Research Article

Silicon Quantum Dots in a Dielectric Matrix for All-Silicon Tandem Solar Cells

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We report work progress on the growth of Si quantum dots in different matrices for future photovoltaic applications. The work reported here seeks to engineer a wide-bandgap silicon-based thin-film material by using quantum confinement in silicon quantum dots and to utilize this in complete thin-film silicon-based tandem cell, without the constraints of lattice matching, but which nonetheless gives an enhanced efficiency through the increased spectral collection efficiency. Coherent-sized quantum dots, dispersed in a matrix of silicon carbide, nitride, or oxide, were fabricated by precipitation of Si-rich material deposited by reactive sputtering or PECVD. Bandgap opening of Si QDs in nitride is more blue-shifted than that of Si QD in oxide, while clear evidence of quantum confinement in Si quantum dots in carbide was hard to obtain, probably due to many surface and defect states. The PL decay shows that the lifetimes vary from 10 to 70 microseconds for diameter of 3.4 nm dot with increasing detection wavelength.

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1. INTRODUCTION

Wafer-based first-generation photovoltaic technologies are presently booming, a situation likely to continue for the next decade. However, second-generation thin-film approaches also appear attractive because of their potential reduction in material costs. Third-generation approaches aim to reduce the manufacturing cost of thin-film second-generation technologies by increasing the efficiency through using multiple energy thresholds, whilst still using abundant and non-toxic materials. The effects of increasing efficiency and lowering the cost of thin-film processes can significantly leverage costs per peak watt (Wp) of generating capacity, perhaps to less than US \$ 0.20/Wp [1].

Figure 1 shows main loss mechanisms in a standard p-n junction solar cell. The most important loss mechanisms in single p-n junction solar cells are the nonabsorption of below-bandgap photons (① in Figure 1) and thermalization of electron-hole pairs generated by absorption of short-wavelength photons, through electron (hole) relaxation to the conduction (valence) band edge (② in Figure 1). Other losses are junction loss (③ in Figure 1) and contact loss (④ in Figure 1), which can be arbitrarily small in an ideal device. Recombination loss (⑤ in Figure 1) can be reduced to purely radiative recombination again in an ideal device.

There have been proposed three families of approaches for tackling these first two major loss mechanisms [2]: (a) increasing the number of energy levels; (b) capturing hot carriers before thermalisation; and (c) multiple electron-hole pair generation per high energy photon or generation of one higher energy-carrier pair with more than one low energy photon. An implementation of strategy (a), the tandem cells, is the only technology thus far to have been realized with efficiencies exceeding the Shockley-Queisser limit.

The concept of the tandem solar cell is the use of several solar cells of different bandgaps stacked on top of each other, each absorbing photons of different energies, such that the uppermost cell has the highest bandgap and lets the photon less than its bandgap pass through to lower bandgap cells underneath. Most commonly, these cells are contacted in series. The highest efficiency examples are monolithically grown single-crystal lattice-matched devices based on a GaInP/GaAs/Ge triple-junction structure [3]. Another example in less exotically grown materials is micromorph a-Si/ μ c-Si tandem cells [4]. Use of silicon also conveys the very significant advantage of use of an abundant nontoxic material.

A further example which shares these advantages is the use of a silicon quantum dot nanostructure in a matrix of

FIGURE 1: Loss mechanism in a standard p-n junction solar cell: (1) nonabsorption of below-bandgap photons, (2) lattice thermalisation loss, (3) junction loss, (4) contact voltage loss, and (5) recombination loss.

silicon oxide, nitride, or carbide to engineer the bandgap of a solar cell material for an “all-Si” tandem cell, whilst also giving a wide range of design flexibility [5, 6]. In the current paper, we report material properties of silicon nanostructures for all-silicon tandem solar cells and recent progress on silicon nanostructures for all-silicon tandem cell fabrication.

