

## Research Article

# The Cooperation Partner Selection of Private Sector under Public-Private-Partnership Projects: An Improved Approach under Group Decision-Making Based on FRS, SAW, and Integrated Objective/Subjective Attributes

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With the intensification of market competition, the choice of partners in the private sector plays a vital role in the success or failure of the government's public sector in the bidding process. Based on FRS (factor risk scoring system), SAW (simple additive weighted), and the integrated subjective or objective fuzzy group decision-making methods, the private sector partner selection is carried out under the PPP (public-private partnership) model in this paper. First of all, a decision committee is established to select attributes and identify potential partners. Secondly, we determine the important decision of the consistency of the manufacturer, introduce linguistic variables, calculate and collect the fuzzy weighted personal attributes, evaluate the importance of the attributes, and get the comprehensive fuzzy evaluation. Thirdly, we establish fuzzy value matrix based on fuzzy evaluation and get the total fuzzy vector by multiplying respective weighted vectors and fuzzy evaluation matrix, then calculate the defuzzification value of each total score, and choose the alternative with the maximum score. Finally, an example is given to demonstrate the rationality of the algorithm.

## 1. Introduction

With the increasing demand for infrastructure, the investment of financial funds alone is far from enough to satisfy people's demand for infrastructure. Insufficient investment has become a major bottleneck restricting China's infrastructure construction. PPP (Public-Private-Partnership) model has been favored by all levels of government in China, because it can alleviate the financial pressure, improve the efficiency of public goods supply, and realize the risk sharing between the public and the private [1]. China attaches great importance to the research on the application of PPP model in the field of infrastructure, but ignores the field of private partner selection [2, 3]. However, private partner selection is responsible for the project design, construction, and operation management of the early project construction, which undoubtedly determines the realization of the final goal of the project [4]. Therefore, this paper will establish a scientific

and reasonable evaluation system for partner selection in PPP mode, which provides reference for selecting private partners in infrastructure projects

From the above analysis, we can see that, under the Public-Private-Partnership Projects, the selection of cooperation partner problem is essentially a multiattribute group decision problem (MAGDM). Lourenzutti proposed a generalized TOPSIS method for group decision-making with heterogeneous information in a dynamic environment. Wang et al. combined the SAW, TOPSIS, and GRA methods [5]. Chen et al. introduced an approach to partner selection with grey target model to minimize the vertical projection distance [2]. Liu et al. proposed a method based on the proposed IFAHA operator and the proposed IFWAHA operator [6].

However, as shown above, there are some limitations on the selection of private sector partners under the MAGDM public and private partnership projects: (1) the existing studies do not take into account the degree of importance

of the objective attribute and subjective attribute in the decision-making problem [5, 7]; (2) the traditional methods usually rely on objective data or subjective judgment, and few studies make more accurate judgments in combination with objective data and subjective judgment [8–10].

Therefore, in order to fill the research gap, a new MAGDM method has been proposed, which has integrated objective/subjective attributes to solve the cooperation partner selection of private sector under Public-Private-Partnership projects. The methods proposed mainly include the following steps: first, we collect decision opinions, establish decision matrices, and normalize them; second, by introducing linguistic variables and integrating objective/subjective attributes, the decision opinions provided by each DM are aggregated into the comprehensive evaluation values. Finally, refer to the comprehensive evaluation values and identify which cooperation partner is suitable for the Public-Private-Partnership projects.

The rest of this paper is structured as follows. Section 2 proposes the evaluation criteria for private enterprise partner selection under Public-Private-Partnership Projects. Section 3 introduces the general procedure of the proposed method and decision analysis. Section 4 demonstrates a numerical example, and Section 5 presents the conclusions.

## 2. The Evaluation Criteria of Private Sector under Public-Private-Partnership Projects

From the perspective of the PPP project operation process and the role of the private sector partners, this paper divides the partner selection evaluation into five parts: construction and operations, risk management ability, environmental practices, business value formation, and finance [4, 11]. Specifically, the five evaluation criteria are construction and operation ability, risk management ability, environmental practices, business value formation, and financial ability, which are shown in Figure 1.

