Review Article

Evidence and Search for Sterile Neutrinos at Accelerators

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The LSND short-baseline neutrino experiment has published evidence for antineutrino oscillations at a mass scale of $\sim 1\text{eV}^2$. The MiniBooNE experiment, designed to test this evidence for oscillations at an order of magnitude higher neutrino energy and distance, observes excesses of events in both neutrino mode and antineutrino mode. While the MiniBooNE neutrino excess has a neutrino energy spectrum that is softer than expected from LSND, the MiniBooNE antineutrino excess is consistent with neutrino oscillations and with the LSND oscillation signal. When combined with oscillation measurements at the solar and atmospheric mass scales, assuming that the LSND and MiniBooNE signals are due to neutrino oscillations, these experiments imply the existence of more than three neutrino mass states and, therefore, one or more sterile neutrinos. Such sterile neutrinos, if proven to exist, would have a big impact on particle physics, nuclear physics, and astrophysics and would contribute to the dark matter of the universe. Future experiments under construction or proposed at Fermilab, ORNL, CERN, and in Japan will provide a definitive test of short-baseline neutrino oscillations and will have the capability of proving the existence of sterile neutrinos.

1. Introduction

Neutrino oscillations have been clearly observed at the solar mass scale of $\Delta m^2 \sim 7.5 \times 10^{-5}\text{eV}^2$ and the atmospheric mass scale of $\Delta m^2 \sim 2.4 \times 10^{-3}\text{eV}^2$ [1]. However, evidence for neutrino oscillations at the $\Delta m^2 \sim 1\text{eV}^2$ mass scale has also been given by the LSND [2–6] and MiniBooNE [7–9] experiments. If the signals reported by LSND and MiniBooNE are indeed due to neutrino oscillations, then there is a problem with the three-neutrino paradigm, because it is not possible to explain oscillations at the three different mass scales with only three types of neutrinos. In order to solve this problem, additional “sterile” neutrinos have been proposed [10–14]. Other explanations include, for example, Lorentz violation [15, 16] and sterile neutrino decay [17, 18]. These additional neutrinos would need to be sterile to the weak interaction due to measurements of the width of the $Z^0$ boson, which determine that there are three and only three active neutrinos [19]. The evidence for neutrino oscillations from LSND and MiniBooNE will be discussed in the following sections, followed by a discussion of global fits to the world data and future experiments, which will have the capability of proving whether short-baseline neutrino oscillations at the $\sim 1\text{eV}^2$ mass scale and light, sterile neutrinos exist in nature.

2. The LSND Experiment

The LSND experiment [20] was designed to search for $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ oscillations with high sensitivity and to measure $\sigma C$ cross-sections. A photograph of the inside of the detector tank is shown in Figure 1. The main characteristics of the LSND experiment are given in Table 1. LSND had the advantage of a very high proton intensity, a large detector mass, and good particle identification. LSND made use of a high-intensity, 798 MeV proton beam that interacted in an absorber to produce a large number of pions.

2.1. Neutrino Beam. LSND made use of the LAMPF accelerator, which was an intense source of low energy neutrinos produced with a proton current of 1 mA at 798 MeV kinetic energy. For the 1993–1995 running period, the production target consisted of a 30 cm long water target (20 cm in 1993) followed by a water-cooled Cu beam dump, while for the 1996–1998 running period, the production target was
Table 1: The main characteristics of the LSND and MiniBooNE experiments. Also the estimated number of neutrino background events and signal events for 100% $\nu_{\mu} \rightarrow \nu_e$ transmutation are shown. The $R_{\nu} > 10$ requirement is assumed for the LSND events.

<table>
<thead>
<tr>
<th>Property</th>
<th>LSND</th>
<th>MiniBooNE $\nu$</th>
<th>MiniBooNE $\bar{\nu}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proton energy</td>
<td>798 MeV</td>
<td>8000 MeV</td>
<td>8000 MeV</td>
</tr>
<tr>
<td>Proton intensity</td>
<td>1000 $\mu$A</td>
<td>4 $\mu$A</td>
<td>4 $\mu$A</td>
</tr>
<tr>
<td>Proton beam power</td>
<td>798 kW</td>
<td>32 kW</td>
<td>32 kW</td>
</tr>
<tr>
<td>Protons on target</td>
<td>28,896 C</td>
<td>104 C</td>
<td>181 C</td>
</tr>
<tr>
<td>Duty factor</td>
<td>$6 \times 10^{-2}$</td>
<td>$8 \times 10^{-6}$</td>
<td>$8 \times 10^{-6}$</td>
</tr>
<tr>
<td>Total mass</td>
<td>167 t</td>
<td>806 t</td>
<td>806 t</td>
</tr>
<tr>
<td>Neutrino distance</td>
<td>30 m</td>
<td>541 m</td>
<td>541 m</td>
</tr>
<tr>
<td>100% $\nu_{\mu} \rightarrow \nu_e$ events</td>
<td>12,987</td>
<td>89,615</td>
<td>38,462</td>
</tr>
<tr>
<td>$\nu$ background events</td>
<td>16.9</td>
<td>797.7</td>
<td>398.2</td>
</tr>
</tbody>
</table>

