Research Article

Design of a Novel High Power V-Band Helix-Folded Waveguide Cascaded Traveling Wave Tube Amplifier

Tianxiang Zhuge and Yulu Hu

School of Physical Electronics, University of Electronic Science and Technology of China, Chengdu 610054, China

Correspondence should be addressed to Yulu Hu; yuluhu@uestc.edu.cn

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A design of a V-band Helix-Folded Waveguide (H-FWG) cascaded traveling wave tube (TWT) is presented. In this cascaded structure, a digitized nonlinear theory model is put forward first to simulate these two types of the tubes by common process. Then, an initial design principle is proposed, which can design these two different kinds of tubes universally. Using this principle, a high-gain helix TWT is carefully designed as a first stage amplifier followed by a FWG TWT to obtain high power. Simulations predict that a peak power of 800 W with saturated gain of 60 dB from 55 GHz to 60 GHz can be achieved.

1. Introduction

The V-band frequency range (50–75 GHz) is a region of the millimeter wave spectrum with great potential application for intersatellite communications and high-performance radar applications, including atmospheric studies, space debris detection, precise tracking, and high resolution imaging [1–3]. However, it has to face to the size and power limitation at this frequency range, when using traditional helical traveling wave tube [1, 4] and some novel structure TWTs [5–7] on such high-frequency band. However, some metal structure TWTs (Coupled Cavity (CC) TWT [8], FWG TWT [9, 10], and so on) can obtain high power but low gains in single tube for strong backward wave oscillation (BWO) instability, also for some FWG cascaded TWTs [11, 12] and CC-FWG cascaded TWTs [13].

In order to obtain a high power and high-gain V-band traveling wave tube in feasible manufacture way, we designed a novel H-FGW cascaded traveling wave tube amplifier. In this design, we use helical traveling wave tube as a first stage amplifier, which is famous for its wide bandwidth and high gain and then exported the amplified signal into the FWG traveling wave tube to get high power. The FWG traveling wave tube has large power capability for its full metal structure and is chosen to get high power in the V-band frequency range.

A digitized beam-wave interaction theory model [14, 15] is used to analyze the performance of the designed helix-FWG cascaded traveling wave tube, which has been developed and included in MTSS [16]. In this model the digitized fields, getting the data from electromagnetic (EM) simulation software for arbitrary SWSs, are used to interact with the beam keeping the energy translation and conservation between the beam and the EM wave. Due to its general way to deal with the beam-wave interaction process, this digitized theory model can be used to simulate and analyze the nonlinear performance of traveling wave tube with different SWS.

A helix-FWG cascaded traveling wave tube testified the design method and is optimized. Finally, the simulation of the saturated output power is above 34 W with the saturated gain above 33 dB in 5 GHz bandwidth in the first stage helical TWT. And, for the cascaded FWG traveling wave tube in same bandwidth, the saturated gain is above 18 dB achieving the output power to be 800 W. After matching the input-output power in the connection, the total cascaded tube achieves 60 dB gain and 800 W in 5 GHz band. The illustration of the helix-FWG cascaded TWT model is presented in Figure 1.

The rest of the paper is organized as follows. Section 2 presents the sketch of the digitized nonlinear beam-wave interaction theory model, and Section 3 introduces the
principle of the TWT design. Based on the design principle and the digitized theory model, the design and analysis of the H-FWG cascaded TWT are detailed in Section 4. A conclusion is followed at the end of the paper.

2. The Digitized Nonlinear Theory Model [14]

The digitized nonlinear theory model is a quasi-3D nonlinear theory model developed and included in MTSS [16]. It gets electromagnetic field distribution of arbitrary SWSs from the numerical simulation software such as HFSS, CST, and HFCS and then uses the energy conservation principle to get the energy exchange between the beam and the EM wave. Consequently, this digitized theory model is allowed to analyze the nonlinear performance of many kinds of traveling wave tube using different periodic high-frequency structures.

