej} = 0.01M_\odot \) with a density structure of \( \rho \propto r^{-2} \) from \( v = 0.01c \) to \( 0.1c \) (with the average velocity of \( v \approx 20,000 \text{ km s}^{-1} \)). The elements in the ejecta are assumed...
to be lanthanide-free: only the elements of $Z = 31$–54 are included with the solar abundance ratios. As shown by previous works [119], the emission from such a wind can peak earlier than that from the dynamical ejecta (Figure 1) and the emission is bluer (Figure 2).

Note that this simple model neglects the presence of the dynamical ejecta outside of the wind component. The effect of the dynamical ejecta in fact important, because it works as a “lanthanide curtain” [119] absorbing the emission from the disk wind. Interestingly, as described in Section 2.2, the polar region of the dynamical ejecta can have a higher $Y_w$, and the “lanthanide curtain” may not be present in the direction. Also, in BH-NS mergers, the dynamical ejecta is distributed in the orbital plane, and disk wind can be directly observed from most of the lines of sight. If the wind component is dominant for kilonova emission and can be directly observed, the spectra are not as smooth as the spectra of dynamical ejecta because of the slower expansion [119]. More realistic simulations capturing all of these situations will be important to understand the emission from the disk wind.

3. Lessons from Observations

Since short GRBs are believed to be driven by NS-NS mergers or BH-NS mergers (see, e.g., [6, 7]), models of kilonova can be tested by the observations of short GRBs. As well known, SN component has been detected in the afterglow of long GRBs (see [121, 122] for reviews). If kilonova emission occurs, the emission can be in principle visible on top of the afterglow, but such an emission had eluded the detection for long time [123].

In 2013, a clear excess emission was detected in the near-IR afterglow of GRB 130603B [67, 68]. Interestingly, the excess was not visible in the optical data. Since this behavior nicely agrees with the expected properties of kilonova, the excess is interpreted to be the kilonova emission.

Figure 4(a) shows kilonova models compared with the observations of GRB 130603B. The observed brightness of the near-IR excess in GRB 130603B requires a relatively large ejecta mass of $M_{ej} \geq 0.02 M_\odot$ [67, 68, 73, 124]. As pointed out by Hotokezaka et al. [124], this favors a soft EOS for a NS-NS merger model (i.e., more shock-driven ejection) and a stiff EOS for a BH-NS merger model (i.e., more tidally driven ejection). Another possibility to explain the brightness may be an additional emission from the disk wind (green line in Figure 4; see [118, 119]).

Note that the excess was detected only at one epoch in one filter. Therefore, other interpretations are also possible, for example, emission by the external shock [125] or by a central magnetar [126, 127], or thermal emission from newly formed dust [128]. Importantly, a late-time excess is also visible in X-ray [129], and thus, the near-IR and X-ray excesses might be caused by the same mechanism, possibly the central engine [130, 131].

Another interesting case is GRB 060614. This GRB was formally classified as a long GRB because the duration is about 100 sec. However, since no bright SN was accompanied, the origin was not clear [132–135]. Recently the existence of a possible excess in the optical afterglow was reported [69, 70]. Figure 4(b) shows the comparison between GRB 060614 and the same sets of the models. If this excess is caused by kilonova, a large ejecta mass of $M_{ej} \sim 0.1 M_\odot$ is required. This fact may favor a BH-NS merger scenario with a stiff EOS [69, 70]. It is however important to note that the emission from BH-NS merger has a large variation, and such an effective mass ejection requires a low BH/NS mass ratio and a high BH spin [110]. See also [136] for possible optical excess in GRB 050709, a genuine short GRB with a duration of 0.5 sec [137–140]. If the excess is attributed to kilonova, the required ejecta mass is $M_{ej} \sim 0.05 M_\odot$.

Finally, an early brightening in optical data of GRB 080503 at $t \sim 1$–5 days can also be attributed to kilonova [141] although the redshift of this object is unfortunately unknown. Kasen et al. [119] give a possible interpretation with the disk wind model. Note that a long-lasting X-ray emission was also detected in GRB 080503 at $t \lesssim 2$ days, and it may favor a common mechanism for optical and X-ray emission [131, 142].

