Research Article

On Two-Ridge Structure in Two-Particle Azimuthal Correlations in Proton-Lead Collisions at Large Hadron Collider Energy

Fu-Hu Liu, Tian Tian, and Ya-Qin Gao

Institute of Theoretical Physics, Shanxi University, Taiyuan, Shanxi 030006, China

Correspondence should be addressed to Fu-Hu Liu; fuhuliu@163.com

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Two-particle azimuthal correlations are studied in the framework of a multisource thermal model. Each source is assumed to produce many particles. Each particle pair measured in final state is considered to be produced at two emission points (subsources) in a single or two sources. The first emission point corresponds to the production of “trigger” particle and the second one corresponds to that of “associated” particle. There are oscillations and other interactions between the two emission points. In the rest frame of the “associated” particle’s emission point, the oscillations and other interactions cause the momentum of the “trigger” particle to depart from the original value. The modelling results are in agreement with the experimental data of proton-lead (p -Pb) collisions at $\sqrt{s_{NN}} = 5.02$ TeV, one of the Large Hadron Collider energies, measured by the ALICE and ATLAS Collaborations.

1. Introduction

Two-particle correlations are important experimental phenomena in high energy collisions. These correlations contain azimuthal correlations, (pseudo)rapidity correlations, momentum correlations, and so on. As a type of long-range correlation, two-particle azimuthal correlations were studied in recent years. Particularly, at the eras of the Relativistic Heavy Ion Collider (RHIC) and the Large Hadron Collider (LHC), particle and nuclear physicists have been obtaining some interesting results on the azimuthal correlations in proton-proton (pp), proton-nucleus, and nucleus-nucleus collisions. Some features are observed in the three types of collisions.

For example, the first studies of two-particle azimuthal correlation function in highest-multiplicity pp collision at the LHC present an enhancement of particle pair production at relative azimuth $\Delta\phi \approx 0$, which results in a “ridge” structure at the “near-side” [1]. However, in peripheral proton-lead (p -Pb) collisions in which there are only a few nucleons to take part in the collisions and which are similar to pp collision, a ridge structure is observed at the “away-side” ($\Delta\phi \approx \pi$) [2]. The different results between pp and peripheral p -Pb collisions are possibly caused by the infection of nuclear

effects (spectator nucleons). In central p -Pb collisions, a double ridge structure is observed, which is consistent with Pb-Pb collisions [3].

To explain the near-side and away-side ridges, many physics mechanisms are proposed in literature, such as the parton saturation [4, 5], gluon saturation and color connections [6–11], parton-induced interactions [12–14], multiparton interactions [15], collective expansion of the final state [16], and collective effects arising in a high-density system [17–23]. If we regard a parton as an emission point and multiple emission points are assumed to form a source, the high energy collisions can be treated by a multisource interacting system. Thus, a multisource thermal model [24–26] can be considered in the studies of near-side and away-side ridges in the two-particle azimuthal correlations. The effects listed here are not completely included in this study, but the collective effect is included.

In this paper, in the framework of the multisource thermal model [24–26], we consider two emission points (subsources) in a single or two sources. The two emission points are assumed to emit respectively the “trigger” particle and the “associated” particle in a particle pair. After considering oscillations and other interactions between the two emission points, the azimuthal correlations are studied.

2. The Model and Method

In the multisource thermal model [24–26], we assume that many emission points (subsources) are formed in high energy collisions. These subsources can form a few sources which stay in local equilibrium states. The Maxwell, Boltzmann, and other distributions can be used to describe spectrums of final-state particles in which productions of particle pairs are included. For a particle pair measured in final state, both the two emission points take part in the production process. The two emission points may be in a single or two sources. The first emission point corresponds to the production of “trigger” particle and the second one corresponds to the production of “associated” particle. There are oscillations between the two emission points, which results in the momentum of produced particle to depart from the original one. In the meantime, the multiple partons interactions [15], collective expansion of the final state [16], and other collective effects [17–23] can affect the momentum spectrums of final-state particles. Because the total physical extent of the interacting system is about 2 times the nuclear size, the average extent of a source is only a few fm in the case of considering two or three sources (temperatures).

