Research Article

Constraining the Parameters of Modified Chaplygin Gas in Einstein-Aether Gravity

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We have assumed FRW model of the universe in Einstein-Aether gravity filled with dark matter and modified Chaplygin gas (MCG) type dark energy. We present the Hubble parameter in terms of some unknown parameters and observational parameters with the redshift \( z \). From observed Hubble data (OHD) set (12 points), we have obtained the bounds of the arbitrary parameters \((A, B)\) of MCG by minimizing the \( \chi^2 \) test. Next due to joint analysis of BAO and CMB observations, we have also obtained the best fit values and the bounds of the parameters \((A, B)\) by fixing some other parameters. We have also taken type Ia supernovae data set (union 2 data set with 557 data points). Next due to joint analysis with SNe, we have obtained the best fit values of parameters. The best fit values and bounds of the parameters are obtained by 66%, 90%, and 99% confidence levels for OHD, OHD + BAO, OHD + BAO + CMB, and OHD + BAO + CMB + SNe joint analysis. The distance modulus \( \mu(z) \) against redshift \( z \) for our theoretical MCG model in Einstein-Aether gravity has been tested for the best fit values of the parameters and the observed SNe Ia union2 data sample.

1. Introduction

Observational evidence strongly points to an accelerated expansion of the universe, but the physical origin of this acceleration is unknown. The observations include type Ia supernovae and cosmic microwave background (CMB) [1–5] radiation. The standard explanation invokes an unknown “dark energy” component which has the property of positive energy density and negative pressure. Observations indicate that dark energy occupies about 70% of the total energy of the universe, and the contribution of dark matter is ~26%. This accelerated expansion of the universe has also been strongly confirmed by some other independent experiments like Sloan Digital Sky Survey (SDSS) [6], baryonic acoustic oscillation (BAO) [7], WMAP data analysis [8, 9], and so forth. Over the past decade there have been many theoretical models for mimicking the dark energy behaviors, such as the simplest (just) cosmological constant in which the equation of state is independent of the cosmic time and which can fit the observations well. This model is the so-called \( \Lambda \)CDM, containing a mixture of cosmological constant \( \Lambda \) and cold dark matter (CDM). However, two problems arise from this scenario, namely “fine-tuning” and the “cosmic coincidence” problems. In order to solve these two problems, many dynamical dark energy models were suggested, whose equation of state evolves with cosmic time. The scalar field or quintessence [10, 11] is one of the most favored candidates of dark energy which produce sufficient negative pressure to drive acceleration. In order to alleviate the cosmological-constant problems and explain the acceleration expansion, many dynamical dark energy models have been proposed, such as K-essence, tachyon, phantom, quintom, and Chaplygin gas model [12–16]. Also the interacting dark energy models including modified Chaplygin gas [17], holographic dark energy model [18], and braneworld model [19] have been proposed. Recently, based on principle of quantum gravity, the agegraphic dark energy (ADE) and the new agegraphic dark energy (NADE) models were proposed by Cai [20] and Wei and Cai [21], respectively. The theoretical models have been tally with the observations with different data sets say TORNQY, Gold sample data sets [3, 22–24]. In Einstein's gravity, the modified Chaplygin gas [17] best fits with the 3-year WMAP and the SDSS data with the choice of parameters.
\[ A = 0.085 \text{ and } \alpha = 1.724 \] which are improved constraints compared to the previous ones \(-0.35 < A < 0.025\) [26].

Another possibility is that general relativity is only accurate on small scales and has to be modified on cosmological distances. One of these is modified gravity theories. In this case cosmic acceleration would arise not from dark energy as a substance but rather from the dynamics of modified gravity. Modified gravity constitutes an interesting dynamical alternative to \(\Lambda CDM\) cosmology in that it is also able to describe the current acceleration in the expansion of our universe. The simplest modified gravity is DGP brane-world model [27]. The other alternative approach dealing with the acceleration problem of the Universe is changing the gravity law through the modification of action of gravity by means of using \(f(R)\) gravity [28, 29] instead of the Einstein-Hilbert action. Some of these models, such as \(1/R\) and logarithmic models, provide an acceleration for the universe at the present time [30]. Other modified gravity includes \(f(T)\) gravity, \(f(G)\) gravity, Gauss-Bonnet gravity, Horava-Lifshitz gravity, and Brans-Dicke gravity [31–35].

