Review Article

Application of Electron Beam Melting to the Removal of Phosphorus from Silicon: Toward Production of Solar-Grade Silicon by Metallurgical Processes

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Removal methods of impurity from metallurgical-grade silicon (Si) are intensively studied to produce solar-grade silicon (SoG-Si) with a smaller economical load and lower cost. Removal of phosphorus (P) has been an important issue because of difficulties in application of conventional metallurgical methods such as solidification refining. Because P evaporates preferentially from molten Si due to its high vapor pressure, electron beam (EB) melting has been applied to the purification of Si. The evaporation of impurity P from Si is considered based on previous thermodynamic investigations here, and several research reports on EB melting of Si are reviewed.

1. Application of EB Melting to Removal of P from Si

Photovoltaic power generation is drawing attention, and the most prevalent material for solar cells is silicon (Si). Monocrystalline, polycrystalline, and amorphous Si accounted for 90% of total solar cell production in 2011 [1]. Conversion efficiency of solar cells depends on the purity of Si [2], and it is generally believed that a purity of 99.9999% is required for solar grade silicon (SoG-Si). The Siemens process, which is used to produce semiconductor grade silicon (99.99999999%), has been applied to SoG-Si; however, the process consumes a large amount of energy because it includes chlorination, distillation, and reduction of Si. Therefore, a less expensive purification method of Si is required for widespread use of solar cells.

To decrease the energy consumed in the production of SoG-Si, methods of removing impurities from metallurgical

grade Si (MG-Si, ~99%) have been developed. These methods include, for example, directional solidifications making use of different solubility of impurity elements into solid and liquid Si. These methods are referred to as “metallurgical processes” to distinguish them from “chemical processes” such as the Siemens process. Table 1 shows examples of acceptable concentrations of impurities in SoG-Si. In one case, the values were defined as the impurity concentration which degrades the conversion efficiency of a solar cell by 10% [3]. Acceptable concentrations were defined more strictly elsewhere [4]. Table 1 also shows the segregation coefficient, which is the ratio of solubility of the element in solid Si and liquid Si at the melting point [5]. Elements with small segregation coefficients, such as Fe and Ti, can be removed from Si by directional solidification. Phosphorus (P) and boron (B), however, are difficult to remove by this means because of their large segregation coefficient. Therefore, new processes have been intensively studied to remove these

TABLE 1: Acceptable contents of impurity in SoG-Si ($C_{\text{SoG-Si}}$) and their equilibrium segregation coefficients (k).

Element	Fe	Al	Cu	Ti	Ca	C	O	P	B
Acceptable content, $C_{\text{SoG-Si}}$ (ppmw) [3]	<1	0.005–0.05	—	<1	<–2	0.5–1	10–20	0.02–2	0.1–10
Acceptable content, $C_{\text{SoG-Si}}$ (ppmw) [4]	<0.007	<0.06	—	$<4 \times 10^{-5}$	—	<3	<4	<0.1	0.1–0.3
Segregation coefficient, k	8×10^{-6}	2×10^{-3}	4×10^{-4}	3.6×10^{-6}	—	0.034–0.3 [3]	0.2–1.25 [3]	0.35	0.72–0.8

elements. The removal of P and B from Si is also a key problem in the recycling of Si from waste products because they are generally used as dopants.

Although removal of a low level of P was previously believed to be impossible, one of the authors (Maeda) applied electron beam (EB) melting under 10^{-2} Pa and demonstrated that removal could be successful [6]. This research showed that the evaporation of P can be promoted by melting under high vacuum. EB melting also has the following additional advantages. (i) Contamination from the atmosphere is prevented. (ii) Contamination from a crucible is also prevented by using a water-cooled copper crucible, with which the bottom part of Si does not melt. (iii) Localized heating by EB generates a convective flow in molten Si, which enhances the removal of P.

Figures 1(a)–1(c) show previously proposed processes to produce SoG-Si from MG-Si [7–9]. These included the vacuum refining to remove P and other elements with high vapor pressure. On the other hand, previous research employed an oxidative removal of boron by applying a steam-added plasma melting method [10, 11]. The proposed processes still require an improvement, and thus techniques for removing B are under intensive investigation. To produce SoG-Si at the lowest possible cost, however, an innovative and simpler process will be needed as Figure 1(d) shows.

