Research Article

The Preventive Control of Zoonotic Visceral Leishmaniasis: Efficacy and Economic Evaluation

Helio Junji Shimozako,1 Jianhong Wu,2 and Eduardo Massad1,3

1Faculty of Medicine, University of São Paulo and LIM 01-HCFMUSP, Avenida Dr. Arnaldo 455, 01246-903 São Paulo, SP, Brazil
2Centre for Disease Modelling, York Institute for Health Research, York University, 4700 Keele Street, Toronto, ON, Canada M3J IP3
3London School of Hygiene and Tropical Medicine, University of London, London, UK

Correspondence should be addressed to Helio Junji Shimozako; hjunji21@usp.br

Received 4 January 2017; Revised 23 March 2017; Accepted 28 March 2017; Published 15 May 2017

Academic Editor: Chung-Min Liao

Copyright © 2017 Helio Junji Shimozako et al. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Zoonotic Visceral Leishmaniasis (ZVL) is one of the world’s deadliest and neglected infectious diseases, according to World Health Organization. This disease is one of major human and veterinary medical significance. The sandfly and the reservoir in urban areas remain among the major challenges for the control activities. In this paper, we evaluated five control strategies (positive dog elimination, insecticide impregnated dog collar, dog vaccination, dog treatment, and sandfly population control), considering disease control results and cost-effectiveness. We elaborated a mathematical model based on a set of differential equations in which three populations were represented (human, dog, and sandfly). Humans and dogs were divided into susceptible, latent, clinically ill, and recovery categories. Sandflies were divided into noninfected, infected, and infective. As the main conclusions, the insecticide impregnated dog collar was the strategy that presented the best combination between disease control and cost-effectiveness. But, depending on the population target, the control results and cost-effectiveness of each strategy may differ. More and detailed studies are needed, specially one which optimizes the control considering more than one strategy in activity.

1. Introduction

Zoonotic Visceral Leishmaniasis (ZVL) is one of the world’s deadliest and neglected infectious diseases, according to World Health Organization. This disease is endemic in 80 countries worldwide, in which 90% of all cases occur in Bangladesh, Brazil, India, Nepal, and Sudan. Thus, about 360 million of people are exposed to risk of infection in the world [1–4]. The ZVL is a disease of major human and veterinary medical significance that involves a complex interplay between trypanosomatids protozoan from Leishmania complex, arthropod vectors (in Brazil, we find the female sandflies Lutzomyia longipalpis and Lutzomyia cruzi), environmental influence on vector distribution, small companion animal (dog) reservoir of infection, and susceptible human populations. In American continent, Leishmania infantum chagasi is the most important species from Leishmania complex.

From the last few years, ZVL has been emerging within nonendemic areas, mostly because of transportation of dogs from endemic areas and climatic changes with the expansion of the geographical range of the sandfly vector. Thus, the effective control will essentially involve interdisciplinary teams of microbiologists, parasitologists, entomologists, ecologists, epidemiologists, immunologists, veterinarians, public health officers, and human physicians [5].

Besides the publication of guidelines of ZVL control and the investments made in general surveillance activities, the sandfly and the reservoir in urban areas remain among the major challenges for the control activities. These challenges are due to (1) the necessity to better understand the vector behavior in urban environment, (2) the operational and logistic difficulties to carry out activities in sufficient time to obtain good results, and (3) the high costs involved in these activities [2, 6].
Usually, health is not analyzed as an economical activity. However, economical analysis in health studies is important for comprehension of health polices dynamics and trends. From those results, it is possible to obtain arguments and support to organize and supervise health polices programs. In short, economic health expresses the universal desire of reaching the best investment, not only in terms of clinical effectiveness, but also in terms of approaching cost-effectiveness about healthcare procedures [7, 8].

Marinho et al. [9] observed that there are few studies that analyzed the economical impact on visceral leishmaniasis considering social and collective approach. In addition, there are several difficulties to develop economical analysis of visceral leishmaniasis transmission due to (I) the interval of time between the intervention and epidemiological impact or/and (II) the difficulty to relate the intervention activities to the resulting impact. Considering those difficulties and still open-questions about ZVL dynamics and impact, the use of mathematical models should become a very interesting alternative of analysis.

Some deterministic models have been published in literature and all of them analyze the dynamic of this disease and make any evaluation of strategies controls. In particular, since 1998 our research group has been working on ZVL modeling. Burattini et al. [10] worked on a mathematical model to visceral leishmaniasis where both humans and dogs were considered source of infection. Later, Ribas et al. [11] developed a model, based on Burattini et al. [10], which was restricted to LVZ and some preventive control strategies were also considered. Newly, an original article was published by Shimozako et al. [12], where they reviewed the model published by Burattini et al. [10] and not only updated some parameters but also provided a more complete mathematical analysis. In this most recent paper, we were able to fit the model to real data from Araçatuba/SP city (Brazil), carrying out a very robust model and results. And, besides those models published by our research team, we also have other researchers who published mathematical models for LVZ, as Zhao et al. [13], in which their model differs from ours by the adopted mathematical structure and the presence of backward bifurcation.

Even though the result from mathematical model indicates epidemiological availability for visceral leishmaniasis control, we should evaluate carefully the practical and economical viability. In this case, regarding public health, the disease control activities should work considering the best cost-effectiveness, since the available resources are limited. We also know that it is important to be aware of the time-response and applicability-practicality conditions. In other words, it is necessary to be careful with investment time and method application relationship and the respective expected result [5, 14–17].

In this work we propose an evaluation of five ZVL control strategies (positive dog elimination, insecticide impregnated dog collar, dog vaccination, dog treatment, and sandfly population control), by mathematical modeling. This mathematical model was based on the previous models published by Burattini et al. [10] and Ribas et al. [11]. We studied the impact of those control strategies on human and dog population by approaching the epidemiological control and cost-effectiveness. Then, we discussed the most efficient control strategies and how they act on visceral leishmaniasis epidemiological chain.

2. The Model

We used a mathematical model that is an adaptation of the one proposed by Burattini et al. [10]. In our model, we assume

(1) a human and a dog population, with the biological vector transmitting the infection within and between the two populations;

(2) those three populations (humans, dogs, and vectors) being constants;

(3) both human (indexed as $h$) and dog (indexed as $d$) populations being divided into four categories: susceptible ($x_h$ and $x_d$), infected but without noticeable disease ($y_h$ and $y_d$) (i.e., “latent”), clinically ill ($z_h$ and $z_d$), and recovering immunes ($e_h$ and $e_d$). On the other hand, the vector population is divided into three categories: noninfected, infected but not infective, and infective individuals, denoted as $s_1, s_2,$ and $s_3,$ respectively.

The flowchart and compartment model (Figure 1) and the set of differential equations describing the model’s dynamics (system (1)) are presented as shown in Figure 1 and are as follows:

$$
\begin{align*}
\dot{x}_h(t) & = \mu_h (\bar{x}_h(t) + \bar{y}_h(t) + \bar{z}_h(t)) + r_d \bar{x}_h(t) + \alpha_h \bar{y}_h(t) \\
& \quad + \gamma_h \bar{z}_h(t) - b_h \alpha_m \bar{m}_h(t) s_3(t) x_h(t) \\
\dot{\bar{y}}_h(t) & = (b_h \alpha_m \bar{m}_h(t) s_3(t) x_h(t)) - (\mu_h + r_h + \delta_h + \phi_h) \bar{y}_h(t) \\
\dot{\bar{z}}_h(t) & = \delta_h \bar{y}_h(t) + \alpha_d \bar{y}_h(t) - (\mu_h + \gamma_h + \delta_h) \bar{z}_h(t) \\
\dot{x}_d(t) & = (\mu_d + \xi_d) (\bar{I}_d(t) + \bar{y}_d(t) + \bar{z}_d(t)) + r_d \bar{I}_d(t) \\
& \quad + \alpha_d \bar{y}_d(t) + \gamma_d \bar{z}_d(t) \\
& \quad - b_d \alpha_m \bar{m}_d(t) s_3(t) x_d(t) \\
\dot{\bar{I}}_d(t) & = (b_d \alpha_m \bar{m}_d(t) s_3(t) x_d(t)) - (\mu_d + r_d + \delta_d + \phi_d + \xi_d) \bar{I}_d(t) \\
\dot{\bar{y}}_d(t) & = \delta_d \bar{I}_d(t) + \alpha_d \bar{y}_d(t) - (\mu_d + \gamma_d + \delta_d) \bar{z}_d(t) \\
\dot{\bar{z}}_d(t) & = \delta_d \bar{I}_d(t) + \alpha_d \bar{y}_d(t) - (\mu_d + \gamma_d + \delta_d) \bar{z}_d(t) \\
\dot{s}_1(t) & = \mu_s (s_2(t) + s_3(t)) - a_s (c_I \bar{I}_d(t) + c_y \bar{y}_d(t)) s_1(t) \\
\dot{s}_2(t) & = a_s (c_I \bar{I}_d(t) + c_y \bar{y}_d(t)) s_1(t) - \mu_s s_2(t) \\
& \quad - a_s (c_I \bar{I}_d(t) - \tau + c_y \bar{y}_d(t) - \tau) s_1(t - \tau) e^{-\mu \tau}
\end{align*}
$$
The last three equations of system (1) refer to the flies. When infected, a fly remains in a latent stage for a period of time \(\tau\). This time corresponds to the extrinsic incubation period of the parasite inside the vector fly. Numerically it lasts for about half the life expectancy of the flies.