Figure 1: A photograph of the inside of the LSND detector tank.

reconfigured with the water target replaced by a close-packed, high-Z target. The resulting decay-at-rest (DAR) neutrino fluxes are well understood because almost all detectable neutrinos arise from $\pi^+$ or $\mu^+$ decay; $\pi^-$ and $\mu^-$ that stop are readily captured in the Fe of the shielding and Cu of the beam stop [21, 22]. The production of kaons or heavier mesons is negligible at these proton energies. The primary oscillation search in LSND is for $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$ oscillations, where the $\bar{\nu}_{\mu}$ arise from $\mu^+$ DAR in the beam stop and the $\bar{\nu}_e$ are identified through the reaction $\bar{\nu}_e p \rightarrow e^+ n$. This reaction allows a two-fold signature of a positron with a 52.8 MeV endpoint and a correlated 2.2 MeV $\gamma$ from neutron capture on a free proton. The veto shield enclosed the detector on all sides except the bottom. Additional counters were placed below the veto shield after the 1993 run to reduce cosmic-ray background entering through the bottom support structure. The main veto shield [24] consisted of a 15 cm layer of liquid scintillator in an external tank and a 15 cm of lead shot in an internal tank. This combination of active and passive shielding tagged cosmic-ray muons that stopped in the lead shot. A veto inefficiency of $<10^{-5}$ was achieved for incident charged particles.

2.2. Detector. The LSND detector [20] consisted of an approximately cylindrical tank 8.3 m long by 5.7 m in diameter. A schematic drawing of the detector is shown in Figure 3. The center of the detector was 30 m away from the neutrino source. On the inside surface of the tank, 1220 8-inch Hamamatsu PMTs covered 25% of the area with photocathode. The tank was filled with 167 t of liquid scintillator consisting of mineral oil and 0.031 g/L of b-PBD. This low scintillator concentration allows the detection of both Cherenkov light and scintillation light and yields an attenuation length of more than 20 m for wavelengths greater than 400 nm [23]. A typical 45 MeV electron created in the detector produced a total of ~1500 photoelectrons, of which ~280 photoelectrons were in the Cherenkov cone. PMT time and pulse-height signals were used to reconstruct particle tracks with an average RMS position resolution of ~14 cm, an angular resolution of ~12°, and an energy resolution of ~7% at the Michel endpoint of 52.8 MeV. The Cherenkov cone for relativistic particles and the time distribution of the light, which is broader for nonrelativistic particles [20], gave excellent separation between electrons and particles below Cherenkov threshold. Identification of neutrons was accomplished through the detection of the 2.2 MeV $\gamma$ from neutron capture on a free proton. The veto shield enclosed the detector on all sides except the bottom. Additional counters were placed below the veto shield after the 1993 run to reduce cosmic-ray background entering through the bottom support structure. The main veto shield [24] consisted of a 15 cm layer of liquid scintillator in an external tank and a 15 cm of lead shot in an internal tank. This combination of active and passive shielding tagged cosmic-ray muons that stopped in the lead shot. A veto inefficiency of $<10^{-5}$ was achieved for incident charged particles.

2.3. Oscillation Results. The primary oscillation search in LSND is for $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$ oscillations, where the $\bar{\nu}_{\mu}$ arise from $\mu^+$ DAR in the beam stop and the $\bar{\nu}_e$ are identified through the reaction $\bar{\nu}_e p \rightarrow e^+ n$. This reaction allows a two-fold signature of a positron with a 52.8 MeV endpoint and a correlated 2.2 MeV $\gamma$ from neutron capture on a free proton. There are only two significant neutrino backgrounds with a positron/electron and a correlated neutron. The first background is from $\mu^-$ DAR in the beam stop followed by $\bar{\nu}_e p \rightarrow e^+ n$ scattering in the detector. This background is highly suppressed due to the requirements that a $\pi^-$ be produced, the $\pi^-$ decays in flight, and the $\mu^-$ decays at rest prior to capture. The second background is from $\pi^-$ decay in flight (DIF) in the beam stop followed by $\bar{\nu}_\mu p \rightarrow \mu^+ n$ scattering in the detector. Additional contributions are from $\bar{\nu}_\mu C \rightarrow \mu^+ nX$ and $\nu_e C \rightarrow \mu^- nX$. This background will mimic the oscillation reaction if the $\mu^+$ is...
Figure 2: The neutrino energy spectra from π⁺ and μ⁺ DAR.