In general, the evaluation criteria of private sector under PPP projects can be classified into the below several categories:

- (i) **Construction and Operation Ability.** The PPP project is obviously different from the traditional construction model in the talent echelon and organizational structure. Therefore, the whole process of construction is not the superposition of the process of design and construction. The construction and operation ability is more focused on the whole process control of the whole life cycle of the PPP project [1]. Hence, we classify construction and operation ability into human resources status, planning rationality and relevant experience. By these criteria, we can select the most suitable partners of PPP projects in construction and operation ability.
- (ii) **Risk Management Ability.** PPP project financing structure is complex and the investment is huge; the construction and operation of the project will be a variety of unknown factors at any time. These show that the reasonable risk sharing is one of the key

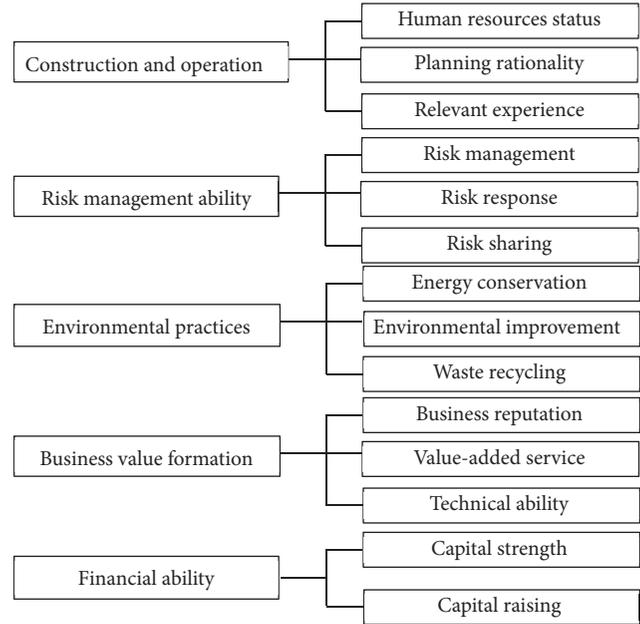


FIGURE 1: The evaluation criteria of private sector under PPP projects.

factors of the success of the PPP project [4]. Therefore, private partners must effectively identify risk factors and respond to risk management measures in a timely and reasonable manner [2, 12]. Among them, risk management system, risk response measures, and risk sharing plan are important indicators to measure the risk management level of private partners.

- (iii) **Environmental Practices.** Environmental protection has become the consensus of all countries in the world, especially in China. Many studies also considered that environmental issues should be fully taken into account in the implementation of PPP projects [13–15]. The environmental practices involve many aspects, such as industrial pollution and domestic pollution [16]. We deem that environmental practices should be given enough thought in the cooperation partner selection of PPP projects, because otherwise the environmental issues will not be in control. The secondary indicators of environmental practices can be classified into energy conservation, environmental improvement, and waste recycling, which can reflect well the PPP partner's practical attitude and action toward environmental issues.
- (iv) **Business Value Formation.** PPP, as an important part of a financing mode, usually is used to relieve infrastructure funding pressure and raise the funds rate for local governments in China [15]. PPP is a long-term collaboration between the public and private sectors for joint construction of town and country infrastructure projects, or offering public goods and service [17, 18]. In the PPP projects, we think the public and private sectors are to cooperate

TABLE 1: Linguistic variables and fuzzy numbers for weights.

Linguistic variables	fuzzy number
Very low (VL)	(0, 0, 0, 3)
Low (L)	(0, 3, 3, 5)
Middle (M)	(2, 5, 5, 8)
High (H)	(5, 7, 7, 10)
Very high (VH)	(7, 10, 10, 10)

\*Note: from [21].

to complete not only infrastructure construction, but also the formation of business value. Hence, we propose the secondary indicators of business value formation as business reputation, value-added service, and technical ability, which can effectively reflect the shared value of partners in PPP projects.

- (v) **Financial Ability.** It is an important index to judge the strength of private partners. If the ability of the use and management of funds is weak, the rational planning and financing of funds cannot be carried out, so the funding gap will appear, which will affect the construction of the project [19, 20]. The financial ability of the partner can be divided into capital strength and capital raising. Capital strength is a core indicator to measure the private partner's financing ability. A good partner's financing ability is mainly reflected in the guarantee of stable funds, the timely and rational use of funds, and the schedule of fund utilization according to the progress of projects. Hence, we propose the secondary indicators of financial ability as capital strength and capital raising, which can guarantee the ability of investors in the economic convenience to carry out investment projects

### 3. Preliminary

**3.1. Fuzzy Set Theory.** Since linguistic variables cannot be directly handled by mathematical methods, in order to solve this problem, each linguistic variable is related to the fuzzy number representing the meaning of each common linguistic term. In FST, transform values are applied to convert linguistic terms into fuzzy numbers [22]. Determining the number of transformation values is usually intuitive: however, too few transformations reduce the resolution, while too many transformations make the system too complicated and unrealistic. In the current study, 1-5 is used as an important weight, and 1-9 is used for ranking behavior [22–24].