2. ALL-SILICON QUANTUM DOT TANDEM SOLAR CELL

Silicon is unique in that it has an almost ideal bandgap not only for a standard single p-n junction cell (just a little on the low side of optimal) but also for the lower cell in a two-cell or even a three-cell tandem stack (a little on the high side). The efficiency limit for a single silicon cell is 29%, when only radiative and Auger recombination is considered, but this increases to 42.5% and 47.5% for two-cell and three-cell stacks, respectively [1]. The optimal bandgap of the top cell to maximize conversion efficiency is $1.7 \sim 1.8$ eV for a two-cell tandem with an Si bottom cell [7]. The optimal upper and middle bandgaps for a three-cell tandem are 1.5 eV and 2.0 eV, respectively. Figure 2 shows the schematic diagram of a silicon-based or “all-silicon” tandem solar cell. The top cell is connected to the bottom cell by an interband tunnel junction, most likely using a defect dominated high interband recombination junction. The material in the interconnection region could also be comprised of quantum dot material, but most likely employing smaller dots than the absorbing regions.

The quantum confinement, achieved by restricting at least one dimension of silicon less to the Bohr radius of the bulk crystalline silicon (around 5 nm), causes its effective bandgap to increase. Our early experiments involved carefully thinning the thin silicon layer (50 nm thick) in commercially available silicon-on-insulator (SOI) wafers, resulting in an $\text{SiO}_2/\text{Si}/\text{SiO}_2$ quantum well [8]. For possibly the first time, clear evidence for a quantum-confined bandgap in an $\text{SiO}_2/\text{Si}/\text{SiO}_2$ quantum well increase was demonstrated by photoluminescence measurements on such devices, with a lowest energy level (the effective bandgap) of up to 1.7 eV measured for layers about 1 nm thick. The blue shift of the PL and its rapidly increasing intensity with decreasing Si thickness are indicative of quantum confinement effects. Enhanced PL intensity is directly related to the absorption

from the principle of detailed balance [9], which provides an added bonus for solar applications.

The strongest quantum confinement effect is obtained if the silicon is constrained in all three dimensions, as in quantum dots, such that the same increase in effective bandgap can be achieved with a much less stringent size constraint. If these dots are spaced close enough and there is a significant overlap of the wavefunction, carriers can tunnel between them to produce a true quantum dot superlattice. Such a superlattice can then be used as the higher bandgap material in a tandem cell.

Each of the n-type and p-type regions will typically include 20–50 bilayers formed by alternating the growth of a quantum dot (QD) and a dielectric barrier layer. The n-type and p-type regions are typically each in the range of 75–200 nm thick.

The material requirements for the dielectric layers are ease of thin-film growth and use of abundant nontoxic materials, hence it is most likely to be an oxide, nitride, or carbide of silicon. It is also necessary that carriers from the quantum dot layers have a high probability of tunneling through the dielectric layers. This is achieved by creating each dielectric layer with a thickness in the range of 1.5 to 2.5 nm for the case of oxide.

The semiconductor material of the quantum dots is preferably silicon or another group IV element such as tin or germanium, or a group IV alloy such as silicon germanium. For a nanostructure to have a high conductivity requires formation of a true superlattice with overlap of the wave function for adjacent quantum dots; which in turn requires either close spacing between QDs or a low barrier height. The wavefunction of an electron confined to a spherical dot penetrates into the surrounding material, decaying approximately as $\exp(-r/L_d)/r$, where r is the distance from the centre of the dot. The decay length L_d is determined by the barrier height of the material in which the dot is embedded, which in the present case is either a silicon carbide, nitride, or oxide matrix [10]. In the simplest case, the decay length (L_d) is given by (1):

$$L_d = \frac{1}{\sqrt{2m^*(V_0 - E_n)}} = \frac{0.1952 \text{ nm}}{\sqrt{m^* \cdot \Delta E/m_0}}. \quad (1)$$

The latter expression holds when ΔE , the difference between the conduction band edge of the matrix and the confined energy level, is in eV. m^* and m_0 are the effective mass and electron mass in the matrix material, respectively. V_0 is the corresponding band offset and E_n is the confined energy level in a quantum dot. Without considering the confined energy of QDs, energy difference ΔE [5] are 3.2 eV, 1.9 eV, and 0.5 eV for the conduction edge of bulk Si and SiO_2 , Si_3N_4 , and SiC, respectively. Electrons effective masses of SiO_2 , Si_3N_4 , and 3C-SiC are 0.86 [11], 0.05–0.13 [12], and 0.24 ± 0.1 [13], respectively. Following this line of argument, the results suggest that dots in an SiO_2 matrix would have to be separated by no more than 1–2 nm of matrix for a reasonable overlap of the wavefunction and hence of conductivity, while they could be separated by more than 4 nm of SiC. The same type of calculation allows the effect of fluctuations in spacing and size

FIGURE 2: Schematic of (a) three-cell and (b) two-cell tandem solar cell with an Si bottom cell.

of the dots to be investigated. It is found that the calculated Bloch mobilities do not depend strongly on variations in the dot size but do depend strongly on dot spacing uniformity within the QD material [14].