Let \(S_t\) be the number of susceptible flies. In an infinitesimal period of time \(dt\), \( (a_5(L_d(t) + Y_d(t))/N_j(t))dt \) bites due to uninfected flies occur on latent and infected dogs (humans are not considered to be infective for flies; see Tesh [18]). A fraction, \( c_3\), of the flies that bites latent and clinically ill dogs, (resp.) becomes latently infected as a result. Therefore, we have

\[
dS_t = (a_5(L_d(t) + Y_d(t))/N_j(t))dt  
- a_5 \left( c_3 y_d (t) + c_p y_d (t) \right) S_t dt. \tag{3}
\]

Dividing by \(S(t) = S_t(t) + S_j(t) + S_k(t)\) and by \(dt\), we get the equation for noninfected sandflies (\(S_t(t)\)).

Although this is a brief but detailed description of the noninfected categories equations (i.e., \(X_k, x_d,\) and \(s_j\)), we can note that each term of our system equation has a biological meaning. The meaning of each term depends on the respective parameters that set them (e.g., \( \delta, \phi, (t) + \sigma_d\) means the amount of latent dogs that develop immunity per day).

### 3. The Number of Clinically Ill Humans and Reported Cases

In Brazil, ZVL is a notifiable disease [17, 34]. Thus, we can assume the following:

(i) An infected human should look for medical treatment when he/she will become clinically ill (\(y_h(t)\)).

(ii) Only a fraction of those humans that are clinically ill will be reported to sanitary authorities. The remaining fraction (I) will not look for medical help, even if the clinical symptoms and signs appear or (II) will not be correctly reported in the hospitals.

Now, let us see again the equation for \(y_h(t)\) in system (1):

\[
y_h(t) = \phi_h l_h(t) - (\mu_h + \alpha_h + \sigma_h) y_h(t). \tag{4}
\]

The term \(\phi_h l_h(t)\) in (4) means the rate of latent humans who become clinically ill per day. Thus, in order to calculate the total of humans that become clinically ill along an interval of time, we have

\[
T_{y_h}(t_f) = \phi_h \int_{t_0}^{t_f} l_h(t) dt, \tag{5}
\]

where \(T_{y_h}(t_f)\) is the total of humans that become clinically ill from an initial moment, \(t_0\), to a final one, \(t_f\).

Now, let us consider that, per day, the number \(\phi_h l_h(t)\) of humans is eligible to look for medical help. However, only a fraction \((1 - \eta_h)\) of those clinically ill humans will be correctly notified to sanitary authorities, where \(\eta_h = 0.705\) means the
Table I: Parameters adopted in our model. The indexes h, d, and s stand for humans, dogs, and sandflies, respectively.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
<th>Value</th>
<th>Dimension</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \mu_h )</td>
<td>Natural mortality rate</td>
<td>( 3.67 \times 10^{-5} )</td>
<td>1/day</td>
<td>Brazilian Institute of Geography and Statistics, Brazil [19]</td>
</tr>
<tr>
<td>( \alpha_h )</td>
<td>Kalazar specific lethality</td>
<td>( 6.31 \times 10^{-3} )</td>
<td>1/day</td>
<td>World Health Organization [20]</td>
</tr>
<tr>
<td>( a_h )</td>
<td>Average daily bitten humans rate</td>
<td>( 2.00 \times 10^{-1} )</td>
<td>Human/(sandfly \times day)</td>
<td>Epidemiological Surveillance Direction, Santa Catarina State, Brazil [21]</td>
</tr>
<tr>
<td>( m_h(t) )</td>
<td>Vector density per host (time-dependent)</td>
<td>Variable</td>
<td>Sandfly/human</td>
<td>Fitted</td>
</tr>
<tr>
<td>( w_{hh} )</td>
<td>Human : house ratio</td>
<td>3</td>
<td>Human/house</td>
<td>Brazilian Institute of Geography and Statistics, Brazil [22]</td>
</tr>
<tr>
<td>( b_h )</td>
<td>Proportion of infective bites</td>
<td>( 1.00 \times 10^{-2} )</td>
<td>Dimensionless</td>
<td>Molineaux and Gramiccia [23]</td>
</tr>
<tr>
<td>( r_h )</td>
<td>Spontaneous recovery rate</td>
<td>( 5.48 \times 10^{-4} )</td>
<td>1/day</td>
<td>Badaro et al. [24]</td>
</tr>
<tr>
<td>( \gamma_h )</td>
<td>Loss of immunity rate</td>
<td>( 5.48 \times 10^{-4} )</td>
<td>1/day</td>
<td>Kault and Marsh [25]</td>
</tr>
<tr>
<td>( \delta_h )</td>
<td>Latent recovery rate</td>
<td>( 1.10 \times 10^{-2} )</td>
<td>1/day</td>
<td>Badaro et al. [24]</td>
</tr>
<tr>
<td>( \phi_h )</td>
<td>Inverse of incubation period</td>
<td>( 4.00 \times 10^{-4} )</td>
<td>1/day</td>
<td>Pearson and Souza [26]</td>
</tr>
<tr>
<td>( \sigma_h )</td>
<td>Recovery rate to immunes</td>
<td>( 2.50 \times 10^{-3} )</td>
<td>1/day</td>
<td>Ministry of Health, Brazil [17]</td>
</tr>
<tr>
<td>( \mu_d )</td>
<td>Natural mortality rate</td>
<td>( 2.28 \times 10^{-4} )</td>
<td>1/day</td>
<td>Selman et al. [27]</td>
</tr>
<tr>
<td>( \alpha_d )</td>
<td>Kalazar specific lethality</td>
<td>( 1.81 \times 10^{-3} )</td>
<td>1/day</td>
<td>Lanotte et al. [28]</td>
</tr>
<tr>
<td>( a_d )</td>
<td>Average daily bitten dogs rate</td>
<td>( 2.00 \times 10^{-1} )</td>
<td>Dog/(sandfly \times day)</td>
<td>Epidemiological Surveillance Direction, Santa Catarina State, Brazil [21]</td>
</tr>
<tr>
<td>( w_{dh} )</td>
<td>Human : dog ratio for Araçatuba/SP city</td>
<td>10/1.8</td>
<td>Human/dog</td>
<td>Andrade et al. [29]</td>
</tr>
<tr>
<td>( m_d(t) )</td>
<td>Vector density per host</td>
<td>( w_{dh} \times m_s(t) )</td>
<td>Sandfly/dog</td>
<td>—</td>
</tr>
<tr>
<td>( \phi_d )</td>
<td>Inverse of incubation period</td>
<td>( 3.78 \times 10^{-4} )</td>
<td>1/day</td>
<td>Greene [30]</td>
</tr>
<tr>
<td>( b_d )</td>
<td>Proportion of infective bites</td>
<td>( 1.00 \times 10^{-2} )</td>
<td>Dimensionless</td>
<td>Molineaux and Gramiccia [23]</td>
</tr>
<tr>
<td>( r_d )</td>
<td>Spontaneous recovery rate</td>
<td>( 2.74 \times 10^{-4} )</td>
<td>1/day</td>
<td>Lanotte et al. [28]</td>
</tr>
<tr>
<td>( \gamma_d )</td>
<td>Loss of immunity rate (recovery to susceptible)</td>
<td>( 2.74 \times 10^{-3} )</td>
<td>1/day</td>
<td>Kault and Marsh [25]</td>
</tr>
<tr>
<td>( \sigma_d )</td>
<td>Recovery rate from clinically ill to immunes</td>
<td>( 9.04 \times 10^{-4} )</td>
<td>1/day</td>
<td>Lanotte et al. [28]</td>
</tr>
</tbody>
</table>

The Centre of Epidemiological Surveillance of São Paulo State (CES-SP) [36] is the institution that administers the data about ZVL in São Paulo State. In order to validate our model, we decided to use the data of human reported cases from the municipality of Araçatuba (São Paulo State, Brazil) as reference, because it is an endemic city for this disease. Those data are presented in Table 3 and are available on CES-SP website [36].

Note that we have the total of reported cases per year. Thus, since our time scale is day, we estimated an average of human reported cases per day for each year (dividing the total from each year by 365). Finally, we also have to consider that our model works with normalized population (all three populations are constant). Thus, as a last step, we have to divide each rate of human reported cases per day by the official population size of Araçatuba municipality. The population size of Araçatuba municipality is available on Brazilian Institute of Geography and Statistics website [22].

In order to fit and compare our results to real data, we also calculated a normalized average of reported cases per day from every 365 days of simulation. This simulation was run considering 60 years and the obtained curve was fitted by simple handling along the time-axis (e.g., we could assume the initial day \( t_0 = 1 \) as the first day of 1970 or 1980, depending on how best the simulated curve fits on the real data). Thus, we could obtain the yearly average of reported human cases per day and compare it to the real yearly average provided by CES-SP [36] (Table 3).