In the digitized nonlinear theory, RF fields acting on the electron beam propagating in a SWS are represented as

\[
\begin{align*}
E_{rf}(x, t) &= \sum_{n} E_{rf}^{(n)}(x, t) = \sum_{n} \left[ f_n(z) e_n(x) e^{-iwnz} \right], \\
H_{rf}(x, t) &= \sum_{n} H_{rf}^{(n)}(x, t) = \sum_{n} \left[ h_n(z) h_n(x) e^{-iwnz} \right].
\end{align*}
\]

(1)

The RF electric field \(E_{rf}\) and magnetic field \(H_{rf}\) are composed of many different time harmonics, whose angular frequency is \(\omega_n\) and complex amplitude varying along the \(z\) axial is \(f_n(z)\). Subscript \(n\) indicates the harmonic number and \(e_n(x)\) and \(h_n(x)\) are the RF field profiles without electron beam loaded, which will be obtained by EM simulation of HFSS [17], HFCS [16], CST [18], and so forth. Once obtaining the RF field profiles, the evolution of the RF field amplitude can be developed based on the law of energy conservation, and finally we get

\[
\begin{align*}
\left[ \frac{\partial}{\partial z} + \alpha_n(z) \right] f_n(z) &= - \frac{1}{2} \int_{z}^{z+\lambda_h} \frac{dz}{\lambda_h} \int_{t}^{t+T} dt \frac{d}{dt}, \\
\sum_{n} \int_{A} j \cdot e_n^{*}(x, z_0) e^{-i\omega_n t} e^{i\omega_n z} ds, \quad z_0 \in [0, \lambda_h].
\end{align*}
\]

(2)

Here \(\alpha_n\) means the attenuation constant, \(\lambda_h\) is the axial period length of the structure, and \(T\) is the period time. \(j = \rho v\) is the beam current density. \(m\) is the number of the period among which \(z\) is solving. And \(\phi_n\) is the phase shift for the \(n\)th RF signal in one period.

For different type of slow-wave structure (SWS), \(e_n(x)\) and \(h_n(x)\) are quite different. Without care for the analytic model of the slow-wave structure, we can use (1) to get the EM field and then to push the particles in the beam. The beam current then affects the field amplitude \(f_n(z)\), which will inevitably change the status of the beam and thus the current. Following this circulation, we can trace the process of the beam-wave interaction and get the nonlinear performance of the TWT.

3. Design Principle of TWT

As a first step, to get the desired output power and gain, the beam voltage and the beam density in the tunnel (FWG or helix) in beam-wave interaction region have to be carefully selected, which are of the most important factors limiting the output power and gain. As it is well known, the output power \(P_o\) can be estimated by beam voltage \(V\), beam current \(I_o\), and efficiency \(\eta\); that is,

\[
P_o = \eta V I_o.
\]

(3)

From (3), we get beam current:

\[
I_0 = \frac{P_o}{\eta V}.
\]

(4)

And the beam density in the tunnel (FWG or helix) in beam-wave interaction region is

\[
J = \frac{I_0}{\pi b^2} = \frac{I_0}{\pi (\rho r_a)^2} = \frac{P_o}{\pi (\rho r_a)^2 V},
\]

(5)

Here \(b\) is the beam radius, \(\rho\) is the beam filling ratio, and \(r_a\) is the radius of the tunnel (FWG or helix). On the other hand, the relativity factor \(\gamma = 1/\sqrt{1 - v_0^2/c^2}\) can be estimated by

\[
\gamma - 1 = \frac{V}{m c^2},
\]

(6)

where \(e/m\) is the electron charge to mass ratio and \(c\) is speed of light, from which we get the initial beam speed \(v_0\):

\[
v_0 = \sqrt{\frac{e}{m} \left( \gamma + \frac{1}{\gamma^2} \right) V}.
\]

(7)

Define a slow-varying and dimensionless parameter \(\Gamma\) as

\[
\Gamma = \frac{\omega}{v_0 r_a} \approx \frac{\omega}{v_0 r_a}.
\]

(8)

And combining (7) and (8), the tunnel radius \(r_a\) can be presented as

\[
r_a = \frac{\Gamma}{\omega} \sqrt{\frac{e}{m} \left( \gamma + \frac{1}{\gamma^2} \right) V}.
\]

