Research Article

Predictions for the Isolated Diphon Production through NNLO in QCD and Comparison to the 8 TeV ATLAS Data

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We present cross-section predictions for the isolated diphon production in next-to-next-to-leading order (NNLO) QCD using the computational framework MATRIX. Both the integrated and the differential fiducial cross-sections are calculated. We found that the arbitrary setup of the isolation procedure introduces uncertainties with a size comparable to the estimation of the theoretical uncertainties obtained with the customary variation of the factorization and renormalization scales. This fact is taken into account in the final result.

1. Introduction

Considerable attention, both experimental and theoretical, has been paid to the study of the diphon productions. This process is relevant for testing the standard model predictions and is of great importance in Higgs studies. The diphon final state is also important in new physics researches: the extra-dimensions, the supersymmetry, and the new heavy resonances are three important topics among others.

The theoretical calculations are possible thanks to the codes DIPHOX [1], ResBos [2], 2gRes [3], 2gNNLO [4], MCFM [5], and recently MATRIX [6].

In addition to the direct production from the hard subprocess, photons can also result from the fragmentation subprocesses of QCD partons. The complete NLO one- and two-fragmentation contributions are implemented in DIPHOX. In ResBos only a simplified one-fragmentation contribution is considered but the resummation of initial-state gluon radiation to NNLL accuracy is included. Both DIPHOX and ResBos implement the \( g g \rightarrow \gamma \gamma \) component, to LO and NLO in QCD, respectively. In the (NLO) MCFM calculations, the fragmentation component is implemented to LO accuracy.

Thanks to the high rate of production of final diphon pairs (considered as relatively clean), experimentalists make precise measurements, pushing the experimental uncertainties down to the percent level; thus, NLO calculations have become insufficient and therefore more precise investigations are required in order to reproduce the data and to provide a precise modeling of the SM backgrounds.

During the first run of the LHC (Run I), measurements of the production cross-section for two isolated photons at a center-of-mass energy of \( \sqrt{s} = 7 \) TeV are performed by ATLAS [7] and CMS [8], based on an integrated luminosity of 4.9 fb\(^{-1}\) and 5.0 fb\(^{-1}\), respectively. This is concluded by ATLAS [9] at \( \sqrt{s} = 8 \) TeV using an integrated luminosity of 20.2 fb\(^{-1}\) which gives a much more accurate result.

In [9], the authors reported that NLO calculations fail to reproduce the data and even if there is improvement of the result with 2gNNLO, it remains insufficient.

Although the NNLO isolated diphon production cross-sections can be calculated using the 2gNNLO and MCFM public codes, we used the most recent code MATRIX, because, in addition to its NNLO accuracy, it allows us to estimate systematic errors related to the \( q_T\)-subtraction procedure in an automatic way (see below).

Our work is organized as follows. In Section 2.1, we give a short description of the MATRIX code. In Section 2.2, we present the two isolation prescriptions used in the analysis. We propose a precise estimation of the uncertainties in
NNLO QCD calculations containing at least one photon in the final state. In Section 2.3, the NNLO cross-section results are presented and compared to LHC data. We finish with the conclusion in Section 3.

2. NNLO Cross-Sections

2.1. The MATRIX Code. The parton-level Monte Carlo generator MATRIX performs fully differential computations at the next-to-next-to-leading order (NNLO) QCD; it is based on a number of different computations and tools from various people and groups [6, 10–15]. It achieves NNLO accuracy by using the $q_T$-subtraction formalism in combination with the Catani–Seymour dipole subtraction method. The systematic uncertainties inherent to the $q_T$-subtraction procedure may be controlled down to the few per mille level or better for all NNLO predictions. To do this, a dimensionless cut-off $r_{cut}$ is introduced which renders all cross-section pieces separately finite and the power-suppressed contributions vanish in the limit $r_{cut} \rightarrow 0$. MATRIX simultaneously computes the cross-section at several $r_{cut}$ values and then the extrapolated result is evaluated, including an estimate of the uncertainty of the extrapolation procedure, in an automatic way.

We can apply realistic fiducial cuts directly on the phase-space. The core of MATRIX framework is MUNICH Monte Carlo program, allowing us to compute both QCD and EW corrections at NLO accuracy. The loop-induced $gg$ contribution entering at the NNLO is available for the diphoton production process.