Figure 3: A schematic drawing of the LSND detector.

Table 2 shows the estimated number of events in the 20 < $E_e$ < 60 MeV energy range due to 100% $\mu^+ \rightarrow e^+$ transmutation and for the two beam-related backgrounds with neutrons.

Table 3 shows the LSND statistics for events that satisfy the electron selection criteria for the primary $\mu \rightarrow e$ oscillation search. An excess of events is observed over that expected from beam-off and neutrino background that is consistent with neutrino oscillations [2–6]. A $\chi^2$ fit to the $R_\gamma$ distribution, as shown in Figure 4, gives $f_c = 0.0567 \pm 0.0108$ ($\chi^2 = 10.7/9$ DOF), which leads to a beam on-off excess of 117.9 ± 22.4 events with a correlated neutron. $R_\gamma$ is the likelihood that the $\gamma$ is a correlated $\gamma$ from neutron capture divided by the likelihood that the $\gamma$ is an accidental $\gamma$, while $f_c$ is the fraction of electron candidate events with a correlated $\gamma$.

Subtracting the neutrino background from $\mu^-$ DAR followed by $\bar{\nu}_e p \rightarrow e^+ n$ scattering (19.5 ± 3.9 events) and $\pi^-$ DIF followed by $\bar{\nu}_\mu p \rightarrow \mu^+ n$ scattering (10.5 ± 4.6 events) (this background also includes contributions from $\bar{\nu}_\mu C \rightarrow \mu^+ nX$ and $\bar{\nu}_\mu C \rightarrow \mu^- nX$) leads to a total excess of 87.9 ± 22.4 ± 6.0 events. This excess corresponds to an oscillation probability of (0.264 ± 0.067 ± 0.045)% , where the first error is statistical and the second error is the systematic error arising from uncertainties in the backgrounds, neutrino flux (7%), $e^+$ efficiency (7%), and $\gamma$ efficiency (7%).

A clean sample of oscillation candidate events can be obtained by requiring $R_\gamma > 10$, where, as shown in Table 3, the beam on-off excess is 49.1 ± 9.4 events, while the estimated neutrino background is only 16.9 ± 2.3 events. Figure 5 displays the energy distribution of events with $R_\gamma > 10$. The shaded regions show the combination of neutrino background plus neutrino oscillations at low $\Delta m^2$. The data agree well with the oscillation hypothesis. Finally, Figure 6 shows the $L/E_e$ distribution for events with $R_\gamma > 10$ and

Table 2: The LSND estimated number of events in the 20 < $E_e$ < 60 MeV energy range due to 100% $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ transmutaion and the two beam-related backgrounds with neutrons, $\mu^-$ DAR in the beam stop followed by $\bar{\nu}_e p \rightarrow e^+ n$ scattering in the detector and $\pi^-$ DIF in the beam stop followed by $\bar{\nu}_\mu p \rightarrow \mu^+ n$ scattering. The events must satisfy the electron selection criteria, but no correlated $\gamma$ requirement is imposed.

<table>
<thead>
<tr>
<th>Neutrino source</th>
<th>Reaction</th>
<th>Number of events</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mu^+$ DAR</td>
<td>$100% \bar{\nu}_\mu \rightarrow \bar{\nu}_e$</td>
<td>33300 ± 3300</td>
</tr>
<tr>
<td>$\mu^-$ DAR</td>
<td>$\bar{\nu}_e p \rightarrow e^+ n$</td>
<td>19.5 ± 3.9</td>
</tr>
<tr>
<td>$\pi^-$ DIF</td>
<td>$\bar{\nu}_\mu p \rightarrow \mu^+ n$</td>
<td>10.5 ± 4.6</td>
</tr>
</tbody>
</table>

sufficiently low in energy that it is below the threshold of 18 hit PMTs, corresponding to $E_\mu < 4$ MeV. Table 2 shows the estimated number of events in the 20 < $E_e$ < 60 MeV energy range satisfying the electron selection criteria for 100% $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ transmutation and for the two beam-related backgrounds with neutrons.
Table 3: Numbers of LSND beam-on events that satisfy the selection criteria for the primary $\overline{\nu}_\mu \rightarrow \overline{\nu}_e$ oscillation search with $R_\gamma > 1$, $R_\gamma > 10$, and $R_\gamma > 100$. Also the beam-off background, the estimated neutrino background, and the excess of events that is consistent with neutrino oscillations are shown.

