Research Article

Degradation Behavior of Concrete after Freeze-Thaw Cycles and Then Exposure to High Temperatures

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Concrete behavior usually degrades due to freeze-thaw cycles, fire, or both. Existing studies on the degradation behavior of concrete due to exposure to high temperatures were primarily focused on unfrozen concrete. In this paper, the degradation behavior of damaged concrete, after different freeze-thaw cycles (25, 35, 45, and 55 cycles), exposure temperatures (20°C, 300°C, 400°C, and 500°C), and cooling methods (water-cooled and air-cooled), was tested with seventy-five prism specimens. The degradation behavior of the damaged concrete, such as surface characteristics, weight loss, compressive strength, peak strains, and elastic modulus, was studied and analyzed. Results show that (i) the surface color of the concrete does not change significantly throughout the test. As the number of freeze-thaw cycles and temperatures increase, the weight loss of the concrete specimens increases gradually. (ii) After freeze-thaw cycles, the relative strengths and elastic modulus of the concrete specimens significantly degrade compared with those of the unfrozen ones at same temperatures. (c) At elevated number of freeze-thaw cycles and exposure temperatures, the peak strain of the concrete increases gradually. (d) Cooling methods have different effects on the degradation of concrete under different number of freeze-thaw cycles. Finally, a uniaxial compression constitutive model for concrete after freeze-thaw cycles and then exposure to high temperatures was established and a good agreement was observed with test results.

1. Introduction

Concrete structures are sometimes subjected to fire and also freeze-thaw cycles, which will degrade the behavior of the concrete and then the structures. It is necessary to clearly understand the behavior of degradation of the concrete caused by freeze-thaw cycles, fire, or both.

Many researchers have investigated the performance of the concrete after exposure to high temperatures, including the change in the microstructure [1–3], the degradation of mechanical performance of ordinary concrete [4–7] and high-strength concrete [8, 9], and the effect of different cooling methods [10, 11]. It is noted that the mechanical behavior of concrete (both ordinary concrete and high-performance concrete) after exposure to high temperatures degraded to different degrees and is affected by cooling methods.

For the concrete structures in cold areas, the change of concrete performance after freeze-thaw cycles is critical. In order to predict the performance of concrete under freeze-thaw cycles, a model was proposed based on the damage accumulation theory [12]. For the microstructure observation of concrete and damage assessment after freeze-thaw cycles, X-ray and CT are widely used [13, 14]. Generally, researchers pay more attention to the degradation of mechanical properties after freeze-thaw cycles, for both ordinary concrete [15, 16] and air-entrained concrete [17, 18].

The above studies are mainly concerned with the degradation of concrete after freeze-thaw cycles or exposure to high temperatures only, and few research studies concerned...
with the degradation under two or more effects. Xie et al. [19] studied the high-temperature resistance of concrete after carbonization and proposed a constitutive equation for predicting the compressive properties of carbonized concrete after exposure to high temperatures. Mao et al. [20] focused on the durability of fly ash concrete under alternative interactions of freeze-thaw and carbonization and used microscopic techniques to reveal the damage mechanisms of the concrete. Cheng et al. [21] studied the effect of crack, freeze-thaw, and carbonization on reinforced concrete specimens in practical engineering through a series of tests. Wu and Wu [22] studied the behavior of the concrete subjected to high temperatures and then freeze-thaw cycles and concluded that the durability of freeze-thaw for the concrete was evidently reduced after exposure to high temperatures. However, the degradation of the concrete subjected to freeze-thaw cycles and then high temperatures (i.e., a reverse experimental processing [22]) was seldom reported. In cold regions, concrete structures with freeze-thaw damage may also suffer high-temperature (fire) damage. Thus, the research on the degradation of the concrete after freeze-thaw cycles and then exposure to high temperatures is very significant to evaluate the durability of concrete structures.

In this study, a series of experimental studies on the concrete specimens after freeze-thaw cycles and then exposure to high temperatures were conducted. The objectives are to obtain the degradation laws of mechanical properties and establish the constitutive model for uniaxial compression concrete after freeze-thaw cycles and then high-temperature exposures.

