Research Article

Design of Strained Ge Schottky Diode on Si Substrate for Microwave Rectifier Circuit

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1. Introduction

Wireless energy transmission technology refers to transmission from the source to the receiver without the need for a conventional wire. Currently, the wireless energy transmission is divided into two categories according to the near-field and far-field. The near-field infinite energy transmission includes electromagnetic induction transmission and electromagnetic resonance transmission. The former uses a magnetic field as a medium and realizes wireless transmission through a transformer coupling, and the transmission power is large. The latter causes electromagnetic resonance when the natural frequency of the antenna is consistent with the frequency of the transmitting field, and strong electromagnetic coupling occurs to achieve wireless transmission, and the power is up to kilowatts. The far-field wireless energy transmission is mainly microwave wireless power transfer (MWPT), which converts microwave energy into electrical energy and then transmits it to the destination through free space. It can be converted into DC power and supplied to the load through rectification, thereby achieving nonphysical connected energy transfer [1].

As a kind of wireless power transmission technology, MWPT has the advantages of small transmission attenuation in the atmosphere, long transmission distance, and large transmission power. It is an industry with great application prospects. The transmitting end and the receiving end make up the MWPT. As shown in Figure 1, the transmitting end converts the DC energy into microwave energy and transmits the energy through the transmitting antenna. The receiving end functions to receive the microwave energy through the rectifying antenna converted to DC energy to supply the load [2–5]. Microwave source generates microwave energy (power) into free space
through transmitting antenna. The receiving antenna converts the captured energy into DC energy and delivers it to the rectifier circuit load.

At present, the core components used in the rectifier circuit of microwave wireless energy transmission system are commonly used by Agilent’s HSMS-282X, HSMS-285X, HSMS-281X, and HSMS-286X Ge-based Schottky diodes, which can cover low energy density to high energy density applications [6–8]. Compared with Ge semiconductor, strained Ge semiconductor on Si substrate (s-Ge/Si) has the advantages of compatibility with Si process, low cost, and high electron mobility [9–12]. It is an ideal replacement material for Ge semiconductor applications. As shown in Figure 2, Ge layer has tension. The thermal expansion coefficients of Si and Ge are different. The 0.2% tensile strain is introduced into the Ge epitaxial layer during annealing, resulting in band structure change and mobility enhancement.

In view of this, firstly, this paper uses kp perturbation theory and Monte Carlo simulation method to establish s-Ge/Si band structure and electron mobility model. On this basis, the Silvaco TCAD simulation tool is used, and a relationship model between s-Ge/Si Schottky diode performance and device geometry parameters and material physical parameters was established. An s-Ge/Si suitable for the MWPT system is the proposed Schottky diode device structure. The purpose of this paper is to explore the feasibility of s-Ge/Si replacement for Ge Schottky diodes and provide a valuable reference for the design and development of core components of MWPT system rectifier circuits.

2. Strained Ge Semiconductor on Si Substrate Band and Electron Mobility

Energy band structure and electron mobility are one of the theoretical foundations for research and design based on s-Ge/Si Schottky diodes. At present, the quantitative conclusions of s-Ge/Si semiconductor electron mobility are still lacking. Thus, this section first uses the kp perturbation theory to establish the s-Ge/Si band structure model (for details, see [11–14]) and further gives the electron mobility model of s-Ge/Si semiconductor. Under the one-electron approximation of periodic potential energy, the Schrödinger equation for strained Ge materials has the following form:

$$\begin{align} 
\left\{ \frac{\hbar^2}{2m^*_f} \frac{\partial^2}{\partial \mathbf{r}^2} + U_{\text{unstrain}}(r) + U_{\text{Deformation}}(r) \right\} \Psi(r) &= e\Psi(r). 
\end{align}$$

In formula (1), $U_{\text{unstrain}}(r)$ represents the lattice periodicity potential field of relaxed Ge material, and $U_{\text{Deformation}}(r)$ represents the lattice deformation potential field. The eigen function of (1) has the form of a Bloch wave function, which is $\Psi(\mathbf{k}) = e^{i\mathbf{k} \cdot \mathbf{r}_{\text{unstrain}}} \Psi(\mathbf{r})$, where the wave vector $k$ varies throughout the Brillouin region.

