As an indirect band gap semiconductor, germanium (Ge) can be transformed into a direct band gap semiconductor through some specific modified methods, stress, and alloying effect. Direct band gap-modified Ge semiconductors with a high carrier mobility and radiation recombination efficiency can be applied to optoelectronic devices, which can improve the luminous efficiency dramatically, and they also have the potential application advantages in realizing monolithic optoelectronic integration (MOEI) and become a research hotspot in material fields. Among the various implementations of Ge band gap-type conversion, the related methods that are compatible with the Si process are most promising. It is such a method to etch around the Ge epitaxial layer on the Si substrate and introduce the biaxial tensile stress by SiGe selective filling. However, the influence of the width of the epitaxial layer, Ge composition, and Ge mesa region width on strain distribution and intensity is not clear yet. Accordingly, a finite element stress model of the selective epitaxy-induced direct band gap Ge scheme is established to obtain the material physical and geometric parameters of the Si$_{1-x}$Ge$_x$ growth region. The result of finite element simulation indicates when the Si$_{1-x}$Ge$_x$ epitaxial layer is 150–250 nm wide and the Ge composition is 0.3–0.5, Ge mesa with 20–40 nm in width can be transformed into direct band gap semiconductors in the depth of 0–6 nm. The theoretical results can provide an important theoretical basis for the realization of subsequent related processes.
metal nm−Ge n−Ge Metal Metal n−Ge Metal

Figure 1: A diagram view of the MOEI device.

electrical devices [6]. On the other hand, modified Ge has a quasi-direct band gap structure, which can realize direct band gap luminescence by means of energy band engineering and other means and thus can be applied to light-emitting devices such as lasers and LEDs [7–16]. Most importantly, both Ge and Si belong to IV materials and have significant advantages in process and production costs.

Despite its wide application prospects, the preparation of modified Ge is facing many difficulties [17]. Since the quality is largely affected by the crystallization situation, structural defects, dislocations, and components, the preparation process of modified Ge has become one of the focuses in the basic research of this material. At present, the modified Ge preparation methods mentioned in the literature mainly include tensile strain-induced Ge direct band gap technology and GeSn alloying-induced direct band gap technology [18]. Based on the theory of strain tensor and deformation potential, the physical mechanism of Ge band gap conversion is investigated, which reveals the law that Ge transitions from indirect band gap semiconductors to direct one [19, 20]. The results show the following: (1) The transformation can be achieved when the (001) biaxial tensile stress of the Ge material is about 2.4 Gpa. Figures 2 and 3 show the variation of the energy levels of Ge conduction and the strain generated with the stress applied under (001) biaxial tensile stress, respectively. Under (101) and (111) biaxial stresses, the transformation of the Ge band gap type cannot be realized. (2) For the uniaxial stress, the Ge semiconductor can be converted into a direct band gap semiconductor only under the (001) plane uniaxial 0°-[100] crystal-orientation tensile stress and the requiring stress is about 4.8 GPa [21]. (3) In the Sn alloying scheme, Ge is changed to direct band gap when the Sn component is dissolved in Ge by about 8% [22, 23].

At present, the direct band gap technique of GeSn alloying has the problems of low solid solubility of Sn in Ge (about 1%), serious surface segregation, and incompatibility with the Si process, and the tensile strain-induced direct band gap Ge technology has the defects of difficult process realization, many crystal defects, poor quality, and so on [24]. To this end, this paper uses a direct band gap Ge implementation method compatible with the Si process—etching around the Ge epitaxial layer on the Si substrate and selectively filling Si1−xGex to properly introduce the biaxial tensile stress to realize the conversion of the Ge band gap type [25]. The structure of this method is shown in Figure 4, where d, T, and l correspond to the Ge mesa region width, Si1−xGex stressor thickness, and the distance between adjacent mesas, respectively. This scheme is compatible with the Si process and relatively easy to implement, with the prospect of being a source material for MOEI.

Based on the theoretical model of the linear elastic material and COMSOL finite element analysis software, a finite element stress model is established by selecting the Si1−xGe region in the Ge epitaxial layer on the Si substrate to implement this method. On the basis of the finite element physical model, the material physical and geometrical parameters of the Si1−xGe selective growth region can be determined, which provides an important theoretical basis for the preparation process of the “direct band gap Ge implementation method compatible with the Si process.”