2. Experimental Program

2.1. Materials. Materials used in the tests are a same batch commercial concrete of C35, which is widely used in practical construction. The detailed mixture proportions of the concrete are shown in Table 1.

2.2. Designing and Grouping of Specimens. Seventy-five concrete prism specimens (i.e., twenty-five types each with three specimens) were prepared with a size of 100 mm × 100 mm × 300 mm. Through three additional specimens, the average measured compressive strength of the 28-day cube without freeze-thaw and high temperatures was 32.2 MPa, and the standard deviation was 0.7. All the specimens were poured and cured in accordance with the Chinese Standard for Test Method of Mechanical Properties on Ordinary Concrete (GB/T 50081-2002) [23] and divided into five groups and named as shown in Table 2.

2.3. Freeze-Thaw Cycle Test of Concrete Specimens

2.3.1. Test Apparatus of Freeze-Thaw Cycle Test. The KDR-V9 concrete rapid freeze-thaw test machine (shown in Figure 1) was used in the freeze-thaw cycle test, consisting of 28 chambers.

2.3.2. Freeze-Thaw Cycle Test Methods and Process. The freeze-thaw cycle tests were performed by the rapid freeze-thaw method in accordance with the Chinese Standard for Test Methods of Long-Term Performance and Durability of Ordinary Concrete (GB/T 50082-2009) [24]. Detailed test procedures are as follows: the concrete specimens were cured for 24 days under standard conditions (temperature 20°C ± 2°C and humidity ≥95%). Then, the concrete specimens were soaked in water of 20 ± 2°C for 4 days for saturation. The water surface should be 20–30 cm higher than the tops of the specimens. After that, the specimens were taken out of the water and then placed in a freeze-thaw device for testing. The temperature of the freeze-thawed specimen was reduced from +3°C to −16°C and then raised +3°C every 2 h for each cycle.

2.3.3. Observations of Specimens after Freeze-Thaw Cycles. After the freeze-thaw cycle tests, the surface layers of the concrete specimens had different degrees of damage, as shown in Figure 2. From the figure, the following can be observed:

(a) At relatively small number of freeze-thaw cycles (N = 25 or 35), the cracks on the concrete surface were not obvious, and few superficial layers of concrete spalled off.

(b) At relatively large number of freeze-thaw cycles (N = 45 or 55), the surfaces of specimens spalled off severely, exposing coarse aggregates. The edges of the specimens became incomplete, especially at N = 55.

2.4. Thermal Treatment of Concrete Specimens

2.4.1. Test Apparatus of Thermal Treatment. A high-temperature furnace with a working size of 1500 mm × 500 mm × 500 mm was used for thermal treatment (as shown in Figure 3), whose temperature ranged from room temperature to +1000°C with 4°C/min heating rate and precision ±1°C.

2.4.2. Thermal Treatment Test Methods and Process. A day after the freeze-thaw cycle test, thermal treatment test began. Firstly, the freeze-thawed concrete specimens were heated to 80°C and held for 24 hours to evaporate free water and capillary water [6]. Then, the temperature was elevated to the exposure temperature designed in Table 2 at a rate of 4°C/min and kept constant for 3 h. Finally, the specimens were taken out of the furnace and then cooled by spray water or air-cooling.

2.4.3. Observations of Specimens after High Temperatures. The surface deterioration of concrete specimens after freeze-thaw cycles and exposure to high temperatures is shown in Figure 4. From the figure, the following can be clearly observed:

(a) With the increase of the number of freeze-thaw cycles, more and more cracks can be clearly seen on
the surfaces of the specimens under different temperatures.

(b) When the temperature is 400°C, cracks can be clearly seen on the concrete surfaces, and the phenomenon was more obvious at relatively high freeze-thaw cycle levels. The surface layers of the mortar became loose and spalled off with the rising temperatures, especially when the temperature reached 500°C.