Another requirement for a tandem cell element is the presence of some form of junction for carrier separation. This can either be a grown or a diffused p-n junction or a p-i-n junction with the superlattice as i-region. The latter requires careful control of the work functions (and therefore doping) of the p- and n-regions, but also means that it is not essential for the superlattice itself to be doped.

3. SILICON QUANTUM DOT SUPERLATTICE

3.1. Fabrication of silicon quantum dots

3.1.1. Phase precipitation from Si-rich layer

The effect of quantum confinement obtained by limiting at least one spatial dimension of material has been understood since at least the 1960s and superlattices have been known since 1970. Superlattices were manufacturable with the epitaxial growth techniques available to III-V compound semiconductor technology at that time [15]. Amorphous silicon superlattices of a-Si : H and a-Si_{1-x}N_x : H were first reported [16]. Lu et al. reported quantum confinement and light emission of superlattices of silicon and SiO₂ fabricated by molecular beam epitaxy (MBE) [17].

Several techniques have been reported for fabricating silicon quantum dots from one of two directions—“bottom up” and “top down.” The “bottom up” approach builds up QDs from individual atoms or molecules. This is the basis of most “cluster science” as well as crystal materials synthesis, usually via chemical or vacuum deposition techniques. The methods include gas evaporation [18], high temperature aerosol reaction [19], phase separation of silicon-rich oxide (SRO) by a sputtering [20] and reactive evaporation [21], chemical vapor deposition (CVD) [22], Si implantation into the SiO₂ substrate [23], laser ablation [24], and solution synthesis [25].

The “top down” approach generates silicon nanostructures by breaking up bulk materials. This is the basis for

techniques such as mechanical milling [26], particle selection formed by electrochemical etching of the silicon substrate (i.e., porous silicon) [27], and precision oxidation of SOI substrates [8]. Approaches explored for producing two-dimensional superlattices in a low cost have not previously proved to be particularly encouraging [8, 28]. We have demonstrated a bandgap, as measured by PL, of up to 1.7 eV, using both an Si/SiO₂ quantum well [8] and an Si/SiO₂ superlattice [28] for layers about 1 nm thick. The reproducibility of such a thin silicon layer is questionable. The quantum dot superlattice is a promising material because of the additional degree of confinement which gives greater design flexibility than the two-dimensional quantum well structures. The first confined energy level in a 1 nm wide quantum well will be approximately the same as in a 2 nm diameter quantum dot [5].

Si ion implantation into an oxide layer can be used to produce Si QDs at an irregular position with a relatively large size distribution. Solution synthesis, mechanical milling, and particle selection from porous silicon can be used to fabricate a volume of Si QDs, but it is difficult to control the size uniformity of distributed QDs or an additional process to select the particle with the same size.

Si QD fabrication by various vacuum deposition techniques is preferable because of the greater potential of integration into conventional devices. Gas phase in situ Si QD growth in an Si₃N₄ matrix film [29] and nanocrystalline precipitations from silicon-rich layers [21] are two examples of fabrication of Si QD systems by means of vacuum deposition techniques. In situ, Si QD growth is an interesting method because a high temperature annealing process is not required. For Si precipitation from an Si-rich layer, high temperature annealing of excess Si in an inert atmosphere is necessary to form Si nanocrystals with a few nm diameters, for example, Si QD precipitation in oxide [21, 28, 30], nitride [31], and carbide [32, 33] (Figure 3(a)). Equation (2) describes this Si precipitation mechanism:

FIGURE 3: Si QDs from phase separation of (a) a single silicon-rich precursor layer and (b) a multilayer structure.

FIGURE 4: Transmission electron microscopy (TEM) images of Si QDs in SiO_2 matrix with (a) low magnification and (b) HRTEM lattice image of Si quantum dots.

