Research Article

Exploring the Occurrence of Clogging in Highly Permeable Coarse Soils of Dam Foundations

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Leakage through the permeable coarse soils of dam foundations in Tibet, China, lessened over time without any additional antiseepage measures. In fact, clogging generated during the infiltration process is recognized as the major factor in reducing leakage. A laboratory study was conducted to understand clogging in highly permeable coarse soil of a dam foundation with the primary aim of determining the clogging patterns and optimum clogging particle size (PS). Seven replicate experiments were constructed using soil media with PS ranges of 32–64 mm, 16–32 mm, 8–16 mm, 4–8 mm, 2–4 mm, 1–2 mm, and 0.5–1 mm to observe clogging after feeding the soil media with sediments of different PSs. The experimental results showed that four clogging patterns were formed in different PSs of the coarse foundation soil. The ratio of the effective aperture of the soil \( D_{ea} \) and the equivalent clogging particle size \( d_e \) \( (d_e/D_{ea}) \) had a dominant effect on the four clogging patterns (surface clogging, \( (d_e/D_{ea}) > 1 \); surface-internal clogging, \( 0.5 < (d_e/D_{ea}) \leq 1 \); internal partial pore blockage, \( 0.25 < (d_e/D_{ea}) \leq 0.5 \); and unclogging, \( (d_e/D_{ea}) \leq 0.25 \)). The assessment criterion of the optimum clogging pattern was determined by \( 0.5 < (d_e/D_{ea}) \leq 1 \), and from that, the optimum clogging PS \( d_e \) was calculated.

1. Introduction

Leakage is a major safety issue that influences the economic value of dams and threatens dam stability [1–4]. It was reported that the sediments of the reservoir dam foundation in Shannan, located in the south of Tibet Province, China, were deep and overlain by coarse-grained soils originating from glacial deposits and characterized by physical weathering and high permeability [5, 6], creating a risk of leakage [7, 8]. Due to continuing seepage and erosion of the dam’s foundation, the flow rate in the soil foundation increased gradually. This increased the seepage through the dam foundation and caused concentrated erosion of the fine-grained material at the soil interface with the dam foundation, finally leading to failure of the dam’s foundation [9, 10]. A decades-long survey of five reservoirs (Daranduo Reservoir, Jiangxiong Reservoir, Jiaripu Reservoir, Qiongguo Reservoir, and Awoduo Reservoir, as shown in Figure 1(a)) in the Shannan area found that the state of leakage in the dam foundations at these sites lessened with time without any additional antiseepage measures [11–13]. The reason for this phenomenon was verified under seepage conditions in the dam foundation and was attributed to fine soil particles that were transported and retained in the pores, thus reducing leakage [6]. Therefore, placing fine sediments into foundation soil pores can serve as a recovery technology approach for leakage in foundation soil, similar to using geomembranes, as an effective method of clogging.

Sedimentation of fine particles can influence the permeability of soil [14], which has been verified in soil filters in geotechnical engineering. By preventing the erosion of base soils and building up pore pressure, clogging provided an effective method to obtain internal stability [9, 15]. It is evident from research in porous media that physical
Clogging may be more likely to occur under constant head conditions than under constant flow rates [16], similar to the highly permeable coarse soils of the dam foundations in Qiongguo reservoir and Jiangxiong reservoir [12]. The study on the permeability and mechanical properties of saturated cohesionless soil by laboratory tests shows that hydraulic gradient would drop and flow velocity would increase under long-term infiltration and large amounts of fine particles are eroded away, which finally caused the reduction of the soil strength at the major stage of drained shearing [7, 17].

In surveys of clogging events in the disciplines of environmental engineering, geotechnical engineering, and biological engineering, clogging particles were mostly fine particles, such as sandy-silt [18], suspended solids [19–22],
2. Experimental Works

2.1. Materials. The materials used in this study were natural materials similar to the real dam foundation media obtained upstream of Zhuo Yu Gou in the middle of the Qiongguo and Jiangxiong Reservoirs, Shannan, Tibet (Figure 1). The materials were divided into two parts, soil media (as skeleton particles in the experiments) and incoming sediments (the particles added in the column to checking clogging or not in the experiments). To assess the impact of particle size on clogging, the particle size distributions (PSDs) of all the materials are in accordance with the Udden-Wentworth scale [37, 38].

