Among many engineering advantages in concrete, low thermal conductivity is an attractive property. Concrete has been widely used for nuclear vessels and plant facilities for its excellent radiation shielding. The heat isolation through low thermal conductivity is actually positive for nuclear power plant concrete; however the property may cause adverse effect when fires and melt-down occur in nuclear vessel since cooling down from outer surface is almost impossible due to very low thermal conductivity. If concrete containing atomic reactor has higher thermal conductivity, the explosion risk of conductive may be partially reduced. This paper presents high thermally conductive concrete development. For the work, magnetite with varying replacements of normal aggregates and steel powder of 1.5% of volume are considered, and the equivalent thermal conductivity is evaluated. Only when the replacement ratio goes up to 30%, thermal conductivity increases rapidly to 2.5 times. Addition of steel powder is evaluated to be effective by 1.08−1.15 times. In order to evaluate the improvement of thermal conductivity, several models like ACI, DEMM, and MEM are studied, and their results are compared with test results. In the present work, the effects of steel powder and magnetite aggregate are studied not only for strength development but also for thermal behavior based on porosity.

1. Introduction

Concrete, as a construction material, has many engineering advantages and an effectiveness to corrosion control [1, 2]. Several weaknesses like cracking caused by drying shrinkage and hydration heat have been reported and they can cause more rapid steel corrosion accelerated. For chloride attack, crack effect on enlarged diffusion has been studied [3, 4] and it has been also investigated for rapid carbonation behavior [5–7]. However concrete still has been widely used for its cost-benefit and stable dimensional behavior. Nuclear containment and vessels need strong barrier against radioactivity so that concrete structure is mainly constructed for the use [8, 9]. Another engineering merit is very low thermal conductivity compared with steel by 1/40–1/50 [10, 11], which can provide very stable conditions for nuclear reactor inside [12, 13]. A few years ago, nuclear explosion at Fukushima in Japan happened and the disastrous effects are still in progress [14, 15]. When temperature of reactor is rapidly raised and cooling system inside is out, the huge concrete container acts as insulation vessel so that the explosion risk increases as well. In the disaster at Fukushima, cooling water is poured to the outer surface concrete but the effect is almost negligible since concrete intrinsically has low thermal conductivity. Even if concrete with high thermal conductivity has little effect on cooling down of reactor, the risk of additional explosion may be reduced.

This paper presents a concrete mix design for higher thermal conductivity adopting MA (magnetite aggregate) and SP (steel powder). Concrete is composite material containing gravel, sand, and air in pore. The individual thermal properties have already been studied [16, 17] and the mineral admixtures such as FA (Fly Ash) and GGBFS (Ground Granulated Blast Furnace Slag) are also investigated. ACI 122R provided a guideline for calculation of thermal conductivity using weight measurement of concrete; however the techniques are only for normal concrete [18].
In the present paper, MA and SP with high thermal conductivity are partially replaced with normal aggregates. Enlarging up to 42.3% of MA and 1.5% of SP for concrete volume, thermal conductivities of concrete are evaluated and the results are compared with those from several models like ACI 122R Model, DEMM (Differential Effective Medium Model), and MEM (Modified Eshelby Model) which can consider equivalent thermal conductivity in three-phase composites. The thermal behaviors and basic engineering properties of concrete are discussed in the work with varying volume ratios of MA and SP.

2. Analysis Technique for Thermal Conductivity

2.1. Background Theory

2.1.1. Upper and Lower Level of Thermal Conductivity. The upper and lower equivalent thermal conductivity in layered-composite can be determined as the two conditions in Figure 1, whose theory can be applied to mass transport like water [19, 20].

The upper and lower conductivity can be obtained as (1) and (2), respectively, which are based on the assumptions like (1) without exothermic reaction, (2) constant thermal conduction, and (3) isolated from input/output of heat flow:

\[ Q_{eq} = \frac{A}{(A_{1}/Q_{1} + A_{2}/Q_{2} + \cdots + A_{n}/Q_{n})} = \frac{1}{\sum A_i/Q_i}, \quad (1) \]
\[ Q_{eq} = \frac{(A_{1}/Q_{1} + A_{2}/Q_{2} + \cdots + A_{n}/Q_{n})}{A} = \sum A_i/Q_i, \quad (2) \]

where \( Q_{eq} \) is equivalent thermal conductivity and \( Q_i \) is thermal conductivity in each material, \( A_i \) and \( A_f \) are each area and area fraction of each material, respectively. The above models cannot present the changes in thermal conductivity of concrete since concrete itself is not homogeneous with pores, aggregates, and cement hydrates.