2.2. Isolation Parameters. An isolation requirement is necessary to prevent contamination of the photons by hadrons produced during the collision, arising from the decays of $\pi^0, \eta, \text{etc.}$ Two prescriptions may be used for this purpose:

(i) The standard cone isolation criterion, used by collider experiments: a photon is assumed to be isolated if the amount of deposited hadronic transverse energy

$$\sum_n E_T^n \leq E_T^{\text{max}},$$

in the cone of radius $R$ in azimuthal $\phi$ and rapidity $y$ angle centered around the photon direction:

$$r = \sqrt{(\phi - \phi_g)^2 + (y - y_g)^2} \leq R.$$  

(ii) The “smooth” cone or Frixione isolation criterion [16]: in this case $E_T^{\text{max}}$ is multiplied by a function $\chi(r)$ such that

$$\lim_{r \rightarrow 0} \chi(r) = 0$$

$$0 < \chi(r) < 1 \quad \text{if } 0 < r < R;$$

a possible (and largely used) choice is

$$\chi(r) = \left[ \frac{1 - \cos(r)}{1 - \cos(R)} \right]^n$$

so that

$$\sum_n E_T^n \chi \left[ \frac{1 - \cos(r)}{1 - \cos(R)} \right]^n E_T^{\text{max}},$$

$$r = \sqrt{(\phi - \phi_g)^2 + (y - y_g)^2} \leq R,$$

(typically $n = 1$).

Despite the fact that the Frixione criterion (formally) eliminates all fragmentation contribution, it is not yet included in the experimental studies. On the other hand, the use of this criterion by the theoretical investigations at NNLO is necessary to ensure an Infra-Red (IR) safe definition of the cross-section since no fragmentation functions are included.

In ATLAS measurement [9], the standard criterion is adopted for DIPHOX and ResBos but the “smooth” prescription is used for 2gNNLO, assuming $E_T^{\text{max}} = 11$ GeV. This is far from the Les Houches accord 2013 recommendations which state that to match experimental conditions to theoretical calculations with reasonable accuracy, the isolation parameters must be tight enough: $E_T^{\text{max}} \leq 5$ GeV or $\epsilon < 0.1$ (assuming $n = 1$) [17].

In [18], the authors presented a rather complete study of the impact of the isolation parameters on the diphoton cross-sections. We can lift the following points from this study:

(i) The NNLO cross-sections are more sensitive to the variation of the parameters of isolation in comparison with the NLO results.

(ii) At fixed $n = 1$, the total NNLO cross-section for the “smooth” isolation increases by 6% in going from $E_T^{\text{max}} = 2$ to 10 GeV.

(iii) Considering the interval $0.5 < n < 2$, at fixed $E_T^{\text{max}} = 4$ GeV, the total NNLO cross-section with $n = 1$ increases by about 4% with $n = 0.5$ and decreases by about 5% with $n = 2$; the corresponding scale uncertainty is less than ±8.7%.

We notice that the isolation uncertainties due to the choice of the isolation parameters are comparable to the scale uncertainties; thus, we have to consider the arbitrary choice of these parameters as a major source of the theoretical systematic errors as well as uncertainties related to the choice of the scale. This must be included in the final result.
To evaluate these isolation uncertainties (i.e., to determine both the central value and deviations), we use MATRIX to calculate the NLO integrated cross-sections by varying the parameters \( n = 0.1, 0.5, 1, 2, 4, 10 \) and \( E_T^{\text{max}} = 2, 3, 4, 5, 8, 11 \text{ GeV} \); then the results are compared to the NLO cross-sections obtained by running the DIPHOX code using the standard isolation prescription with the same \( E_T^{\text{max}} \) and \( R \) parameters.

\[
\sigma^{\text{NLO}} = \left( \sigma^{\text{NLO, MATRIX}} \right)_{n = n_0} = \sigma^{\text{NLO, DIPHOX}},
\]

\( R \) and \( E_T^{\text{max}} \) are fixed according to the isolation experimental requirement;

The isolation uncertainties are evaluated by varying \( n \) from \( \sim 1/2n_0 \) to \( \sim 2n_0 \). This procedure is adopted in our NNLO calculations (see Section 2.3).

The “central value” of the parameter \( n = n_0 \) depends on the value of \( E_T^{\text{max}} \) (see Table 2); this is consistent with the results of [18].