### 4. Fitting the Human : Sandflies Ratio \( (m_h(t)) \)

Among all used parameters for this work, the sandfly/human ratio is one of the most challenging to be estimated. Although we had found some field studies that tried to estimate sandfly population size and other demographic characteristics [37], we did not find any study regarding this ratio for Araçatuba city. Therefore, in our simulation, we decided to fit this ratio according to real data of human cases. Since we are studying visceral leishmaniasis dynamics, it is necessary that the disease is persistent in the population. Considering this condition, we assumed the condition \( R_0 > 1 \) and estimated the minimum value for \( m_h(t) \) (calculation is not shown, but we followed the method described by van den Driessche and Watmough [38]).

The proportion of unreported cases [35]. Therefore, the daily rate of reported human cases \( \text{Rep}(t) \) is defined by

\[
\text{Rep}(t) = (1 - \eta_h) \ f_h l_h(t).
\]

The Centre of Epidemiological Surveillance of São Paulo State (CES-SP) [36] is the institution that administers the data about ZVL in São Paulo State. In order to validate our model, we decided to use the data of human reported cases from the municipality of Araçatuba (São Paulo State, Brazil) as reference, because it is an endemic city for this disease. Those data are presented in Table 3 and are available on CES-SP website [36].

Note that we have the total of reported cases per year. Thus, since our time scale is day, we estimated an average of human reported cases per day for each year (dividing the total from each year by 365). Finally, we also have to consider that our model works with normalized population (all three populations are constant). Thus, as a last step, we have to divide each rate of human reported cases per day by the official population size of Araçatuba municipality. The population size of Araçatuba municipality is available on Brazilian Institute of Geography and Statistics website [22].

In order to fit and compare our results to real data, we also calculated a normalized average of reported cases per day from every 365 days of simulation. This simulation was run considering 60 years and the obtained curve was fitted by simple handling along the time-axis (e.g., we could assume the initial day \( t_0 = 1 \) as the first day of 1970 or 1980, depending on how best the simulated curve fits on the real data). Thus, we could obtain the yearly average of reported human cases per day and compare it to the real yearly average provided by CES-SP [36] (Table 3).
The real data provided in Table 3 suggests that the incidence was not constant along those years in which the data was collected (1999 to 2015). One reasonable hypothesis is the climate changes that have been occurring for the last years [39]. Thus, since the sandfly population dynamics depend on climate and geographical conditions, we can include this idea in our model by fitting $m_h(t)$ as time-function. It is not the scope of this paper to model the sandfly population dynamics according to climatic and geographic variations. Therefore, we will assume that a simple function for $m_h(t)$, which can fit the simulation data to the real data, should include those climatic and geographic variabilities.

Let us consider the following function for $m_h(t)$:

$$m_h(t) = m_{h0} + \left( \frac{te^{-(L+K_1)}}{K_1} \right) \left( A + B \sin \left( \frac{2\pi t}{T} \right) \right)$$

$$\lim_{t \to +\infty} m_h(t) = m_{h0}.$$  

The parameter values for (7) are in Table 4. Biologically, we can suppose that sandfly population reaches stability and oscillations decrease over time. Thus, note that for $t \to +\infty$ we have $m_h(t)$ trending to $m_{h0}$.

### 5. Modeling the Dynamic of Control Strategies

System (1) models the disease dynamics over time, considering humans, dogs, and sandfly population. In order to evaluate the effect of preventive controls, we have to introduce new terms that indicate each of those methods. Since our focus is preventive control method, the target populations are dogs and sandflies.

In the following sections we present the inclusion of those new terms on system (1). We consider the parameters from Araçatuba municipality for simulation of those methods.

Each of the five control strategies considered in this work acts in a specific point of the ZVL dynamics. Because of this, it becomes clearer if we redriecte our model for each strategy separately. Therefore, we simulated 6 sceneries (one without control strategies and one for each strategy) and, for each evaluated strategy, we counted the number of individuals (dog or houses) that were controlled. The estimation of control strategy rates is presented apart in the following sections.

#### 5.1. Elimination of Positive Dogs

$$\dot{x}_d(t) = \left( \mu_d + \xi_d + \xi'_d \right) \left( l_d(t) + y_d(t) + z_d(t) \right)$$

$$+ r_d l_d(t) + \alpha_d y_d(t) + \gamma_d z_d(t)$$

$$- b_d a_d m_d(t) s(t) x_d(t)$$

$$\dot{l}_d(t) = (b_d m_d(t) s(t)) x_d(t)$$

$$- \left( \mu_d + r_d + \delta_d + \varphi_d + \xi_d + \xi'_d \right) l_d(t)$$

$$\dot{y}_d(t) = \varphi_d l_d(t) - \left( \mu_d + \alpha_d + \sigma_d + \xi_d + \xi'_d \right) y_d(t)$$

$$\dot{z}_d(t) = \delta_d l_d(t) + \sigma_d y_d(t)$$

$$- \left( \mu_d + y_d + \xi_d + \xi'_d \right) z_d(t).$$  

(8)

The elimination of positive dogs has already been indicated as $\xi_d$ in system (1), in the equations for dog population, and in Table 1. In this case, we suppose that this elimination rate is in accordance with the average produced by epidemiological surveillance system of Araçatuba [31]. In other words, $\xi_d$ means the usual dog elimination rate (i.e., the dog elimination provided by health authorities in a common routine). In addition, since the official diagnosis method is serology, we assume any dog that is indicated as having antibody against *Leishmania* parasite as disease positive.

Note from Figure 1 that dog population is considered constant in our model. As a result, if the dog mortality is intensified due to elimination of positive ones (i.e., there is an extra/additional elimination rate by $\xi'_d$, e.g., if the health services receive better working conditions and if they are supplied by more materials), it induces an increase of dog population renewing. This renewing makes sense, since, ecologically, an eliminated dog allows a new one to replace it. In addition, as the official diagnostic techniques are based on serology, only susceptible dogs $x_d$ are not eligible to be eliminated. We adopted this idea because we considered the latent ($l_d$), clinically ill ($y_d$), and recovering ($z_d$) dogs had contracted the *Leishmania* antigen in any moment of its life. Therefore, they are eligible to be positive for diagnostic test.

#### 5.2. Deltamethrin 4% Impregnated Dog Collar

Theoretically, the deltamethrin 4% impregnated dog collar could be applied in any dog. Therefore, we can assume that all of the four classes of dog in our model are eligible to use it and we adopted $\theta_d$ as the rate of dogs using collar per day. In this case, we indicated by $C$ the categories of dogs that use collar (susceptible dogs using collar $x^C_d$, latent dogs using collar $l^C_d$, clinically ill dogs using collar $y^C_d$, and recovering dogs using collar $z^C_d$) from those that do not use it. Basically, once a dog has this collar, it becomes protected from sandfly biting. If there is no contact between them, there will not be parasite transmission (either from infected dog to noninfected sandfly or from infective sandfly to susceptible dog).

Also, let us assume that those collars are available for inhabitants at local health centers. Thus, we suppose that owners would actively go to health center and acquire the collar for each dog they have. Since we consider that all preventive activities are supported by health policies, we can consider that the owner acquires the collar with no charge. If we imagine this simple hypothesis, we conclude that the only additional cost to the health policies is the purchasing of the collar.

Figure 2 refers to the flowchart considering the inclusion of deltamethrin 4% impregnated dog collar. Next, we have system (9), in which we included the collar-classes, and Table 5 where we describe the additional parameters for this control.
Note from Figure 2 that once the collar is fitted, there is a loss rate $\xi_d$ and a decrease of insecticide effect rate $u_c$. Also, according to Halbig et al. [42], the efficacy of the collar is around 80%. Therefore, we considered that a proportion $\varepsilon_c$ of those dogs using collar is protected.

$$\dot{x}_d(t) = B(t) + (u_c + \zeta_c)x_d^C(t) + r_d x_d(t) + y_d x_d(t) - (\theta_d + b_d \alpha_d m_d s_d(t) x_d(t)$$

$$\dot{y}_d(t) = (u_c + \zeta_c) y_d^C(t) + b_d \alpha_d m_d s_d(t) x_d(t) - (\mu_d + r_d + \delta_d + \varphi_d + \xi_d + \theta_d) y_d(t)$$

Note from Figure 2 that once the collar is fitted, there is a loss rate $\xi_c$ and a decrease of insecticide effect rate $u_c$. Also, according to Halbig et al. [42], the efficacy of the collar is around 80%. Therefore, we considered that a proportion $\varepsilon_c$ of those dogs using collar is protected.