(9)

Inserting (9) into (5), the beam density can finally be written as

\[
J = \frac{m P_o}{\pi \eta \gamma + 1} \left( \frac{\gamma \omega}{\rho V} \right)^2.
\]

(10)
And the Brillouin magnet field will be

\[ B_B = \frac{1}{b} \left( \frac{2mI}{\pi e_0 v_0} \right)^{1/2} \]
\[ = \left[ \frac{2J}{\varepsilon_0 (e/m)^3 \left( (y + 1)/y^2 \right) V} \right]^{1/2} \]
\[ \approx 17.5 \times \left( \frac{y}{(y + 1) V} \right)^{1/4} \text{ (Gs)} \]  

(11)

Based on the current density limitation of certain kind of TWT, (10) and (9), we can get the relationship between voltage and output power as well as the tunnel radius and voltage. After choosing proper electronic efficiency, beam filling ratio, and parameter \( \Gamma \), a proper voltage and the tunnel radius can be selected to meet our design.

4. Design of the H-FWG Cascaded Traveling Wave Tube

In the design of H-FWG cascaded traveling wave tube, we first select a proper voltage and tunnel radius and then optimize the SWS and beam-wave interaction profile of the helix TWT and the FWG TWT separately. Cascading these two sections, an output power of 800 W and a gain of 55 dB are expected in the V-band of 55 GHz to 60 GHz.

4.1. Choice of Voltage. In this V-band cascaded TWT design, we first set a proper parameter \( \Gamma \) and electronic efficiency \( \eta \) (here we set \( \eta = 8\% \) and \( \Gamma = 1.5 \) as initial value). The beam density of helix TWT is chosen less than 150 A/cm\(^2\) and the filling ratio is set to be 0.45 for helix TWT. For FWG TWT with greater power capacity, the beam density is chosen as 300 A/cm\(^2\) and the filling ratio is 0.75. Using (9) and (10), we get the relationship between output power and voltage, as well as the tunnel radius and voltage, as shown in Figure 2.

After careful optimization, a voltage of 14.5 KV is selected for the first stage helix TWT, whose corresponding output power is 34 W and helix radius is 0.25 mm, shown as the black star in Figure 2. For the FWG TWT, the voltage is set to 20 KV, corresponding to an output power of 800 W and tunnel radius of 0.3 mm, demonstrated as the red triangle in Figure 2. And the current is to be 32.5 mA for helix TWT and 450 mA for FWG TWT.

4.2. Design of Helix TWT. A simple helix SWS with three APBN sector support rods is selected (shown in Figure 3), which can be manufactured easily. The design principle of the other SWS parameters, except fixed helix radius to 0.25 mm,
is seeking the suitable dimensions to maximize the coupling impedance and to obtain flat dispersion between 55 GHz and 60 GHz. After careful optimization, the helix SWS structure parameters are shown in Table 1. The helix pitch ranges from 0.45 mm to 0.55 mm. For later beam-wave interaction optimization, the helix SWS with different helix pitch will be simulated with a step of 0.02 mm.

The normalized velocity, coupling impedance, and attenuation constant for the helix SWS with helix pitch ranging from 0.45 mm to 0.55 mm are shown in Figure 4.

It is simulated and optimized of the beam-wave interaction with pitch and attenuation profile (shown in Figure 5), using the simulation code developed on the model discussed in Section 2. Also BWO is considered by using an additional attenuator in input circuit and pitch step in output circuit. The pitch of the circuit is finally set to be 0.505 mm and then step to 0.49 mm, respectively. The profile of output power and gain along z-axis at 57 GHz is shown in Figures 6(a) and 6(b). And the saturated output power and saturated gain in band are shown in Figure 6(c). Obviously, the output power of the first
Figure 6: (a) Output power versus $z$ at 57 GHz, (b) gain versus $z$ at 57 GHz, and (c) saturated output power and saturated gain ranging from 55 GHz to 60 GHz.

Figure 7: Illustration of (a) side view and (b) front view of the FWG SWS.
Figure 8: (a) Dispersion curve, (b) coupling impedance, and (c) attenuation constant for FWG SWS.