Let the beam direction be the oz axis, and let the transverse momentum direction of the “associated” particle be the positive direction of the ox axis. A right-hand reference frame is established. In the rest frame of the second emission point, let p_x and p_y denote, respectively, the x - and y -components of the “trigger” particle momentum with oscillations and other interactions, and let p'_x and p'_y denote those without oscillations and other interactions. The simplest relations between p_x and p'_x , as well as p_y and p'_y are linear:

$$p_x = a_x p'_x + b_x \sigma, \quad p_y = a_y p'_y + b_y \sigma, \quad (1)$$

where $a_{x,y}$ and $b_{x,y}$ are parameters to characterize the strength of oscillations, and σ is a parameter to characterize the distribution width of original momentum components. The default values of $a_{x,y}$ and $b_{x,y}$ are 1 and 0, respectively.

From the original $p'_{x,y}$ to the final-state $p_{x,y}$, a detailed consideration on the relativistic effect needs Lorentz transformation. Although there is no particular consideration on the relativistic effect in the above equations for the purpose of convenience, the present expression reflects approximately the mean result of the relativistic effect [24]. Meanwhile, the conservation laws are applicable in the interacting system. We would like to point out that in the above consideration both the “trigger” and “associated” particles are firstly assumed to emit isotropically from two subsources which have no oscillations and other interactions at this assumption state. Then, the momentum components are transformed from original $p'_{x,y}$ to final-state $p_{x,y}$ due to the oscillations and other interactions between the two subsources.

As the first approximation, the original momentum components $p'_{x,y}$ are assumed to obey Gaussian distribution with the width σ , which results in the transverse momentum, momentum, and nonrelativistic kinetic energy spectrums to

be Rayleigh, Maxwell, and Boltzmann distributions, respectively. In the Monte Carlo calculation, let $r_{1,2,3,4}$ be random numbers distributed evenly in $(0, 1]$. We have

$$\begin{aligned} p'_x &= \sigma \sqrt{-2 \ln r_1} \cos(2\pi r_2), \\ p'_y &= \sigma \sqrt{-2 \ln r_3} \cos(2\pi r_4), \end{aligned} \quad (2)$$

which distributes the azimuth of the particle randomly. The relative azimuth between the “trigger” and “associated” particles is

$$\Delta\phi = \arctan \left[\frac{\sqrt{-2 \ln r_3} \cos(2\pi r_4)}{a_x \sqrt{-2 \ln r_1} \cos(2\pi r_2) + b_x} \right], \quad (3)$$

due to $a_y = 1$ and $b_y = 0$ for the near-side and away-side ridge structures in general. A statistical calculation can give the normalization distribution $f(\Delta\phi)$ of $\Delta\phi$.

We would like to point out that (3) simply calculates the ϕ of the “trigger” particle using $\phi = \arctan(p_y/p_x)$. Although implied in the description of the coordinate system, it might be specified reiterated that $\Delta\phi = \phi_{\text{trig}} - \phi_{\text{assoc}} = \phi_{\text{trig}}$ due to $\phi_{\text{assoc}} = 0$ (the transverse momentum direction of the “associated” particle being the positive direction of the ox axis) can be represented using (3), where ϕ_{trig} and ϕ_{assoc} denote the azimuths of “trigger” and “associated” particles, respectively. Then, (3) uses (1) to obtain $\Delta\phi$. In addition, because we focus our attention on the relative magnitudes of a_x and a_y (b_x and b_y), we may choose $a_x = 1$ ($a_y = 0$) or $a_y = 1$ ($b_y = 0$). Conventionally, we have $a_y = 1$ and $b_y = 0$.

The physics condition gives that $a_x \geq 1$. Generally, $a_x = 1$ and $b_x = 0$ describe the state without oscillations and other interactions. $a_x > 1$ reflects an expansion of the subsurface along ox axis in the momentum space. $b_x > 0$ and $b_x < 0$ present respectively a near-displacement and an away-displacement of the first subsurface to the second one along the ox axis. The near-side and away-side phenomenons are partly determined by $b_x > 0$ and $b_x < 0$, respectively, and partly determined by $a_x > 1$.