$$\dot{x}_d(t) = B(t) + (u_c + \zeta_c)x_d^C(t) + r_d x_d(t) + y_d x_d(t) - (\theta_d + b_d \alpha_d m_d s_d(t) x_d(t)$$

$$\dot{y}_d(t) = (u_c + \zeta_c) y_d^C(t) + b_d \alpha_d m_d s_d(t) x_d(t) - (\mu_d + r_d + \delta_d + \varphi_d + \xi_d + \theta_d) y_d(t)$$
\[ \dot{z}_d (t) \]
\[ = (u_c + \zeta_c) z_C^c (t) + \delta_d l_d (t) + \sigma_d y_d (t) \]
\[ - (\mu_d + \gamma_d + \xi_d + \theta_d) z_d (t) \]
\[ B (t) \]
\[ = \mu_d \left( 1 - x_d (t) \right) + \xi_d \left( 1 - x_d (t) - x^C_d (t) \right) \]
\[ + \alpha_d \left( y_d (t) + y^C_d (t) \right) \]
\[ x^C_d (t) \]
\[ = \theta_d x_d (t) \]
\[ - (\mu_d + \gamma_d + \xi_d + \zeta_c + u_c + \zeta_c) x^C_d (t) \]
\[ + r \dot{d} C (t) + y_d z^C_d (t) \]
\[ \dot{y}^C_d (t) \]
\[ = \theta_d y_d (t) + \varphi_d \dot{C} (t) \]
\[ - (\mu_d + \alpha_d + \sigma_d + \zeta_c + u_c + \zeta_c) y^C_d (t) \]
\[ \dot{\xi}^C_d (t) \]
\[ = \theta_d \dot{z}_d (t) + \delta_d \xi^C_d (t) + \sigma_d y^C_d (t) \]
\[ - (\mu_d + r_d + \delta_d + \varphi_d + \xi_d + u_c + \zeta_c) \xi^C_d (t) \]
\[ s_1 (t) = \mu_d (s_2 (t) + s_3 (t)) - a_1 \left( I_d (t) + I^C_d (t) \right) s_1 (t) \]
\[ s_2 (t) \]
\[ = a_s \left( I_d (t) + I^C_d (t) \right) s_1 (t) - \mu_d s_2 (t) \]
\[ - a_s \left( I_d (t) - \tau + I^C_d (t) - \tau \right) s_1 (t - \tau) e^{-\mu_d \tau} \]
\[ s_3 (t) \]
\[ = a_s \left( I_d (t) + I^C_d (t) \right) s_1 (t - \tau) - \mu_d s_3 (t) \]
\[ I_d (t) = c_l l_d (t) + c_r y_d (t) \]
\[ I^C_d (t) = \left( 1 - u_c \right) \left( c_l^c l_d (t) + c_r y^C_d (t) \right) . \]

5.3. Dog Vaccination. Biologically, the vaccination would be effective only in susceptible dogs \( x_d \), avoiding them to become infected by infective sandfly bites. Thus, if the vaccine distribution was only for susceptible dogs, it would be necessary to submit several dogs to diagnostic procedure. However, in practical terms, this is not feasible. Therefore, we suppose that all dogs are eligible to be vaccinated and this category of vaccinated dogs is indicated by \( v_d \).

In our model, we considered that leishmaniasis vaccination would be offered together with rabies vaccine. In other words, we suppose that the rabies vaccination campaign would distribute not only rabies vaccines but also leishmaniasis vaccine. Since the rabies vaccination campaign has been already included in the annual municipality budget, the minimum additional cost to operation of vaccination as control strategy would be only the leishmaniasis vaccine purchasing. This is an idea similar to the one adopted to dog collar. However, in this model we are considering only the leishmaniasis vaccination rate \( v_d \) (lowercase “ipsilon”) and its respective impact as control activity.

Figure 3 refers to the flowchart considering the inclusion of leishmaniasis vaccination. Next, we have system (10), in which we included the vaccinated dog compartment, and Table 6 where we describe the additional parameters for this control.

Note from Figure 3 that once the dog is vaccinated, there is a loss of immunity rate \( p_c \) [43]. Also, according to Fernandes et al. [44], the efficacy of leishmaniasis vaccination is around 96.4%. Therefore, we considered that a proportion \( e_v \) of these vaccinated dogs against leishmaniasis is immunized.

\[ x_d (t) = B (t) + r_d l_d (t) + y_d z_d (t) + p x_d (t) \]
\[ - (b_l a_d m_d s_3 (t)) x^C_d (t) \]
\[ y^C_d (t) \]
\[ = \theta_d y_d (t) + \varphi_d \dot{C} (t) \]
\[ - (\mu_d + \alpha_d + \sigma_d + \zeta_c + u_c + \zeta_c) y^C_d (t) \]
\[ \dot{z}^C_d (t) \]
\[ = \theta_d \dot{z}_d (t) + \delta_d \dot{C}^C (t) + \sigma_d y^C_d (t) \]
\[ - (\mu_d + r_d + \delta_d + \varphi_d + \xi_d + u_c + \zeta_c) z^C_d (t) \]
\[ s_1 (t) = \mu_d (s_2 (t) + s_3 (t)) - a_1 \left( I_d (t) + I^C_d (t) \right) s_1 (t) \]
\[ s_2 (t) \]
\[ = a_s \left( I_d (t) + I^C_d (t) \right) s_1 (t) - \mu_d s_2 (t) \]
\[ - a_s \left( I_d (t) - \tau + I^C_d (t) - \tau \right) s_1 (t - \tau) e^{-\mu_d \tau} \]
\[ s_3 (t) \]
\[ = a_s \left( I_d (t) + I^C_d (t) \right) s_1 (t - \tau) - \mu_d s_3 (t) \]
\[ I_d (t) = c_l l_d (t) + c_r y_d (t) \]
\[ I^C_d (t) = \left( 1 - u_c \right) \left( c_l^c l_d (t) + c_r y^C_d (t) \right) . \]

5.4. Dog Treatment. In this control strategy, the objective is reducing the number of infected dogs, which works as source of infection. However, the probability of treating a latent dog is quite null, since this category of dog is visually healthy. Thus, we assume that only dogs that present clinical signs and/or symptoms are eligible to be treated and the dog treatment rate is indicated as \( \omega_j \).

We will consider the treatment protocol described by Miró et al. [45], which was composed by meglumine antimoniate plus allopurinol. In this work, the authors found a proportion of dogs that healed but still continued to be infected. In other words, once a dog is treated, there is a probability of a dog eliminating the parasitemia or not.

Furthermore, we also consider that the dog treatment would be offered by public health policies. Therefore, if the public health services have already included veterinarians
in the staff, the minimum additional cost would be the acquisition of the medicine (meglumine antimoniate and allopurinol) and hospital material (e.g., syringes and needles).

Figure 4 refers to the flowchart considering the inclusion of dog treatment. Then, we have system (11), in which we included the treated dogs flux (from clinically ill to susceptible or to latent), and Table 7 where we describe the additional parameters for this control.

Note from Figure 4 that once the dog is treated, there is a probability to be recovered, but without parasitemia elimination. We adopt $c_k$ as a proportion of dogs that obtain only clinical recovery but are still infected [45]. Also, once the treatment started, we assumed that any dog gives up on the treatment process over time (i.e., the proportion of dogs that receive the complete treatment is $\psi_d = 1$).

$$
\dot{x}_a(t) = B(t) + (1 - c_k) \psi_d \omega_d y_d(t) + r_d I_d(t) + y_d z_d(t)
$$

$$
\dot{y}_d(t) = c_k \psi_d \omega_d y_d(t) + b_d \omega_d m_d(t) s_3(t) x_d(t)
$$

$$
\dot{z}_d(t) = \beta_d \omega_d m_d(t) s_3(t) x_d(t) - (\mu_d + \delta_d + \psi_d + \xi_d) I_d(t)
$$

$$
\dot{y}_d(t) = \psi_d \omega_d(t) - (\mu_d + \alpha_d + \sigma_d + \xi_d + \psi_d \omega_d) y_d(t)
$$
5.5. Sandfly Population Control. The activities of sandfly population control focus on two approaches, both of them on the environment. First, according to Brazilian Ministry of Health [17], the sandfly population control includes a chemical control (spraying of insecticide on the houses) and a land clearing (that reduces the sandfly carry capacity). In order to simplify our study, we just considered that those both approaches included in the sandfly population control result in an increase of sandfly mortality rate, $\xi$. On the other hand, it is unfeasible to organize a sandfly control considering the sandfly mortality rate, as “eliminated sandfly/day” (i.e., working in function of the amount $\xi \times S$). Because of this, we considered as sandfly control rate the dimension of “treated houses/(sandfly x day)”: $\epsilon$. Therefore, once the number of treated houses to be treated per day and per sandfly is determined, we can easily find the additional sandfly mortality rate:

$$\epsilon = \xi \times w_{hc} \times m_{ho}.$$  

(12)

where $w_{hc}$ means the average human/house and $m_{ho}$ is the ratio sandfly/human.

It would be very complex to estimate the sandfly population control budget, but for this model we considered the economical evaluation presented by Camargo-Neves [31] (Table 8).

Figure 5 refers to the flowchart considering the inclusion of sandfly population control. Then, we have system (13), in which we presented the additional sandfly mortality rate $\epsilon = \xi \times w_{hc} \times m_{ho}$.

In a proportional approach, note from Figure 5 that sandfly population is considered constant in our model (we remember that our three populations in our model are normalized). As a result, the proportional increase of its mortality rate induces an increase of population renewing at the same proportion. This acceleration of population renewing refers to the conception of carry capacity. Here, carry capacity means the maximum population size of biological species in an environment. Thus, whenever the sandfly population is under the carry capacity, it will tend to increase until it becomes fitted to it. Also, the opposite occurs if it is over the carry capacity (the population will decrease until its size fits the carry capacity). Finally, as our model considers the sandfly population proportionally constant, it means that when sandflies die, the population will decrease and it will be under the maximum size allowed by carry capacity. As a consequence, the population will increase by recruitment of new individuals (mathematically, this is the entrance term $\mu_h (S_2(t) + S_3(t))$). Therefore, in short, we conclude that if the sandfly mortality rate increases, the sandfly population renewing rate will also increase.