In the present work, we concentrate on the generalized Einstein-Aether theories as proposed by Zlosnik et al. [36, 37], which is a generalization of the Einstein-Aether theory developed by Jacobson and Mattingly [38, 39]. These years a lot of work has been done in generalized einstein-aether theories [40–46]. In the generalized Einstein-Aether theories by taking a special form of the Lagrangian density of Aether field, the possibility of Einstein-Aether theory as an alternative to dark energy model is discussed in detail, that is, taking a special Aether field as a dark energy candidate and the constraints have been found from observational data [47, 48]. Since modified gravity theory may be treated as alternative to dark energy, so Meng and Du [47, 48] have not taken by hand any types of dark energy in Einstein-Aether gravity and shown that the gravity may generate dark energy. Here if we exempt this assumption, so we need to consider the dark energy from outside. So we assume the FRW universe in Einstein-Aether gravity model filled with the dark matter and the modified Chaplygin gas (MCG) type dark energy. The basic concepts of Einstein-Aether gravity theory are presented in Section 2. The modified Friedmann equations and their solutions are given in Section 3. The observational data analysis tools in observed Hubble data (ODH), ODH + BAO, ODH + BAO + CMB, and ODH + BAO + CMB + SNe for \(\chi^2\) minimum test will be studied in Section 4 and investigate the bounds of unknown parameters \((A, B)\) of MCG dark energy by fixing other parameters. The best fit values of the parameters are obtained by 66%, 90%, and 99% confidence levels. The distance modulus \(\mu(z)\) against redshift \(z\) for our theoretical model of the MCG in Einstein-Aether gravity models for the best fit values of the parameters and the observed SNe Ia union2 data sample. Finally we present the conclusions of the work in Section 5.

2. Einstein-Aether Gravity Theory

In order to include Lorentz symmetry violating terms in gravitation theories, apart from some noncommutative gravity models, one may consider existence of preferred frames. This can be achieved admitting a unit timelike vector field in addition to the metric tensor of spacetime. Such a timelike vector implies a preferred direction at each point of spacetime. Here the unit timelike vector field is called the Aether and the theory coupling the metric and unit timelike vector is called the Einstein-Aether theory [38]. So Einstein-Aether theory is the extension of general relativity (GR) that incorporates a dynamical unit timelike vector field (i.e., Aether). In the last decade there is an increasing interest in the Aether theory.

The action of the Einstein-Aether gravity theory with the normal Einstein-Hilbert part action can be written in the form [36, 47]

\[
S = \int d^4x \sqrt{-g} \left[ \frac{R}{16\pi G} + \mathcal{L}_E + \mathcal{L}_A \right],
\]

where \(\mathcal{L}_E\) is the vector field Lagrangian density while \(\mathcal{L}_A\) denotes the Lagrangian density for all other matter fields. The Lagrangian density for the vector part consists of terms quadratic in the field [36, 47]:

\[
\mathcal{L}_A = \frac{M^2}{16\pi G} F(K) + \frac{1}{16\pi G} \lambda (A^a A_a + 1),
\]

\[
K = M^{-2} K_{cd} \nabla^a A^c \nabla_b A^d,
\]

\[
K_{cd} = c_1 g_{cd} + c_2 g^{ab} \delta_{cd} \delta_{ab} + c_3 g^{ab} g_{cd} - c_4 g_{ab} g_{cd},
\]

where \(c_i\) are dimensionless constants, \(M\) is the coupling constant which has the dimension of mass, \(\lambda\) is a Lagrange multiplier that enforces the unit constraint for the time-like vector field, \(A^a\) is a contravariant vector, \(g_{ab}\) is metric tensor, and \(F(K)\) is an arbitrary function of \(K\). From (1), we get the field equations

\[
G_{ab} = T_{ab}^{EA} + 8\pi GT_{ab}^E
\]

\[
\nabla_a \left( F' J_a^b \right) = 2\lambda A_b,
\]

where

\[
F' = \frac{dF}{dK} , \quad J_a^b = 2K_{cd} \nabla_d A_c^a.
\]