2. Finite Element Simulation Model

The finite element method (FEM) is used to analyze the strain result from the lattice constant mismatch of semiconductor materials. Different virtual thermal expansion coefficients are usually set to simulate the distribution of stress or strain in materials caused by lattice mismatch [15]. In the simulation, it is assumed that the material properties are isotropic, in which case the strain effect caused by thermal expansion is very similar to that caused by the lattice constant mismatch [26, 27]. Therefore, the strain caused by lattice mismatch between heterogeneous materials can be simulated by setting different thermal expansion coefficients for materials in the finite element simulation process.

Before the simulation analysis of the selective epitaxial modified Ge scheme, this section firstly uses the channel strain induced by selective epitaxy of the Si PMOS source and drain as the reference object to verify the correctness of the COMSOL finite element strain analysis software and the thermal expansion stress simulation method.

Based on the simulation principle of thermal expansion stress calculation mentioned above, the channel strain simulation of Si PMOS source-drain selective epitaxy is carried out. The expansion/contraction of the material due to temperature variation is the same as the strain due to lattice constants mismatch in practical devices, that is, \( \Delta T \), where \( \Delta T \) is the temperature variation of the material, \( C \) is the thermal expansion coefficient set manually, and \( f \) is the lattice mismatch rate between heterogeneous materials. For the epitaxial SiGe layer on the Si substrate, the lattice mismatch rate \( f \) can be obtained from the following equation:

\[
 f = \frac{a_{Si} - a_{SiGe}}{a_{Si}} = -0.0418x,
\]

where the minus indicates that the Si material is subjected to compressive strain.

The heating method is adopted in the simulation process. Assuming a 1000°C rise in temperature, the virtual thermal expansion coefficient of Si0.5Ge0.5 is \( 2.09 \times 10^{-5} / K \). The critical material parameters required for COMSOL simulation are listed in Table 1, and Young’s modulus and
Poisson’s ratio of the SiGe material are obtained by linear interpolation. The geometric parameters are as follows: the length of channel is 50nm, the depth of source and drain zone is 20nm, and the length of source and drain zone is 200nm.

After visualization of the results, the $\varepsilon_{xx}$ and $\varepsilon_{zz}$ strain distributions of the channel region are shown in Figure 5. Careful observation of the following Figure 5 shows that the distribution and magnitude of strains simulated by COMSOL software are in good agreement with the results obtained by Yeo and Sun indicating that the method for studying strain distribution based on virtual thermal expansion is correct and feasible [28].

After verifying the correctness of COMSOL finite element analysis software and thermal expansion stress simulation method, next we modeled the selective epitaxy-induced direct band gap Ge scheme. The realization principle of this scheme is introduced first. Its preparation process is as shown in Figure 6.

Figure 7 shows the local three-dimensional (3D) structure and profile of the selective epitaxy-induced direct band gap Ge scheme, where $L$ is the width of the epitaxial layer, which is equal to the distance between adjacent mesas. Since the lattice constant of Ge is larger than that of Si$_{1-x}$Ge$_x$, the principle of lattice mismatch-induced stress is used to grow Si$_{1-x}$Ge$_x$ around the etched Ge mesa epitaxially, and the biaxial tensile stress will be introduced in the central region of Ge semiconductors.

According to the above structure diagram, a simulation model of selective epitaxy-induced direct band gap Ge is established based on the COMSOL simulation software. Because the force in the X direction is identical to that in the Y direction, and in order to obtain more precise simulation results, this section establishes a two-dimensional simulation model [21]. The modeling process is as follows: (1) analyze the problem and determine the simulation model; (2) create the geometric model; (3) set the material properties; (4) set the boundary conditions; (5) meshing; (6) solve and set the
solution parameters; (7) post processing and visualization of results.

Firstly, through the model wizard, the modeling options such as spatial dimension, physical field, and research type are built. The solid mechanics is selected in the module. After that, the corresponding geometric model is established and the material types and physical parameters in relevant regions are set. In the process, common Si and Ge Material Models in Semiconductor Material Library can be invoked, including basic material parameters, Shockley–Read–Hall
composite model, band gap model, and other important models.