2. Considerations on the Evaporation of P from Molten Si Based on Thermodynamics

For effective removal of P from molten Si, it is necessary to understand the mechanism of its preferential evaporation. In this section, the evaporation is discussed based on thermodynamic information on the reaction and then its kinetics is considered.

2.1. Evaporation of P from Molten Si Estimated from Thermodynamic Measurement. Phosphorus evaporates in the forms of P_4 (g), P_2 (g), and P (g) and Gibbs energies of formation of the gas species have been reported [12]. Figure 2 shows predominant gaseous species (i.e., species having the highest vapor pressure) at various temperatures. The vertical axis is the thermodynamic activity of P with reference to red phosphorus. Pure P evaporates at relatively low temperatures mainly as P_4 (g), and the boiling point of white phosphorus is 552 K. Figure 2 also shows that evaporation of P_2 (g) or P (g) becomes more dominant when the activity of P is lower and the temperature is higher. Therefore, in the removal of impurity P from molten Si, evaporations of P_2

(g) and P (g) are important. These reactions have been investigated by performing thermodynamic measurements on Si-P alloys equilibrated with P in the gas phase [13–15]. Miki et al. expressed the standard Gibbs energy changes for monoatomic and diatomic evaporations of P the following, respectively [13]:

$$\begin{aligned} P(g) &= \underline{P}(\text{mass pct, in Si}), \\ \Delta G_1^\circ &= -387,000 + 103T \text{ (J/mol)}, \end{aligned} \quad (1)$$

$$\begin{aligned} \frac{1}{2}P_2(g) &= \underline{P}(\text{mass pct, in Si}), \\ \Delta G_2^\circ &= -139,000 + 43.4T \text{ (J/mol)}. \end{aligned} \quad (2)$$

Figure 3 shows vapor pressure of P (g) and P_2 (g) (p_P and p_{P_2} , resp.) at 1800 and 2000 K calculated by the previous equations. Evaporation of P (g) is more dominant than P_2 (g) when P content in Si is lower. Raising temperature also causes the evaporation of P to become dominant. Vapor pressure of Si (g), p_{Si} , was calculated by (3) [16] and is shown in Figure 3:

$$\begin{aligned} \text{Si(g)} &= \text{Si(l)}, \\ \log p_{\text{Si}} &= -20900 \times \left(\frac{1}{T}\right) - 0.565 \times \log T + 12.9. \end{aligned} \quad (3)$$

2.2. Evaporation Rate of P from Molten Si and Evaporation Coefficient. When impurity P evaporates from molten Si, the following steps might determine the rate of the entire reaction [17, 18]:

- (i) transport of P atoms in the molten Si to liquid/gas surface,
- (ii) formation of P atoms adsorbed on the liquid surface,
- (iii) formation of P_2 molecules from the P atoms on the surface,
- (iv) evaporation of the adsorbed P atoms or P_2 molecules,
- (v) transport of the P (g) or P_2 (g) through the gas phase away from the liquid/gas surface.

Because EB melting generates a convective flow in molten Si, step (i) is not believed to determine the reaction rate, especially when a small amount of Si is melted. Kemmotsu et al. examined the P removal from molten Si stirred by injecting Ar gas and confirmed that the stirring did not enhance the removal [19]. Step (v) is also assumed to be ignorable because P evaporates under high vacuum. Experimental results by Miyake and his colleagues showed that removal rate of P

FIGURE 1: Proposed refining processes to purify MG-Si to SoG-Si.

FIGURE 2: Estimation of predominant gaseous species in equilibrium [12]. Reference state of phosphorus activity is red phosphorus.

under low vacuum (higher than 1 Pa) was similar to that under higher vacuum, suggesting there was no influence of the pressure in this range [20]. Therefore, steps (ii)~(iv) are the most likely rate-determining steps. The rate of evaporation might be expressed by the Hertz-Knudsen-Langmuir equation [21]:

$$J_i = \beta p_i \sqrt{\frac{M_i}{2\pi RT}}, \quad (4)$$

where J_i (kg/m²·s) is the evaporation rate of chemical species i , p_i (Pa) is equilibrium vapor pressure, M_i (kg/mol) is molar mass, and R is gas constant. β is a coefficient assumed to be unity here.