FIGURE 5: Si QDs dispersed in an Si_3N_4 matrix fabricated by gas phase in situ deposition: (a) low-magnification TEM and (b) high-resolution TEM.

More accurate size control and a narrow size distribution were achieved by growth of an Si QD multilayer structure, which is fabricated by alternating layers of stoichiometric insulating materials and silicon-rich layers [21, 28] shown in Figure 3(b). Depending on the annealing conditions, silicon precipitates from the silicon-rich layers as approximately spherical QDs of a diameter close to the original layer thickness. Hence controls of the diameter and of one spatial coordinate of the dots are possible. Si QDs in oxide [6, 28] and nitride [31] are actively studied materials, but Si QDs in carbide has only recently been attempted [32, 33]. TEM images in Figure 4 show Si QDs interspersed in the oxide matrix.

3.1.2. Si quantum dots in a nitride matrix

The bandgap of Si_3N_4 is significantly lower than that of SiO_2 . Hence Si QDs in the nitride offer a lower barrier height and much increased carrier tunneling probability between quantum dots. (SiC offers a lower barrier still.) For this reason, we have explored transferring the technology of Si QDs in SiO_2 to the growth of Si nanocrystals in silicon nitride by both sputtering and PECVD [31]. For sputtering, growth parameters are very similar to the oxide. In addition, two separate PECVD systems, remote plasma and parallel capacitor plasma, have been used for the growth of Si nanocrystals by depositing alternate Si-rich and stoichiometric nitride layers. Annealing is carried out again at 1100°C but with a preannealing at 500°C to drive off hydrogen incorporated from the PECVD process. Again, HRTEM images showing even clearer nanocrystals have been obtained. To the best of our knowledge, this is the first Si QDs in multilayered structure in nitride matrix [31].

We have now also extended the layered Si QDs in nitride technology to gas phase in situ deposition. Figure 5 shows in situ Si QD dispersed in a nitride matrix. A stoichiometric Si_3N_4 layer and an in situ Si QD layer are alternately deposited on an Si substrate. This technique allows QDs to form during deposition without a postdeposition annealing. We are actively studying this technique because it is a low temperature process and may be potentially beneficial to doping of Si QDs owing to high equilibrium temperature of the plasma and free of high temperature postannealing described in Figure 3.

3.1.3. Si QDs in silicon carbide

SiC nanocrystals of a few nm diameters in an SiO_2 matrix were produced by silicon and carbon implantation into thermal oxide [34]. However, to our knowledge, little has been reported on the experimental properties of Si QDs embedded in an SiC matrix [32, 33].

A Si-rich amorphous silicon carbide precursor layer can be achieved by control of the sputtering parameters of Si and carbon containing targets (e.g., pure carbon, silicon carbide, boron carbide, etc.). One way to fabricate Si-rich silicon carbide is cosputtering from silicon and carbon containing targets. Alternatively, small chips of carbon attached to a silicon target can produce an Si-rich silicon carbide precursor layer. A high temperature anneal ($800\text{--}1200^\circ\text{C}$ in an inert gas or

in vacuum) of a silicon-rich carbide precursor layer precipitates Si and/or SiC nanocrystals, depending on its chemical composition as shown in (2).

Raman, TEM, and XRD spectra for a silicon-rich $\text{Si}_{0.75}\text{C}_{0.25}$ precursor layer grown on a quartz substrate with subsequent annealing are shown in Figure 6. There is clear evidence for the formation of nanocrystalline Si at an anneal temperature greater than 1000°C . This is shown in the Raman peak at $\sim 508\text{ cm}^{-1}$ [35]. TEM lattice fringe spacing, consistent with $\{111\}$ Si planes and XRD, peaks at $2\theta = 28.4^\circ$ with peak broadening indicating nanocrystal of 3–7 nm (estimated using the Scherrer equation). (It should be noted that the nanocrystal size determined by TEM is, in our experience, always slightly smaller than that determined by XRD.)

Other Si and C concentrations were also investigated [33]. As the concentration of C in $\text{Si}_{1-x}\text{C}_x$ is increased to the nearly stoichiometric $\text{Si}_{0.495}\text{C}_{0.505}$, Raman evidence (not shown here), for the stretching vibration modes of Si–C and C–C bonds, can be easily identified. Intensities of both TO and LO bands of Raman spectra are increased with increasing annealing temperature, indicating the formation of crystalline SiC during annealing. In addition, there is a dramatic decrease in the intensity of Si–Si vibration modes, indicating the formation of far fewer Si nanocrystals.