2.3. NNLO Results and Comparison with Data. We consider proton-proton collisions at the 8 TeV LHC. We choose the invariant mass of the photon pair at the central scale, i.e.,

\[
\mu = m_{\gamma\gamma} < 1700 \text{ GeV},
\]

the Frixione isolation with \( 0.5 < n < 2, E_T^{\text{max}} = 11 \text{ GeV} \), and \( R = 0.4 \) (see (5)), and the following fiducial cuts:

\[
\begin{align*}
\eta_1^\gamma & > 40 \text{ GeV}, \\
\eta_2^\gamma & > 30 \text{ GeV}, \\
|\eta| & < 2.37;
\end{align*}
\]

\[
(m_{\gamma\gamma})_{\text{min}} = \sqrt{2 \left( \eta_1^\gamma \right)_{\text{min}} \left( \eta_2^\gamma \right)_{\text{min}} \cosh (y_1 - y_2) - \cos \sqrt{R_{\gamma\gamma}^2 - (\phi_1 - \phi_2)^2}}_{\text{min}} = 13.7 \text{ GeV}.
\]

The appropriate value of the fine structure constant \( \alpha \) is the value of the electromagnetic coupling at the invariant mass final state \( m_{\gamma\gamma} \), and since \( m_{\gamma\gamma} > 0 \), a value such as \( \alpha_{\text{em}}(\mu = M_Z) \) might be more appropriate than \( \alpha_{\text{em}}(\mu = 0) = 1/137 \). Then \( \alpha \) is fixed to 1/128.9.

Several modern NNLO PDF sets are used (CT14 [21], MMHT14 [22], and NNPDF3.1 [23]); the evolution of \( \alpha \), at 3-loop order is provided by the corresponding PDF set.

For CT14, the central value of the NNLO integrated fiducial cross-section is evaluated at the isolation parameters \( n = n_0 = 0.84, E_T^{\text{max}} = 11 \text{ GeV} \) within the scale choice \( \mu_R = \mu_F = m_{\gamma\gamma} \) (central scale):

\[
\left( \sigma^{\text{NNLO}} \right)_{n=0.84} = 15.60 \pm 0.09 \text{ (num) pb},
\]

calculated at \( r_{\text{cut}} \) extrapolated to zero.

The so-called box (NNLO) contribution to the channel \( gg \rightarrow \gamma\gamma \) is removed from the DIPHOX results to ensure that the comparison holds at the same NLO-order and the fine structure constant \( \alpha \) is fixed to 1/137; the setup is summarized in Table 1 and results are shown in Figures 1-2.

To minimize the difference between the isolation definitions used in the theoretical and the experimental analyses, the central value \( \sigma^{\text{NLO}} \) is determined at the value \( n = n_0 \) so that

\[
\begin{align*}
1.37 & < |\eta| < 1.56, \\
\cosh (y_1 - y_2) & - \cos \sqrt{R_{\gamma\gamma}^2 - (\phi_1 - \phi_2)^2} & \geq & 0.4, \\
\cosh (y_1 - y_2) - \cos \sqrt{0.4^2 - (\phi_1 - \phi_2)^2} & \geq & 0.08,
\end{align*}
\]

and then

\[
1/2 m_{\gamma\gamma} \leq \mu_R, \\
\mu_F \leq 2 m_{\gamma\gamma},
\]

with the constraint

\[
1/2 \leq \frac{\mu_R}{\mu_F} \leq 2.
\]

The relative scale uncertainty in the integrated cross-section is \( \lesssim 5.6 \% \).
Figure 1: The MATRIX integrated fiducial cross-section $\sigma^{NLO}_{tot}$ as a function of the parameter $n$ related to Frixione isolation criterion (see (5)) for different values of $E_T^{max}$.

Figure 2: The MATRIX and the DIPHOX integrated fiducial cross-section $\sigma^{NLO}_{tot}$ as a function of the parameter $n$ related to Frixione isolation criterion (see (5)) for several values of $E_T^{max}$. The “central values” of the parameter $n = n_0$ depend on the value of $E_T^{max}$; they are reported in Table 2.
Table 1: Setup of the diphoton production process used in the NLO runs.

<table>
<thead>
<tr>
<th>DIPHOX v.1.2</th>
<th>MATRIX v.1.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pdf [19]: cteq6</td>
<td>cteq6</td>
</tr>
<tr>
<td>$\alpha$ fixed to 1/137</td>
<td>$\alpha$ fixed to 1/137</td>
</tr>
<tr>
<td>$p_T^\gamma &gt; 25$ GeV, $</td>
<td>\eta\gamma</td>
</tr>
<tr>
<td>80 &lt; $m_{\gamma\gamma}$ &lt; 1700 GeV</td>
<td>80 &lt; $m_{\gamma\gamma}$ &lt; 1700 GeV</td>
</tr>
<tr>
<td>isolation: $R = 0.4$, standard, $E_T^{\text{max}}$.</td>
<td>$R = 0.4$, &quot;smooth&quot;, ($E_T^{\text{max}}$, n)</td>
</tr>
<tr>
<td>fragmentation functions [20]:</td>
<td>-</td>
</tr>
<tr>
<td>BFG set II</td>
<td>-</td>
</tr>
<tr>
<td>The direct part: born only, no box contributions</td>
<td>-</td>
</tr>
</tbody>
</table>

Table 2: The "central values" of the parameter $n = n_\gamma$.