In the research of foundation leakage in Shannan, the dam foundation soil mainly included boulders, pebbles, gravel, sand and contained cohesive soil, rounded but poorly sorted with particle sizes mainly larger than 0.5 mm [5, 39]. In this study, the soil media particle size (PS) was sieved into 32–64 mm, 16–32 mm, 8–16 mm, 4–8 mm, 2–4 mm, 1–2 mm, and 0.5–1 mm ranges. Similar to particle migration and erosion processes, these media cover a range of gravel and sand sizes [40]. The dry density and porosity of the soil media and the PSs of the incoming sediments are shown in Table 1. To obtain soils that were inert to each other, all soil particles were sieved by soaking in water.

2.2. Experimental Apparatus. For the purpose of the experimental works, a special infiltration-clogging monitoring system was built. The infiltration-clogging monitoring system comprised four parts: sample column, feeding column connected to a feeding pipe, monitoring equipment, and water supply tank with circulation function. Both the sample column and feeding column were 500 mm in height and 370 mm in diameter and made of Plexiglas (Figure 1). As recommended for seepage studies in coarse-particle soils [41], the ratio of the sample column diameter to the soil media particle diameter was more than 5 to 6, appropriate for media particles smaller than 64 mm. Hydraulic head distributions along the soil media were measured by pore water pressure sensors, which were connected to a computer and laterally buried to the sample column. To avoid a preferential flow path between the soil and the Plexiglas cell wall, the monitoring point of hydraulic head change was selected at the center of the sample.

From the feeding pipe, incoming sediments filled in, and the damping plates in the feeding column ensured even distribution of the incoming particles. Reddi et al. [42] and Alem et al. [16] indicated that clogging appeared to be greater under the condition of a constant head than under a constant flow rate. During the operation period, a submersible pump was used to continuously supply water to the constant head controller using a pressure tank and to circulate water in the water supply tank. In the experiment, a 6 m water head was provided by a pressure tank and was stabilized by the top sensor. Figure 2 shows a schematic and photograph of the system.

2.3. Experimental Procedure and Data Analysis. After placing the fully compacted soil media layer by layer, the sample column was checked for leakage before each test. To release air bubbles in the soil media, after one layer of soil media was fully saturated, another was placed. After the device was installed and after setting a constant hydraulic head, the experiment started. Before feeding sediment particles, the hydraulic head and flow velocity were first stabilized. Then, incoming sediments were slowly and uniformly fed into the apparatus. For soil media in the same PS, the same stable time was selected for feeding in each experiment. The clogging phenomenon was monitored by the flow velocity and hydraulic gradient. The hydraulic gradient was calculated by monitoring the hydraulic head, which is the rate of change in hydraulic head per unit distance of flow. A 6 m stable head height was set in the test. The hydraulic gradient for different soil media PSs should be approximately 12 for a specimen height of 0.5 m. However, to ensure hydraulic head stability, the hydroscale (Figure 2) was adjusted to change the flow velocity. Thus, the flow velocity
varied with time and was different than the hydraulic gradient for the 34 experiments. However, for the flow velocity obtained in the 34 experiments, Darcy’s law does not apply. If the hydraulic conductivity was not selected to illustrate the results, and instead, a discussion of the experimental hydraulic characteristics based on the hydraulic gradient and flow velocity is provided.

After feeding the particles for a period of time, the monitoring data reach the secondary stable state, and the experiment was deemed finished. If the lost particles under the drainage pipe were collected, and the soil media in the sample column were layered and sieved after the experiment.

### 3. Results and Discussion

#### 3.1. Laboratory Experiment Results


According to Figure 3, it can be seen that the hydraulic gradient remained relatively constant at first (approximately 12) and increased significantly with time after some particle sizes were introduced before it dropped with time and finally became stable at the initial value (approximately 12).