HRTEM data (not shown here) shows crystallites with lattice fringes corresponding to $\beta\text{-SiC}$ $\{111\}$ planes, with a mean size in the range of 3–10 nm. However, in contrast to the spherical Si nanocrystals in the oxide and nitride matrices (see Figures 4 and 5), SiC nanocrystals are irregular with some nanocrystals joined together to form an extended crystal. The difference of nanocrystal shapes from silicon-rich SiC and near-stoichiometric SiC is due to the differing mechanisms for nanocrystal formation. For the Si-rich carbide precursor, nanocrystals precipitate to nucleating sites, due to an excess of Si in the matrix, with surface energy minimization favoring the formation of spheres. For the near-stoichiometric composition, SiC nanocrystals formation does not depend on precipitation and hence random shapes occur, dependent more on local concentration variations.

Hence the best data so far for Si nanocrystals in an SiC matrix are obtained for an $\text{Si}_{0.75}\text{C}_{0.25}$ precursor composition. Optical bandgap of $\text{Si}_{0.75}\text{C}_{0.25}$ thin film is in the ranges of ~ 1.4 (as-deposited) to $\sim 2.0\text{ eV}$ (annealed at 1100°C). In order to control the size of Si nanocrystals multilayer structures, based on this concentration, have been fabricated and further measurement is underway.

As before, a multilayer approach was used to fabricate Si QDs in carbide of uniform size. A multilayer with stoichiometric SiC and silicon-rich $\text{Si}_{1-x}\text{C}_x$ precursor layer was fabricated, as shown in Figure 7(a), and annealed at a high temperature to selectively precipitate Si nanocrystals in a carbide matrix. However, the lattice fringes in HRTEM image correspond to $\beta\text{-SiC}$ $\{111\}$ crystalline planes (Figure 7(b)). One possible reason for SiC QDs, instead of Si QDs, is that the C/Si ratio in layered structure has an increase, compared to the original design.

FIGURE 6: Silicon-rich SiC precursor layer: (a) Raman spectra with different annealing temperature, (b) cross-sectional HRTEM image, and (c) X-ray diffraction pattern.

3.2. Bandgap engineering of silicon nanostructure

In indirect bandgap semiconductors, the optical transitions are allowed only if photons are absorbed or emitted to conserve the crystal momentum. The spatial confinement of electrons and holes inside a QD relaxes this k -conservation requirement and creates a quasidirect bandgap [36]. Our measurements of photoluminescence (PL) from Si QDs in silicon oxide confirmed that we get the 1.7 eV bandgap from 2 nm quantum dots [5, 6, 28]. They also show that there is a large increase in PL intensity as the QD size decreases, which is consistent with the increase in radiative efficiency with the onset of pseudodirect bandgap behavior.

The photoluminescence peaks from Si QDs in nitride are more blue-shifted than that of Si QD in oxide. Figure 8 shows the PL peak energies from Si QD dispersed in oxide [37–39] and nitride [40, 41]. PL peak energies of Si QDs in oxide are less than 2.0 eV, while Si QDs in nitride have peak energies less than 3.0 eV. Puzder et al. [42] have explained that the main reason for the PL peak energy reduction in oxide matrix is the distortion of the local sp^3 network by double-bonded oxygen. However, Yang et al. [43] claimed that the reason for the stronger blue shift in nitride is better passivation of Si QDs by nitrogen atoms, eliminating the strain at the Si/Si₃N₄ interface nearly completely. Our PL results from the Si precipitation are in quite good agreement with the results from other authors [37–43].

Clear evidence of confinement in Si quantum dots in carbide was hard to obtain, probably due to many surface and defect states which dominate the photoluminescence process [34]. An observation of clear quantum confinement in the Si QDs, dispersed in SiC matrix, is also very challenging since usually metastable alloy films relax by diffusion and/or misfit dislocation formation to reduce chemical modulation and strain. It is likely that the mechanism of precipitation of excess Si atoms to nucleating sites in Si-rich SiC is a less active process than in nitride or oxide. This would be because the difference in Si–Si and Si–C lattice spacing is less than in the nitride and oxide. Also because SiC is an isoelectronic covalently bonded material as is Si; there is a much smaller tendency for segregation of Si than in oxide or nitride matrices.