Before giving comparisons with experimental data, we need to introduce two representations which are used in the literature [2, 3, 27]. The first representation uses unidentified charged tracks as “trigger” particles and combines them with π and p as “associated” particles (denoted by $h - \pi$ and $h - p$, resp.) [2, 3, 27]. The correlation $C(\Delta\eta, \Delta\phi)$ is expressed in terms of the “associated” yield per “trigger” particle where both particles are from a given transverse momentum (p_T) interval and pseudorapidity (η) region:

$$C(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{d^2 N_{\text{assoc}}}{d\Delta\eta d\Delta\phi} = \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}, \quad (4)$$

where N_{trig} and N_{assoc} are the numbers of “trigger” and “associated” particles, respectively, and $S(\Delta\eta, \Delta\phi)$ and $B(\Delta\eta, \Delta\phi)$ are the signal and background distributions [3, 27] and constructed from the same event and “mixed events,” respectively

TABLE 1: Values of parameters and χ^2/dof corresponding to the curves in Figures 1–3.

Figures	Type	a_x	b_x	$c_1(c_2)$	b_0	χ^2/dof
Figure 1(a)	0–20%, $h - \pi$	1.045 ± 0.002	-0.020 ± 0.002	1.197 ± 0.012	—	0.872
Figure 1(b)	(0–20%)–(60–100%), $h - \pi$	1.040 ± 0.002	-0.005 ± 0.001	0.915 ± 0.010	—	1.129
Figure 1(c)	(0–20%)–(60–100%), $h - p$	1.030 ± 0.002	-0.003 ± 0.001	0.208 ± 0.002	—	1.105
Figure 2(a)	$0.3 < p_T^a < 0.5 \text{ GeV/c}, C$	1.040 ± 0.002	-0.024 ± 0.002	16.498 ± 0.172	-2.528 ± 0.026	1.051
Figure 2(b)	$0.5 < p_T^a < 1 \text{ GeV/c}, C$	1.040 ± 0.002	-0.020 ± 0.002	25.146 ± 0.310	-3.840 ± 0.040	0.595
Figure 2(c)	$1 < p_T^a < 2 \text{ GeV/c}, C$	1.040 ± 0.002	-0.019 ± 0.002	40.516 ± 0.422	-6.200 ± 0.065	0.470
Figure 2(d)	$2 < p_T^a < 3 \text{ GeV/c}, C$	1.040 ± 0.002	-0.020 ± 0.002	60.233 ± 0.650	-9.230 ± 0.096	0.282
Figure 2(e)	$3 < p_T^a < 4 \text{ GeV/c}, C$	1.040 ± 0.002	-0.025 ± 0.003	66.202 ± 0.680	-10.100 ± 0.105	0.356
Figure 2(f)	$4 < p_T^a < 5 \text{ GeV/c}, C$	1.040 ± 0.002	-0.029 ± 0.003	69.403 ± 0.710	-10.600 ± 0.110	0.819
Figure 2(a)	$0.3 < p_T^a < 0.5 \text{ GeV/c}, P$	1.010 ± 0.001	-0.045 ± 0.005	7.540 ± 0.080	-1.145 ± 0.012	0.755
Figure 2(b)	$0.5 < p_T^a < 1 \text{ GeV/c}, P$	1.010 ± 0.001	-0.035 ± 0.004	14.363 ± 0.145	-2.215 ± 0.024	1.322
Figure 2(c)	$1 < p_T^a < 2 \text{ GeV/c}, P$	1.012 ± 0.001	-0.030 ± 0.003	27.830 ± 0.303	-4.315 ± 0.045	1.101
Figure 2(d)	$2 < p_T^a < 3 \text{ GeV/c}, P$	1.013 ± 0.001	-0.030 ± 0.003	45.741 ± 0.470	-7.100 ± 0.072	0.575
Figure 2(e)	$3 < p_T^a < 4 \text{ GeV/c}, P$	1.013 ± 0.001	-0.030 ± 0.003	60.354 ± 0.630	-9.360 ± 0.095	1.634
Figure 2(f)	$4 < p_T^a < 5 \text{ GeV/c}, P$	1.013 ± 0.001	-0.025 ± 0.003	86.098 ± 0.900	-13.390 ± 0.135	1.903
Figure 3(a)	$0.3 < p_T^a < 0.5 \text{ GeV/c}, C - P$	1.040 ± 0.002	-0.006 ± 0.001	12.533 ± 0.122	-1.950 ± 0.020	1.808
Figure 3(b)	$0.5 < p_T^a < 1 \text{ GeV/c}, C - P$	1.040 ± 0.002	0.000 ± 0.000	21.923 ± 0.220	-3.400 ± 0.037	0.938
Figure 3(c)	$1 < p_T^a < 2 \text{ GeV/c}, C - P$	1.040 ± 0.002	0.000 ± 0.000	32.036 ± 0.332	-4.950 ± 0.051	0.912
Figure 3(d)	$2 < p_T^a < 3 \text{ GeV/c}, C - P$	1.040 ± 0.002	0.002 ± 0.001	42.163 ± 0.405	-6.520 ± 0.066	0.353
Figure 3(e)	$3 < p_T^a < 4 \text{ GeV/c}, C - P$	1.040 ± 0.002	0.004 ± 0.001	50.203 ± 0.527	-7.790 ± 0.080	1.074
Figure 3(f)	$4 < p_T^a < 5 \text{ GeV/c}, C - P$	1.040 ± 0.002	0.002 ± 0.001	40.485 ± 0.500	-6.280 ± 0.065	1.278