<table>
<thead>
<tr>
<th>$E_T^{\text{max}}$(GeV)</th>
<th>$n_0$</th>
<th>$\sigma_{\text{NLO}}$(pb)</th>
</tr>
</thead>
<tbody>
<tr>
<td>11</td>
<td>0.84</td>
<td>13.78 ± 0.12(num)(_{\pm 1.2})(scale)</td>
</tr>
<tr>
<td>8</td>
<td>1.2</td>
<td>13.36 ± 0.10(num)(_{\pm 9})(scale)</td>
</tr>
<tr>
<td>5</td>
<td>2.0</td>
<td>13.01 ± 0.10(num)(_{\pm 8})(scale)</td>
</tr>
<tr>
<td>2</td>
<td>3.2</td>
<td>13.69 ± 0.11(num)(_{\pm 7})(iso)</td>
</tr>
</tbody>
</table>

The relative isolation uncertainty (at the central scale) is calculated by varying $n$ from 0.5 to 2:

$$\frac{\sigma_{n=0.5} - \sigma_{n=0.84}}{\sigma_{n=0.84}} = +3.8\%$$

$$\frac{\sigma_{n=2} - \sigma_{n=0.84}}{\sigma_{n=0.84}} = -5.5\%$$

(17)

The impact of the variation of the strong coupling constant is also investigated. The change of $\alpha_s(M_Z^2)$ by ±0.001 from the central value 0.118 leads to variations (±0.6%) in the fiducial integrated cross-section. The cross-sections related to CT14, MMHT14, and NNPDF3.1 modern PDF sets are very close to each other with an uncertainty less than 0.4%.

We can write our theoretical prediction of the integrated fiducial cross-section as:

$$\sigma_{\text{tot}}^{\text{fid}} = 15.60$$

$$\pm 0.09 \, \text{(num)} \pm 6.7\% \, \text{(scale)} \pm 3.8\% \, \text{(iso)}$$

$$= 15.60$$

$$\pm 0.09 \, \text{(num)} \pm 1.05 \, \text{(scale)} \pm 0.59 \, \text{(iso)}$$

$$= 15.60^{+1.21}_{-1.24} = (15.6 ± 1.2) \, \text{pb}$$

which is consistent with the experimental data [9]: (16.8 ± 0.8) pb.

Note that the theoretical uncertainties are dominated by both the scale and the isolation systematic errors which are of the same order.

Since this process involves isolated photons in the final state it has a relatively large numerical uncertainty at NNLO after the $r_{\text{cut}} \rightarrow 0$ extrapolation, and as recommended by authors of [6], the distribution calculated at fixed $r_{\text{cut}} = 0.05\%$ must be multiplied by the correction factor:

$$\frac{\sigma_{\text{tot}}^{\text{fid}, r_{\text{cut}}=0.05\%}}{\sigma_{\text{tot}}^{\text{fid}, r_{\text{cut}}=0}} \approx (0.98).$$

The MATRIX differential cross-section is consistent with data as shown in Figures 3-4.

3. Conclusion

We presented the calculation of the integrated and differential cross-sections for the isolated diphoton production in pp collisions at the center–of–mass energy $\sqrt{s} = 8$ TeV in next-to-next-to-leading order (NNLO) QCD using the computational framework MATRIX. A special care was paid to the choice of the Frixione isolation parameters. We kept the same value of $E_T^{\text{max}} = 11$ GeV and $R = 0.4$ used by experimentalists but we adjusted the value of the parameter $n$ until the integrated cross-section calculated by MATRIX matches that calculated by DIPHOX at the same NLO-order (without the Box-contribution to the channel $gg \rightarrow \gamma\gamma$).

Once these parameters were fixed, we calculated the central value of the MATRIX (NNLO) cross-sections and by varying the Frixione parameter $n$ from 0.5 to 2, we estimated the relative isolation uncertainty (±3.8%). The scale uncertainty is found to be equal to (±5.7%).

Both the scale and the isolation uncertainties were of the same order and represent the main source of the theoretical errors; the uncertainties inherent to the $Q_T$-subtraction procedure (≈ 0.6%) and to the variation of the coupling constant $\alpha_s(M_Z^2)$ (≈ 0.8%) were negligible.

Our predictions for the differential and the integrated cross sections are in good agreement with the data. In
The authors declare that they have no conflicts of interest.

Conflicts of Interest

The data used to support the findings of this study are available from the corresponding author upon request.

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