The fuzziness of partner selection problem, the individual attributes of the candidate, and the importance weight of ratings to various subjective criteria are used as linguistic variables in this study [8]. Table 1 lists the weights of individual attributes, and Table 2 gives the evaluation of the program and various subjective criteria as linguistic variable values. Trapezoidal fuzzy number is easy to use and convenient to explain. For example, the weight of a very important specific attribute can be measured with trapezoidal fuzzy numbers represented by (7, 10, 10, 10). The linguistic variables and

TABLE 2: Language variables and fuzzy numbers for ratings.

Linguistic variables	fuzzy number
Very poor (VP)	(0, 0, 0, 20)
Between very poor and poor (B VP& P)	(0, 0, 20, 40)
Poor (P)	(0, 20, 20, 40)
Between poor and feasible (B P& F)	(0, 20, 50, 70)
Feasible (F)	(30, 50, 50, 70)
Between feasible and good (B F& G)	(30, 50, 80, 100)
Good (G)	(60, 80, 80, 100)
Between good and very good (B G& VG)	(60, 80, 100, 100)
Very good (VG)	(80, 100, 100, 100)

\*Note: from [21].

fuzzy numbers for weights and ratings proposed by [21] are as shown in Tables 1 and 2.

**3.2. FRS and SAW.** This part describes a new fuzzy multiple attribute decision method (FMADM), which integrates the fuzzy set theory (FST), the traditional factor risk scoring system (FRS), and the simple additive weighted (SAW) method to locate the system. This program is suitable for individual and collective decisions. In the collective setting, the fuzzy evaluation of the decision-makers can be calculated in several ways. In these methods, there are five commonly used methods, including mean, median, maximum, minimum, and mixed operation. This paper uses the mean method to evaluate the importance of decision-makers; that is, the importance of decision-makers is the same (called homogeneous group). Under this condition, a new FSAWS method is proposed to solve the facility location problem for homogeneous groups in fuzzy environment.

In order to establish the decision matrices of decision-makers, decision-makers express their opinions (or performance appraisals) and investigate alternative alternatives of each attribute by questionnaire. These evaluations are usually fuzzy data forms. Fuzzy data can be a linguistic term or speech assessment. The purpose of this state is to convert the fuzzy data into trapezoid fuzzy data. The weights and attributes of the decision-makers of the same/heterogeneous group are aggregated based on the aggregation method. After normalization weight is calculated and the importance degree of decision-makers is evaluated, all performance evaluations are aggregated to each choice under each subjective attribute. The fuzzy weight of the individual attribute and the fuzzy total score of the decision-maker's individual selection of the same/heterogeneous group are blurred in the final state. Then, these alternatives are ranked according to the total score.

### 4. The Proposed Method

The proposed method has the following three steps. First, preparation stage: in this stage, we collect decision-making advice, establish decision matrices, and convert all verbal terms into trapezoidal fuzzy numbers. Second, aggregation stage: in this stage, we use aggregate FRS and SAW. Third, selection stage: in this stage, we construct fuzzy evaluation matrix and select the best option based on the total fuzzy