[2, 28]. If we integrate over $\Delta\eta$ in the above equation or if $\Delta\eta$ is a small value in general, we have

$$C(\Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{dN_{\text{assoc}}}{d\Delta\phi} = \frac{S(\Delta\phi)}{B(\Delta\phi)}. \quad (5)$$

Because the background $B(\Delta\phi)$ constructed from the isotropic “mixed events” in our model is a constant, we have

$$C(\Delta\phi) = c_1 S(\Delta\phi) = c_1 f(\Delta\phi), \quad (6)$$

where c_1 is the normalization constant and the signal $S(\Delta\phi) \equiv f(\Delta\phi)$.

The second representation uses the “per-trigger yield” $Y(\Delta\phi)$ to measure the average number of particles correlated with each “trigger” particle, folded into $[0, \pi]$ [1, 29–31] and integrated over $\Delta\eta$ in $C(\Delta\eta, \Delta\phi)$, $S(\Delta\eta, \Delta\phi)$, and $B(\Delta\eta, \Delta\phi)$:

$$Y(\Delta\phi) = \frac{\int B(\Delta\phi) d\Delta\phi}{\pi N_a} \cdot C(\Delta\phi) - b_{\text{ZYAM}}, \quad (7)$$

where N_a denotes the number of efficiency-weighted “trigger” particles and b_{ZYAM} represents the pedestal arising from uncorrelated pairs [3, 27]. By using a zero-yield-at-minimum (ZYAM) method [29, 32], the parameter b_{ZYAM} can be determined in experiments [3, 27, 29, 32]. Because $C(\Delta\phi) = c_1 f(\Delta\phi)$, we have

$$Y(\Delta\phi) = c_2 f(\Delta\phi) + b_0, \quad (8)$$

where b_0 is a shift parameter which can be obtained by fitting experimental data and c_2 is the normalization constant.

To perform the calculation, we probe a set of a_x and b_x and use (3) to give a lots of $\Delta\phi$ by using many random numbers. Then, the normalized distribution $f(\Delta\phi)$ which is normalized to 1 can be obtained. Introducing $f(\Delta\phi)$ into (6) (or (8)) which is normalized to the experimental cross section or yield, the parameter c_1 (or the parameters c_2 and b_0) can be sounded out. By changing the parameters step by step, many repeating calculations can determine the best parameters and their uncertainties. In the real calculation, we can use the idea of the least-square fitting method. The minimum χ^2 corresponds to the best parameter values, and the acceptable χ^2 determines the uncertainties of the parameters.