According to Burattini et al. [10], the acceleration of the sandfly population renewing (or, in other words, the decrease of life expectancy of sandfly population) affects directly the LVZ dynamics, since the infected sandfly $S_2$ is also eliminated in a shorter time. As a consequence, the parasite Leishmania $S_3$ will not have time enough to complete its development inside the sandfly and the proportion of infective $S_3$ will also naturally decrease.

$$s_1(t) = (\mu + \xi \times w_{hc} \times m_{ho}) (s_2(t) + s_3(t))$$

$$s_2(t) = a_s I_d (t - \tau) s_1(t) \left( -\mu + \xi \times w_{hc} \times m_{ho} \right) s_3(t)$$

$$s_3(t) = a_s I_d (t - \tau) s_1(t - \tau) e^{-(\mu_s + \xi \times w_{hc} \times m_{ho}) \tau}$$
Table 2: Parameters adopted in our model. The indexes $h$, $d$, and $s$ stand for humans, dogs, and sandflies, respectively (continuation of Table 1).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
<th>Value</th>
<th>Dimension</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta_d$</td>
<td>Latent recovery rate</td>
<td>$8.22 \times 10^{-3}$</td>
<td>1/day</td>
<td>Neve and Sacks [32]</td>
</tr>
<tr>
<td>$\xi_d$</td>
<td>Dog elimination rate</td>
<td>$3.36 \times 10^{-4}$</td>
<td>1/day</td>
<td>Camargo-Neves [31]</td>
</tr>
<tr>
<td>$\mu_s$</td>
<td>Natural mortality rate</td>
<td>$5.00 \times 10^{-2}$</td>
<td>1/day</td>
<td>Ministry of Health, Brazil [17]</td>
</tr>
<tr>
<td>$\tau$</td>
<td>Extrinsic incubation period</td>
<td>$7$</td>
<td>Day</td>
<td>Estimated as Epidemiological Surveillance Direction, Santa Catarina State, Brazil [21]</td>
</tr>
<tr>
<td>$a_d$</td>
<td>Average daily biting rate (on dogs)</td>
<td>$2.00 \times 10^{-1}$</td>
<td>1/day</td>
<td>Estimated as Epidemiological Surveillance Direction, Santa Catarina State, Brazil [21]</td>
</tr>
<tr>
<td>$c_l$</td>
<td>Probability of latent dog to infect the sandfly</td>
<td>0.385</td>
<td>Dimensionless</td>
<td>Laurenti et al. [33]</td>
</tr>
<tr>
<td>$c_y$</td>
<td>Probability of clinically ill dog to infect the sandfly</td>
<td>0.247</td>
<td>Dimensionless</td>
<td>Laurenti et al. [33]</td>
</tr>
</tbody>
</table>

\[
s'_d(t) = a_s L_h(t - \tau) s_1 (t - \tau) e^{-(\mu_s + \xi_d w_h) m_h(t)}
- (\mu_s + \xi_d w_h m_h(t)) s_3 (t)
L_d(t) = c_1 I_d(t) + c_y y_d(t).
\]

(13)

6. The Estimated Costs and Calculation of Control Strategy Rates

It is very important to consider not only the result of the control strategy at the light of epidemiological approach but also the economical one too. Therefore, since the number of controlled elements is in dimension of elements/day, the estimation of the cost/elements would provide us with the estimated cost per day (i.e., cost/individual × individual/day = cost/day). Here we suppressed the cost calculation of each method, but we indicated the references from where we preceded our estimations. Table 8 summarizes those costs.

Usually, the operating of preventive control strategies is limited by logistic and financial resources. Therefore, in order to estimate the preventive control rates, firstly it is necessary to estimate those restrictions.

First, considering the data from Table 8. From "Human reported cases per year" column we estimated the year average, which is 20.18 human cases/year. Then, from Table 8, the estimated cost for human treatment is around 397.25 USD/human [46]. Therefore, per year, the average expenses with human treatment are around 20.18 × 397.25 = 8015 USD/year. If we consider the costs per day, we have around 22 USD/day. For simplicity, we will consider that this value includes not only financial aspects but also logistic one.

Now, let’s suppose that instead of this 22 USD/day that is invested on preventive treatments, it would be invested on preventive control strategies. However, we should consider that this 22 USD/day is invested on the prevention of the whole dog population or houses. If we consider the human : dog ratio for Araçatuba/SP city of 10/1.8 human/dog [29] and the human : house ratio of 3 humans/house [22], the estimation of dog population and the number of houses for 2016 is around 34889 dogs and 64609 houses. Then, the invested cost per dog is estimated as 22/34889 = 6.29 × 10^{-4} USD/(dog × day) and, considering houses, 22/64609 = 3.40 × 10^{-5} USD/(house × day). Since we obtained the estimated costs for each control strategy (Table 8), it is possible to estimate the maximum rate of each control. As example, if the cost for elimination of one positive dogs is 170.71 USD/dog, the maximum rate of elimination dog per day would be 6.29 × 10^{-4}/170.71 = 3.69 × 10^{-6}/day. In the same way, we just repeated the calculation process and estimated the maximum rate of each control strategy, but in the case of vector control we used the estimated number of houses instead of estimated dog population. All estimated control rates are in Table 8.

It is important to present a special consideration about $\xi_c$ dimension. According to (12), $\xi_c$ dimension is "houses/(sandfly × day)." Since the dimension of estimated investment cost per house is "USD/(house × day)," we concluded that the cost estimated of sandfly population control presents the dimension "USD × sandfly/house." This dimension can be splitted as "(USD/house) × (sandfly/house)." Thus, we can observe that the cost of sandfly population control depends on density sandfly/house. The higher this density sandfly/house is, the more expensive the cost becomes. Therefore, we considered the sandfly population control average cost as 23.24 USD × sandfly/(house)^2.

7. The Impact of Control Strategies on Total of Saved Humans

According to Table 2, we accessed official data of Araçatuba municipality from 1999 to 2015. Later, from those data, we were able to fit the model from system (1) by observing the resulting curve from reported human cases in (4) from fitting $m_h(t)$ in (7).

Once we have the model from system (1) defined and calibrated, we are able to evaluate the dynamics of each control strategy and compare them with the no-control strategy scenery.

First, we considered the numerical simulation of system (1) from 1999 to 2025. Since we are interested in understanding the dynamics of the disease over time in an as real as possible behavior, we present Figure 6 with bars
Table 3: Human and dog demographic data from Araçatuba municipality and estimated human reported cases.

<table>
<thead>
<tr>
<th>Year</th>
<th>Human reported cases per year (CES-SP) [36]</th>
<th>Aracatuba’s human population size (BIGS) [22]</th>
<th>Average of normalized human reported cases per day</th>
<th>Estimated dog population according to Andrade et al. [29]</th>
<th>Estimated number of houses (BIGS) [22]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1999</td>
<td>15</td>
<td>169303</td>
<td>$2.43 \times 10^{-7}$</td>
<td>30475</td>
<td>56434</td>
</tr>
<tr>
<td>2000</td>
<td>12</td>
<td>170296</td>
<td>$1.93 \times 10^{-7}$</td>
<td>30653</td>
<td>56765</td>
</tr>
<tr>
<td>2001</td>
<td>29</td>
<td>171289</td>
<td>$4.64 \times 10^{-7}$</td>
<td>30832</td>
<td>57096</td>
</tr>
<tr>
<td>2002</td>
<td>52</td>
<td>172768</td>
<td>$8.25 \times 10^{-7}$</td>
<td>31098</td>
<td>57589</td>
</tr>
<tr>
<td>2003</td>
<td>40</td>
<td>174399</td>
<td>$6.28 \times 10^{-7}$</td>
<td>31392</td>
<td>58133</td>
</tr>
<tr>
<td>2004</td>
<td>41</td>
<td>177823</td>
<td>$6.32 \times 10^{-7}$</td>
<td>32008</td>
<td>59274</td>
</tr>
<tr>
<td>2005</td>
<td>16</td>
<td>179717</td>
<td>$2.44 \times 10^{-7}$</td>
<td>32349</td>
<td>59906</td>
</tr>
<tr>
<td>2006</td>
<td>20</td>
<td>181598</td>
<td>$3.02 \times 10^{-7}$</td>
<td>32688</td>
<td>60533</td>
</tr>
<tr>
<td>2007</td>
<td>42</td>
<td>181371</td>
<td>$6.34 \times 10^{-7}$</td>
<td>32647</td>
<td>60457</td>
</tr>
<tr>
<td>2008</td>
<td>27</td>
<td>181143</td>
<td>$4.08 \times 10^{-7}$</td>
<td>32606</td>
<td>60381</td>
</tr>
<tr>
<td>2009</td>
<td>15</td>
<td>182204</td>
<td>$2.26 \times 10^{-7}$</td>
<td>32797</td>
<td>60735</td>
</tr>
<tr>
<td>2010</td>
<td>4</td>
<td>182365</td>
<td>$6.01 \times 10^{-8}$</td>
<td>32826</td>
<td>60788</td>
</tr>
<tr>
<td>2011</td>
<td>5</td>
<td>182526</td>
<td>$7.51 \times 10^{-8}$</td>
<td>32855</td>
<td>60842</td>
</tr>
<tr>
<td>2012</td>
<td>6</td>
<td>183441</td>
<td>$8.96 \times 10^{-8}$</td>
<td>33019</td>
<td>61147</td>
</tr>
<tr>
<td>2013</td>
<td>3</td>
<td>190536</td>
<td>$4.31 \times 10^{-8}$</td>
<td>34296</td>
<td>63512</td>
</tr>
<tr>
<td>2014</td>
<td>12</td>
<td>191662</td>
<td>$1.72 \times 10^{-7}$</td>
<td>34499</td>
<td>63887</td>
</tr>
<tr>
<td>2015</td>
<td>4</td>
<td>192757</td>
<td>$5.69 \times 10^{-8}$</td>
<td>34696</td>
<td>64252</td>
</tr>
</tbody>
</table>