Applying the steady-state perturbation theory, the zero-order wave function is used to expand any one of the extreme values of the conduction band energy valley. Finally, the analytical model of the conduction band $E-k$ relationship of the strained Ge material is obtained as follows:

$$
E'(k) = E_c(k_0) + U_{k_i} + \frac{\hbar^2}{2} \left[ \frac{(k_x - k_{0x})^2}{m^*_i} + \frac{(k_y - k_{0y})^2}{m^*_i} + \frac{(k_z - k_{0z})^2}{m^*_i} \right].
$$

(2)

In the formula, $E_c(k_0)$ is the bottom energy valley energy level of the relaxed Ge conduction band, $(k_{0x}, k_{0y}, k_{0z})$ is the $k$-vector position of the bottom energy valley energy level of the conduction band, $m^*_i$ is the longitudinal effective electron mass, and $m^*_f$ is the transverse electron effective mass. $U_{k_i}$ can be obtained from the deformation potential theory:

$$
H_{\epsilon,\nu} = \Xi_d \epsilon_{xx} + \Xi_d \epsilon_{yy} + \Xi_d \epsilon_{zz} + \Xi_d \epsilon_{xy}.
$$

(3)

Among them, $\nu = x, y, z, \Xi_d$ and $\Xi_u$ are deformation potential constants, $\epsilon_{xx}, \epsilon_{yy}, \epsilon_{zz}, \epsilon_{xy}$ are strain tensors, and their expressions are determined by the deformation potential model. The strain tensor results of the (001) substrate, (101) substrate, and (111) substrate are shown in (4) to (6) below, where the parameters in the formula are arranged in Table 1.
energy diagram of the 
energy valley. L’he two figures on the right correspond to 
abscissa is about 0.21%, the ordinate corresponds to the 
conduction band 
Γ electron effective mass isoenergy (the constant energy contours). 

the strained Ge energy bands and the changes in stress can be 
drawn. Figure 3 shows the conduction band energy band diagram of the s-Ge/Si device and the corresponding 
electron effective mass isoenergy (the constant energy contours).

Figure 3 shows the energy levels of the strain energy 
conduction band Γ energy valley, L energy valley, and Δ energy valley. When the relative strain intensity on the 
absissa is about 0.21%, the ordinate corresponds to the 
energy level values of the strain Ge conductance 
band energy valley. The two figures on the right correspond to 
the effective energy isoenergy diagram of the L energy 
valley electron is ellipsoidal; the effective energy iso-
energy diagram of the Γ energy valley electron is spherical, 
and its effective mass is shown to be isotropic.

The simulation method of Monte Carlo is used to 
establish its electron mobility model. It is a numerical analysis 
method commonly used in the research of semiconductor 
carrier transport mechanisms. The effect of some random 
independent events (such as scattering events) on the carrier 
transport results is simulated by randomly taking some 
parameters within a certain range. Since the Schottky diode 
is a majority carrier device, the electron mobility is con-sidered. For the s-Ge/Si electron scattering mechanism, 
there are mainly the following: lattice scattering, ionized 
impurity scattering, and intervalley phonon scattering [12, 13]:

\[
P_{ac} = \frac{2^{1/2} m^{3/2} k_B T_c \sqrt{2}}{\pi \hbar^2 \epsilon_c L} E^{1/2},
\]

\[
P_{II} = \frac{\sqrt{2} m^2 e^3}{\pi \hbar^2 n (8 m \epsilon_c E K^2 T^2 + \hbar^2 e^2 n)}.
\]

Based on the analytical model of the E-k relationship of 
the strained Ge conduction bands of (1) and (2), the 
functional relationship between the physical parameters of 
the strained Ge energy bands and the changes in stress can be 
drawn. Figure 3 shows the conduction band energy band diagram of the s-Ge/Si device and the corresponding 
electron effective mass isoenergy (the constant energy contours).