Figure 4(a) shows evaporation rate of P and Si calculated by (4) using p determined by (1), (2), and (3). As discussed by others [13], the content of P in Si decreases when a ratio of

FIGURE 3: Equilibrium vapor pressure of impurity P and Si at 1800 K (broken line) and 2000 K (solid line).

the evaporation rate of P to that of Si is larger than the weight concentration of P in molten Si (see (5)):

$$\frac{J_P + J_{P_2}}{J_{Si}} > \frac{[P]}{100}. \quad (5)$$

Using (5), an evaporation coefficient, α , is defined by the following as an index of purification:

$$\alpha = \frac{J_P + J_{P_2}}{J_{Si}} \frac{100}{[P]}. \quad (6)$$

When α is larger than 1, P content in molten Si decreases during melting. As plotted in Figure 4(b), α becomes almost constant for smaller $[P]$ because the evaporation of P_2 is less

FIGURE 4: (a) Evaporation rate of P and Si from molten Si at 1800 K (broken line) and 2000 K (solid line). (b) Evaporation coefficient.

significant. If the evaporation of P_2 is ignored, α is expressed by the following which was derived from (4) and (6):

$$\alpha = \frac{100 p_{[P]=1} \sqrt{M_P}}{p_{\text{Si}}^\circ \sqrt{M_{\text{Si}}}}, \quad (7)$$

where $p_{[P]=1}$ is vapor pressure of P (g) equilibrated with P in Si at $[P] = 1$ wt%.

2.3. Estimated Weight of Si and P during Melting. Because energy cost and yield are important in the production of SoG-Si, the evaporation of Si during EB melting should not be ignored. The change of Si weight and P content during the melting is estimated based on (4). Purification of Si of W_{Si} (kg) containing P of W_P (kg) is considered. The weight percentage of P in Si, $[P]$, is expressed as follows:

$$[P] = 100 \times \frac{W_P}{W_{\text{Si}}}. \quad (8)$$

Surface area of molten Si is assumed to be constant at A (m^2), and evaporations of Si and monoatomic P are taken into account. The evaporation rate of P is expressed as follows:

$$J_P = p_{[P]=1} \sqrt{\frac{M}{2\pi RT}} \times [P]. \quad (9)$$

By defining $a = p_{[P]=1} \sqrt{M/2\pi RT}$, the temporal change in W_P is expressed as follows:

$$\frac{dW_P}{dt} = -AJ_P = -Aa[P]. \quad (10)$$

An evaporation rate of Si is expressed as follows:

$$\frac{dW_{\text{Si}}}{dt} = -AJ_{\text{Si}} = Ab, \quad (11)$$

where $b = p_{\text{Si}} \sqrt{M_{\text{Si}}/2\pi RT}$ from (4). From (10) and (11), W_{Si} and W_P are expressed by (12) and (13) as functions of time using the initial weight, W_P° and W_{Si}° :

$$W_P = W_P^\circ \left(1 - \frac{Abt}{W_{\text{Si}}^\circ} \right)^{100a/b}, \quad (12)$$

$$W_{\text{Si}} = W_{\text{Si}}^\circ - Abt. \quad (13)$$

Figure 5 shows changes in W_P and W_{Si} at 1800 and 2000 K, calculated by (12) and (13) assuming $W_P^\circ = 0.0000025$, $W_{\text{Si}}^\circ = 0.25$, and $A = 10^{-2} \text{ m}^2$. Initially, $[P]$ is 0.001, and its change is also plotted below. Looking at the time required for purification, smelting at higher temperature is advantageous.

3. Reported Research and Rate Constants

Previous research findings on the removal of P by EB melting are listed in Table 2. Ikeda and Maeda [6] investigated the effect of the EB power and surface temperatures of molten Si on the removal rate of impurities. Miyake et al. [20] melted P-doped Si under a low vacuum (5–7 Pa) and found little influence of the pressure on the removal rate. Hanazawa et al. [22, 23] reported that the content of P decreased to 0.1 ppm, which is below the acceptable content for SoG-Si. More recently, large-scale demonstration, numerical simulation, and optimization of melting techniques have been reported. Table 3 shows that research on P removal from molten Si not by EB melting but by induction furnaces.

In some research, experimental results on P removal were assessed by estimating the apparent mass transfer coefficient. When a first-order reaction is assumed, the coefficient, k_1 , is defined as follows:

$$-\frac{d[P]}{dt} = k_1 \frac{A}{V} [P]. \quad (14)$$

If the evaporation is the rate-determining step, the following is derived from (4):

$$k_1 = \frac{100}{\rho_{\text{Si}}} \sqrt{\frac{M_P}{2\pi RT}} \exp \frac{\Delta G_1^\circ}{RT}. \quad (15)$$

A mass transfer coefficient assumed, a second-order reaction (i.e., evaporation of P_2) is defined as k_2 in the following:

$$-\frac{d[P]}{dt} = k_2 \frac{A}{V} [P]^2. \quad (16)$$

Miki et al. [13] estimated the time variation of P content in Si using k_1 and k_2 derived from (1), (2), and (4). Previous

FIGURE 5: Estimated changes in W_P and W_{Si} during melting at (a) 1800 and (b) 2000 K.