Under the same hydraulic head and for a fixed sample column, clogging in a smaller PS of the soil media resulted in a higher increase in the amplitude of the hydraulic gradient. Moreover, for the same PS of the soil media, the increased amplitude of the hydraulic gradient was different after introducing different sizes of incoming particles. For instance, the hydraulic gradient increased to its highest point after incoming PSs of 0.063–0.125 mm were introduced following soil media particles sizes of 0.5–1 mm, as shown in Figure 3(g), and the same was observed for soil media PSs of 1–2 mm following incoming PSs of 0.125–0.25 mm in Figure 3(f), soil media PSs of 2–4 mm following incoming PSs of 0.25–0.5 mm in Figure 3(e), soil media PSs of 4–8 mm following incoming PSs of 0.5–1 mm in Figure 3(d), soil media PSs of 8–16 mm following incoming PSs of 1–2 mm in Figure 3(c), soil media PSs of 16–32 mm following incoming PSs of 2–4 mm in Figure 3(b), and soil media PSs of 32–64 mm following incoming PSs of 4–8 mm in Figure 3(a), respectively.

In addition to the above variation, the hydraulic gradient curve shows exhibited fluctuations. This does not necessarily represent variations in the hydraulic gradient because when the water pump feeds the water circulated from the column,
Figure 3: Continued.
Figure 3: Evolution of the hydraulic gradient and the flow velocity in six groups of soil media samples. (a) Soil media PS of 32–64 mm. (b) Soil media PS of 16–32 mm. (c) Soil media PS of 8–16 mm. (d) Soil media PS of 4–8 mm. (e) Soil media PS of 2–4 mm. (f) Soil media PS of 1–2 mm. (g) Soil media PS of 0.5–1 mm.
some air is entrained into the sample column, which might cause fluctuations in the hydraulic gradient.

The initial flow velocity in the experimental columns of different soil media was found to vary around 25% within replicates (Figure 3). This can be attributed to the natural variability in media, and these observed variations were within the ranges reported in the literature, e.g., Sébastien et al. [43] around 49% and Kandra et al. [20] around 30% for different sand media.

The flow velocity remained relatively constant initially. It is logical that the larger the PS of the soil media is, the higher the initial stable flow velocity is. However, there were distinct differences in flow velocity after introducing incoming particles. For soil media of 2–4 mm (Figure 3(e)), the flow velocity decreased significantly after introducing particles of 0.125–0.25 mm, 0.25–0.5 mm, and 0.5–1 mm, especially 0.25–0.5 mm. However, no changes were observed after introducing PSs of 0.063–0.125 mm. A similar evolution of the flow velocity for the other six soil media is shown in Figure 3. This suggests that there is a clogging of particles in the sample column due to introducing different particle sizes.

A comparison of the flow velocity at the start and end of these experiments shows that the smaller the PS of the soil media is, the more obvious the variations in the flow velocity are; conversely, the variations in the flow velocity become more stable. A maximum decline was observed in the experiments of soil media PSs of 0.5–1 mm (Figure 3(g)), which results in an order of magnitude difference. This indicates that the particle size of soil media influences the properties of permeability and clogging.

3.1.2. Image Analysis. For porous media, like soil, physical clogging can be influenced by not only hydraulic characteristics but also porosity, size, type, and percent of fines [44]. For different PSs of soil media, due to smaller pore sizes of soil media than the size of the incoming particles, some incoming particles could not penetrate the pores; instead, they were mainly retained on the top of the soil media, forming a surface mat (Figure 4(a)). The particles could be transported by infiltration; however, some of them were trapped in the soil media (Figures 4(b) and 4(c)), while others were lost. Therefore, different PSs of incoming sediments can induce clogging of the soil column for different PSs of the soil media.

3.1.3. Sieve Analysis. For the same size of soil media particles, with incoming particles of different sizes, clogging changes with depth and thickness. To quantify the changes in the behavior of physical clogging due to incoming particles, relationships in the size of the soil media particles, the weight of the clogging particles, and accurate positions of the clogging were constructed, as shown in Figure 5. From top to bottom, the soil media in the sample column were divided into four layers by sieve analysis. The term $\alpha_i$ indicates the mass percentage of some incoming particle size in layer $i$, $\beta$ indicates the mass percentage of some incoming particle size in the collection column, and the total is $\sum \alpha_i + \beta = 100\%$.

Values of $\sum \alpha_i + \beta$ ranging from 96.3 to 99.1% are attributed to measurement errors in Table 2.