In equations (7) – (9) P_{ac}, P_{II}, and P_{im}, respectively, 
represent acoustic phonon scattering, ionized impurity scattering, and intervalley phonon scattering; Ξ is the 
deformation potential constant, and m’ is the effective mass 
of the density of electronic states. Table 2 shows the specific 
values of other parameters.

This paper uses Monte Carlo method and electron 
scattering mechanism to simulate the carrier transport 
process. The result is shown in Figure 4.

Figures 4(a) and 4(b) show the relationship between 
the average electron energy and drift velocity in s-Ge/Si with the 
applied electric field strength under different strain levels. As 
shown in Figures 4(c) and 4(d), at the same energy level, 
the scattering rate of the ionized impurity in the conduction 
band of the strained Ge material decreases with the increase 
of the tensile strain. In contrast to the acoustic phonon 
scattering, electron acoustic phonon scattering rate of the 
conduction band of strained Ge material increases with 
increasing tensile strain. It can be seen from Figure 4(e) that, 
with the increase of the electric field strength, the average 
electron energy also increases, and the electron drift speed 
increases rapidly before the electric field strength reaches the 
order of 10^3 V/cm, and then gradually becomes saturated. 
However, under different strains, the variation curves 
slightly increased, and the values on the curves produced 
random fluctuations. As shown in Figure 4(f), the rela-
tionship between the conduction band electron mobility in 
s-Ge/Si and the strain is obtained. The conduction band 
mobility of the strained Ge material increases only slightly 
with the increase of the stress during the tensile loading, 
and the highest is 4130 cm^2/Vs. Comparing 4(e) and 4(f), we can 
see that the trends are consistent, as s-Ge/Si devices increase 
in stress, and their electron mobility also increases.

3. Strained Ge Semiconductor on Si Substrate 
Schottky Diode

According to the kp perturbation theory and Monte Carlo 
simulation method in the second section, the s-Ge/Si band 
structure and electron mobility model are established, and 
the mobility of the epitaxial strain Ge on the Si substrate is 
4130 cm^2/Vs. The maximum reverse breakdown voltage of 
the Schottky diode is designed to be 15 V, and the zero-bias 
capacitance of the special diode is 0.7 pF.

According to the spice parameter of the above device, the 
physical parameters of the material of the s-Ge/Si Schottky 
diode can be calculated as follows:

Table 1: Coefficient of elastic stiffness of IV semiconductor 
material.

<table>
<thead>
<tr>
<th>dyn/cm² (×10¹¹)</th>
<th>C_{11}</th>
<th>C_{12}</th>
<th>C_{44}</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si</td>
<td>16.56</td>
<td>6.39</td>
<td>7.95</td>
</tr>
<tr>
<td>Ge</td>
<td>12.87</td>
<td>4.77</td>
<td>6.67</td>
</tr>
</tbody>
</table>

\[
P_{im} = \frac{D_i^2 (m')^{3/2} Z_f}{2^{1/2} \pi \hbar^2 \rho \omega_i} \left( N_i + \frac{1}{2} + \frac{1}{2} \right) \left( E \pm \hbar \omega_i - \Delta E_{f, l} \right)^{1/2}.
\]
Doping concentration of the epitaxial layer: 
\[ N_d = 6 \times 10^{-17} \text{ cm}^{-3} \]

Minimum epitaxial layer thickness: \( t_{epi} \approx 0.7 \mu \text{m} \)

The thickness of the epitaxial layer is calculated to be 0.7 \( \mu \text{m} \). In order to prevent breakdown of the Schottky diode, the thickness of the epitaxial layer of the Schottky diode is 1 \( \mu \text{m} \). According to the above spice parameters and physical parameters of the material in s-Ge/Si Schottky diodes, the mobility of Ge is about three times that of Si. In order to ensure a relatively large current, a lateral Schottky diode structure is used. The left side lightly blends with the metal to form a Schottky contact, and the proportion of light blending needs to be properly adjusted. The right side is heavily doped to form an ohmic contact.