4. Prospects for EM Follow-Up Observations of GW Sources

Figure 2 shows the expected brightness of compact binary merger models at 200 Mpc (left axis). All the models assume a canonical ejecta mass of $M_{ej} = 0.01 M_\odot$, and therefore, the emission can be brighter or fainter depending on the merger parameters and the EOS (see Section 2). Keeping this caveat in mind, typical models suggest that the expected kilonova brightness at 200 Mpc is about 22 mag in red optical wavelengths ($i$- or $z$-bands) at $t < 5$ days after the merger. The brightness quickly declines to $>24$ mag within $t \sim 10$ days after the merger. To detect this emission, we ultimately need 8 m class telescopes. Currently the wide-field capability for 8 m class telescopes is available only at the 8.2 m Subaru
Figure 4: Comparison of kilonova models with GRB 130603B (a) and GRB 060614 (b). The models used in these plots are those with relatively high ejecta masses: APR4-1215 (NS-NS, $M_{ej} = 0.01M_\odot$ [48]), H4Q3a75 (BH-NS, $M_{ej} = 0.05M_\odot$ [59]), and a wind model with $M_{ej} = 0.03M_\odot$ (this paper). The H4Q3a75 model is a merger of a 1.35 $M_\odot$ NS and a 4.05 $M_\odot$ BH with a spin parameter of $a = 0.75$. This model adopts a “stiff” EOS H4 [65, 66] which gives a 13.6 km radius for 1.35 $M_\odot$ NS. For GRB 130603B, the afterglow component is assumed to be $f_\gamma \propto t^{-2.7}$ [67, 68]. For GRB 060614, it is assumed to be $f_\gamma \propto t^{-2.3}$ [69], which is a conservative choice (see [70] for a possibility of a steeper decline). The observed and model magnitudes for GRB 060614 are given in the Vega system as in the literature [70].

A big challenge for identification of the GW source is contamination of SNe. NS-NS mergers and BH-NS mergers are rare events compared with SNe, and thus, much larger number of SNe are detected when optical surveys are performed over 10 deg$^2$ (see [21–23] for the case of GW150914). Therefore, it is extremely important to effectively select the candidates of kilonova from a larger number of SNe.

To help the classification, color-magnitude and color-color diagrams for the kilonova models and Type Ia SNe are shown in Figure 5. The numbers attached with the models are days after the merger while dots for SNe are given with 5-day interval. According to the current understanding, the light curves of kilonova can be characterized as follows.

1. The timescale of variability should be shorter than that of SNe (Figure 2). This is robust since the ejecta mass from compact binary mergers is much smaller than SNe.

2. The emission is fainter than SNe. This is also robust because of the smaller ejecta mass and thus the lower available radioactive energy (Figure 1).

3. The emissions are expected to be redder than SNe. This is an outcome of a high opacity in the ejecta, but the exact color depends on the ejecta composition ([58, 90, 118, 119], Section 2).

Therefore, in order to effectively search for the EM counterpart of the GW source, multiple visits in a timescale of <10 days will be important so that the rapid time evolution can be captured. Surveys with multiple filters are also helpful to use color information. As shown in Figure 5, observed magnitudes of kilonovae at ~200 Mpc are similar to those of SNe at larger distances ($z \gtrsim 0.3$ for Type Ia SNe). Therefore,
if redshifts of the host galaxies are estimated, kilonova candidates can be further selected by the close distances and the intrinsic faintness.

5. Summary

The direct detection of GWs from GW150914 opened GW astronomy. To study the astrophysical nature of the GW sources, the identification of the EM counterparts is essentially important. In this paper, we reviewed the current understanding of kilonova emission from compact binary mergers.

Kilonova emission from the dynamical ejecta of 0.01$M_\odot$ has a typical luminosity is an order of $10^{40} - 10^{41}$ erg s$^{-1}$ with the characteristic timescale of about 1 week. Because of the high opacity and the low temperature, the spectral peak is located at red optical or near-IR wavelengths. In addition to the emission from the dynamical ejecta, a subsequent disk wind can cause an additional emission which may peak earlier with a bluer color if the emission is not absorbed by the precedent ejecta.

The detection of excess in GRB 130603B (and possibly GRB 060614) supports the kilonova scenario. If the excesses found in these objects are attributed to the kilonova emission, the required ejecta masses are $M_{\text{ej}} \gtrsim 0.02M_\odot$ and $M_{\text{ej}} \sim 0.1M_\odot$, respectively. The comparison between such observations and numerical simulations gives important insight to study the progenitor of compact binary mergers and EOS of NS.

At 200 Mpc distance, a typical peak brightness of kilonova emission is about 22 mag in the red optical wavelengths ($i$- or $z$-bands). The emission quickly fades to $>24$ mag within $\sim$10 days. To distinguish GW sources from SNe, observations with multiple visits in a timescale of $<10$ days are important to select the objects with rapid temporal evolution. The use of multiple filters is also helpful to select red objects. Since the extremely high expansion velocities ($v \sim 0.1 - 0.2c$) are unique features of dynamical mass ejection from compact binary mergers, detection of extremely smooth spectrum will be the smoking gun to conclusively identify the GW sources.

Competing Interests

The author declares that there is no conflict of interests regarding the publication of this paper.

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