3. Comparison with Experimental Data and Discussions

Figure 1 presents the correlations versus $\Delta\phi$ in transverse momentum interval $1.5 < p_T < 2.0 \text{ GeV/c}$ in p -Pb collisions at $\sqrt{s_{NN}} = 5.02 \text{ TeV}$, one of the LHC energies. The circles represent the experimental data of the ALICE Collaboration [3, 27] and the curves are our results calculated by the multisource thermal model. Figures 1(a), 1(b), and 1(c) correspond to $h - \pi$ in centrality 0–20%, $h - \pi$ in centrality (0–20%)–(60–100%), and $h - p$ in centrality (0–20%)–(60–100%), respectively. The values of free parameters a_x and b_x , normalization constant c_1 , and χ^2 per degree of freedom (χ^2/dof) obtained by fitting the experimental data are listed in Table 1. In the Monte Carlo calculation, we have used the idea of least-square fitting method. Many tries on the calculation have been applied to get the minimum and acceptable χ^2 . Then, the best parameter values and their

FIGURE 1: The correlations versus $\Delta\phi$ in transverse momentum interval $1.5 < p_T < 2.0$ GeV/c in p -Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV. The circles represent the experimental data of the ALICE Collaboration [3, 27] and the curves are our results calculated by the multisource thermal model. Figures 1(a), 1(b), and 1(c) correspond to $h - \pi$ in centrality 0–20%, $h - \pi$ in centrality (0–20%)–(60–100%), and $h - p$ in centrality (0–20%)–(60–100%), respectively.

uncertainties can be determined. From the table, one can see that the model describes well the experimental data of the ALICE Collaboration. The subsources have an expansion and an away-displacement along the ox axis.

Figure 2 shows $Y(\Delta\phi) - |\Delta\phi|$ relations in p -Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV. The closed and open circles represent, respectively, the central (denoted “C” in the panel) and peripheral collisions (denoted “P” in the panel) measured by the ATLAS Collaboration [2], and the curves are our results calculated by the model. From Figures 2(a) to 2(f), different transverse momentum intervals for the “trigger” particle (p_T^a) and for the “associated” particle (p_T^b) are shown in the panels. The values of related parameters a_x , b_x , c_2 , and b_0 as well as χ^2/dof are listed in Table 1. Once more, the model describes well the experimental data of the ATLAS Collaboration. In most cases, the subsources in central collisions have a larger expansion and a smaller away-displacement along the ox axis, while the subsources in peripheral collisions are opposite. These differences between the central and peripheral collisions are rendered by the number of participant nucleons.

The difference (C – P) on $Y(\Delta\phi) - |\Delta\phi|$ relations between the central and peripheral p -Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV is shown in Figure 3. The circles represent the experimental data of the ATLAS Collaboration [2] and the curves are our results calculated by the model. The values of related parameters and χ^2/dof are given in Table 1. We see that the model describes the difference between the

central and peripheral collisions. The values of a_x (≈ 1.04) and b_x (≈ 0) obtained from Figure 3 are consistent with those obtained from Figures 1(b) and 1(c). Because there is no direct proportional relation between the parameter values and the correlation magnitude, we cannot obtain simply the parameter values for Figure 3 by the method of central minus peripheral collisions.

From the above comparisons we see that we have used the same method to describe the central, peripheral, and central-peripheral collisions. Different participant nucleon numbers (different spectator nucleon numbers) in central and peripheral collisions reflect different parameter values. As an integrative result, the oscillation and other interactions existing between the two subsources cause a_x to be greater than 1 and b_x to be less than 0. Generally, a_x in central collisions is greater than that in peripheral collisions, and $|b_x|$ in central collisions is less than that in peripheral collisions, due to the effect of participant nucleon number. By comparison with Figures 1(a) and 2, as the difference between the central and peripheral collisions, Figures 1(b), 1(c), and 3 do not contain new content but the effect of participant nucleon number.