The light doping and heavy doping are separated by a silicon dioxide insulating layer, and the distribution of the electric field can be adjusted. To obtain a better current-voltage curve, the lateral structure of the Schottky diode is used as a buffer layer under light doping and redoping to prevent device breakdown [11–14], and the device structure is simulated in Silvaco TCAD software. The concentration distribution of the device structure is shown in Figure 5.

The s-Ge/Si Schottky diode applies a potential distribution inside the diode when the forward voltage is turned on, as shown in Figure 6.

It can be seen from Figure 6 that, from the anode to the cathode, the potential of inside the device generally decreases first and then increases, and the potential of the heavily doped region remains unchanged. The potential near the anode rises first and then decreases, and this distribution is consistent with the principle of metal to semiconductor contact. At the interface with different doping concentrations, the potential change is obvious because the original Fermi level is different. The substrate layer is charged with a high potential near the anode, and a low potential is applied near the cathode, which tends to become gradually lower.

When a positive voltage is applied according to the s-Ge/Si Schottky diode anode, the characteristic curve of the device is obtained by scanning the forward voltage as shown in Figure 7.

From the I-V curve of the s-Ge/Si Schottky diode in Figure 7, the internal resistance of the s-Ge/Si Schottky diode can be extracted using the Model Editor of OrCAD software, \( R_{s-Ge/Si} = 5.2 \Omega \). It can be seen that the internal resistance \( R \) of the s-Ge/Si Schottky diode is reduced. Secondly, the reverse breakdown characteristics and C-V characteristics of the device can be simulated in Silvaco software, as shown in Figures 8 and 9.

It can be seen from Figures 8 and 9 that the breakdown voltage of the s-Ge/Si Schottky diode is \( B_V = 15 \text{V} \), and the zero-bias capacitance is \( C_{j0} = 7 \times 10^{-13} \text{F} \).

In summary, compared with s-Ge/Si Schottky diodes and commercial Ge Schottky diodes, the introduction of
Figure 4: s-Ge/Si Monte Carlo and electron scattering mechanism simulation carrier transport results. (a) The average electron energy of s-Ge/Si under different strains varies with the applied electric field. (b) The average electron drift speed of s-Ge/Si under different strains varies with the applied electric field. (c) The relationship between the scattering rate of s-Ge/Si electron ionized impurities and the strain. (d) s-Ge/Si electronic acoustic phonon scattering rate as a function of strain. (e) s-Ge/Si average mobility changes with strain. (f) s-Ge/Si electron mobility as a function of strain.
strained Ge in the s-Ge/Si Schottky diode device structure proposed in this paper can improve the electron mobility of the device and the internal resistance is reduced. It does not affect the zero offset capacitance and reverse breakdown voltage of the device.

4. Strained Ge Semiconductor on Si Substrate Schottky Diode ADS Emulation

According to the s-Ge/Si Schottky diode device structure and device parameters in the third section, the device is used in the rectifier circuit of the MWPT system. Figure 10 shows the design of the rectifier circuit.

\[
\eta_{\text{eff}} = \frac{P_{\text{DC}}}{P_t} \times 100\%.
\]

\( P_{\text{in}} \) is the maximum possible input power that can be input, \( P_{\text{DC}} \) is the power absorbed by the load, \( P_t \) is the power loss in the case of impedance mismatch, and \( P_t \) is the input power of the Schottky diode [3]. According to the rectification circuit of Figure 11, ADS software simulation is used to obtain a series load resistor and capacitor with better transmission efficiency in the rectifier circuit. Figure 12 shows the rectification efficiency of different capacitors in the rectifier circuit. Using the impedance self-matching model, the conversion efficiency of the Schottky diode in the rectifier circuit can be defined as follows:
Figure 8: s-Ge/Si Schottky diode breakdown characteristics.