FIGURE 6: Apparent mass transfer coefficient of P removal from molten Si.

research discussed their experimental results assuming first-order reaction and reported values of k_1 as shown in Tables 2 and 3. Although there are differences between reported values, k_1 is roughly in agreement. These values are plotted in Figure 6 with the estimated values from (15). Some experiments obtained k_1 higher than the estimated line below 1900 K. One possible reason is that P evaporates in forms of P and P_2 . Temperature inhomogeneity of molten Si also might have caused the deviation; that is, local temperature

of Si surface might be higher than estimated because of localized heating with EB, and P might have evaporated there preferentially. In addition, because P is a surface-active element, it is assumed to concentrate on the surface of molten Si [40]. This effect is believed to enhance its evaporation, although previous research has discussed this only minimally. Deviations at higher temperatures might be caused by mass transport of P in molten Si or gas phase. Shi et al. [31] and Zheng et al. [36] discussed their results by considering an overall mass transfer coefficient, which was a combination of the reaction step and the mass transport.

4. Additional Availability of EB Melting

As previously reported, EB melting of Si can remove not only P but also other impurities which have high vapor pressures. The authors' group reported removal of Ca, Al [6], and Sb [20] from molten Si during EB melting. More recent studies confirmed removals of not only these impurities but also other elements [29, 41–43]. Among impurities, however, C and B were not removed by the melting because of low vapor pressure. On the other hand, the element might be removed by oxidizing (Figure 1) similar to decarburization in steel making. Therefore, plasma melting [11] and slag refining [44–46] are under development for B removal from Si. After the oxidizing treatment, oxygen in Si is easily removed by EB melting because of the high vapor pressure of SiO (g).

In addition to the processes mentioned previously, various methods have been developed to remove impurities

TABLE 2: Previous research on removal of P by EB melting.

	EB power/kW	Weight of Si sample/kg (or supply rate)	Temperature/K	Chamber pressure/Pa	P content in ppm (time)	Apparent mass transfer coefficient, $k_1/m \text{ s}^{-1}$
Ikeda and Maeda (1992) [6]	3.8~6.5	0.05	1867~1967	$10^{-3} \sim 10^{-2}$	38~45 $\rightarrow$ 3 (900 s)	
Hanazawa et al. (2003, 2004) [22, 23]						
(i) Batch process in laboratory scale	30~100	1.2~6.6	1950~2300	$1.3 \sim 6.7 \times 10^{-2}$	30 $\rightarrow$ 0.05~0.06 (2200 s)	
(ii) Batch process in industrial scale	190, 210	45		$2.7 \sim 8.0 \times 10^{-2}$		
(iii) Continuous process in laboratory scale	80	2~12 kg h^{-1} (supply rate)		$1.3 \sim 6.7 \times 10^{-2}$	25~30 $\rightarrow$ 0.3 (4600 s)	
(iv) Continuous process in industrial scale	220, 250	16~70 kg h^{-1} (supply rate)		$1.3 \sim 8.0 \times 10^{-2}$	25~30 $\rightarrow$ 0.1 (4200 s)	
Pires et al. (2003) [24]						
Observation of segregation	14~17	0.28 (powder)	NA	$10^{-4} \sim 10^{-2}$	? $\rightarrow$ 0.28~5.5 (1200 s)	
Pires et al. (2005) [25]	15~17	0.28 (powder) 0.28 (massive)	NA	$10^{-4} \sim 10^{-2}$	23 $\rightarrow$ 0.41 (1200 s) 38 $\rightarrow$ 0.39 (1200 s)	
Miyake et al. (2006) [20]						
Glow discharge EB	2.6~4.8	0.04	1850	5~7	140~230 $\rightarrow$ 1 (3600 s)	
Kemmotsu et al. (2011) [19]						
(i) Water-cooled Cu crucible	2.6	0.04	1860	10^{-2}	87 $\rightarrow$ 2.9 (1800 s)	2.0×10^{-5} (1860 K)
(ii) Graphite crucible	2.6	0.04	1980	10^{-2}	166 $\rightarrow$ 0.9 (1800 s)	
(iii) Graphite crucible	4.8	0.04	2520	10^{-2}	62 $\rightarrow$ 5.2 (180 s)	
(iv) Stirred by Ar bubbling					37 $\rightarrow$ 10 (90 s)	
(v) 0.1% O_2 - H_2 blowing					37 $\rightarrow$ 9.4 (90 s)	
(vi) 0.1% O_2 - H_2 bubbling					37 $\rightarrow$ 1.5 (180 s)	
(vii) Glow discharge EB	4.8	0.04	1860	1	106 $\rightarrow$ 5.2 (900 s)	
Luo et al. (2011) [26]	10~15	0.4	NA	$2.5 \sim 5.0 \times 10^{-3}$	20 $\rightarrow$ 1 (1200 s)	
Jiang et al. (2012) [27]						
Candle melting	6	0.7	NA	2×10^{-3}	144 $\rightarrow$ 60 (300 s)	
Mei et al. (2012) [28]	11~13	0.2	NA	10^{-3}	50 $\rightarrow$ 1.8 (20 min melting followed by zone melting)	—
Liu et al. (2012) [29]						
Industrial scale	350	500	NA	10^{-3}	15 $\rightarrow$ 0.07	—
Tan et al. (2013) [30]	21	0.3	2001	10^{-3}	16 $\rightarrow$ 0.16 (1400 s)	
	9	0.3	1941	$0.5 \sim 5 \times 10^{-2}$		1.07×10^{-5} (1941 K)
Shi et al. (2013) [31]	15		1964			1.44×10^{-5} (1964 K)
	21		2051		3320 $\rightarrow$ 7 (1920 s)	2.59×10^{-5} (2051 K)
Choi et al. (2013) [32]	12	0.25		1×10^{-2}	34 $\rightarrow$ 4.5 (2640 s)	