In this paper, the strain distribution is studied based on the thermal expansion method, so the thermal expansion model of the linear elastic material in the solid mechanics module is selected. The next most important step is to set the temperature load and boundary conditions: adding a preset temperature load to the thermal expansion model; subsequently, in order to simulate the real physical conditions, all the nodes on the bottom of the substrate are set as fixed constraints in the two-dimensional direction, and the other boundaries are free. Then, the selective epitaxy-induced direct band gap Ge model is meshed. Since the Ge mesa region is the key area of observation, the mesh for the Ge mesa region is densely divided, and the meshing effect is shown in Figure 8. Finally, the calculation type is selected to perform the operation; after the calculation result is completed, the data type is needed to set for image and drawing processing.

Both the composition of Ge in SiGe and parameters of the SiGe epitaxial layer will affect the strain distribution and magnitude in the mesa; therefore, the influence of the variation of the simulation parameters on the strain in Ge mesa is studied by the strain situation in the $X$ direction.

3. Results and Discussion

3.1. The Effect of Width of the Epitaxial Layer on the Strain.

Referring to the height of the source and drain regions in the Si PMOS channel strain, the Ge step width is set to 20 nm, the Ge composition is taken as 0.5, and the strain situation is analyzed by changing the width of the epitaxial layer. The width of the epitaxial layer is changed from 40 nm to 200 nm, and the strain value at 5 nm in the Ge mesa is as shown by the red curve in Figure 9. From the graph, it can be seen that the strain increases linearly with the increase in the width of the SiGe epitaxial layer when the width is less than 100 nm. However, when the width of the epitaxial layer is 140–160 nm, the strain varies slightly with the increase in the width and tends to be stable gradually; that is, the tensile strain no longer changes as the width of the epitaxial layer increases.

It is possible to obtain the epitaxial layer size for stable strain under different step widths by setting the Ge step width to 25 nm, 30 nm, 35 nm, and 40 nm, respectively. And through a series of simulation experiments, the relationship between the width of the epitaxial layer for a stable strain value and the Ge step width is determined, as shown in Figure 10. It can be found that there is a linear relationship between them. The fitted formula is $y = 5.1x + 52$ ($x$ is the step width, $y$ is the width of the epitaxial layer, and the unit is nanometer).

3.2. The Effect of Ge Composition on the Strain. The theoretical analysis shows that as the Ge composition decreases, the stress in the Ge step increases. The reason is that the lattice constant of the epitaxial layer decreases with the decrease of Ge composition and the lattice constant

![Figure 8: Meshing diagram of the Ge mesa region.](image)

![Figure 9: Variation of strain with the width of the epitaxial layer when the width of the Ge step is 20 nm.](image)

![Figure 10: Variation of the SiGe epitaxial layer width for stable strain with the Ge step width.](image)
difference between the Ge and SiGe epitaxial layers becomes larger, so does the introduced tension strain. Keeping the parameters of Ge step width and epitaxial layer width unchanged, the Ge component in the SiGe epitaxial layer increased from 0.2 to 0.5 and the relationship between the Ge component and the \( X \)-direction strain can be obtained [29].

Table 2 shows the material parameters of the Si\(_{1-x}\)Ge\(_x\) epitaxial layer under different Ge components. Young’s modulus and Poisson’s ratio are calculated by linear interpolation, while the virtual thermal expansion coefficient is calculated from the lattice mismatch rate.

The Ge step width is fixed at 20 nm, and the Ge component is selected to be 0.2, 0.3, 0.4, and 0.5. From the analysis in the previous section, it can be seen that if the width of the Ge step is 20 nm, the maximum strain value can be achieved when the width of the SiGe epitaxial layer is set to about 150 nm. Therefore, the width of the SiGe epitaxial layer is set to 150 nm in the simulation. The obtained simulation results are shown in Figure 11. The strain distribution in the four images is basically the same, just that there are differences in the magnitude of the strain.

Figure 12 shows the horizontal distribution of \( \varepsilon_{xx} \) at a depth of 5 nm from the mesa’s surface. It can be seen that when the Ge component is 0.3, the strain of the Ge material at 5 nm depth has all reached 1.7% or more, which can realize the transition from the indirect band gap to direct band gap. But when the Ge component continues to increase, such as 0.4, only parts of the strain near the boundary in the mesa exceed 1.7%.