(c) The surface colors of the specimens after different freeze-thaw cycles and exposure to high temperatures were almost the same irrespective of the cooling methods used. At 400°C, the surface cracks of

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**Table 1: Mixture proportions of concrete specimens.**

<table>
<thead>
<tr>
<th>Cement (kg/m³)</th>
<th>Water (kg/m³)</th>
<th>Coarse aggregate (kg/m³)</th>
<th>Fine aggregate (kg/m³)</th>
<th>Fly ash (kg/m³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>320</td>
<td>180</td>
<td>870</td>
<td>870</td>
<td>90</td>
</tr>
</tbody>
</table>

**Table 2: Details of the test specimens.**

<table>
<thead>
<tr>
<th>Group</th>
<th>Notation</th>
<th>Freeze-thaw cycles</th>
<th>Number of specimens</th>
<th>Exposure temperature (°C)</th>
<th>Exposure time (h)</th>
<th>Cooling method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group 1</td>
<td>F0-T20W</td>
<td>0</td>
<td>3</td>
<td>20</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F0-T300W</td>
<td>0</td>
<td>3</td>
<td>300</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F0-T400W</td>
<td>0</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F0-T400A</td>
<td>0</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Air</td>
</tr>
<tr>
<td></td>
<td>F0-T500W</td>
<td>0</td>
<td>3</td>
<td>500</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td>Group 2</td>
<td>F25-T20W</td>
<td>25</td>
<td>3</td>
<td>20</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F25-T300W</td>
<td>25</td>
<td>3</td>
<td>300</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F25-T400W</td>
<td>25</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F25-T400A</td>
<td>25</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Air</td>
</tr>
<tr>
<td></td>
<td>F25-T500W</td>
<td>25</td>
<td>3</td>
<td>500</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td>Group 3</td>
<td>F35-T20W</td>
<td>35</td>
<td>3</td>
<td>20</td>
<td>3</td>
<td>Water</td>
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<tr>
<td></td>
<td>F35-T300W</td>
<td>35</td>
<td>3</td>
<td>300</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F35-T400W</td>
<td>35</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F35-T400A</td>
<td>35</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Air</td>
</tr>
<tr>
<td></td>
<td>F35-T500W</td>
<td>35</td>
<td>3</td>
<td>500</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td>Group 4</td>
<td>F45-T20W</td>
<td>45</td>
<td>3</td>
<td>20</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F45-T300W</td>
<td>45</td>
<td>3</td>
<td>300</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F45-T400W</td>
<td>45</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F45-T400A</td>
<td>45</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Air</td>
</tr>
<tr>
<td></td>
<td>F45-T500W</td>
<td>45</td>
<td>3</td>
<td>500</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td>Group 5</td>
<td>F55-T20W</td>
<td>55</td>
<td>3</td>
<td>20</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F55-T300W</td>
<td>55</td>
<td>3</td>
<td>300</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F55-T400W</td>
<td>55</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Water</td>
</tr>
<tr>
<td></td>
<td>F55-T400A</td>
<td>55</td>
<td>3</td>
<td>400</td>
<td>3</td>
<td>Air</td>
</tr>
<tr>
<td></td>
<td>F55-T500W</td>
<td>55</td>
<td>3</td>
<td>500</td>
<td>3</td>
<td>Water</td>
</tr>
</tbody>
</table>

Note. “F#” denotes the freeze-thaw cycles (F0 = 0 cycles, F25 = 25 cycles, F35 = 35 cycles, F45 = 45 cycles, and F55 = 55 cycles); “T#” denotes the target temperature of high-temperature heating; “W” or “A” represents water- or air-cooling (natural cooling), respectively. For example, “F25-T400W” indicates that the specimen subjected to 400°C after 25 freeze-thaw cycles and then cooled by the water spray method.

**Figure 1: Freeze-thaw test apparatus.**
the water-cooled concrete specimens were more obvious than those of the concrete specimens cooled by air, indicating that the damage caused by the water-cooling method to the concrete specimen is greater.