2.1.2. Models for Equivalent Thermal Conduction of DEMM, MEM, and ACI 122R. The above theories in Section 2.1.1 have very limited application to thermal conduction in concrete since it contains pores and aggregates arbitrarily. The lower and upper limitation can be applied to thin plate and fiber composites. The pores and aggregates in concrete can be assumed as spherical shape which are irregularly scattered in concrete. The models of DEMM and MEM can handle equivalent thermal conductivity in composite with 3 phases.

(1) DEMM (Differential Effective Medium Model) [21–23]. The generalized DEMM with different components can be written as (3) with 1st differential equation form:

\[ \frac{dk_c}{df} = \frac{k_c \cdot k_c - k_f \cdot k_f}{(1 - f) \cdot S - k_c}, \quad (3) \]

where \( k_c, k_f, S, f, \) and \( f_i \) are equivalent thermal coefficient in composite, each thermal coefficient in spherical particle, polarization coefficient, total volume ratio (=1.0), and each volume ratio of component, respectively. In order to consider 3 components, one component is firstly calculated and the result is reconsidered as original medium. The thermal conductivity in reconsidered medium \( (k_{m1}) \) can be written as

\[ (k_{m1})^{3} - 3 \left( \frac{k_{f1}}{k_{m1}} \right) \left( \frac{k_{m1}}{k_{m1}} \right)^{2} + 3 \left( \frac{k_{f1}}{k_{m1}} \right)^{2} \left( \frac{k_{m1}}{k_{m1}} \right) \]
\[ + (1 - f'_{1})^{3} \left( \frac{k_{f1}}{k_{m1}} - 1 \right)^{3} \frac{k_{m1}}{k_{m1}} - \left( \frac{k_{f1}}{k_{m1}} \right)^{3} = 0, \]

where \( k_{m1} \) is thermal conductivity in original medium and \( k' \) is obtained as

\[ f'_{1} = \frac{f_{1}}{1 - f_{2}}. \]

The final equivalent thermal conductivity \( (k_e) \) can be obtained through recalculating \( k_{m1} \) as

\[ (k_{e})^{3} - 3 \left( \frac{k_{f1}}{k_{e}} \right) \left( \frac{k_{e}}{k_{m1}} \right)^{2} + 3 \left( \frac{k_{f1}}{k_{m1}} \right)^{2} \left( \frac{k_{e}}{k_{m1}} \right) \]
\[ + (1 - f_{2})^{3} \left( \frac{k_{f2}}{k_{m1}} - 1 \right)^{3} \frac{k_{m1}}{k_{m1}} - \left( \frac{k_{f2}}{k_{m1}} \right)^{3} = 0. \]

The derived equivalent thermal conductivity is compared with the results of test, MEM, and ACI 122R.

(2) MEM (Modified Eshelby Model) [22–24]. In the MEM, 2 spherical components with different thermal conductivity are irregularly arranged in concrete with constant thermal conductivity and it is subject to constant thermal velocity of \( q^{0} \) (x3 direction). The MEM is shown in Figure 2 [22].

In Figure 2, constant thermal velocity \( q^{0} \) can be written as (7) in which \( K_{m} \) and \( Z^{0} \) are equivalent thermal conductivity matrix and constant thermal gradient without components. When the fluctuating temperature in the composite is integrated, the result is zero so that the condition of (8) can be assumed [22, 23]:

\[ q^{0} = -K_{m}Z^{0}, \quad (7) \]
\[ \overline{Z} + f_{1} \left( Z^{1} - Z^{*1} \right) + f_{2} \left( Z^{2} - Z^{*2} \right) = 0, \quad (8) \]
where $Z^i$ and $Z^{i\ast}$ are disturbed temperature gradient and intrinsic temperature gradient from Eshelby model in $i$ component. $Z$ is average of disturbed temperature gradient.