From Figure 5, for different soil media particles, incoming sediments of the same PSs were trapped in different layers. For instance, sediments of PSs of 0.125–0.25 mm were concentrated on top of the soil media of PSs of 0.5–1 mm as in Figure 3(g), were clogged in layer 1 and layer 2 in the soil media of PSs of 1–2 mm shown in Figure 3(f), accumulated in layer 2, layer 3, and layer 4 in the soil media of PSs of 2–4 mm in Figure 3(e), and were lost from the soil media of PSs of 32–64 mm, 16–32 mm, 8–16 mm, and 4–8 mm shown in Figures 3(a)–3(d). Again, the mass percentage of incoming sediment clogging in different PSs of soil media was different. For instance, the mass percentage of sediments of PSs of 0.125–0.25 mm in layer 1 was 90.2% for soil media 0.5–1 mm, the mass percentage in layer 1 and layer 2 was 79.4% for soil media 1–2 mm, and the mass percentage for the sum or layer 1, layer 2, layer 3, and layer 4 was 77.1% for soil media 2–4 mm. However, the mass percentage loss was 75%, 92.4%, 92.1%, and 95.1% for soil media of 4–8 mm, 8–16 mm, 16–32 mm, and 32–64 mm, respectively. Clogging for different PSs of incoming sediments in different soil media particles also suggests similar regularity, as shown in Table 2.

3.2. Division of Clogging Patterns and Determination of the Dominant Clogging Pattern. According to the sieve analysis, two results were found. First, four kinds of proportion characteristics of the mass percentage for different incoming sediment PSs clogging in different PSs of soil media were identified (Table 3-left). The mass percentage was determined by observations from Kandra et al. [20]. Clogging occurred if the incoming sediment mass percentage was more than 75%. Second, four different clogging patterns were observed in different layers in the laboratory experiments, corresponding to the aforementioned mass percentage characteristics (Table 3). The idealized clogging was indicative of pure size exclusion, where clogging events occur only if particles enter a pore that is equal to their own diameter. However, soil pores were always inhomogeneous and anisotropic. We can, therefore, conclude that four different patterns were formed, which have been described in the image analysis results.

A comparison of the clogging patterns in the above seven experiments indicated that the mass percentage of incoming sediments forming surface clogging and surface-internal clogging patterns was $\alpha_1 > \alpha_2 > \alpha_3 > \alpha_4$, and the mass percentage of incoming sediments forming an internal partial pore blockage pattern was $\alpha_2 > \alpha_3 > \alpha_4$. However, the mass percentage of incoming sediments forming an unclogging pattern was $\beta > \alpha_4 > \alpha_3 > \alpha_2$. As expected, each clogging pattern developed a dominant layer. For the surface clogging and surface-internal clogging patterns, the dominant layer was layer 1, and layer 2 was dominant for the internal partial pore blockage pattern. Moreover, incoming sediments were lost for the unclogging pattern.

In addition, the flow velocity varied much for incoming sediments forming patterns of surface clogging, surface-
internal clogging, and internal partial pore blockage, and the velocity was lower and variable for surface-internal clogging (Figure 3). At the same time, the hydraulic gradient for incoming sediments forming surface-internal clogging was slightly higher than that of the other two patterns (Figure 3). This indicates that the particles causing a lower flow velocity than the other size particles represented the dominant clogging particles, and the pattern of surface-internal clogging was the dominant clogging pattern. The dominant clogging PS for the soil media PSs of 16–32 mm was 2–4 mm, for 8–16 mm, it was 1–2 mm, for 4–8 mm, it was 0.5–1 mm, for 2–4 mm, it was 0.25–0.5 mm, for 1–2 mm, it was 0.125–0.25 mm, and for 0.5–1 mm, it was 0.063–0.125 mm (Table 2). Moreover, the 34 groups of experiments formed four patterns after being induced to incoming sediments of continuously graded soil, with only the soil media PSs of 32–64 mm not being representative of the surface-internal clogging pattern (Table 2). However, the clogging results showed that the flow velocity dropped and formed a surface clogging pattern. This is due to the lower head height and weaker carrying capacity of the water, while for incoming sediment PSs of 4–8 mm, sediment particles that were not transported accumulated on the surface of soil media PSs of 32–64 mm.