Table 4: Parameter values for (7) and their biological meaning.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
<th>Value</th>
<th>Dimension</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>$m_{h0}$</td>
<td>Vector density per host (baseline value)</td>
<td>0.75</td>
<td>Sandfly/human</td>
<td>Fitted</td>
</tr>
<tr>
<td>$A$</td>
<td>Vector density per host</td>
<td>3.4</td>
<td>Sandfly/human</td>
<td>Fitted</td>
</tr>
<tr>
<td>$B$</td>
<td>Vector density per host</td>
<td>8.3</td>
<td>Sandfly/human</td>
<td>Fitted</td>
</tr>
<tr>
<td>$L$</td>
<td>Linear constant</td>
<td>3.0</td>
<td>Dimensionless</td>
<td>Fitted</td>
</tr>
<tr>
<td>$K_1$</td>
<td>Proportionality constant</td>
<td>$3.5 \times 365$</td>
<td>Day</td>
<td>Fitted</td>
</tr>
<tr>
<td>$T$</td>
<td>Sandfly population dynamics period</td>
<td>$5.5 \times 365$</td>
<td>Day</td>
<td>Fitted</td>
</tr>
</tbody>
</table>

Table 5: Additional parameters adopted for evaluation of deltamethrin 4% impregnated dog collar.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
<th>Value</th>
<th>Dimension</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta_d$</td>
<td>Rate of dogs using collar</td>
<td>Variable</td>
<td>1/day</td>
<td>—</td>
</tr>
<tr>
<td>$u_c$</td>
<td>Inverse of activity period of collar</td>
<td>$6.70 \times 10^{-3}$</td>
<td>1/day</td>
<td>Scalibor® [40]</td>
</tr>
<tr>
<td>$\xi_c$</td>
<td>Loss of insecticide impregnated collar</td>
<td>$6.00 \times 10^{-3}$</td>
<td>1/day</td>
<td>Reithinger et al. [41]</td>
</tr>
<tr>
<td>$\varepsilon_c$</td>
<td>Decrease of biting rate due to insecticide impregnated collar</td>
<td>$8.00 \times 10^{-1}$</td>
<td>Dimensionless</td>
<td>Halbig et al. [42]</td>
</tr>
</tbody>
</table>

Table 6: Additional parameters adopted for evaluation of dog vaccination.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
<th>Value</th>
<th>Dimension</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\nu_d$</td>
<td>Leishmaniasis vaccination rate</td>
<td>Variable</td>
<td>1/day</td>
<td>—</td>
</tr>
<tr>
<td>$P_d$</td>
<td>Loss of immunity rate (Leishmune® vaccination)</td>
<td>$2.74 \times 10^{-3}$</td>
<td>1/day</td>
<td>Moreira [43]</td>
</tr>
<tr>
<td>$\varepsilon_v$</td>
<td>Efficacy of ZVL vaccination</td>
<td>0.964</td>
<td>Dimensionless</td>
<td>Fernandes et al. [44]</td>
</tr>
</tbody>
</table>
Table 7: Additional parameters adopted for evaluation of dog treatment.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Meaning</th>
<th>Value</th>
<th>Dimension</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \omega_d )</td>
<td>Dog treatment rate</td>
<td>Variable</td>
<td>1/day</td>
<td>—</td>
</tr>
<tr>
<td>( c_k )</td>
<td>Proportion of clinically recovered dogs but that are still infected</td>
<td>0.154</td>
<td>Dimensionless</td>
<td>Miró et al. [45]</td>
</tr>
<tr>
<td>( \psi_d )</td>
<td>Proportion of dogs that receive the complete treatment</td>
<td>1</td>
<td>Dimensionless</td>
<td>Assumed</td>
</tr>
</tbody>
</table>

Figure 6: Total disease dynamics and plotting of official data over time. The control strategies were supposed to be introduced from 2018. Observe that the prediction of reported human cases from 2018 for each control strategy is quite close and, therefore, in this scale the curves are overlapped (see Figure 7 for a larger scale).

that indicate the official data. However, considering the prediction evaluation of the control strategies, we assumed in our simulation that those control strategies would start to be operated in 2018. Therefore, we observe in Figure 6 the numerical simulation and the prediction result if we consider the introduction of those strategies starting from 2018 (for a better view, see Figure 7).

Once we observed the control strategy dynamics in terms of reported human cases, it is very useful to estimate the quantity of people that avoided the infection. Just for simplification, in this text we refer to those people as “saved” human.

Since we developed a computational simulation, we had the control of sceneries. Therefore, in order to evaluate the impact of each control strategy, we compared the simulation results between introduced control strategy and no-control simulations. It is important to remember that in all simulations we computed the real total of clinically ill humans, according to (14). However, if we calculate the difference between the no-control simulation and introduced control simulation, we have the quantity of humans that were prevented to become clinically ill (the saved one).

\[
\mathcal{T}^i_{\text{saved}} = T^i_{\text{no-control}} (t_f) - T^i_{\psi_h} (t_f) = \phi_h \int_{t_0}^{t_f} (l^i_{\text{no-control}} (t) - l^i_h (t)) \, dt,
\]  

where \( \mathcal{T}^i_{\text{saved}} \) is the total of saved humans until time \( t_f \) and \( i \) is the correspondent control strategy. Figure 8 represents the result of those totals of saved humans for each control strategy.

According to Figure 8, the dog treatment was the strategy that presented the lower number of saved people. It makes some sense, since the dog treatment does not eliminate the parasitemia status. Therefore even if an infected dog is treated, it may still continue being source of infection. On the other hand, the insecticide impregnated dog collar and dog vaccination were the strategies that most saved
<table>
<thead>
<tr>
<th>Meaning</th>
<th>Cost</th>
<th>Cost dimension</th>
<th>Source</th>
<th>Normalized cost (in terms of patient cost)</th>
<th>Normalized cost dimension</th>
<th>Control rate</th>
<th>Control rate dimension</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\xi'$ Elimination of positive dog</td>
<td>170.71 USD/dog</td>
<td>Estimated as Camargo-Neves [31]</td>
<td>0.43 Patient/dog</td>
<td>$3.69 \times 10^{-6}$ 1/day</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\theta_d$ Deltamethrin 4% impregnated dog collar</td>
<td>12.00 USD/dog</td>
<td>Estimated as Camargo-Neves et al. [47]</td>
<td>0.03 Patient/dog</td>
<td>$5.25 \times 10^{-5}$ 1/day</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\omega_d$ Dog treatment with allopurinol and meglumine antimoniate</td>
<td>265.76 USD/dog</td>
<td>Estimated as Miró et al. [45]</td>
<td>0.67 Patient/dog</td>
<td>$2.37 \times 10^{-6}$ 1/day</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\nu_d$ Vaccine</td>
<td>33.00 USD/dog</td>
<td>F. E Gonzales (Personel communication, 2016)</td>
<td>0.08 Patient/dog</td>
<td>$1.91 \times 10^{-5}$ 1/day</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\xi_c$ Sandfly population control</td>
<td>23.24 USD $\times$ sandfly/(house)$^2$</td>
<td>Estimated as Camargo-Neves [31]</td>
<td>0.06 Patient $\times$ sandfly/(house)$^2$</td>
<td>$1.46 \times 10^{-5}$ House/(sandfly $\times$ day)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Human patient treatment</td>
<td>397.25 USD/patient</td>
<td>Estimated as Akhavan [46]</td>
<td>1.00 Patient/patient</td>
<td>—</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Table 8:** Summary of average costs for strategy controls and for human patient treatment.
Figure 7: Disease dynamics considering the introduction of control strategies. Here we present a larger scale of the vertical and horizontal axis in order to provide a better observation of the curves. Note that the insecticide impregnated dog collar is the strategy that generates lower reducing of reported human cases. On the other hand, the dog treatment curve is overlapped with the no-control curve. Therefore, it is the strategy that presented the worst result in terms of reported human cases reduction.

Figure 8: Total of saved humans over time, according to each strategy. Observe that using of deltamethrin impregnated collar and vaccination were the strategies which saved more humans. On the other hand, the dog treatment saved around hundred times fewer individuals, if compared to those two best strategies. Since those curves exponentially grow up, we used a log-scale in vertical axis.