Figure 9: Pitch and attenuation profile of the FWG TWT (black and white).

<table>
<thead>
<tr>
<th>Table 1: Parameters of the helix slow-wave structure.</th>
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</thead>
<tbody>
<tr>
<td><strong>Parameter</strong></td>
</tr>
<tr>
<td>Helix radius ($R_a$)</td>
</tr>
<tr>
<td>Helix tape thickness</td>
</tr>
<tr>
<td>Helix tape width</td>
</tr>
<tr>
<td>Helix pitch</td>
</tr>
<tr>
<td>Rod material</td>
</tr>
<tr>
<td>Rode wedge angle ($\theta$)</td>
</tr>
<tr>
<td>Shield radius ($R_c$)</td>
</tr>
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</table>

stage helix TWT can achieve 34 W and the saturated gain of 35 dB from 55 GHz to 60 GHz.

4.3. Design of FWG TWT. Similar optimization is done for the FWG TWT (structure is shown in Figure 7). To get large
coupling impedance and suitable synchronized velocity, we scan the structure parameters and finally get the FWG SWS with parameters listed in Table 2.

The normalized velocity, coupling impedance, and attenuation constant of the optimized FWG SWS are plotted in Figure 8. We can see that the relative discrepancy of normalized velocity is less than 1% from 55 GHz to 60 GHz in Figure 8(a), which indicates well dispersion flatness and

**Table 2: Parameters of the folded slow-wave structure.**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
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<tbody>
<tr>
<td>$r$</td>
<td>0.3 mm</td>
</tr>
<tr>
<td>$b$</td>
<td>3.15 mm</td>
</tr>
<tr>
<td>$a$</td>
<td>0.85 mm</td>
</tr>
<tr>
<td>$H$</td>
<td>0.8 mm</td>
</tr>
<tr>
<td>$L$</td>
<td>2.0 mm</td>
</tr>
</tbody>
</table>
can satisfy the synchronization condition. As shown in Figure 8(b), the coupling impedance is greater than 2.5 Ohms within the designed V-band 55 GHz to 60 GHz and a strong beam-wave interaction can be expected. It can be found that the FWG SWS has much lower loss than helix one comparing Figures 8(c) and 4(c). Because it is the surface wave traveling along the helix with strong field in helix TWT, it is light field on the boundary of the waveguide in FWG SWS.

A large amount of optimization processes has been done to determine the profile of the FWG TWT and a high power pitch profile is proposed in Figure 9. A sever is select to cut the input circuit short. Note that the pitch here refers to half-period of the FWG SWS.

The performance of the output power and gain at 57 GHz are provided in Figure 10. And the saturated output power and the corresponding input power, as well as the saturated gain, are shown in Figure 11. Obviously, the saturated output power is greater than 800 W and the saturated gain is larger than 18 dB from 55 GHz to 60 GHz.

After design of the first stage helix TWT and FWG TWT separately, we match the output power of helix TWT to be the same of the input power FWG TWT by modifying the helix input power, keeping the output power of FWG saturated (see Figure 12). Then, the saturated cascaded gain can be obtained by saturated FWG gain plus gain of helix TWT. As shown in Figure 13, the cascaded gain above 60 dB can be expected within the V-band of 55 GHz to 60 GHz.

5. Conclusions

Based on the digitized nonlinear theory model developed in MTSS, a novel high power V-band cascaded helix-FWG TWT is designed, which is expected to generate an output power of 800 W and a gain of 60 dB from 55 GHz to 60 GHz. The digitized nonlinear theory model, which can process the beam-wave interaction universally, is briefly introduced. And then the principle of the TWT design is derive, by which a proper voltage and tunnel radius can be selected. The first stage helix traveling wave tube is designed to have an output power above 34 W and gain above 35 dB. For the cascaded FWG traveling wave tube, the saturated output power is designed to be greater than 800 W and the saturated gain is larger than 18 dB in the 5 GHz bandwidth. As a result, we get the expected output power of 800 W and gain of 60 dB by cascading these two traveling wave tubes.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

Acknowledgment

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References


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