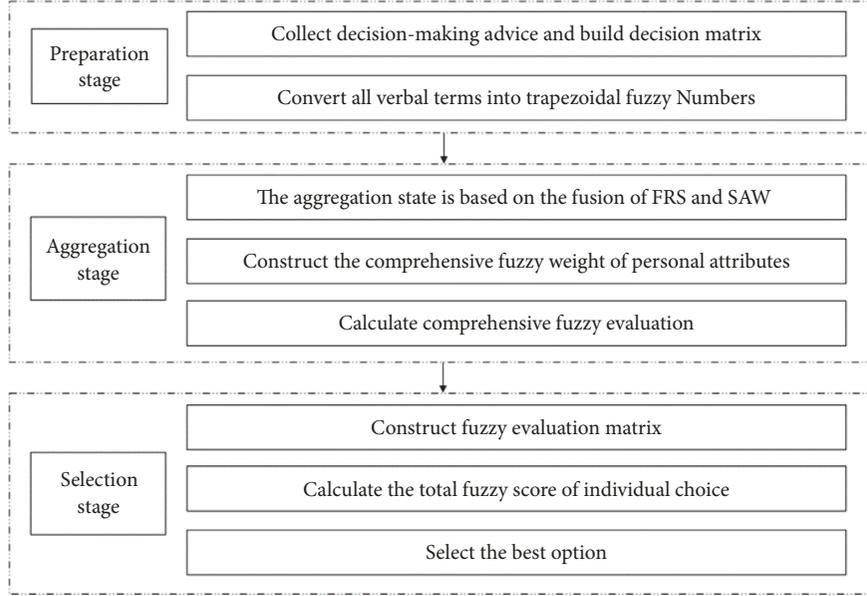


FIGURE 2: The conceptual framework of the proposed approach.

score of individual choice. Figure 2 illustrates the conceptual framework of the proposed method.

*Step 1.* We set up a committee of policy makers, selecting attributes and identifying potential private sector partners.

*Step 2.* We determine the degree of importance (or reliability) of the decision-maker. If the importance (or reliability) of the decision-maker is equal, then the decision within the group is considered to be homogeneous. Otherwise, the group is considered to be heterogeneous (nonhomogenous).

Suppose there are  $k$  decision committees (or experts) ( $D_t$ ,  $t = 1, 2, \dots, k$ ) who are responsible for evaluating the  $M$  candidate address ( $A_i$ ,  $i = 1, 2, \dots, m$ ) under the condition of each  $n$  attribute ( $C_j$ ,  $j = 1, 2, \dots, n$ ) and attribute weight. The importance (or reliability) of a decision-maker is expressed as  $I_t$ ,  $t = 1, 2, \dots, k$ , where  $I_t$  belongs to  $[0, 1]$  and  $\sum_{t=1}^k I_t = 1$ . If the importance (or reliability) and the weight of each decision-maker are taken into account, then the decision-maker fuzzy weight  $\omega_t$ ,  $t = 1, 2, \dots, k$ , was assigned according to the importance of determining the final decision of the interview. Finally, the weight degree of  $I_t$  can be defined as follows:

$$I_t = \frac{d(\omega_t)}{\sum_{t=1}^k d(\omega_t)}, \quad t = 1, 2, \dots, k, \quad (1)$$

Here,  $d(\omega_t)$  gives the fuzzy weight of the fuzzy value by means of symbolic distance. If  $I_1 = I_2 = \dots = I_k = 1/k$ , the decision-maker group is called a homogeneous group; otherwise, the decision-maker group is called heterogeneous (heterogeneous) group.

*Step 3.* We introduce linguistic weighting variables (Table 2) for decision-makers, evaluate the importance of attributes, and calculate the fuzzy weights of individual attributes [25].

Let  $W_{jt} = (a_{jt}, b_{jt}, c_{jt}, d_{jt})$   $j = 1, 2, \dots, n$ ;  $t = 1, 2, \dots, k$  be the linguistic weight, and the decision-maker  $D_t$  gives the subjective attribute  $c_1, c_2, \dots, c_n$  and the objective attribute  $c_{h+1}, c_{h+2}, \dots, c_n$ . The fuzzy attribute weight  $C_j$  of the aggregation of attribute  $W_{jt} = (a_{jt}, b_{jt}, c_{jt}, d_{jt})$   $j = 1, 2, \dots, n$  is evaluated by the  $k$  decision committee, whose definition can be listed as follows:

$$W_j = (I_1 \otimes W_{j1}) \oplus (I_2 \otimes W_{j2}) \oplus \dots \oplus (I_k \otimes W_{jk}) \quad (2)$$

Herein,

$$\begin{aligned} a_j &= \sum_{t=1}^k I_t a_{jt}, \\ b_j &= \sum_{t=1}^k I_t b_{jt}, \\ c_j &= \sum_{t=1}^k I_t c_{jt}, \\ d_j &= \sum_{t=1}^k I_t d_{jt}, \end{aligned} \quad (3)$$

*Step 4.* Defuzzify fuzzy weight of individual attributes; calculate normalized weights and construct weighted vector. In order to solve the weight of fuzzy attributes, the symbolic distance is adopted. Fuzzy solution  $W_j$  is denoted as  $d(W_j)$ , so it can be expressed by the following formula:

$$d(W_j) = \frac{1}{4} (a_j + b_j + c_j + d_j), \quad j = 1, 2, \dots, n \quad (4)$$

The normalized weight of the attribute  $C_j$  is denoted as  $W_j$  and is given by the following formula:

$$W_j = \frac{d(\omega_j)}{\sum_{j=1}^n d(\omega_j)}, \quad j = 1, 2, \dots, n, \quad (5)$$

Here,  $\sum_{j=1}^n W_j = 1$ . The weight vector  $W = [W_1, W_2, \dots, W_n]$  is thus formed.