Humans. Those two strategies reduce the amount of exposed susceptible individuals to infective sandfly biting. As a consequence, the proportion of infected humans decreases. However, although this interpretation is correct, we did not consider the restriction of resources, as financial, material, or human support. In the next section, we will include our observations about this.

8. Number of Controlled Elements and the Estimation of Total Cost

According to Table 8, each control strategy has a cost per controlled element (dog or house). Therefore, it is essential to understand how to find the equilibrium between the disease control and the available resources (material and/or financial).

In general idea, to count the controlled elements it is necessary to sum the amount of controlled elements per day over an interval of time: total of controlled elements = controlled elements/day × interval of time (days).

From total of controlled elements it is simple to estimate the invested total. Here, we are interested to compare the cost of the control strategies with the cost of human treatment. Therefore, if the cost of each strategy per element has already been normalized in terms of the human treatment cost, we are able to estimate the total cost as total cost = total of
Table 9: Summary of the expressions for total of controlled elements and for total cost. The initial values of the time interval and the ending are represented by $t_0$ and $t_f$, respectively. $N_d = 34889$ is the estimated dog population and $H = 64609$ is the estimated total of houses, both for Aracatu municipality in 2016.

<table>
<thead>
<tr>
<th>Meaning</th>
<th>Total of controlled elements $(T_i)$</th>
<th>Normalized cost* $(C_i)$</th>
<th>Normalized cost dimension</th>
<th>Total cost* $(C_i)^\dagger$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\xi'_d$ Elimination of positive dog</td>
<td>$N_d \int_{t_0}^{t_f} (l_d(t) + y_d(t) + z_d(t)) , dt$</td>
<td>0.43</td>
<td>Patient/dog</td>
<td>$T_{\xi'<em>d} \times \mathcal{C}</em>{\xi'_d}$</td>
</tr>
<tr>
<td>$\theta'_d$ Deltamethrin 4% impregnated dog collar</td>
<td>$N_d \theta'<em>d \int</em>{t_0}^{t_f} (x_d(t) + l_d(t) + y_d(t) + z_d(t)) , dt$</td>
<td>0.03</td>
<td>Patient/dog</td>
<td>$T_{\theta'<em>d} \times \mathcal{C}</em>{\theta'_d}$</td>
</tr>
<tr>
<td>$\omega'_d$ Dog treatment with allopurinol and meglumine antimonialie</td>
<td>$N_d \omega'<em>d \int</em>{t_0}^{t_f} y_d(t) , dt$</td>
<td>0.67</td>
<td>Patient/dog</td>
<td>$T_{\omega'<em>d} \times \mathcal{C}</em>{\omega'_d}$</td>
</tr>
<tr>
<td>$v'_d$ Vaccine</td>
<td>$N_d v'<em>d \int</em>{t_0}^{t_f} (x_d(t) + l_d(t) + y_d(t) + z_d(t)) , dt$</td>
<td>0.08</td>
<td>Patient/dog</td>
<td>$T_{v'<em>d} \times \mathcal{C}</em>{v'_d}$</td>
</tr>
<tr>
<td>$\xi'_c$ Vector control</td>
<td>$H \xi'<em>c \int</em>{t_0}^{t_f} dt$</td>
<td>0.06</td>
<td>Patient/house</td>
<td>$T_{\xi'<em>c} \times \mathcal{C}</em>{\xi'_c}$</td>
</tr>
</tbody>
</table>

* In terms of patient cost.

† The index $i$ stands for the respective control strategy.

Figure 9: Total of controlled individuals (dogs or houses) over time, according to each strategy. Note that the dynamics of total number of treated houses for vector control and the number of vaccinated dogs are very similar. Since those curves exponentially grow up, we used a log-scale in vertical axis.

Figure 10: Total cost of each strategy over time, normalized by cost of human treatment. Note that three curves are overlapped: vector control, dog vaccination, and dog using deltamethrin impregnated collar. Since those curves exponentially grow up, we used a log-scale in vertical axis.

controlled elements $\times$ cost (normalized by human patient cost)/element.

Table 9 presents the expressions that calculate the total of controlled elements and the total cost of each strategy. Figures 9 and 10 present, respectively, the dynamics of total of controlled dogs or houses and the total cost normalized by human patient cost.

From Figures 9 and 10, it is possible to observe a similarity and correspondence between the curve responses. In terms of costs, vector control, dog vaccination, and dog collar are very close to each other. But, the difference is related to the number of controlled elements, in which we found that there were more dogs with collar than vaccinated dogs or treated houses. Also, although dog treatment and dog elimination presented reduced costs, they also controlled fewer elements too.

9. Calculation of $R_0$ as Function of Each Preventive Control and Evaluation of $R$ Dynamics

For each evaluation, we calculated the respective $R_0$ (Basic Reproduction Number) in function of the preventive control method. The Basic Reproduction Number indicates the quantity of infected individuals generated from one infective individual, when introduced in a population in disease-free equilibrium state [48]. We assumed that $R_0$ is calculated
Table 10: Summary of the expressions for total of controlled elements and for total cost. The initial values of the time interval and the ending are represented by $t_i$ and $t_f$, respectively. $N_d = 34889$ is the estimated dog population and $N_{houses} = 64609$ is the estimated total of houses, both for Araçatuba municipality in 2016.

<table>
<thead>
<tr>
<th>Meaning</th>
<th>$R_0$ expression</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\xi_d'$</td>
<td>Elimination of positive dog</td>
</tr>
<tr>
<td>$R_0 \xi_d' = \frac{w_{i,0}m_{i,0}a_{i}b_{i}e^{-r_{i}t}}{a_{i}a_{i}(1 + a_{i} + \theta_{d})} \times (P_1 + P_2)$,</td>
<td></td>
</tr>
<tr>
<td>$\theta_d$</td>
<td>Deltamethrin 4% impregnated dog collar</td>
</tr>
<tr>
<td>$\omega_d$</td>
<td>Dog treatment with allopurinol and meglumine antimoniate</td>
</tr>
<tr>
<td>$\nu_d$</td>
<td>Vaccine</td>
</tr>
<tr>
<td>$\xi_c$</td>
<td>Vector control</td>
</tr>
</tbody>
</table>

where $x(t)$ is the proportion of susceptible individuals in population. Theoretically, we have two host populations for your model: humans and dogs. From those two populations, we have three classes of susceptibles: $x_i(t)$, $x_d(t)$, and $(1 - \epsilon) x_i^c(t)$ (since the collar has a proportion of efficacy). Therefore, we estimated $R(t)$ as

$$R_d(t) = R_0 \times x_d(t) + (1 - \epsilon) x_i^c(t)$$

$$R_h(t) = R_0 \times x_h(t),$$

when the time $t$ is high enough, where $\lim_{t \to +\infty} m_{i,0}(t) = m_{i,0}$. As stated before, the full calculations are not described in this work, but we adopted the review published by van den Driesch and Watmough [38]. Once $R_0$ is calculated, we calculated the respective $R(t)$ (effective reproduction number) and investigated which one of the 5 control strategies (elimination of positive dogs $\xi_d$, use of deltamethrin 4% impregnated dog collar $\theta_d$, dog treatment with allopurinol and meglumine antimoniate $\omega_d$, dog vaccination $\nu_d$, and sandfly population control $\xi_c$) makes $R(t)$ converge fastest to a value lower than 1.

Table 10 summarizes the $R_0$ expressions for each control strategy.

The conception of $R_0$ is restricted on population's disease-free equilibrium state, since the mathematical approach that defines it considers the system in equilibrium states. Usually, a dynamic system has two classes of equilibrium states: a trivial and nontrivial state. If our dynamics system is a disease dynamics one, the trivial equilibrium is this disease-free equilibrium state and it is considering this equilibrium in which $R_0$ is calculated.

However, it is natural that there is generation of infected individuals immediately after the transmission has started. In this case, it is important to consider the susceptible individual dynamics. Therefore, the number of infected individuals generated from an infective one depends on the remaining susceptible individuals in the population:

$$R(t) = R_0 \times x(t),$$

$^*$Note that $R_0^{\epsilon_d}$ does not depend on $\nu_d$. 

Computational and Mathematical Methods in Medicine
In order to make a decision about which control strategy is the most efficient and cost-effective, a simple criterion was adopted. This criterion analyzed the amount of controlled individuals necessary to avoid one human to become clinically ill. In the same way, it is also possible to analyze how much the investment for each strategy to have one saved human is.

For each strategy we calculated the ratio total of controlled individuals/total of saved humans (17) and total cost/total of saved humans (18).

$$\mathcal{F}_i(t_f) = \frac{T_i(t_f)}{\mathcal{T}^{saved}_i(t_f)}, \quad (17)$$

where $\mathcal{F}_i$ means the ratio of total controlled individuals/total saved humans, $T_i$ is the total of controlled elements, $\mathcal{T}^{saved}_i$ means the total of saved humans, $i$ stands for the respective control strategy, and $t_f$ is the final time.

$$\mathcal{C}_i(t_f) = \mathcal{F}_i(t_f) \times \mathcal{C}_i, \quad (18)$$

where $\mathcal{C}_i$ is the cost of the strategy per individual.

Figures 13 and 14 present the result of those ratios over time.