3.3. Mobility-lifetime product

Photo-generated carriers in an Si quantum dot superlattice need to be collected at the metal contacts and hence require a reasonable mobility. A knowledge of mobility variation for the Si QDs in different matrices, with different barrier thickness and different doping densities in the Si QDs, is important to achieving a working device. Simulations of large bandgap cells using PC1D suggest mobility-lifetime products above 10^{-9} cm²/V which are required for good current collection for an indicative top tandem cell design thickness of 100–200 nm (Figure 2). Such a narrow absorber layer is thought reasonable given the improved optical absorption properties of the QD material.

The carrier lifetime of a thin-film material can be characterized by PL decay. Photoluminescence in QD structures involves electron-hole recombination between discrete energy

FIGURE 7: TEM images of SiC/Silicon-rich SiC multilayer (a) deposited and (b) annealed at 1100°C for 20 minutes.

FIGURE 8: Energy gaps of three-dimensionally confined Si nanocrystals in SiO_2 and SiN_x (300°K).

states in the conduction band and the valence band. A PL signal around 750 nm with a very broadband (~ 350 meV) is observed for the QD diameter of 3.4 nm (Figure 9). Despite the broadness of the peaks, there is evidence in Figure 9 that as the excitation intensity is increased the PL intensity of the low energy part of the spectrum (800 and 850 nm in Figure 9) increases more slowly than that of the high energy part. According to state-filling effect theory, lower energy levels with a low density of states (triplet states) will become saturated as intensity increases, but higher energy levels with a larger DOS (singlet states) will still be available for excitation as high excitation intensities increase [44]. These triplet

FIGURE 9: Time-integrated spectrum of Si quantum dot sample measured at different excitation intensities for 3.4 nm dot size.

TABLE 1: Decay time for different detection wavelengths with $\beta = 0.6$ for dot diameter of 3.4 nm and $\beta = 0.54$ for dot diameter of 4.2 nm.

Detection λ (nm)	600	650	700	750	800	850
3.4 nm dots (μs)	4	7	12	20	35	60
4.2 nm dots (μs)	2	4	10	18	20	55

and singlet states seem to occur in Si QDs in oxide matrix at about 820 and 740 nm, respectively, as in Figure 9.

Because the PL spectrum of the Si QDs is very broad and the recombination of carriers in different energy levels cannot be clearly resolved, information about the PL lifetime for different levels (with a spectral window of 2 nm in 50 nm) is spread across the spectrum (600–850 nm). Temporal evolution of the PL can be expressed as a stretched exponential function. This approach is frequently used to describe

FIGURE 10: Time-evolution of the PL intensities (a) at detection wavelengths of 650 nm, 750 nm, and 850 nm for 3.4 nm Si QDs fitted with a stretched exponential function and (b) at a detection wavelength of 700 nm for 3.4 nm and 4.2 nm Si QDs.

dispersive processes in disordered systems, for example, porous silicon, having a distribution of relaxation times, and is given by

$$I(t) = I_0 \cdot \exp \left[- (t/\tau)^\beta \right], \quad (3)$$

where τ is the PL lifetime and $0 \leq \beta \leq 1$ is the dispersion exponent. The PL decay shows that the lifetimes vary from 2 to 60 microseconds for diameter of 3.4 nm dot with increasing detection wavelength [44]. Figure 10 shows time-evolution of the PL intensities (a) at detection wavelengths of 650 nm, 750 nm, and 850 nm for 3.4 nm Si QDs fitted with a stretched exponential function and (b) at a detection wavelength of 700 nm for 3.4 nm and 4.2 nm Si QDs, demonstrating that the stretched exponential makes a good fit to the data at both the long and short time scales. Table 1 summarizes the PL decay times from the different detection wavelengths. The dispersion factor is $\beta = 0.6$ for sample 3.4 nm dot and $\beta = 0.54$ for 4.2 nm dot. β does not reflect microscopic properties which depend on the size of the QD but rather a macroscopic property of the system associated with the character of the medium [45]; thus the two samples exhibit a difference in the structure of the SRO layer and QDs surface states. The stretched function is related to a distribution of relaxation times or a time-dependent relaxation rate which reflects the interlevel relaxation processes in the QD. In all samples, the lifetime of a high energy level is short. The time decay in nitride matrix is under investigation.