Here \(T_{ab}^{EA}\) is the energy momentum tensor for all matter fluids and \(T_{ab}^E\) is the energy momentum tensor for the vector field and they are, respectively, given as follows: [47]

\[
T_{ab} = (\rho + p) u_a u_b + \rho g_{ab},
\]

where \(\rho\) and \(p\) are, respectively, the energy density and pressure of all matter fluids and \(u_a = (1, 0, 0, 0)\) is the fluid 4-velocity vector and

\[
T_{ab}^{EA} = \frac{1}{2} \nabla_d \left[ (J_{(a}^{(d} A_{b)} - J_{(a}^d (A_{b)} - J_{(ab)} A^d) F' \right] - Y_{(ab)} F' + \frac{1}{2} g_{ab} M^2 F + \lambda A_b A_a
\]

with

\[
Y_{ab} = -c_1 \left[ (\nabla_d A_a) (\nabla^d A_b) - (\nabla_d A_b) (\nabla^d A_a) \right],
\]

where the subscript \((ab)\) means symmetric with respect to the indices involved and \(A^a = (1, 0, 0, 0)\) is nonvanishing time-like unit vector satisfying \(A^a A_a = -1\).
3. Modified Friedmann Equations and Solutions

We consider the Friedmann-Robertson-Walker (FRW) metric of the universe as

\[ ds^2 = -dt^2 + a^2(t) \left[ \frac{dr^2}{1 - kr^2} + r^2 (d\theta^2 + \sin^2 \theta d\phi^2) \right], \]  

where \( k(=0, \pm 1) \) is the curvature scalar and \( a(t) \) is the scale factor. From (3) and (4), we get

\[ K = M^{-2} \left( c_1 g^{ab} g_{cd} + c_2 \delta^a_d \delta^b_c + c_3 \delta^a_c \delta^b_d \right) = \frac{3\beta H^2}{M^2}, \]  

where \( \beta = c_1 + 3c_2 + c_3 \) is constant. From (5), we get the modified Friedmann equation for Einstein-Aether gravity as follows [36, 47]:

\[ \beta \left( -\frac{P'}{F} + \frac{F'}{2K} \right) H^2 + \left( H^2 + \frac{k}{a^2} \right) = \frac{8\pi G}{3} \rho, \]  

\[ \beta \frac{d}{dt} \left( HF' \right) + \left( -2H + \frac{2k}{a^2} \right) = 8\pi G (\rho + p), \]  

where \( H (= \dot{a}/a) \) is Hubble parameter. Now we see that if the first expressions of L.H.S. of (12) and (13) are zero, we get the usual field equations for Einstein’s gravity. So first expressions arise for Einstein-Aether gravity. Also the conservation equation is given by

\[ \dot{\rho} + 3\frac{\dot{a}}{a} (\rho + p) = 0. \]  

Now, assume that the matter fluid is combination of dark matter and modified Chaplygin gas type dark energy. So \( \rho = \rho_m + \rho_{ch} \) and \( p = \rho_m + p_{ch} \), where \( \rho_m \) and \( p_m \) are, respectively, the energy density and pressure of dark matter and \( \rho_{ch} \) and \( p_{ch} \) are, respectively, the energy density and pressure of modified Chaplygin gas. Assume that the dark matter follows the barotropic equation of state \( p_m = w_m \rho_m \), where \( w_m \) is a constant. The equation of state of modified Chaplygin gas (MCG) is given by [17]

\[ \rho_{ch} = A\rho_{ch} - \frac{B}{\rho_{ch}^{\alpha}}, \]  

where \( A > 0, B > 0, \) and \( 0 < \alpha \leq 1 \). Now we assume that there is no interaction between dark matter and dark energy. So they are separately conserved. From (14), we obtain the conservation equations for dark matter and dark energy in the form:

\[ \dot{\rho}_m + 3 \frac{\dot{a}}{a} (\rho_m + p_m) = 0, \quad \dot{\rho}_{ch} + 3 \frac{\dot{a}}{a} (\rho_{ch} + p_{ch}) = 0. \]  