Figure 9: s-Ge/Si Schottky diode C-V curve.

Figure 10: s-Ge/Si Schottky diode harmonic balance.
It can be seen from Figure 12 that when the load resistance is 50 Ω, when \( C = 100 \text{ pF} \) and \( C = 470 \text{ pF} \), the conversion efficiency applied in the microwave rectifier circuit is basically the same. When the load capacitance \( C = 1 \text{ pF} \) and \( C = 100 \text{ pF} \), the conversion efficiency in the microwave rectifier circuit is significantly different. Therefore, the capacitance load is selected in the microwave rectifier circuit as \( C = 100 \text{ pF} \).

As shown in Figure 13, the better load capacitance is \( C = 100 \text{ pF} \), using different load resistances \( R = 50 \Omega, 100 \Omega, 1000 \Omega, 1500 \Omega, 3000 \Omega, \) and \( 5000 \Omega \) in the rectifier circuit, and the conversion efficiency reaches the maximum at 1000 Ω. Therefore, the better load in the simulation of the...
ADS microwave rectifier circuit is $R = 1000 \Omega$.

In summary, the optimal load capacitance $C = 100 \text{pF}$ and the better load resistance $R = 1000 \Omega$ are selected in the microwave rectifier circuit of the MWPT system. Rectifier diodes use Agilent’s Ge diodes, and the rectification efficiency is obtained as shown in Figure 14.

The s-Ge/Si Schottky diode model is applied to the rectifier circuit, as shown in Figure 10 for the strained Ge Schottky diode harmonic balance simulation. In the ADS software, the RF frequency is kept at 2.45 GHz, the optimal resistance and capacitance are selected to be 1000 Ohm and 100 pF respectively, and then the frequency is linearly harmonic balanced, and the simulation results are shown in Figure 15.

As can be seen from Figure 15, s-Ge/Si is applied to the microwave rectifier circuit, and the conversion efficiency in the rectifier circuit is 70.1%. It can be seen that the epitaxial strain Ge on Si substrate can be applied to rectifier circuits in microwave wireless energy transmission systems, and the conversion efficiency is improved compared to the commercial Ge Schottky diode.

5. Conclusion

This paper studies the use of s-Ge/Si Schottky diodes instead of traditional Ge Schottky diodes in rectifier circuits for wireless energy transfer. Firstly, the kp perturbation theory is used to establish the s-Ge/Si band structure model, and the electron mobility model of s-Ge/Si semiconductor is further given. The results show that the introduction of 0.2% stress in s-Ge/Si can increase the electron mobility, and the s-Ge/Si Schottky diodes are based on Si-compatible technology and are easy to integrate. Then, using Silvaco TCAD simulation tool, a relationship model was established between s-Ge/Si Schottky diode performance and device geometry parameters and material physical parameters, and s-Ge/Si Schottky diode device structure is proposed. At the same time, the Schottky diode model is applied to the rectifier circuit of the microwave wireless energy transmission system. The simulation of the rectifier circuit is carried out by using ADS software. Simulation results show that the strained Ge semiconductor on Si substrate Schottky diode has a rectification efficiency of 70.1% when the input of the rectifier circuit is 20 dBm, the load resistance is $R = 1000 \Omega$, and the load capacitance is $C = 100 \text{pF}$. Compared with traditional Ge Schottky diodes, this optimal operating point is closer to a low energy density, which is beneficial to a wide range of energy absorption. Finally, the results show that the feasibility of the replacement of Ge Schottky diode can be realized, and the conversion efficiency applied in the rectifier circuit is improved compared with the conventional Ge Schottky diode. Therefore, this paper can provide a valuable reference for the design and development of the core components of MWPT system rectifier circuit.

Data Availability

All data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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