<table>
<thead>
<tr>
<th>Selection</th>
<th>Beam-on events</th>
<th>Beam-off background</th>
<th>$\nu$ background</th>
<th>Event excess</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_\gamma &gt; 1$</td>
<td>205</td>
<td>106.8 ± 2.5</td>
<td>39.2 ± 3.1</td>
<td>59.0 ± 14.5 ± 3.1</td>
</tr>
<tr>
<td>$R_\gamma &gt; 10$</td>
<td>86</td>
<td>36.9 ± 1.5</td>
<td>16.9 ± 2.3</td>
<td>32.2 ± 9.4 ± 2.3</td>
</tr>
<tr>
<td>$R_\gamma &gt; 100$</td>
<td>27</td>
<td>8.3 ± 0.7</td>
<td>5.4 ± 1.0</td>
<td>13.3 ± 5.2 ± 1.0</td>
</tr>
</tbody>
</table>

Figure 4: The LSND $R_\gamma$ distribution for events that satisfy the selection criteria for the primary $\overline{\nu}_\mu \rightarrow \overline{\nu}_e$ oscillation search.

20 $< E_e <$ 60 MeV, where $L$ is the distance travelled by the neutrino in meters and $E_e$ is the neutrino energy in MeV determined from the measured positron energy and angle with respect to the neutrino beam. The data agree well with the expectation from neutrino background plus neutrino oscillations at low $\Delta m^2$ ($\chi^2 = 4.9/8$ D.O.F.) or high $\Delta m^2$ ($\chi^2 = 5.8/8$ D.O.F.).

The $\left(\sin^2 2\theta, \Delta m^2 \right)$ likelihood ($\mathcal{L}$) fitter is applied to beam-on events in the final oscillation sample and calculates a likelihood in the $\left(\sin^2 2\theta, \Delta m^2 \right)$ plane in order to extract the favored oscillation parameters. The $\mathcal{L}$ product in the $\left(\sin^2 2\theta, \Delta m^2 \right)$ plane is formed over the individual beam-on events that pass the oscillation cuts. This three-dimensional contour is sliced to arrive finally at the LSND allowed oscillation region. The beam-related backgrounds are determined from Monte Carlo (MC) event samples for each individual background contribution. The MC contains the trigger simulation and generally very well reproduces the tank response to all particles of interest. Agreement between the data and MC is excellent.

Figure 5: The LSND electron energy distribution for events with $R_\gamma > 10$. The shaded region shows the expected distribution from a combination of neutrino background plus neutrino oscillations at low $\Delta m^2$.

The $(\sin^2 2\theta, \Delta m^2)$ oscillation parameter fit for the entire data sample, 20 $< E_e <$ 200 MeV, is shown in Figure 7. The fit includes both $\overline{\nu}_\mu \rightarrow \overline{\nu}_e$ and $\nu_e \rightarrow \nu_e$ oscillations (although the latter contribution is very small), as well as all known neutrino backgrounds. The inner and outer regions correspond to 90% and 99% CL allowed regions, while the curves are 90% CL limits from the Bugey reactor experiment [25] and the KARMEN experiment at ISIS [26]. Note that the Bugey limit has been relaxed recently due to the reactor neutrino anomaly [27]. The most favored allowed region is the band from 0.2 to 2.0 eV$^2$, although a region around 7 eV$^2$ is also possible.

3. The MiniBooNE Experiment

The MiniBooNE experiment was designed to test the LSND neutrino oscillation signal with a neutrino energy and distance that were an order of magnitude higher than LSND but with an $L/E$ ratio that was approximately the same as for
Figure 6: The LSND $L/E_\nu$ distribution for events with $R_\gamma > 10$ and $20 < E_\nu < 60$ MeV, where $L$ is the distance travelled by the neutrino in meters and $E_\nu$ is the neutrino energy in MeV. The data agree well with the expectation from neutrino background and neutrino oscillations at low $\Delta m^2$.

Figure 7: The $(\sin^2 2\theta, \Delta m^2)$ oscillation parameter fit for the entire LSND data sample, $20 < E_\nu < 200$ MeV. The inner and outer regions correspond to 90% and 99% CL allowed regions, while the curves are 90% CL limits from the Bugey reactor experiment and the KARMEN experiment at ISIS.
LSND. Due to the higher neutrino energies, the backgrounds and systematic errors are completely different between the two experiments.