*Step 5.* Use the language evaluation variables (Table 2) for fuzzy evaluation of subjective attribute evaluation and project decision of the individual, and then focus on fuzzy comprehensive evaluation. Let  $X_{ijt} = (oijt, pijt, qijt, sjit)$ ,  $i = 1, 2, \dots, m$ ,  $j = 1, 2, \dots, h$ ,  $t = 1, 2, \dots, k$  become the appropriateness evaluation of language, and the subjective attribute  $C_j$  given by decision-maker  $D_t$  is assigned to different location  $A_i$ . Let us further define the fuzzy evaluation of  $X_{ij}$  as the subjective attribute of the  $C_j$  candidate  $A_i$  set, which can be derived:

$$X_{ij} = (I_1 \otimes X_{ij1}) \oplus (I_2 \otimes X_{ij2}) \oplus \dots \oplus (I_k \otimes X_{ijk}) \quad (6)$$

This formula can then be said and calculated:

$$X_{ij} = (o_{ij}, p_{ij}, q_{ij}, s_{ij}), \quad (7)$$

$$i = 1, 2, \dots, m, \quad j = 1, 2, \dots, h,$$

Herein,

$$o_{ij} = \sum_{t=1}^k I_t o_{ijt},$$

$$p_{ij} = \sum_{t=1}^k I_t p_{ijt}, \quad (8)$$

$$q_{ij} = \sum_{t=1}^k I_t q_{ijt},$$

$$s_{ij} = \sum_{t=1}^k I_t s_{ijt},$$

*Step 6.* In the committee decision-maker, the fuzzy cost or benefit of the objective attributes is evaluated with various alternatives, and then the fuzzy valued attributes relative to the individual target scheme are calculated.

Objective attributes are determined in each unit and must be transformed into nondimensional indicators (or grades) to ensure linguistic compatibility with subjective attributes. Alternatives with the lowest cost (or maximum benefit) should have the highest rating.

Based on the above principle, let

$$r_{ij} = (a_{ij}, b_{ij}, c_{ij}, d_{ij}), \quad (9)$$

$$i = 1, 2, \dots, m, \quad j = q, q + 1, \dots, n, \quad q = h + 1;$$

It is the fuzzy related cost or benefit of  $C_j$  with the most subjective attribute of alternative address  $A_i$ . Equations (9) and (10) show the transformation objective attributes as follows:

$$x_{ij} = \left\{ r_{ij} \div \max_i \{d_{ij}\} \right\} \otimes 100, \quad (10)$$

$$i = 1, 2, \dots, m, \quad j = q, q + 1, \dots, n,$$

Here,  $\max_i \{d_{ij}\} > 0$ ,  $X_{ij}$  represents the benefit of the transformed fuzzy evaluation  $r_{ij}$ , and  $x_{ij}$  can also be represented by the fuzzy number  $x_{ij} = (o_{ij}, p_{ij}, q_{ij}, s_{ij})$ ,  $i = 1, 2, \dots, m$ ,  $j = q, q + 1, \dots, n$ ,  $q = h + 1$ . In addition, when  $r_{ij}$  becomes larger,  $x_{ij}$  becomes larger.

$$x_{ij} = \left\{ \min_i \{a_{ij}\} \div r_{ij} \right\} \otimes 100, \quad (11)$$

$$i = 1, 2, \dots, m, \quad j = q, q + 1, \dots, n,$$

Among them,  $\min_i \{a_{ij}\} > 0$ ,  $x_{ij}$  means that the cost of fuzzy evaluation of transformation is also  $r_{ij}$ ,  $x_{ij}$  can be expressed by fuzzy number  $x_{ij} = (o_{ij}, p_{ij}, q_{ij}, s_{ij})$ ,  $i = 1, 2, \dots, m$ ,  $j = q, q + 1, \dots, n$ ,  $q = h + 1$ , and when  $r_{ij}$  becomes larger,  $x_{ij}$  becomes smaller.

*Step 7.* We establish a fuzzy valued matrix based on fuzzy evaluation.