2.5. Loading Tests

2.5.1. Loading Test Process and Apparatus. All the specimens were tested for uniaxial loading under a universal testing machine with a maximum capacity of 1000 kN. Four displacement transducers were, respectively, fixed at a distance of 50 mm from the upper and lower ends of the specimens (see Figure 5) to measure the deformation within 200 mm from the middle of the specimens, and the deformation of the middle part represents the deformation of the whole specimens. The loading rates of preloading and loading process were, respectively, controlled at 0.05 mm/min and 0.2 mm/min. The loading rate near the peak point and the falling portion after the peak point were 0.05 mm/min, and then this rate was kept until the test specimen failure. The tests were performed in accordance with the Chinese Standard for Test Method of Mechanical Properties on Ordinary Concrete (GB/T 50081-2002) [23].

2.5.2. Observations during Loading Tests. The failure of the concrete specimens virtually reflected the process of the evolution of the microcracks inside the specimens. Due to the different degrees of damage, the time of occurrence of cracks in each specimen and its development during the loading process are different (see Figure 6), from which the following phenomena can be found:

(a) For the specimens with low exposure temperatures, few cracks appeared when the load was low, but the cracks developed quickly when the load was close to the failure load. By continuing compressive load, the concrete surface formed at least one obliquely penetrating crack due to compressive damage and then concrete specimens broke quickly.

(b) For the specimens subjected to high temperatures, cracks appeared at low load and also developed quickly when the load was close to the failure load. There were no obvious oblique cracks on the surface of the concrete, but the layer of the concrete spalled off severely.

(c) For the specimens with the same exposure temperatures, the more the freeze-thaw cycles were, the more the damage there would be.
3. Test Results and Discussion

3.1. Weight Loss of Concrete after Freeze-Thaw Cycles and Exposure to High Temperatures. In this investigation, the concrete specimens were first treated by freeze-thaw cycles and then subjected to high temperatures. \( m_{af}/m_{bf} \) and \( m_{at}/m_{bt} \) are used to represent the weight loss caused by freeze-thaw cycle treatment and high-temperature treatment, respectively. \( m_{af} \) is the saturated mass of the concrete specimen after freeze-thaw cycles, and \( m_{bf} \) is the saturated mass of the concrete specimen before freeze-thaw cycles. \( m_{at} \) is the dry mass of the concrete specimen after high-temperature treatment, and \( m_{bt} \) is the dry mass of the concrete specimen after freeze-thaw cycle treatment before high-temperature treatment.

The variation in concrete weight ratio (i.e., \( m_{af}/m_{bf} \) and \( m_{at}/m_{bt} \)) with elevated number of freeze-thaw cycles and high temperatures are, respectively, shown in Figures 7 and 8, and the following can be found:

(a) From Figure 7, as the number of freeze-thaw cycles increased, the weight ratio decreased slightly, only 0.8%, meaning that the number of freeze-thaw cycles within the range of 0–55 has a little effect on the weight loss of concrete.

(b) From Figure 8, in the case of same number of freeze-thaw cycles, the weight ratio reduced with elevated temperatures, and the degree of decline was higher than that caused by the freeze-thaw cycle of the previous stage. This is mainly due to the continuous evaporation of moisture inside the specimens with increasing temperatures.

3.1.1. Degradation of Compressive Strength. The degradation of relative compressive strength \( f_{c}(N, T)/f_{c}(0, 20) \) of water-cooled concrete is shown in Figure 9. In which, \( f_{c}(N, T) \)
represents the compressive strength of the concrete after freeze-thaw cycles and then high-temperature treatment, and $f_c(0, 20)$ represents the compressive strength of the unfrozen concrete at 20°C. Figure 10 gives the effect of cooling methods on the relative compressive strength of specimens. From the figures, the following can be observed:

(a) With the number of freeze-thaw cycles and elevated temperatures, the relative compressive strength of concrete declines gradually. When the temperature is elevated from 20°C to 500°C, the relative strengths of the freeze-thawed concrete specimens significantly degrade compared with those of the unfrozen ones at the same temperatures.