3.1. Neutrino Beam. A schematic drawing of the MiniBooNE experiment at FNAL is shown in Figure 8. The experiment is fed by 8 GeV kinetic energy protons from the Booster that interact in a 71 cm long Be target located at the upstream end of a magnetic focusing horn. The horn pulses with a current of 174 kA and, depending on the polarity, either focuses $\pi^+$ and $K^+$ and defocuses $\pi^-$ and $K^-$ to form a pure neutrino beam or focuses $\pi^-$ and $K^-$ and defocuses $\pi^+$ and $K^+$ to form a somewhat pure antineutrino beam. The produced pions and kaons decay in a 50 m long pipe, and a fraction of the neutrinos and antineutrinos [28] interact in the MiniBooNE detector, which is located 541 m downstream of the Be target. For the MiniBooNE results presented here, a total of $6.46 \times 10^{20}$ POT were collected in neutrino mode and $11.27 \times 10^{20}$ POT were collected in antineutrino mode.

3.2. Detector. The MiniBooNE detector [29] consists of a 12.2 m diameter spherical tank filled with approximately 806 tons of mineral oil (CH$_2$). A schematic drawing of the MiniBooNE detector is shown in Figure 9, while a photograph of the inside of the tank is shown in Figure 10. There are a total of 1280 8-inch detector phototubes (covering 10% of the surface area) and 240 veto phototubes. The fiducial volume has a 5 m radius and corresponds to approximately 450 tons. A comparison between the LSND and MiniBooNE experiments is given in Table 1.

3.3. Oscillation Results. Figure 11 shows the estimated neutrino fluxes for neutrino mode and antineutrino mode, respectively. The fluxes are fairly similar (the intrinsic electron-neutrino background is approximately 0.6% for both modes of running), although the wrong-sign contribution to the flux in antineutrino mode (~18%) is much larger than in neutrino mode (~6%). The average $\nu_e$ plus $\bar{\nu}_e$ energies are 0.96 GeV in neutrino mode and 0.77 GeV in antineutrino mode, while the average $\nu_\mu$ plus $\bar{\nu}_\mu$ energies are 0.79 GeV in neutrino mode and 0.66 GeV in antineutrino mode. The estimated backgrounds in the two modes are very similar, especially at low energy.

Figure 12 shows the reconstructed neutrino and antineutrino energy distributions, $E_{\nu}^{QE}$, for candidate $\nu_e$ and $\bar{\nu}_e$ data events (points with error bars) compared to the MC simulation (histogram) [7–9], while Figure 13 shows the event excesses in neutrino and antineutrino mode as a function of $E_{\nu}^{QE}$. $E_{\nu}^{QE}$ assumes that the events are due to charged-current quasi-elastic scattering. The magnitude and energy shape of the excess in antineutrino mode are very similar to what is expected from neutrino oscillations based on the LSND signal, as shown by the pink and green LSND reference.
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\[ \Phi(E_{1/32})(POT/\text{GeV/cm}^2) \]

\[ \begin{array}{cccc}
0 & 0.5 & 1 & 1.5 \\
0 & 0.5 & 1 & 1.5 \\
\end{array} \]

\[ \begin{array}{cccc}
E_{1/32} (\text{GeV}) & \text{\(\mu\)} & \text{\(\mu\)} & \text{\(e\)} & \text{\(e\)} \\
\end{array} \]

(a)

(b)

Figure 11: The estimated MiniBooNE neutrino fluxes for neutrino mode (a) and antineutrino mode (b).

**Figure 12:** The MiniBooNE neutrino mode (a) and antineutrino mode (b) neutrino energy distributions for \(\nu_e\) charged-current quasi-elastic data (points with statistical errors) and background (histogram with systematic errors).

In neutrino mode, the magnitude of the excess is consistent with LSND; however, the energy shape is softer than the pink and green LSND reference histograms.

Table 4 shows the number of data, background, and excess events for neutrino mode, antineutrino mode, and combined in the neutrino oscillation energy range from 200 to 1250 MeV. The uncertainties include both statistical and constrained systematic errors, where the \(\nu_{\mu}\) charged-current data sample is used to normalize the backgrounds. All known systematic errors are included in the systematic error estimate. In neutrino mode, an excess of 162.0 \(\pm\) 47.8 events, corresponding to 3.4\(\sigma\), is observed, while in antineutrino mode, the observed excess is 78.4 \(\pm\) 28.5 events, corresponding to 2.8\(\sigma\). Combining the data in neutrino and antineutrino modes, the total excess is 240.3 \(\pm\) 62.9 events, corresponding to 3.8\(\sigma\).

Figure 14 shows the MiniBooNE oscillation allowed regions [7–9] from fits to the antineutrino data (a) and neutrino data (b). In antineutrino mode, the probability of the best fit is good (66%, corresponding to a \(\chi^2/\text{ndf} = 5.0/7.0\)), and the MiniBooNE allowed region overlaps well with the LSND allowed region for \(\Delta m^2 < 1\ eV^2\), while the KARMEN experiment [26] rules out most of the LSND allowed region for \(\Delta m^2 > 2\ eV^2\). Therefore, the MiniBooNE antineutrino data are consistent with simple two-neutrino oscillations and
Figure 13: The MiniBooNE neutrino mode (a) and antineutrino mode (b) event excesses as a function of neutrino energy. Also the expectations from the best two-neutrino oscillation fits with neutrino energy from 200 to 3000 MeV and from two reference values in the LSND allowed region are shown. All known systematic errors are included in the systematic error estimate.