From Figure 13, we observed that insecticide impregnated dog collar, dog vaccination, and sandfly population control were the strategies that require more elements to be controlled (in the case of collar or vaccination, we refer to dogs; in the case of sandfly population control, we refer to houses). In other words, those three strategies need to be applied in more individuals (or houses) in order to avoid one human being infected by LVZ. Our argument is based on the number needed to be treated (NNT) conception, which means how many individuals need to be controlled in order to avoid one infected individual.
strategy, if used isolated. Impregnated dog collar should be the first-choice control (control). Therefore, according to our model, the insecticide among those three (followed by dog vaccine and sandfly population as the less expensive strategy (per saved human) among those three strategies, we noted that the insecticide among the control strategies studied (Figure 14). However, strategies was also the one which required more investment from dog’s organism. Dog vaccination does not eliminate the treating the dog does not necessarily eliminate the parasite source of infection, but it protects the remaining susceptible dogs to become infected. Thus, there is the reduction of infected dog by natural elimination. The use of insecticide impregnated dog collar (if used by all dogs) works by protecting the susceptible ones (similar to the vaccine activity) and isolating the source of infection (similar to positive dog elimination). Finally, the sandfly population control aims at reducing the chance of disease transmission by intensifying the cycle of life of the mosquito. As a consequence, if the replacing of mosquito is accelerated, there is no time enough to mature the parasite inside the sandfly. In other words, the cycle of life of mosquito is not long enough to support the incubation period.

The comprehension of how each strategy works on the epidemiologic chain allows us to better understand the results of this study. For instance, since the dog treatment has shown a probability of parasitemia elimination around 84.6% [45], some clinically ill dogs would remain as source of infection; besides they become visually healthy. Since it is more probable for noninfected sandfly to acquire the parasite from a latent rather than a clinically ill dog [33], the dog treatment allows some dogs to remain as source of infection. From a public health point of view, this is epidemiologically undesirable, because there is the probability of increasing the proportion of latent dogs. This explains why the curve regarding dog treatment was considered the less efficient one and, in some cases, was overlapped with no-control curve.

On the other hand, we observed some differences among the impacts of control strategies on human and dog populations. All control strategies are applied on dog or sandfly population and, therefore, the impact on those populations reflects on human population. However, the consequences on human population are not immediate. This helps us to understand the fact that the impact on dog population is more intense and faster than on human population.

Although the consequences on each population are different, in both the use of insecticide impregnated dog collar presented the most positive impact in terms of disease control. This strategy not only reduces the frequency of contact between dogs and sandflies but also reduces the infective sandfly population. As a consequence, the probability of a susceptible human acquiring the infection is also decreased.

Following the insecticide impregnated dog collar, we found different strategies depending on the population. If we observe the dog population, dog vaccination presented a good result. Classically, the vaccination is well known as a preventive strategy, as it removes the susceptible individuals to a vaccinated category, in which it is immune to infection. But, if we analyze the human population, we found that sandfly population control and positive dog elimination were the strategies that presented good results. First, we have to remember that humans are not source of infection and, therefore, the objective for this population is to decrease the force of infection. The force of infection is mathematically defined as

\[ \lambda_i = b_i \times a_i \times m_i \times s_i(t) \]  

where \( i = h, d \). According to our results, to reduce the intensity of source of infection, it is necessary to control \( s_i(t) \). Basically, focusing on human population, the reduction of \( s_i(t) \) is most efficient if we consider the sandfly population control.
(as the sandfly life cycle becomes shorter) and positive dog elimination (we obtain the immediate elimination of source of infection). In the case of human population, dog vaccination presented a low impact, since the vaccination of dog does not immediately remove the infected dog. In this case, those dogs would be naturally eliminated and they would be able to continue playing as source of infection.

Our model provided us with those important results, but it is also necessary to consider real-world restrictions. Here we may simplify those restrictions explaining that they include economical, material, and human resources. Regarding visceral leishmaniasis, there are few works that economically evaluated the preventive control strategies [9]. There are studies that presented an economical analysis approaching treatment and diagnosis of human cases [9, 49, 50] and one of the conclusions pointed out was that investing on preventive activities is beneficially economical [49, 51, 52]. In our study, we not only elaborated a cost-effectiveness evaluation but also observed it dynamically. However, even though our study was based on simple analysis (e.g., we did not include disability adjusted life years or potentially productive years of life lost), our results are very important to fulfill a gap between epidemiological and economical analysis.

In our study, we estimated the total of saved humans and of controlled individuals (dogs or houses) over time and we found that insecticide impregnated dog collar, dog vaccination, and sandfly population control were the ones that saved more humans. On the other hand, they required more individuals to be controlled and, as a consequence, they required more investments too (Figures 9 and 10). Observing Figure 10, dog treatment was the less expensive strategy. If we strongly impose the financial resource as restriction (or if our priority is to save financial resources), we should choose treating dog as control strategy. However, we have already known that this strategy presented low effect to control this disease. Therefore, we need to find equilibrium between the control efficacy and cost-effectiveness.

Figure 10 pointed out that the sandfly population control, insecticide impregnated dog collar, and dog vaccination are the most expensive strategies, if we consider the total cost. This result can be biologically explained as follows. First, a dog lives for a time longer than a sandfly and the sandfly/dog ratio is higher than the sandfly/house ratio. Thus, if only sandfly population control operates as control strategy, we would have to keep sandfly elimination rate $\xi$ until the density of latent and clinically ill dogs reduction reflects on the reduction of reported human cases rate. In other words, while sandflies would be eliminated, it would also be necessary to wait for dog's natural death. This fact would result in continued remotion of sandflies, in which it would generate a fixed cost rate. Still, if the latent and clinically ill dogs are reduced by elimination, the impact on prevalence would be more intense, since the positive dog elimination is an immediate way to reduce source of infection. In the course of time, if the positive dog elimination is kept constant, the number of eliminated dogs tends to decrease. However, we should remember that sandfly population control may be an interesting option in terms of cost-effectiveness, depending on social and economical aspects of the area [52].

Although we have not found any economical study regarding dog vaccination, Lee et al. [53] presented an economical analysis for human vaccine. Although the authors considered some disease dynamics hypothesis different from the one from Brazil, it was demonstrated by computational simulations that vaccination can be cost-effective. However, more studies are necessary to understand the real impact of visceral leishmaniasis vaccination as control strategy [6, 44, 53].

In order to make a correct decision, we need to find a relationship between the total of investment on control strategy and the total of saved humans. From this relation, we can understand how expensive it was to prevent human from becoming clinically ill (see expression (18)). Observing Figure 13, we note that, in most of the simulated period, sandfly control population was the strategy that required more elements (houses) to be controlled per saved human. On the other hand, this is the opposite of dog treatment, in which we had fewer elements (dogs) to be treated per saved human. However, despite the fact that dog treatment required fewer elements per saved human, it also resulted in lowest impact among all considered strategies.

But if the controlled elements/saved human ratio is changed to control strategy cost/saved human ratio, we obtain a new approach. According to Figure 14, among those three most efficient strategies (insecticide impregnated dog collar, dog vaccination, and sandfly population control), the insecticide impregnated dog collar was the strategy that showed the best relation of epidemiological control with cost-effectiveness. This is in agreement with a field study developed by Camargo-Neves et al. [47] at Andradina municipality (São Paulo State, Brazil), in which the impacts of insecticide impregnated dog collar against sandfly population control were compared and it was found that the use of dog collar was economically more convenient. In this case, the dog collar is able to repel the sandfly, reducing the contact between dog and sandfly. Also, it avoids both the dog to become infected and the noninfected sandfly to acquire the parasite.

### 12. Conclusion

In this work, we presented an evaluation of ZVL control strategies, considering epidemiological control impact and cost-effectiveness as analysis criteria. Our results pointed out that focusing the control activities on source of infection and on sandfly population is the way to reach the optimal control and that is why insecticide impregnated dog collar was considered the most efficient and cost-effective among the control strategies. However, since human and dog populations play different roles in this epidemiological chain, choosing criteria on the best control strategy is different. Furthermore, as each control strategy works in different points of disease maintenance and transmission, there is the possibility of improving the disease control results by operating more than one strategy simultaneously. The combination of two or more control strategies is in our upcoming works.
Conflicts of Interest
The authors declare that they have no conflicts of interest.

Authors’ Contributions
Helio Junji Shimozako and Eduardo Massad were responsible for study design and planning. Helio Junji Shimozako and Jianhong Wu conducted the mathematical analysis. Helio Junji Shimozako conducted model simulations. Helio Junji Shimozako, Jianhong Wu, and Eduardo Massad contributed to results interpretation and discussion. Helio Junji Shimozako contributed to writing the manuscript. All authors read and approved the final version of the manuscript.

Acknowledgments
The authors would like to acknowledge all suggestions and considerations received from several research colleagues. Particularly, they thank Professor Dr. Eunice Aparecida Biachi Galati, Professor Dr. Dirce Maria T. Revisan Zanetta, Professor Dr. Marcelo Nascimento Burattini, Professor Dr. Maria Irma Seixas Duarte, and Professor Dr. Hiroshi Nishiura for important suggestions. They also acknowledge São Paulo Research Foundation (FAPESP) (Grants 2011/02633-5 and 2013/13347-9) and Mathematics of Information Technology and Complex Systems (MITACS) for partial financial support.

References