(b) The sequence of freeze-thaw cycle treatment and high-temperature treatment has effects on the degradation of compressive strength. The relative compressive strength of the concrete with 25 freeze-thaw cycles and then exposure to high temperature of 300, 400, and 500°C in this paper is lower than that.
cycles. When \( N < 35 \), the difference between different cooling modes is not obvious; but overall, the strength of the concrete after air-cooling is slightly greater than that of the water-cooled concrete. When \( N \geq 35 \), the relative compressive strength of the concrete specimen cooled by air is significantly greater than that of the concrete specimen cooled by spray water. As the number of freeze-thaw cycle increases, the trend becomes greater. This is mainly due to the influence of different cooling methods on the compressive properties of concrete. For water-cooled concrete, the concrete specimen after exposure to high temperatures was suddenly cooled by water and the differences between the internal and external temperatures of the specimens increase rapidly, resulting in the rapid development of cracks.

Based on the test results, an empirical equation for water-cooled concrete specimens is as follows:

\[
\frac{f_c(N,T)}{f_c(0,20)} = 1.016 - 1.084 \times 10^{-6}T - 7.370 \times 10^{-3}N - 1.940 \times 10^{-6}NT - 1.777 \times 10^{-6}T^2 + 1.796 \times 10^{-8}T^2N. \tag{1}
\]

For the air-cooled concrete specimens, an influence coefficient \( \beta(N) \) was introduced for the difference between air-cooling and water-cooling, and \( \beta(N) = 1.0094 + 0.0001 \cdot N^2 - 0.0034 \cdot N \) was obtained by fitting the test results. Equation (1) can be modified for air-cooled concrete specimens as follows:

\[
\frac{f_c(N,T)}{f_c(0,20)} = (1.016 - 1.084 \times 10^{-6}T - 7.370 \times 10^{-3}N - 1.940 \times 10^{-6}NT - 1.777 \times 10^{-6}T^2 + 1.796 \times 10^{-8}T^2N) \cdot \beta(N), \tag{2}
\]

where the letter \( T \) represents the exposure temperature and the letter \( N \) represents the number of freeze-thaw cycles.

Figure 11 shows a good agreement between equation (1) and tests, and the coefficient of correlation for equation (1) is 0.984.

3.1.2. Degradation of Elastic Modulus of Concrete. The elastic modulus was defined as the secant modulus of the point with \( \sigma = 0.4f_c \) in the stress-strain curve. The degradation of relative elastic modulus \( E_c(N, T)/E_c(0, 20) \) of the water-cooled concrete is shown in Figure 12. In which, \( E_c(N, T) \) represents the elastic modulus of the concrete specimen after \( N \) cycles of freeze-thaw and then \( T \) °C treatment, and \( E_c(0, 20) \) represents the elastic modulus of the unfrozen concrete at 20°C. From Figure 12, the following can be observed:

(a) The relative modulus of elasticity gradually reduces with the elevated number of freeze-thaw cycles and

of the concrete with exposure to high temperature of 300, 400, and 500°C and then with 25 freeze-thaw cycles studied by Wu and Wu [22]. This is mainly because for the concrete subjected to high-temperature treatment first, part of water reacts with \( \text{Ca(OH)}_2 \) formed after exposure to high temperatures in subsequent freeze-thaw tests, resulting in the consequence that the deterioration of the strength partially restored.

(c) At 400°C, the relative compressive strength of the concrete specimen under two different cooling methods decreases with the increasing freeze-thaw cycles.
temperatures. The relative elastic modulus of freeze-thawed concrete specimens (25 and 45 cycles) is evidently lower than that of the unfrozen ones at the same temperature.

(b) As the temperature increases, the difference in relative elastic modulus of concrete specimens with different freeze-thaw cycles decreases. The greater the number of freeze-thaw cycles is, the smaller the relative elastic modulus there would be.