Table 4: The number of data, fitted (constrained) backgrounds, and excess events in the $\nu$ and $\bar{\nu}$ analyses for neutrino mode, antineutrino mode, and combined in the neutrino oscillation energy range from 200 to 1250 MeV. The uncertainties include both statistical and constrained systematic errors. All known systematic errors are included in the systematic error estimate.

<table>
<thead>
<tr>
<th>Mode</th>
<th>Data</th>
<th>Background</th>
<th>Excess</th>
</tr>
</thead>
<tbody>
<tr>
<td>Neutrino mode</td>
<td>952</td>
<td>790.0 ± 28.1 ± 38.7</td>
<td>162.0 ± 47.8</td>
</tr>
<tr>
<td>Antineutrino mode</td>
<td>478</td>
<td>399.6 ± 20.0 ± 20.3</td>
<td>78.4 ± 28.5</td>
</tr>
<tr>
<td>Combined</td>
<td>1430</td>
<td>1189.7 ± 34.5 ± 52.6</td>
<td>240.3 ± 62.9</td>
</tr>
</tbody>
</table>

with the LSND oscillation signal. In neutrino mode, the probability of the best fit is not as good (6.1%, corresponding to a $\chi^2$/ndf = 13.2/6, 8), and the MiniBooNE allowed region overlaps a smaller fraction of the LSND allowed region at low $\Delta m^2$, which is already ruled out by the ICARUS experiment [30]. Therefore, in neutrino mode, the data are marginally compatible with a simple two-neutrino oscillation formalism. Indeed, the initial MiniBooNE oscillation publication [34] showed that there is hardly any excess of events above 475 MeV in neutrino mode, ruling out simple two-neutrino oscillations as an explanation of the LSND signal. However, expanded models with several sterile neutrinos can reduce the incompatibility by allowing for CP violating effects between neutrino and antineutrino oscillations [10, 11].

Figure 15 shows the MiniBooNE oscillation allowed regions from a combined fit to the antineutrino plus neutrino data samples [35]. As in neutrino mode, the probability of the best fit is not very good (6.7%). However, as discussed above, expanded models with several sterile neutrinos can improve the fit probability by allowing for CP violating effects between neutrino and antineutrino oscillations [10, 11].

### 4. Global Neutrino Oscillation Analyses

Several global $3+N$ oscillation analyses have been performed on the world neutrino data that include both long-baseline and short-baseline oscillation experiments, including both $\nu_\mu \rightarrow \nu_e$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ appearance data and $\nu_\mu$ and $\bar{\nu}_\mu$ disappearance data [12]. In general, the analyses assume a model with 3 light, mostly active neutrinos, $N$ heavier, mostly sterile neutrinos, and $3+N$ neutrino mass eigenstates. Precision measurements of the $Z^0$ width have determined that the number of active neutrinos is approximately 3 ($2.984 \pm 0.008$ [19]), so that additional neutrinos beyond the three active neutrinos would need to be sterile to the weak interaction. Note that neutrino oscillations depend on the superposition of neutrino mass eigenstates and do not depend on whether neutrinos are active or sterile, so that the $3+N$ neutrino mass eigenstates would result in $2+N$ independent $\Delta m^2$ values. Note also that, for $N > 1$, there would exist CP violation parameters for both short-baseline and long-baseline experiments. Finally, note that, for $3+N$ models, neutrinos in general would be a superposition of both active and sterile components.

Table 5 shows the best fit values from recent $3+1$ global fits to the world neutrino data from [10, 11]. (Additional global fits can be found in [12].) Reference [10] includes data from the LSND, MiniBooNE, KARMEN, NOMAD, CCFR, CDHS, MINOS, Bugey, SAGE, and GALLEX experiments, while [11] also includes data from the E776 and ICARUS experiments. For both global fits, the best fit value of $\Delta m^2_{31}$ is $\sim 0.9$ eV$^2$ and the $\chi^2$ goodness of fit probabilities (GOF)
Figure 14: MiniBooNE allowed regions in antineutrino mode (a) and neutrino mode (b) for events with neutrino energy greater than 200 MeV within a two-neutrino oscillation model. Also the ICARUS [30] and KARMEN [26] appearance limits for neutrinos and antineutrinos are shown, respectively. The shaded areas show the 90% and 99% CL LSND $\nu_\mu \rightarrow \nu_e$ allowed regions. The black stars show the MiniBooNE best fit points, while the circles show two reference values in the LSND allowed region.