3.3. Assessment Criterion of Clogging Patterns and Determination of the Optimum Clogging PS. Based on the above analysis, we found that the relationship between soil media PSs and incoming sediment PSs affected the accurate classification of the clogging patterns. According to the relationship between them, a theoretical model was established.

3.3.1. Theoretical Analysis. The homogeneous soil is idealized as an ensemble of spheres of equal size, including various parallel capillary tubes (cylinders) of the same diameter that are equal to the natural soil pore. The pore is expressed as

\[ n = N \left( \frac{\pi D^2}{4} \right) \times 1, \]  

where \( D \) is the homogeneous soil pore size in the ideal state, \( N \) denotes the number of capillary tubes per unit area, and \( n \) is the porosity of natural soil. The number of capillary tubes per unit area, \( N \), may be expressed as follows:

\[ N = \frac{4n}{\pi D^2}. \]  

In an ideal state, the volume of homogeneous soil media is equal to the volume of natural soil media, written as follows:

\[ M \frac{\pi d^3}{6} = (1 - n), \]  

where \( M \) is the number of homogeneous soil media particles per unit volume, and \( d \) is the size of homogeneous soil media particles in an ideal state.

Based on the above results, the area of the capillary tube wall can be taken as the area of the soil particle surface:

\[ N\pi D = M\pi d^2, \]  

\[ M = N\frac{D}{d^2}. \]

By combining equations (2), (3), and (5), \( D \) is solved as
Figure 5: Continued.
Figure 5: Mass percentage of clogging particles in four layers and loss in the collection column in six groups of soil media samples. (a) Soil media PSs of 32–64 mm. (b) Soil media PSs of 16–32 mm. (c) Soil media PSs of 8–16 mm. (d) Soil media PSs of 4–8 mm. (e) Soil media PSs of 2–4 mm. (f) Soil media PSs of 1–2 mm. (g) Soil media PSs of 0.5–1 mm. \( \alpha_i = (m_i/m_0) \times 100\% \); \( m_i \) is the mass of the incoming particles of some size in layer \( i \), kg; \( m_0 \) is the total mass of incoming particles of some size, kg; \( \beta = (m_i/m_n) \times 100\% \); and \( m_n \) is the mass of incoming particles of some size in the collection column, kg.
Table 2: Mass percentage of incoming particle size in different soil media particles.

<table>
<thead>
<tr>
<th>Incoming particle size (mm)</th>
<th>32–64 mm</th>
<th>16–32 mm</th>
<th>8–16 mm</th>
<th>4–8 mm</th>
<th>2–4 mm</th>
<th>1–2 mm</th>
<th>0.5–1 mm</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\alpha_1$</td>
<td>$\alpha_2$</td>
<td>$\sum_{\alpha_i}$</td>
<td>$\beta$</td>
<td>$\alpha_1$</td>
<td>$\alpha_2$</td>
<td>$\sum_{\alpha_i}$</td>
</tr>
<tr>
<td>4–8</td>
<td>75.2</td>
<td>86.9</td>
<td>97.4</td>
<td>0</td>
<td>S</td>
<td>87</td>
<td>94.4</td>
</tr>
<tr>
<td>2–4</td>
<td>10.8</td>
<td>49.4</td>
<td>90.2</td>
<td>6.7</td>
<td>I</td>
<td>90.1</td>
<td>83.6</td>
</tr>
<tr>
<td>1–2</td>
<td>0</td>
<td>0.3</td>
<td>14.5</td>
<td>84.4</td>
<td>N</td>
<td>1</td>
<td>35.3</td>
</tr>
<tr>
<td>0.5–1</td>
<td>0</td>
<td>0</td>
<td>11</td>
<td>87.7</td>
<td>N</td>
<td>1.1</td>
<td>4.6</td>
</tr>
<tr>
<td>0.25–0.5</td>
<td>0</td>
<td>0</td>
<td>6.1</td>
<td>91.5</td>
<td>N</td>
<td>0</td>
<td>1.1</td>
</tr>
<tr>
<td>0.125–0.25</td>
<td>0</td>
<td>0</td>
<td>1.9</td>
<td>95.1</td>
<td>N</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0.063–0.125</td>
<td>0</td>
<td>0</td>
<td>2.1</td>
<td>96.3</td>
<td>N</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Note. CP denotes clogging patterns. S denotes surface clogging. S–I denotes the surface-internal clogging. I denotes the internal partial pore blockage. N denotes unclogging.
Indeed, each soil particle is an inhomogeneous sphere, the pores formed by soil media particles are also uneven, and the incoming particles are inhomogeneous too. We can choose the equivalent size of soil particles and an effective aperture formed by soil particle pores to substitute inhomogeneous soil particles and their formed voids. For each PS range, the equivalent size was calculated by the particle geometric average:

\[ D_e = \sqrt[3]{D_{max} D_{min}} \]  

(6)

where \( D_e \) denotes the equivalent size of the soil particles, \( D_{max} \) is the maximum PS, and \( D_{min} \) is the minimum PS. The effective aperture of soil is then calculated as follows:

\[ D_{ea} = \frac{2}{3\alpha_i} \left( \frac{n_1}{1-n} \right) D_e. \]  

(8)

where \( D_{ea} \) denotes the effective aperture of the soil, \( n_1 \) is the porosity of the soil equal to \( n \), and \( \alpha_i \) is a particle shape correction factor equal to the ratio of soil particle surface area and sphere surface area in the same volume for ideal sand and gravel materials: \( \alpha_i = 1.5–1.9 \) [45].

### 3.3.2. Assessment Criterion of Clogging Patterns

The equivalent size of soil media particles and incoming particles was calculated using equation (7) to derive \( D_e \) and \( D_{ea} \), and the effective aperture \( D_{ea} \) was calculated using equation (8). Then, the ratio of \( D_e \) and \( D_{ea} \) was obtained. Assuming that the soil particles are spheres of equal size, it is logical that when the ratio of the incoming particle size and the pore size is greater than 1, a mat is formed on the surface of the soil media. Moreover, when the ratio is equal to 1, clogging occurs, and when the ratio is less than 1, incoming particles will penetrate the pores and be lost. However, as already discussed, the soil particles and pores were not uniform in shape or size, as shown in Table 3. Clogging was formed when the \( (d_e/D_{ea}) \) ratio was less than 1, as shown in Table 4. A similar situation was previously observed in wetland tests by Hua et al. [46], where clogging was observed for particles entering pores of a smaller diameter.

According to the results of six groups of soil media PSs from 0.5 mm to 32 mm, if we hypothesized that the criteria of \( 0.5 < (d_e/D_{ea}) \leq 1 \) were representative of the surface-internal clogging pattern, knowing the PS and porosity of the soil media and using equation (8), the clogging PS \( d_{ci} \) could be obtained by calculating \( d_e \) as follows:

\[ \frac{n}{3\alpha_i (1-n)} D_e < d_e < \frac{2n}{3\alpha_i (1-n)} D_e, \]  

(9)

where \( d_e \) denotes the clogging PS that results in the surface-internal clogging pattern. The calculation results agree well with the dominant clogging PS of the surface-internal clogging pattern in the laboratory (Figure 6(a)). The other three criteria were assumed to be represented by \( (d_e/D_{ea}) > 1 \) for the surface clogging pattern, \( 0.25 < (d_e/D_{ea}) \leq 0.5 \) for the internal partial pore blockage pattern, and \( (d_e/D_{ea}) < 0.25 \) for representing the unclogging pattern. The mathematical expressions for these relations are as follows:

\[ d_{ic} > \frac{2n}{3\alpha_i (1-n)} D_e, \]  

(10)

\[ \frac{n}{6\alpha_i (1-n)} D_e \leq d_{ic} < \frac{n}{3\alpha_i (1-n)} D_e, \]  

(11)

\[ d_{ic} < \frac{n}{6\alpha_i (1-n)} D_e. \]  

(12)

where \( d_{ic} \) denotes the PS forming the surface clogging pattern, \( d_{ic} \) denotes the PS forming the internal partial pore blockage pattern, and \( d_{ic} \) denotes the PS not resulting in clogging. The calculation results of the above four criteria confirmed the correspondence between the \( (d_e/D_{ea}) \) ratio and the four clogging patterns (Figure 6). Therefore, the dependence of the clogging pattern on the \( (d_e/D_{ea}) \) ratio is shown in Table 5.