3.4. Doping and work function control

The impurities, like phosphorous and boron in the bulk crystalline silicon, increase the conductivity of bulk Si by several orders of magnitude. There are several questions about the impurity doping in a low-dimensional structure [46]. Important questions arise as to whether the dopants will con-

tinue to play a role similar to that in bulk semiconductors, or alternative methods of work function control will be required. It is not clear at present whether or not the doping of Si QDs provides the generation of free charge carriers [47]. Also when silicon-rich precursor layers experience phase separation process described in (2), doping impurities may be thermodynamically unfavorable to incorporate into QDs since very small QDs are often regarded as structurally perfect. As a result, in worst case, impurity may not exist inside QDs after high temperature postannealing process.

To study the doping in Si QDs, we choose atoms with a high solid solubility in silicon at the annealing temperature. From this aspect, phosphorus and boron would be the best material for n-type and p-type doping materials, respectively. In our experiments, the phosphorus doping in the Si QD superlattices was achieved using P_2O_5 cosputtering during the deposition of silicon-rich oxide (Si and SiO_2 co-sputtering), which forms Si QDs upon high temperature postannealing. The P concentration in the silicon-rich oxide was controlled by the deposition rate of three targets and is initially chosen to be very high in order to increase the chances of detection. Phosphorus 2p X-ray photoelectron spectroscopy (XPS) spectra show that P–O bonds (peak around 135 eV) and P–Si bonds and/or free phosphorus (peak around 129 eV) are observed from highly P-doped silicon-rich oxide (Figure 11). $SiO_{1.41}$ with 0.67 at % phosphorus shows both Si–P and O–P bonding, while silicon-rich $SiO_{0.94}$ with 0.27 at % phosphorus shows only Si–P bonding. Control of the P concentration in this way was high, in the ranges of 0.26 at % $\sim$ 3.02 at %. The XPS results indicate that the phosphorus in silicon-rich oxide may exist in Si–P bonds inside Si QDs. However, it is necessary to carry out more analytical experiments for both n-type and p-type Si QDs in different matrices.

FIGURE 11: XPS spectra of P–Si and P–O bonding from (a) $\text{SiO}_{1.41}$ with phosphorus concentration of 0.67 at % and (b) $\text{SiO}_{0.94}$ with phosphorus concentration of 0.27 at %.

4. CONCLUSIONS

Third generation photovoltaic devices aim to tackle the losses associated with the nonabsorption of below bandgap photons and the thermalisation of above bandgap photons to the band edge. To tackle these losses, we are using silicon-based nanostructures as a high bandgap material for the concept of tandem solar cell.

Silicon has a bandgap just slightly larger than the ideal value for the lower cell in a two-cell or even a three-cell tandem stack. An upper material bandgap of 1.7 ~ 1.8 eV for a two-cell tandem solar cell with an Si bottom cell will maximize conversion efficiency. The optimum bandgaps for a three-cell tandem are 1.5 eV and 2.0 eV for middle and uppermost cells, respectively. The current work discusses the engineering of materials with appropriate bandgaps, using Si QDs dispersed either in silicon oxide, silicon nitride, or silicon carbide.

The formation of Si QDs in oxide and nitride matrices has been demonstrated, with good dot size control and evidence of nanocrystallinity from HRTEM and XRD. Quantum confinement has been demonstrated, using PL for the matrices of oxide and nitride, with PL energy increasing as dot size decreases by the correct relative amounts predicted by confined quantum confinement theory. A transfer of the technology to Si QDs in a silicon carbide matrix has been successfully demonstrated in single layer and multilayer structures, but demonstration of clear quantum confinement in the Si QDs is challenging due to a dominant surface state.

PL decay measurements of Si QDs dispersed in oxide show a slow decay (several tens of microseconds) in the lower part of PL spectrum and fast decay (few microseconds) in the higher part of the PL spectrum. This may be due to singlet-triplet splitting in Si QDs dispersed in oxide. There is some initial evidence for n-type doping in Si QDs, which may enable us to make a fully working device.

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