Figure 13 shows the depths where the strains of the Ge central region equal to 1.7% under different components. For example, when \( x = 0.3 \), the depth at which all the central regions meet the requirement of band gap transition is 5.775 nm. From the figure and the analysis above, it can be seen that the Ge component has a great influence on the strain in the mesa region, and reducing the Ge component can greatly increase the strain. However, if the Ge component is too small, the lattice mismatch between the SiGe epitaxial layer and Ge material will be too large, which is disadvantageous for preparing a high-quality SiGe epitaxial layer. Therefore, the Ge component is selected to be 0.3–0.5. In this range, not only enough strain can be obtained for the Ge material but also the quality of the SiGe film is relatively good, which is conducive to the preparation of the modified Ge devices.

3.3. The Effect of Ge Step Thickness on the Strain. The Ge component is 0.5, the width of the epitaxial layer is \( L = 150 \) nm, and the length and width of the step is 20 nm.

<table>
<thead>
<tr>
<th>Ge components</th>
<th>Young’s modulus (GPa)</th>
<th>Virtual thermal expansion coefficient (10(^{-5})/K)</th>
<th>Poisson’s ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2</td>
<td>156.6</td>
<td>-3.21</td>
<td>0.2786</td>
</tr>
<tr>
<td>0.3</td>
<td>153.5</td>
<td>-2.81</td>
<td>0.2779</td>
</tr>
<tr>
<td>0.4</td>
<td>150.4</td>
<td>-2.41</td>
<td>0.2772</td>
</tr>
<tr>
<td>0.5</td>
<td>147.3</td>
<td>-2.0</td>
<td>0.2765</td>
</tr>
</tbody>
</table>
The influence of SiGe layer thickness on strain tensor of the Ge material is simulated by taking the thickness of the Ge step as 10, 20, 30, and 40 nm. The simulation results are shown in Figure 14.

The simulation results indicate that changing the thickness of the Ge step has little effect on the distribution and magnitude of the strain generated in the Ge step, which can be neglected.

3.4. Verification of Conclusions. Through the above analysis, the influence of the width of the epitaxial layer and the Ge component in the Si$_{1-x}$Ge$_x$ epitaxial layer on the strain magnitude and distribution in the Ge step can be obtained. Then, the final optimization scheme of selective epitaxy-induced direct band gap Ge is proposed: Ge step size is 20–40 nm, SiGe epitaxial layer width is 150–250 nm, and Ge component in the epitaxial layer is 0.3–0.5, which can realize the direct band gap Ge material in the surface of the mesa region. In this paper, the
width of the Ge step is 20 nm, the thickness is 10 nm, the width of the SiGe epitaxial layer is 210 nm, and the Ge component is 0.3. The strain distribution in the Ge step is simulated by the thermal expansion simulation model. Figure 15 is a contour map of $\varepsilon_{xx}$ and $\varepsilon_{zz}$ in the Ge mesa area.

From Figure 16, the distribution trend of stress in the step can be seen. The stress near the SiGe epitaxial layer and distributed on both sides of the Ge step are larger, while the strains generated near the center of the step are smaller, the strains in the horizontal direction of the step center are relatively uniform, and the strains in the vertical direction decrease rapidly with the increase in the distance from the mesa surface. The magnitude of the strain in the Ge material can be adjusted according to the Ge composition and the width of the epitaxial layer. The geometric dimension of the Ge center region is fixed, and the strain in the Ge material increases linearly with the increase in SiGe epitaxial layer width around and tends to be stable. The smaller the Ge component in the Si$_{1-x}$Ge$_x$ epitaxial layer, the larger the area of the direct band gap Ge semiconductor. When the Si$_{1-x}$Ge$_x$ epitaxial layer is 150–250 nm wide and the Ge composition is 0.3–0.5, Ge mesa with 20–40 nm in width can be transformed into the direct band gap semiconductor in the depth of 0–6 nm.

The physical and geometrical parameters of the Si$_{1-x}$Ge$_x$ selective growth region are obtained based on the theoretical results, which can provide an important theoretical basis for the realization of subsequent related processes.

**Data Availability**

All data of this paper used to support the findings of this study are available from the corresponding author upon request.

**Conflicts of Interest**

The authors declare that there are no conflicts of interest regarding the publication of this paper.

**Acknowledgments**

This work was supported by the 111 Project (Grant no. B12026).
References