The intrinsic temperature gradient can be obtained as (9a) and (9b) through matrix transformation:

$$Z^{i\ast} = (A_{11} - A_{12}A_{22}^{-1}A_{21})^{-1}(D_1 - A_{12}A_{22}^{-1}D_2)q^0 = F_1q^0,$$

$$Z^{i2} = (A_{22} - A_{21}A_{12}^{-1}A_{11})^{-1}(D_2 - A_{21}A_{12}^{-1}D_1)q^0 = F_2q^0.$$  \hspace{1cm} (9a)  

$$K_c = (K_m + f_1F_1 + f_2F_2)^{-1},$$

$$\frac{k_c}{K_m} = 1 + 3\left[1 - \frac{1}{(k_{f1} - k_m)}\frac{(k_{f1} + 2k_m)}{f_1 - \frac{(k_{f1} - k_m)}{(k_{f2} + 2k_m)}}\right].$$  \hspace{1cm} (13)  

$$A_{11} = \left\{ (K_{f1} - K_m) \left[ (1 - f_1) S^1 + f_1I \right] + K_m \right\},$$

$$A_{12} = f_2 \left( K_m - K_{f2}^i \right) (S^2 - I),$$

$$D_1 = (K_m - K_{f1}^i) K_m^{-1},$$

$$A_{21} = f_1 \left( K_m - K_{f2}^i \right) (S^3 - I),$$

$$A_{22} = \left\{ (K_{f2} - K_m) \left[ (1 - f_2) S^2 + f_2I \right] + K_m \right\},$$

$$D_2 = (K_m - K_{f2}^i) K_m^{-1}.\hspace{1cm} (10)$$

Then component of $A_{ij}$ and $D_i$ can be written as the following equations [22]:

$$q^0 = -K_cZ_c = q_c.$$  \hspace{1cm} (12)

The equivalent temperature gradient ($Z_c$) is written as (11) with temperature gradient of base media ($Z_m$) and each component ($Z_f$):

$$Z_c = (1 - f)Z_m + f_1Z_{f1} + f_2Z_{f2}.\hspace{1cm} (11)$$

Considering the previous equations of (8)–(12), the equivalent conductivity matrix ($K_c$) is derived as (13). Since the matrix of $K_c$, $F_1$, and $F_2$ is diagonal matrix, the equivalent thermal conductivity with 3 different phases is derived as (14). Consider

$$k_c = 0.0720 e^{0.00125d},\hspace{0.5cm} \text{Oven dried},\hspace{1cm} (15a)$$

$$k_c = 0.0865 e^{0.00125d},\hspace{0.5cm} \text{Air dried},\hspace{1cm} (15b)$$

where $k_c$ and $d$ are thermal conductivity (W/m·K) and weight (kg/m$^3$) in concrete.

3. Experimental Program for High Thermal Conductive Concrete with MA and SP

3.1. Mix Proportions. The previous mix proportions for nuclear power plant concrete are utilized, containing 20% replacement ratio of FA (Fly Ash) and W/C ratio of 0.4 [12]. The mix proportions for the study are listed in Table 1.

In Table 1, M50M25S denotes 50% replacement ratio of MA for gravel, 25% replacement ratio of MA for sand, and addition of SP with 1.5% of total volume. The chemical compositions of OPC and FA are listed in Table 2. The physical properties of aggregates are presented in Table 3 and the physical properties of SP are also presented in Table 4. The photos of SP and MA are shown in Figure 3.

3.2. Thermal Conductivity Test. The samples with 9 cases are prepared and the test is performed referring to KS L ISO 8302 method [25]. The samples have the geometry with 100 × 100 × 50 mm. The test equipment and the samples are shown in Figure 4.
Table 1: Mix proportions for concrete test.

<table>
<thead>
<tr>
<th>Type</th>
<th>W</th>
<th>C</th>
<th>FA</th>
<th>G</th>
<th>S</th>
<th>WRA</th>
<th>MG</th>
<th>MS</th>
<th>SP</th>
<th>R (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Control</td>
<td>163</td>
<td>324</td>
<td>82</td>
<td>935</td>
<td>750</td>
<td>2</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>M50M25</td>
<td>210</td>
<td>420</td>
<td>105</td>
<td>468</td>
<td>563</td>
<td>2</td>
<td>468</td>
<td>188</td>
<td>0</td>
<td>22.9</td>
</tr>
<tr>
<td>M50M25S</td>
<td>210</td>
<td>420</td>
<td>105</td>
<td>468</td>
<td>563</td>
<td>2</td>
<td>468</td>
<td>188</td>
<td>120</td>
<td>22.9</td>
</tr>
<tr>
<td>M50M50</td>
<td>216</td>
<td>432</td>
<td>108</td>
<td>468</td>
<td>375</td>
<td>2</td>
<td>468</td>
<td>375</td>
<td>0</td>
<td>29.3</td>
</tr>
<tr>
<td>M50M25S</td>
<td>216</td>
<td>432</td>
<td>108</td>
<td>468</td>
<td>375</td>
<td>2</td>
<td>468</td>
<td>375</td>
<td>120</td>
<td>29.3</td>
</tr>
<tr>
<td>M90M25</td>
<td>220</td>
<td>440</td>
<td>110</td>
<td>104</td>
<td>563</td>
<td>2</td>
<td>831</td>
<td>188</td>
<td>0</td>
<td>35.9</td>
</tr>
<tr>
<td>M90M25S</td>
<td>220</td>
<td>440</td>
<td>110</td>
<td>104</td>
<td>563</td>
<td>2</td>
<td>831</td>
<td>375</td>
<td>0</td>
<td>35.9</td>
</tr>
<tr>
<td>M90M50</td>
<td>230</td>
<td>460</td>
<td>115</td>
<td>104</td>
<td>375</td>
<td>2</td>
<td>831</td>
<td>375</td>
<td>0</td>
<td>42.3</td>
</tr>
<tr>
<td>M90M50S</td>
<td>230</td>
<td>460</td>
<td>115</td>
<td>104</td>
<td>375</td>
<td>2</td>
<td>831</td>
<td>375</td>
<td>120</td>
<td>42.3</td>
</tr>
</tbody>
</table>