Using polynomial nonlinear fitting method, the calculation model of relative elastic modulus of the water-cooled concrete after freeze-thaw cycles and then exposure to high temperatures was established as follows:

\[
\frac{E_r(N,T)}{E_r(0,20)} = 0.9796 + 3.357 \times 10^{-4}T + 3.349 \times 10^{-3}N
\]
\[+ 3.983 \times 10^{-5}N \cdot T + 8.700 \times 10^{-6}T^2 \]
\[− 2.120 \times 10^{-8}N \cdot T^2, \tag{3}\]

where the letter \(T\) represents the exposure temperature and the letter \(N\) represents the number of freeze-thaw cycles.

Figure 12 shows a good agreement between equation (3) and tests, and the coefficient of correlation for equation (3) is 0.987.

3.1.3. Degradation of Peak Strain. The maximum strain before failure in the uniaxial compression test is the peak strain. Figure 13 shows the variation in relative peak strain \(\varepsilon_P(N, T)\) of the water-cooled concrete specimen. In which, \(\varepsilon_P(N, T)\) is the peak strain of the concrete specimen after \(N\) cycles of freeze-thaw and then \(T\) °C treatment, and \(\varepsilon_P(0, 20)\) is the unfrozen concrete peak strain at 20°C. The effect of cooling methods on the peak strain is shown in Figure 14. From the figures, the following can be observed:

(a) The relative peak strain rises with the elevated temperatures. However, within each temperature range, the peak strain of the unfrozen specimen and the specimen subjected to 25 freeze-thaw cycles shows no significant difference, indicating the internal damage of the concrete specimen after 25 freeze-thaw cycles is very small. The peak strain of the concrete specimen after 45 cycles of freeze-thaw at 500°C is evidently larger than that of the unfrozen one at 20°C. This is because the expansion of internal cracks and pores caused by freeze-thaw and high-temperature test leads to the increase of compaction zone and decline of axial stiffness of the concrete.

(b) The peak strain of the air-cooled concrete is significantly greater than that cooled by the spray water method under the same number of freeze-thaw cycles at 400°C. It indicates that the ductility of the air-cooled concrete specimen is greater than that cooled by water. The difference between the peak strains of the concrete specimens under different cooling modes does not change significantly with the increase of the number of freeze-thaw cycles.

Based on the test results, the calculated model of the relative peak strain for the water-cooled concrete after freeze-thaw cycles and then exposure to high temperatures was established. Details are as follows:

\[
\frac{\varepsilon_P(N, T)}{\varepsilon_P(0, 20)} = 0.9998 − 8.349 \times 10^{-4}T + 6.263 \times 10^{-3}N
\]
\[+ 3.386 \times 10^{-5}N \cdot T + 1.354 \times 10^{-5}T^2 \]
\[− 1.979 \times 10^{-9}N \cdot T^2, \tag{4}\]

Figure 13 shows the variation in relative peak strain \(\varepsilon_P = 0, 20\) of the water-cooled concrete specimen. In equation (3), the letter \(T\) represents the number of freeze-thaw cycles. Details are as follows:
where the letter $T$ represents the exposure temperature and the letter $N$ represents the number of freeze-thaw cycles. A good agreement between equation (4) and tests is shown in Figure 13, and the coefficient of correlation for equation (4) is 0.972.

4. Constitutive Model of Concrete after Freeze-Thaw Cycles and Then High Temperatures

Researches on constitutive model of freeze-thawed concrete after exposure to high temperatures are necessary to accurately evaluate the damage of freeze-thawed concrete structures in fire. According to the basic relationship of continuous damage mechanics [25], the damage constitutive model at room temperature was proposed as $\sigma = (1 - D)E\varepsilon \cdot \exp\left(-\frac{\varepsilon^m}{\alpha}\right)$, in which $D = 1 - \exp(-e^m/\alpha)$ [26]. In this paper, the investigation of the degradation of concrete was based on the uniaxial compression test but did not include complex stress state, so the damage variable $D$ is a scalar used for uniaxial compression.