TABLE 3: Previous research on removal of P by induction furnace.

	Weight of Si sample/kg	Temperature/K	Chamber pressure/Pa	P content in ppm (time)	Apparent mass transfer coefficient, $k_1/\text{m s}^{-1}$
Suzuki et al. (1990) [33]	0.02	1723~1823	2.7×10^{-2}	32 → 6~7 (2700 s)	1.6×10^{-5} (1723 K) 2.0×10^{-5} (1823 K)
Yuge et al. (1997) [34]	0.02, 0.04, 1	1722~1915	$0.8 \sim 3.6 \times 10^{-2}$	7 → <0.1 (7200 s)	$\ln k_1 = -2.29 - 15600/T$
Zheng et al. (2010) [35] (2011) [36, 37]	5	1823	0.03	15 → 11 (7200 s)	(Dependence on pressure was studied) $10^{-5} \sim 10^{-6}$ at 0.01~1 Pa, Below 10^{-9} at over 10000 Pa (1783 K)
		1873	0.03~0.07	15 → 7.3 (7200 s)	
		1923	0.03~0.13	15 → 2.6 (7200 s)	
		1923	0.02~0.09	15 → 1.7 (7200 s)	
		1973	0.04~0.25	15 → 0.41 (7200 s)	
		1973	0.01~0.05	15 → 0.15 (7200 s)	
	—	1873	0.6~0.8	460 → 10 (3600 s)	
Safarian and Tangstad (2012) [38, 39]	0.3	1773	0.5	17 → 9.8 (900 s)	2.3×10^{-6} (1773 K)
		1873		17 → 5.9 (900 s), 1.5 (1800 s)	4.9×10^{-6} (1873 K)
		1873		24 → 19 (3600 s)	2.2×10^{-6} (1873 K)
		1973		24 → 0.4~3 (9000 s)	1.9×10^{-5} (1973 K)

in Si: for example, solidification using solvent metals and acid leaching [47]. To achieve production of SoG-Si by an economic process with low energy consumption, it will be necessary to bring together a great amount of expertise in the metallurgical technologies which have been developed for various metals.

5. Conclusion

EB techniques applied to removal of P from Si were reviewed. EB melting is believed to play an important role in the refining of Si because of its unique heating characteristics. It is necessary to integrate the scientific knowledge based on thermodynamic discussion and metallurgical technologies which have been developed for various metals toward an economical and environmentally friendly refining process for SoG-Si.

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