Table 6 shows the best fit values from recent 3 + 2 global fits to the world neutrino data from [10, 11]. (Additional global fits can be found in [12].) The GOF probabilities are improved from the 3 + 1 fits, although the PGOF probabilities are worse. As mentioned above, we believe that fake data studies would need to be performed in order to calculate the PGOF true probabilities [37].

Table 5: The best fit values from 3 + 1 global fits to the world neutrino data from [10, 11]. Also the goodness of fit probability (GOF) and the parameter goodness of fit probability (PGOF) [36] are shown.

| Ref. | $\Delta m^2_{41}$ (eV$^2$) | $|U_{\mu 4}|$ | $|U_{e 4}|$ | GOF  | PGOF  |
|------|----------------|----------|----------|------|--------|
| [10] | 0.92 | 0.15 | 0.17 | 55%  | 0.043% |
| [11] | 0.93 | 0.15 | 0.17 | 19%  | 0.012% |

At Fermilab, MINOS+ and MicroBooNE provide a well-coordinated program of experiments that should help determine in the near future whether or not sterile neutrinos can explain the existing short-baseline neutrino anomalies. MINOS+ involves running the MINOS detectors with the NuMI beam in medium energy mode for the NoVA experiment, which provides a much higher flux of neutrinos above a few GeV. High $\Delta m^2$ $\nu_\mu$ disappearance into sterile neutrinos can be searched for by comparing the event rates in the near and far detectors at higher energies, where the effect of neutrino oscillations at the atmospheric scale is small [38]. MINOS+ should begin taking data later in 2013. The MicroBooNE experiment is under construction in the Booster Neutrino Beam (BNB) just upstream of MiniBooNE at a distance of 0.47 km from the neutrino source. MicroBooNE [39] consists of a 170-ton (86-ton active volume) liquid argon TPC, that will be able to determine whether the 3.8$\sigma$ excess of events observed by MiniBooNE is due to electron events, as expected for $\nu_\mu \rightarrow \nu_e$ oscillations, or to photon

5. Future Short-Baseline Accelerator Neutrino Experiments

Future accelerator neutrino experiments will have the capability of testing the current evidence for sterile neutrinos.
Table 6: The best fit values from 3+2 global fits to the world neutrino data from [10, 11]. Also the goodness of fit probability (GOF) and the parameter goodness of fit probability (PGOF) are shown.

| Ref. | $\Delta m^2_{41}$ (eV$^2$) | $\Delta m^2_{51}$ (eV$^2$) | $|U_{e4}|$ | $|U_{\mu4}|$ | $|U_{e5}|$ | $|U_{\mu5}|$ | $\phi_{CP}$ | GOF | PGOF |
|------|-----------------|-----------------|-------|-------|-------|-------|---------|------|-------|
| [10] | 0.92            | 17              | 0.15  | 0.17  | 0.069 | 0.16  | $1.8\pi$ | 69%  | 0.0082% |
| [11] | 0.47            | 0.87            | 0.13  | 0.15  | 0.14  | 0.13  | $-0.15\pi$ | 23%  | 0.0034% |

Figure 15: MiniBooNE allowed regions in combined neutrino and antineutrino mode for events with neutrino energy from 200 to 3000 MeV within a two-neutrino $\mu \to e$ and $\mu \to e$ oscillation model. Also shown is the $\overline{\nu}_\mu \to \overline{\nu}_e$ limit from the KARMEN experiment [26]. The shaded areas show the 90% and 99% CL LSND $\overline{\nu}_\mu \to \overline{\nu}_e$ allowed regions. The black star shows the best fit point.

Figure 16: The 3 + 2 best fit $\Delta m^2_{41}$ versus $\Delta m^2_{51}$ values from [10].

Figure 17: The 3 + 2 and 1 + 3 + 1 best fit $\Delta m^2_{41}$ versus $\Delta m^2_{51}$ values from [11].

NuSTORM [31] is a far future proposal that involves building a muon storage ring with $\mu^-$ central momentum of 3.8 GeV/c, and it can be built at either Fermilab or CERN. NuSTORM produces fluxes of neutrinos with well-understood energy spectra: $\nu_\mu$ and $\overline{\nu}_\mu$ for a $\mu^-$ stored beam and $\overline{\nu}_\mu$ and $\nu_e$ for a stored $\mu^+$ beam. Two magnetized iron neutrino detectors will be built downstream of the storage ring at distances of ~30 m and ~1500 m in order to search for $\nu_e \to \nu_\mu$ appearance and $\nu_e$ and $\nu_\mu$ disappearance.
allowed LSND and MiniBooNE oscillation regions can be covered at the $10\sigma$ level, as shown in Figure 19.