In the comparisons, because our calculation is performed on a purely signal sample, and experimental data are usually presented by a admixture of signal and background samples, we need the normalized constants c_1 and c_2 . Our results show that $c_1 > 1$ and $c_2 > 1$ for both the central and

FIGURE 2: The relation $Y(\Delta\phi) - |\Delta\phi|$ in p -Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV. The closed and open circles represent, respectively, the central and peripheral collisions measured by the ATLAS Collaboration [2], and the curves are our results calculated by the multisource thermal model. From Figures 2(a) to 2(f), different transverse momentum intervals for the “trigger” particle (p_T^a) and for the “associated” particle (p_T^b) are shown in the panels.

peripheral collisions, which render that the magnitude of signal is greater than that of background. There are strong correlations between two particles in the production in p -Pb collisions at LHC energy.

Looking at the results in Table 1, the source with oscillations becomes less displaced in peripheral collisions compared to central collisions. The standard deviation of the momentum components also becomes larger in peripheral

FIGURE 3: The same as Figure 2, but showing the difference between the central and peripheral p -Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV.

collisions. These phenomenons may be caused by different numbers of participant nucleons in peripheral and central collisions.

In heavy ion collisions, the current consensus is that a primary component of the ridge effect is caused by fluctuations in the initial state geometry with a major contribution from “triangular flow,” which generates a significant third Fourier coefficient contribution to the azimuthal correlations.

These may be the reasons which cause oscillations and other interactions between the two subsources. In fact, other reasons can cause similar results.

High energy collisions contain abundant contents such as multiplicity, transverse energy, entropy [33], phase transition [34], and flow effects [35]. There are strong relations between flow effects and azimuthal distributions and correlations. Particularly, the azimuthal distribution and correlations of

produced particles, target fragments, and projectile fragments have important worth of studies. The present work can be referenced in further.

4. Conclusions

From the above discussions, we obtain following conclusions.

(a) The near-side and away-side ridge structures in two-particle azimuthal correlation produced in high energy collisions can be explained by the multisource thermal model. The modelling results are in agreement with the experimental data of p -Pb collisions at $\sqrt{s_{NN}} = 5.02$ GeV measured by the ALICE and ATLAS Collaborations. This renders that our modelling assumption is correct. The two correlated particles are initially assumed to produce isotropically in two rest sub-sources. Then, the momentum components are transformed from original one to final-state one due to the oscillations and other interactions between the two sub-sources.

(b) Two emission points (subsources) are assumed and used to perform the calculation. One subsource corresponds to the production of “trigger” particle, and the other sub-source corresponds to the production of “associated” particle. There are oscillations and other interactions between the two sub-sources, which results in the momentum of “trigger” particle, in the rest frame of “associated” particle’s source, to depart from the original one.

(c) There are two main parameters, a_x and b_x , in the modelling calculation on correlations. $a_x = 1$ and $b_x = 0$ describe the state without oscillations and other interactions. $a_x > 1$ reflects an expansion of the subsource along the ox axis in the momentum space. $b_x > 0$ and $b_x < 0$ present, respectively, a near-displacement and an away-displacement of the “trigger” particle’s subsource to the “associated” particle’s subsource along the ox axis. The magnitude of near-side and away-side ridges is partly determined by $b_x > 0$ and $b_x < 0$, respectively, and partly determined by $a_x > 1$.

(d) In central and peripheral p -Pb collisions at the LHC energy, our modelling results show that $a_x > 1$ and $b_x < 0$. In most cases, the subsource in central collisions has a larger expansion and a smaller away-displacement along the ox axis, while the subsource in peripheral collisions is opposite. The difference between the central and peripheral collisions shows a very small b_x (≈ 0) which means a nearly zero displacement of the subsource. The values of a_x and b_x extracted from the central and difference ($C - P$) data of the ALICE and ATLAS Collaborations are consistent with each other.

(e) The present model describes the central and peripheral p -Pb collisions by using a uniform method. Although there are different participant nucleon numbers (or spectator nucleon numbers) between the central and peripheral collisions, the interacting mechanisms which include the oscillations and other interactions between the two sub-sources are the same except the intensity. The treatment on the difference $C - P$ does not introduce new content but the effect of participant nucleon number.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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