Using equation of states and the conservation equations (17), we obtain \( \rho_m = \rho_{m0}(1 + z)^{(3+\omega_m)} \) and

\[ \rho_{ch} = \left[ \frac{B}{1 + A} + C (1 + z)^{(3+\omega_m)} \right]^{1/(1+\alpha)}, \]  

where \( \rho_{m0} \) and \( C \) are positive constants in which \( \rho_{m0} \) represents the present value of the density of dark matter and \( z = 1/a - 1 \) is the cosmological redshift (choosing \( a_0 = 1 \)). The above expression can be written in the form:

\[ \rho_{ch} = \rho_{ch0} \left[ A_s + (1 - A_s)(1 + z)^{(3+\omega_m)} \right]^{1/(1+\alpha)}, \]  

where \( \rho_{ch0} \) is the present value of the MCG density and \( A_s = B/(1 + A)C + B \). So \( 0 \leq A_s \leq 1 \).

Now since \( F(K) \) is a free function of \( K \). Some authors have chosen \( F(K) \) in the following forms: (i) \( F(K) = \gamma(-K)^n \) [36, 43], (ii) \( F(K) = \gamma \sqrt{-K + \sqrt{3}K/\beta} \ln(-K) \) [47, 48]. Here we may choose another form of \( F(K) \) for our next calculations in simplified form as \( F(K) = (2/\beta)K(1 - \epsilon K) \), where \( \epsilon \) is a constant. So solving (13), we obtain the expression of \( H^2 \) in terms of redshift \( z \) in the following:

\[ H^2(z) = \frac{M}{3\sqrt{3e}\beta} \times \left[ -3k(1 + z)^2 + 8\pi G \rho_{m0}(1 + z)^{3(1+\omega_m)} + 8\pi G \rho_{ch0} \left\{ A_s + (1 - A_s)(1 + z)^{(3+\omega_m)} \right\}^{1/(1+\alpha)} \right]^{1/2}. \]  

Now defining the dimensionless parameters \( \Omega_{m0} = 8\pi G \rho_{m0}/3H_0^2, \Omega_{ch0} = 8\pi G \rho_{ch0}/3H_0^2, \Omega_k = k/H_0^2, \) and \( \Omega_{EA} = M/3H_0 \sqrt{e}\beta, \) we obtain the form of \( H(z) \):

\[ H(z) = H_0 \sqrt{\Omega_{EA}} \times \left[ -\Omega_{k0}(1 + z)^2 + \Omega_{m0}(1 + z)^{3(1+\omega_m)} + \Omega_{ch0} \left\{ A_s + (1 - A_s)(1 + z)^{(3+\omega_m)} \right\}^{1/(1+\alpha)} \right]^{1/4}. \]  

Due to the above solution, (13) gives the following relation:

\[ \sqrt{\Omega_{EA}} \left[ \Omega_{m0} + \Omega_{ch0} - \Omega_k \right] = 1. \]  

4. Observational Data Analysis Tools

In this section, we will investigate some bounds of the parameters of the modified Chaplygin gas (MCG) in Einstein-Aether gravity by observational data fitting. The parameters are determined by observed Hubble data (OHD), BAO, CMB, and SNe data analysis [47–57]. We will use the \( \chi^2 \) minimization technique (statistical data analysis) from Hubble-redshift data set to get the constraints of the parameters of MCG model in Einstein-Aether gravity.
4.1. Analysis with Observed Hubble Data (OHD). We analyze the MCG model in Einstein-Aether gravity using observed value of Hubble parameter data (OHD) [58, 59] at different redshifts consisting of twelve data points. The observed values of Hubble parameter \( H(z) \) and the standard error \( \sigma(z) \) for different values of redshift \( z \) are listed in Table 1. The \( \chi^2 \) statistics for OHD is given as follows:

\[
\chi^2_{OHD} = \sum \frac{(H(z) - H_{obs}(z))^2}{\sigma^2(z)},
\]

where \( H(z) \) and \( H_{obs}(z) \) are, respectively, the theoretical and observational values of Hubble parameter at different redshifts and \( \sigma(z) \) is the corresponding error which is given in Table 1. We consider the present value of Hubble parameter \( H_0 = 72 \pm 8 \text{ Kms}^{-1} \text{ Mpc}^{-1} \). Here we will determine two parameters of MCG model out of 3 parameters \( A, B, \alpha \) by fixing any one parameter from minimizing the above distribution \( \chi^2_{OHD} \). There are other parameters of the model say \( \Omega_{m0}, \Omega_{k0}, \Omega_{\Lambda0}, \omega_m \). Fixing the one parameter \( \alpha \) of MCG model, the relation between the other parameters \((A, B)\) can be determined by the observational data. Now for OHD analysis, \( \chi^2_{OHD} \) is minimized for best fit values of \( A = 0.238303 \) and \( B = 0.18176 \) and the minimum value of \( \chi^2_{OHD} = 7.08613 \) where we have assumed \( \alpha = 0.1 \). We also plot the graph for different confidence levels (66%, 90%, 99%) in Figure 1.

4.2. Analysis with OHD + BAO. Another constraint is from the baryonic acoustic oscillations (BAO) traced by the Sloan Digital Sky Survey (SDSS). The BAO peak parameter value has been proposed by Eisenstein et al. [7]. Here we examine the parameters \( A \) and \( B \) for MCG gas model from the measurements of the BAO peak for low redshift \((0 < z < 0.35)\) using standard \( \chi^2 \) analysis. The BAO peak parameter may be defined by [47]

\[
\mathcal{d} = \frac{\sqrt{\Omega_m}}{\sqrt{E(z_1)}} \left[ \frac{1}{z_1} \sinh \left( \sqrt{\Omega_k} \int_{z_1}^{z_c} \frac{dz}{E(z)} \right) \right]^{2/3},
\]

where \( E(z) = H(z)/H_0 \) may be called the normalized Hubble parameter and the redshift \( z_1 = 0.35 \) is the typical redshift of the SDSS. The value of the parameter \( \mathcal{d} \) for the universe is given by \( \mathcal{d} = 0.469 \pm 0.017 \) using SDSS data [7]. Now the \( \chi^2 \) function for the BAO measurement can be written as

\[
\chi^2_{BAO} = \frac{(\mathcal{d} - 0.469)^2}{(0.017)^2}.
\]

Now the total joint data analysis of BAO with OHD for the \( \chi^2 \) function may be defined by

\[
\chi^2_{total} = \chi^2_{OHD} + \chi^2_{BAO}.
\]

According to OHD + BAO joint analysis the best fit values of \( A \) and \( B \) are \( A = 0.238693 \) and \( B = 0.209932 \) with \( \chi^2 \) minimum being 7.07842. Finally we draw the contours \( B \) versus \( A \) for the 66%, 90%, and 99% confidence limits depicted in Figure 2.

<table>
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<th>( H(z) )</th>
<th>( \sigma(z) )</th>
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</tr>
<tr>
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<td>83</td>
<td>±8</td>
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<tr>
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</table>

4.3. Analysis with OHD + BAO + CMB. In addition to OHD and BAO analysis, we use the cosmic microwave background (CMB) shift parameter. The CMB shift parameter (CMB power spectrum first peak) is defined by [60–62]

\[
\mathcal{R} = \frac{\sqrt{\Omega_m}}{\sqrt{\Omega_k}} \sinh \left( \sqrt{\Omega_k} \int_{z_1}^{z_c} \frac{dz}{E(z)} \right),
\]

where \( z_c \) is the value of redshift at the last scattering surface. From 7-year WMAP data [63], the value of the parameter has been obtained as \( \mathcal{R} = 1.726 \pm 0.018 \) at the redshift \( z_2 = 1091.3 \). Now the \( \chi^2 \) function for the CMB measurement can be written as

\[
\chi^2_{CMB} = \frac{(\mathcal{R} - 1.726)^2}{(0.018)^2}.
\]
Now when we consider OHD, BAO, and CMB analysis together, the total joint data analysis (OHD + BAO + CMB) for the $\chi^2$ function may be defined by

$$\chi^2_{\text{TOTAL}} = \chi^2_{\text{OHD}} + \chi^2_{\text{BAO}} + \chi^2_{\text{CMB}}.$$ (29)