In addition, for soil media PSs of 32–64 mm and incoming PSs of 4–8 mm, the calculation result was consistent with the surface-internal clogging pattern, although the surface clogging pattern was observed in the laboratory. This difference may be explained by the lower head height and weaker carrying capacity of the water, as discussed in Section 3.2. This implies that it is more difficult for larger pore structure media to form clogs, as observed by Hua et al. [46]. Furthermore, for soil media PSs of 0.5–1 mm and 1–2 mm, no unclogging pattern was observed after feeding the particles, which has also been reported in the literature, e.g., Wang [19] and Fetzer et al. [47]. The observations eventually resulted in the above criteria, which are more suitable for smaller PS pebbles and gravel and larger PS sand.

### 3.3.3. Optimum Clogging PS

The calculated clogging PSs for different clogging patterns were compared with the data observed in the laboratory (Figure 6). The calculated results...
Table 4: Calculation results.

<table>
<thead>
<tr>
<th>$D_s$ (mm)</th>
<th>$D_a$ (mm)</th>
<th>$n_s$</th>
<th>$D_{ea}$ (mm)</th>
<th>$d_a$ (mm)</th>
<th>$d_e$ (mm)</th>
<th>$d_e/D_{ea}$</th>
<th>Clogging patterns from the experimental observations</th>
</tr>
</thead>
<tbody>
<tr>
<td>2−4</td>
<td>2.83</td>
<td>0.39</td>
<td>0.58−0.74</td>
<td>S</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1−2</td>
<td>1.41</td>
<td>0.15</td>
<td>0.18−0.20</td>
<td>N</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.25−0.5</td>
<td>0.36</td>
<td>0.04</td>
<td>0.03−0.05</td>
<td>N</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.125−0.25</td>
<td>0.18</td>
<td>0.02</td>
<td>0.03−0.05</td>
<td>N</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.063−0.125</td>
<td>0.09</td>
<td>0.01</td>
<td>0.01−0.02</td>
<td>N</td>
<td></td>
<td></td>
<td></td>
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32−64

| 4−8        | 5.66       | 1.25  | 0.04−0.05     | S           |             |              |                                                      |
| 2−4        | 2.83       | 0.63  | 0.36−0.44     | S−I         |             |              |                                                      |
| 1−2        | 1.41       | 0.31  | 0.17−0.22     | N           |             |              |                                                      |
| 0.25−0.5   | 0.35       | 0.07  | 0.03−0.05     | N           |             |              |                                                      |
| 0.125−0.25 | 0.18       | 0.03  | 0.03−0.05     | N           |             |              |                                                      |
| 0.063−0.125| 0.09       | 0.01  | 0.01−0.03     | N           |             |              |                                                      |

16−32

| 2−4        | 2.83       | 1.38  | 0.63−0.87     | S           |             |              |                                                      |
| 1−2        | 1.41       | 0.69  | 0.34−0.44     | S−I         |             |              |                                                      |
| 0.25−0.5   | 0.35       | 0.31  | 0.17−0.22     | N           |             |              |                                                      |
| 0.125−0.25 | 0.16       | 0.08  | 0.03−0.11     | N           |             |              |                                                      |
| 0.063−0.125| 0.08       | 0.04  | 0.04−0.06     | N           |             |              |                                                      |

8−16

| 1−2        | 1.41       | 1.27  | 0.63−0.80     | S           |             |              |                                                      |
| 0.25−0.5   | 0.35       | 0.31  | 0.17−0.22     | N           |             |              |                                                      |
| 0.125−0.25 | 0.18       | 0.15  | 0.17−0.22     | N           |             |              |                                                      |
| 0.063−0.125| 0.09       | 0.07  | 0.07−0.10     | N           |             |              |                                                      |