ICARUS-NESSIE [32] is another far future proposal for an experiment at CERN to test the LSND and MiniBooNE oscillation signals. A new neutrino beamline would be built from the SPS with both near and far liquid argon TPC detectors (ICARUS) and muon spectrometers (NESSIE). The near detector location would be at a distance of 300 m from the neutrino source and would contain a 150-ton (T150) liquid argon TPC followed by a muon spectrometer with a dipole magnetic field and iron slabs. The far detector location would be at a distance of 1600 m from the neutrino source and would contain a 600-ton LAr TPC (T600) followed by a muon spectrometer. ICARUS-NESSIE will be able to search for both $\nu_\mu$ disappearance and $\nu_\tau$ appearance. Figure 20 shows the expected sensitivities for $\nu_\mu \rightarrow \nu_\tau$ oscillations (a) and $\overline{\nu}_\mu \rightarrow \overline{\nu}_\tau$ oscillations (b) after one year and two years of data taking, respectively. ICARUS-NESSIE will fully cover the LSND and MiniBooNE oscillation allowed regions.

The OscSNS and IsoDAR proposals offer the unique opportunity to observe actual oscillations in the detector (i.e., an oscillation of the number of events in the detector as a function of distance from the neutrino source, correcting for the $1/r^2$ falloff of the neutrino flux), which would be unmistakable proof for short baseline neutrino oscillations. The OscSNS proposal [40] involves building a cylindrical detector approximately 60 m from the SNS spallation target [41]. The 1.4 MW beam power of the SNS is a prodigious source of neutrinos from the decay of $\pi^+$ and $\mu^+$ at rest. These decays produce a well specified flux of neutrinos via $\pi^+ \rightarrow \mu^+\nu_\mu, \tau_\pi = 2.7 \times 10^{-8}$ s and $\mu^+ \rightarrow e^+\nu_e\overline{\nu}_\mu, \tau_\mu = 2.2 \times 10^{-6}$ s. The low duty factor of the SNS ($\sim695$ ns beam pulses at 60 Hz, $DF = 4.2 \times 10^{-5}$) is more than 1000 times less than that found at LAMPF. This smaller duty factor provides a reduction in backgrounds due to cosmic rays, and allows the $\nu_\mu$ induced events from $\pi^+$ decay to be separated from the $\nu_e$ and $\overline{\nu}_\mu$ induced events from $\mu^+$ decay. The OscSNS detector will be centered at a location 60 meters from the SNS target, in the backward direction. The cylindrical detector design is based upon the LSND and MiniBooNE detectors and will consist of an 800-ton tank of mineral oil (with a small concentration of b-PBD scintillator dissolved in the oil) that is covered by approximately 3500 8-inch phototubes, yielding a photocathode coverage of 25%. Figure 21 shows the expected sensitivity for $\overline{\nu}_e$ appearance after two and six calendar years of run time. The LSND allowed region is fully covered by more than $5\sigma$.

The IsoDAR proposal [33] involves the construction of a high-intensity proton cyclotron near an underground detector to search for $\overline{\nu}_e$ disappearance. The proposed cyclotron would accelerate $H^+_2$ ions up to 60 MeV/amu at an intensity of 5 mA. The 60 MeV proton beam then interacts on a $^8$Be target that is surrounded by a $^7$Li sleeve. Neutrons produced in the Be target interact in the sleeve to produce $^8$Be, which decay to produce $\overline{\nu}_e$ with an average energy of 6.4 MeV. The $\overline{\nu}_e$ can then interact in a kiloton underground detector, such as KamLAND [42] in Japan. By fitting for oscillations in the detector, IsoDAR would have excellent sensitivity to $\overline{\nu}_e$ disappearance, as shown in Figure 22.
6. Conclusions

The LSND and MiniBooNE experiments both observe excesses of $\nu_e$ candidate events at the 3.8$\sigma$ level. Combining these two experiments results in a total excess that is over 5$\sigma$ in significance. Whereas no standard model explanation for these excesses has yet been found, $3 + N$ oscillation models with 3 light, mostly active neutrinos and $N$ heavy, mostly sterile neutrinos provide a fairly good fit to the world neutrino oscillation data, although there is some tension at present between appearance and disappearance oscillation experiments. Future experiments at Fermilab, CERN, ORNL, and in Japan will test this neutrino oscillation evidence and have the potential to prove the existence of light, sterile neutrinos. Such sterile neutrinos would have a big impact on particle physics, nuclear physics, and astrophysics.
Figure 22: The sensitivity of the IsoDAR experiment to $\nu_e$ disappearance in a five-year physics run (from [33]).

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References