Table 2: Chemical compositions of binder (OPC and FA).

<table>
<thead>
<tr>
<th>Type</th>
<th>SiO₂</th>
<th>Fe₂O₃</th>
<th>CaO</th>
<th>MgO</th>
<th>SO₃</th>
<th>Al₂O₃</th>
<th>TiO₂</th>
<th>The others</th>
<th>Ig.loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>OPC</td>
<td>21.95</td>
<td>2.81</td>
<td>60.12</td>
<td>3.32</td>
<td>2.11</td>
<td>6.59</td>
<td>—</td>
<td>3.1</td>
<td>1.85</td>
</tr>
<tr>
<td>FA</td>
<td>53.60</td>
<td>9.40</td>
<td>4.70</td>
<td>2.60</td>
<td>1.80</td>
<td>4.2</td>
<td>3.8</td>
<td>3.4</td>
<td></td>
</tr>
</tbody>
</table>

Table 3: Physical properties of aggregate.

<table>
<thead>
<tr>
<th>Types</th>
<th>Gₘₐₓ (mm)</th>
<th>Density (kg/m³)</th>
<th>Absorption ratio (%)</th>
<th>Fineness modulus</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sand</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Normal</td>
<td>5</td>
<td>2,550</td>
<td>2.20</td>
<td>2.40</td>
</tr>
<tr>
<td>Magnetite</td>
<td>5</td>
<td>4,200</td>
<td>2.21</td>
<td></td>
</tr>
<tr>
<td>Coarse aggregate</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Normal</td>
<td>19</td>
<td>2,500</td>
<td>0.80</td>
<td>7.10</td>
</tr>
<tr>
<td>Magnetite</td>
<td>19</td>
<td>4,180</td>
<td>—</td>
<td>6.80</td>
</tr>
</tbody>
</table>

4. Evaluation of Strength, Weight, and Thermal Conductivity

4.1. Test Results of Compressive Strength, Weight, and Thermal Conductivity. Compressive strength is measured after submerged curing for 28 days, referring to KS F 2403. The samples show compressive strength higher than 40 MPa and the effect of MA and SP on strength development is not significant. The test results of compressive strength with weight are shown in Figure 5 considering replacement ratio of MA. The weight increases to 127% when replacement of volume reaches 42.3% (M90M50S).

The strength shows slight reduction when MA replacement ratio goes up to 40% with SP addition. The reasons are different fineness modulus of MA from normal aggregate and absorbed WRA around SP with carbon [26, 27].

The previous studies report that thermal conductivities of SP and MA are in the range of 46.5–58.2 (W/m·K) and 6–23 (W/m·K), respectively [28]. The values vary with moisture content. The thermal conductivities in normal concrete components are summarized in Table 5 [29].

The test results of thermal conductivity are shown in Figure 6, which shows increment by 2.54–2.74 times in the case of maximum replacement (42.3% volume of replacement). Up to 22.9% of replacement ratio, the effect of replacement of MA on thermal conductivity seems to be small but from 29.3% the values of thermal conductivity rapidly increase to 3.441 W/m·K. The effect of SP shows reasonable increase in thermal conductivity with increasing MA replacement as shown in Figure 7.

4.2. Comparison of Test Results with Previous Models. In the chapter, models of DEMM, MEM, and ACI explained in Section 2.1.2 are attempted for comparison with test results. The variables of MA and SP are assumed based on the previous research [29, 30]. Table 6 lists the analysis conditions for equivalent thermal conductivity in composite with 3 phases.