The $\chi^2$ function for SNe Ia is given by

$$\chi^2_{\text{SNe}} = \sum \frac{(\mu(z) - \mu_{\text{obs}}(z))^2}{\sigma^2(z)},$$ (32)

where $\mu_{\text{obs}}(z)$ is observational value of distance modulus parameter at different redshifts and $\sigma(z)$ is the corresponding error. In this work, we take Union2 data set consisting of 557 supernovae data points. Now we consider four cosmological tests together, the total joint data analysis (Stern + BAO + CMB + SNe) for the $\chi^2$ function may be defined by

$$\chi^2_{\text{TOTAL}} = \chi^2_{\text{OHD}} + \chi^2_{\text{BAO}} + \chi^2_{\text{CMB}} + \chi^2_{\text{SNe}}.$$ (33)

From the joint analysis, we found the minimum value of $\chi^2$ which is 7.06716. The best fit values of the parameters are $A = 0.239158$ and $B = 0.255814$. The confidence contours are drawn in Figure 4. The best fit value of distance modulus $\mu(z)$ for our theoretical model and the supernova type Ia union2 sample are drawn in Figure 5 for our best fit values of $A$ and $B$. From the curves, we see that the theoretical MCG model in Einstein-Aether gravity is in agreement with the union2 sample data.

5. Discussions and Concluding Remarks

We have assumed FRW model of the universe in Einstein-Aether gravity filled with dark matter and modified Chaplygin gas (MCG) type dark energy. Dark matter has the equation of state parameter $w_m$, which is small. We assumed the dark matter and dark energy separately conserved and hence we found the solutions in this gravity. Since $F(K)$ is a free function of $K$, so we have chosen quadratic form of

\[
F(K) = -\frac{K^2}{2},
\]

where $K$ is a function of the dark energy parameter $\omega$.
\[ F(K) \] for simplicity of the calculation. Defining dimensionless parameters, we present the Hubble parameter in terms of some unknown parameters and observational parameters with the redshift \( z \). From observed Hubble data (OHD) set (12 points), we have obtained the bounds of the arbitrary parameters \( (A, B) \) of MCG by minimizing the \( \chi^2 \) test where we have chosen \( \alpha = 0.1 \). The minimum values of the parameters are \( A = 0.238303 \) and \( B = 0.18176 \) for OHD analysis. Next due to joint analysis of BAO and CMB observations, we have also obtained the best fit values and the bounds of the parameters \( (A, B) \). The best fit values of the parameters (i) for OHD + BAO are \( A = 0.238695 \) and \( B = 0.209932 \) and (ii) for OHD + BAO + CMB are \( A = 0.239018 \) and \( B = 0.240047 \). We have also taken type Ia supernovae data set (union 2 data set with 557 data points). Next due to joint analysis with SNe, we have obtained the best fit values of the parameters \( (A, B) \). The best fit values of the parameters for OHD + BAO + CMB + SNe are \( A = 0.239158 \) and \( B = 0.255814 \). The best fit values and bounds of the parameters are obtained by 66%, 90%, and 99% confidence levels for OHD, OHD + BAO, OHD + BAO + CMB, and OHD + BAO + CMB + SNe joint analysis in Figures 1–4. The distance modulus \( \mu(z) \) against redshift \( z \) for our theoretical MCG model in Einstein-Aether gravity has been tested for the best fit values of the parameters and the observed SNe Ia union2 data sample and drawn in Figure 5. The observations do in fact severely constrain the nature of allowed composition of matter energy by constraining the range of the values of the parameters for a physically viable MCG in Einstein-Aether gravity model.

**Conflict of Interests**

The author declares that there is no conflict of interests regarding the publication of this paper.

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