For the concrete after exposure to high temperatures, the model was modified by adding the temperature coefficient, as shown [19, 27–30] in the following:

$$\sigma = K_T(T) \cdot \eta(T) \cdot E\varepsilon \cdot \exp\left(-\frac{\varepsilon^m}{\alpha}\right),$$

where $K_T(T)$ is the temperature softening coefficient, $\eta(T)$ represents the strain correction coefficient, $\alpha$ represents the scale coefficient, and $m$ represents the shape influence coefficient.

In this paper, the following model was proposed based on equation (5) considering the effects of freeze-thaw cycles:

$$\sigma = K_F(N) \cdot K_T(T) \cdot \eta(T) \cdot E\varepsilon \cdot \exp\left(-\frac{\varepsilon^m}{\alpha(N,T)}\right),$$

Figure 13: Strain of the water-cooled concrete after freeze-thaw cycles at different heating temperatures. (a) Stress-strain curves of the unfrozen concrete at different temperatures. (b) Stress-strain curves of the freeze-thawed concrete with 25 cycles at different temperatures. (c) Stress-strain curves of the freeze-thawed concrete with 45 cycles at different temperatures. (d) Relative peak strain after freeze-thaw cycles at different temperatures.
where $K_F(N)$ is the freeze-thaw cycle softening parameter. $K_F(N)$ and $K_T(T)$ are, respectively, expressed as

$$K_F(N) = \frac{E_c(N)}{E_c} = 1.0 - 2.45 \times 10^{-3} N - 1.67 \times 10^{-4} N^2,$$

$$K_T(T) = \frac{E_c(T)}{E_c} = 1.047 - 2.410^{-3} T + 1.533 \times 10^{-6} T^2. \quad (7)$$

Based on the test results and using the least-squares method, the parameters in constitutive model equation (6) are determined and are shown in Table 3 and equations (8) and (9):

$$\eta(T) = 1 + 1.56 \times 10^{-5} T - 1.937 \times 10^{-6} T^2, \quad (8)$$

$$\alpha(N, T) = 4.013 \times 10^{-5} - 2.900 \times 10^{-7} \cdot T + 7.281 \times 10^{-7} \cdot N - 1.128 \times 10^{-8} \cdot T \cdot N + 1.674 \times 10^{-9} \cdot T^2 + 4.452 \times 10^{-11} \cdot T^2 \cdot N. \quad (9)$$

Comparison between the calculated data (in this paper, $E_c = 30134$ MPa) obtained from the established uniaxial compression constitutive model (i.e., Equation (6)) and test
5. Conclusions

Based on the test results, the conclusions can be summarized as follows:

(a) The surface color of the concrete does not change significantly throughout the test. In the freeze-thawed concrete after exposure temperature of 400°C, the cracks can be clearly seen on the concrete surfaces and were more significant for concrete with more freeze-thaw cycles.

(b) As the number of freeze-thaw cycles and temperatures increase, the weight loss of the concrete increases. However, within a range of 0–55 freeze-thaw cycles and 20–500°C, the weight loss is relatively small, only 8%.

(c) The relative compressive strength and modulus of elasticity of concrete decreased with the freeze-thaw cycles or temperature increase. After freeze-thaw cycles, the relative strength and elastic modulus of the concrete specimens significantly degrade compared with those of the unfrozen ones at same temperatures. For the concrete with the same freeze-thaw cycles and temperatures, the damaged degree is relative to the sequence of the freeze-thaw cycles and high-temperature treatment.

(d) As the number of freeze-thaw cycles and temperatures increase, the peak strain of the concrete increases. And there is no significant difference between the relative peak strain of the freeze-thawed concrete with 25 cycles and the unfrozen concrete.

(e) Cooling methods have different effects on the degradation of concrete under different number of freeze-thaw cycles. When \( N \leq 35 \), there is no significant difference in the effect of different cooling methods on compressive strength, but when \( N > 35 \), water-cooling is more disadvantageous on the compressive strength of concrete.

(f) A constitutive model for uniaxial compression concrete after freeze-thaw cycles and then exposure to high temperatures was established and a good agreement can be seen with the test results.

Data Availability

All data analyzed during this study are included in this article.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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