Actually the tested concrete has several components containing different thermal conductivities such as air content, cement hydrates, coarse aggregate, sand, and FA. However, MA and SP have relatively higher thermal conductivity than the components in normal concrete, so that 3 phases are determined as normal concrete, MA, and SP for thermal conductivity evaluation. In the case without SP, two-phase analysis is conducted. The comparisons with test and equivalent models are shown in Figure 8 including ACI model.

As shown in Figure 8, the results from DEMM, MEM, and ACI models are reasonably in agreement with those from test over 30% replacement of MA, which shows about 2/3 level of upper limit.

The reasons for the relatively big errors can be explained in several ways. The sample was prepared with 100 × 100 × 50 mm and has thickness of 50 mm with 1 hour of test period. If thickness decreases below 50 mm, prompt increase can be expected; however concrete has 19 mm of coarse aggregated size. If normal aggregate and pores are concentrated in the particular area, concrete cannot reflect the effect of magnetite.
Table 4: Physical properties of SP.

<table>
<thead>
<tr>
<th>Density (g/cm³)</th>
<th>Purity (%)</th>
<th>Melting point (°C)</th>
<th>Particle size (mm)</th>
<th>Carbon content (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>7.87</td>
<td>over 98.0</td>
<td>932</td>
<td>&lt;5 mm</td>
<td>&lt;1.5%</td>
</tr>
</tbody>
</table>

Table 5: Thermal conductivity in normal concrete component (in room condition).

<table>
<thead>
<tr>
<th>Types</th>
<th>OPC mortar</th>
<th>FA mortar</th>
<th>Normal aggregate</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thermal conductivity (W/m·K)</td>
<td>1.2</td>
<td>0.9</td>
<td>1.3–2.8</td>
</tr>
</tbody>
</table>

4.3. Porosity and Thermal Conductivity. The thermal conductivity in concrete is much lower than that in SP and MA so that concrete as media is assumed as containing constant thermal conductivity in Section 4.2. However, the conductivities of air, cement hydrates, and normal aggregate are all different. The larger pores it has, the lower thermal conductivity it also has, since conductivity of air is much lower than that of concrete by about 70 times [10, 11]. The measured porosities through MIP are shown in Figure 9 and the reduced porosity is consistent with the increased thermal conductivities.
Compressive strength (MPa)
Compressive strength with SP (MPa)
Control (MPa)

(a) Volume and strength

Figure 5: Changes in physical performance with varying MA replacement ratios.

(b) Volume and self-weight

Figure 6: Measured thermal conductivity varying replacement ratios.

The addition of SP (2~4% of volume) is reported to cause the reduced porosity and enhancement of chloride resistance [31, 32]. The used MA has more small particles, which leads to pore compaction. Pores and its connectivity play an important role in thermal conductivity and heat transfer. The relatively higher porosity before replacing MA has lower thermal conductivity and it rapidly increases with reduced porosity and addition of MA and SP with much higher thermal conductivity.

In the paper, concrete mix technique which can increase thermal conductivity is attempted through replacing magnetite aggregate and adding steel powder, and the results are compared with several models aiming at equivalent conductivity with 3 different phases. With consideration of each component’s characteristics, these models can provide more reasonable results. In the mix proportions for concrete with high thermal conductivity, fundamental performances such as strength and workability should be satisfied. More replacement of MA and addition of SP can increase the self-weight and thermal conductivity in nuclear power plant concrete; however its performances should be considered in advance.

5. Conclusions

(1) Replacing normal aggregates with magnetite aggregates (42.3% of volume) and adding steel powder (1.5% of volume), thermal conductivity increases to 2.54~2.74 times to control mixture. Several models like DEMM, MEM, and ACI show reasonable agreement with test results and the overall test results are in the range of 2/3 of upper limit.
(2) The replacement of MA is evaluated to be effective when it is up to 30%. Steel powder is also effective, which shows 106∼113% increment of thermal conductivity with increasing MA replacement ratio. The reduced porosity due to SP and MA is also effective for increasing thermal conductivity.

(3) The low increasing thermal conductivity below 30% of magnetite replacement is caused by heterogeneous property in concrete since it randomly has pores, hydrates, and aggregates in the test sample thickness. The late response of thermal conductivity is also affected by relatively high thickness with big size of aggregate.

**Conflict of Interests**

The authors declare that there is no conflict of interests regarding the publication of this paper.

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