4−8

| 0.5−1      | 0.71       | 1.09  | 0.54−0.69     | S−I         |             |              |                                                      |
| 0.25−0.5   | 0.35       | 0.54  | 0.27−0.35     | I           |             |              |                                                      |
| 0.125−0.25 | 0.18       | 0.35  | 0.27−0.35     | I           |             |              |                                                      |
| 0.063−0.125| 0.09       | 0.29  | 0.29−0.36     | I           |             |              |                                                      |

2−4

| 1−2        | 1.41       | 1.13  | 0.58−0.72     | S−I         |             |              |                                                      |
| 0.25−0.5   | 0.35       | 0.54  | 0.27−0.35     | I           |             |              |                                                      |
| 0.125−0.25 | 0.18       | 0.35  | 0.27−0.35     | I           |             |              |                                                      |
| 0.063−0.125| 0.09       | 0.29  | 0.29−0.36     | I           |             |              |                                                      |

1−2

| 0.125−0.25 | 0.18       | 1.13  | 0.58−0.72     | S           |             |              |                                                      |
| 0.063−0.125| 0.09       | 0.56  | 0.29−0.36     | S−I         |             |              |                                                      |

0.5−1

| 0.125−0.25 | 0.18       | 1.13  | 0.58−0.72     | S           |             |              |                                                      |
| 0.063−0.125| 0.09       | 0.56  | 0.29−0.36     | S−I         |             |              |                                                      |

Note. $D_s$ denotes soil skeleton particle size. $D_a$ denotes incoming particle size. $D_{ea}$ is the equivalent size of soil skeleton particles. $D_e$ denotes the equivalent size of incoming particles. $n_s$ is the porosity of the soil skeleton. $a_i$ is the particle shape correction factor. $D_{ea}$ is the effective aperture of soil in different $a_i$. 

Figure 6: Continued.
using the inequalities in equation (9) showed the best agreement with the observed clogging PS in the laboratory, which can be adopted to estimate the optimum clogging PS. Ultimately, \( d \) was confirmed as the optimum clogging PS, and \( 0.5 < \left( \frac{d_e}{D_{ea}} \right) \leq 1 \) was used as the assessment criterion of the optimum clogging pattern.

### 4. Conclusions

A lab-based approach was carried out by studying the effects of the PS and the effective aperture of soil on the clogging performance in highly permeable coarse soil of dam foundations. The results showed that due to the soil particles and pores being inhomogeneous in shape or size, four different clogging patterns were formed in the studied coarse soil. The assessment criterion of clogging patterns can be depicted through the \( \left( \frac{d_e}{D_{ea}} \right) \) ratio as follows:

(i) \( \left( \frac{d_e}{D_{ea}} \right) > 1 \) for surface clogging  
(ii) \( 0.5 < \left( \frac{d_e}{D_{ea}} \right) \leq 1 \) for surface-internal clogging  
(iii) \( 0.25 < \left( \frac{d_e}{D_{ea}} \right) \leq 0.5 \) for internal partial pore blockage  
(iv) \( \left( \frac{d_e}{D_{ea}} \right) \leq 0.25 \) for unclogging

Due to the lower head height and weaker carrying capacity of the water, leading to the above criteria being more suitable for pebbles and gravels of smaller PSs and sand of larger PSs, for the soil media larger than 32 mm, most of the incoming particles were lost.

Moreover, from the results of experiments and formula calculations, surface-internal clogging was the optimum clogging pattern. The optimum clogging particle in the pattern of surface-internal clogging was confirmed by the following:

\[
\frac{n}{3a_1(1-n)}D_e < d_e \leq \frac{2n}{3a_1(1-0.5)}D_e. \tag{13}
\]

The classification of clogging patterns, the calculation of the optimum clogging PS, and the determination of the equivalent PS can provide an effective way to study shrinking leakage problems in highly permeable coarse soil of dam foundations.

### Data Availability

The data used to support the findings of this study are included within the article.

### Disclosure

Jianquan Ma is responsible for this article.

### Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

### Authors’ Contributions

Jianquan Ma and Shibo Li designed experiments; Hao Peng, Shibo Li, and Xinshe Zhang carried out experiments; Hao Peng analyzed experimental results; Jianquan Ma assisted...
with the conceptualization of the study and the data interpretations; Shibo Li drew figures. All authors provided valuable critical revisions of the manuscript and also agreed to both contents and form of the final version.

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