The fuzzy evaluation matrix  $M$  can be expressed concisely as the following matrix format:

$$M = \begin{bmatrix} X_{11} & X_{12} & \dots & X_{1n} \\ X_{21} & X_{22} & \dots & X_{2n} \\ \vdots & \vdots & \vdots & \vdots \\ X_{m1} & X_{m2} & \dots & X_{mn} \end{bmatrix} \quad (12)$$

Here,  $x_{ij}, \forall i, j$  is the aggregate fuzzy evaluation of attribute  $A_i$ ,  $i = 1, 2, \dots$ , and  $m$  is related to attribute  $C_j$ .

*Step 8.* The fuzzy total score of individual alternatives is obtained by multiplying the fuzzy evaluation matrix with each weight vector. By fuzzy evaluation matrix  $M$  multiplied by the corresponding weight vector  $W$ , the total fuzzy subvector is obtained, exactly:

$$F = M \otimes W^T = \begin{bmatrix} X_{11} & X_{12} & \dots & X_{1n} \\ X_{21} & X_{22} & \dots & X_{2n} \\ \vdots & \vdots & \vdots & \vdots \\ X_{m1} & X_{m2} & \dots & X_{mn} \end{bmatrix} \otimes \begin{bmatrix} W_1 \\ W_2 \\ \vdots \\ W_n \end{bmatrix}$$

$$= \begin{bmatrix} x_{11} \otimes W_1 \oplus x_{12} \otimes W_2 \oplus \dots \oplus x_{1n} \otimes W_n \\ x_{21} \otimes W_1 \oplus x_{22} \otimes W_2 \oplus \dots \oplus x_{2n} \otimes W_n \\ \vdots \\ x_{m1} \otimes W_1 \oplus x_{m2} \otimes W_2 \oplus \dots \oplus x_{mn} \otimes W_n \end{bmatrix} \quad (13)$$

$$= \begin{bmatrix} f_1 \\ f_2 \\ \vdots \\ f_m \end{bmatrix} = [f_i]_{m+1}$$

here,  $f_i = (r_i, s_i, t_i, u_i)$ ,  $i = 1, 2, \dots, m$

TABLE 3: Importance weight of attributes.

Standard	Decision maker			
	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>
C <sub>1</sub>	M	VH	M	H
C <sub>2</sub>	H	VH	VH	M
C <sub>3</sub>	VH	H	H	VH
C <sub>4</sub>	H	VH	H	M
C <sub>5</sub>	VH	H	VH	VH

TABLE 4: Fuzzy weights and set fuzzy weights of attributes.

Attribute	Decision maker				AFW
	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	
C 1	(2, 5, 5, 8)	(7, 10, 10, 10)	(2, 5, 5, 8)	(5, 7, 7, 10)	(4, 6.75, 6.75, 9)
C 2	(5, 7, 7, 10)	(7, 10, 10, 10)	(7, 10, 10, 10)	(2, 5, 5, 8)	(5.25, 8, 8, 9.5)
C 3	(7, 10, 10, 10)	(5, 7, 7, 10)	(5, 7, 7, 10)	(7, 10, 10, 10)	(6, 8.5, 8.5, 10)
C 4	(5, 7, 7, 10)	(7, 10, 10, 10)	(7, 10, 10, 10)	(2, 5, 5, 8)	(5.25, 8, 8, 9.5)
C 5	(7, 10, 10, 10)	(5, 7, 7, 10)	(7, 10, 10, 10)	(7, 10, 10, 10)	(6.5, 9.25, 9.25, 10)

Step 9. We calculate the brittleness for each score, use the defuzzification method, and choose the alternative with the largest total score.

The ranking of the best positions is determined according to the distance of the fuzzy total score. The following fuzzy equation determines the individual position clear total score:

$$d(f_i) = \frac{1}{4}(r_i + s_i + t_i + u_i) \tag{14}$$

Here, the ambiguity value of the total fuzzy number of the address is given by the location of the symbol distance.

Then the ranking of the position can be defined as the fuzzy value of the total score of the individual choice.

### 5. Example Analysis

In this paper, a nuclear power plant project in Fujian, China (hereinafter referred to as X nuclear power plant), as an example, the tender announcement by the relevant government departments approved by the public release, and finally, A<sub>1</sub>, A<sub>2</sub>, and A<sub>3</sub> three combinations were selected as alternatives for further assessment.

Step 1. Committees with four decision-makers, D<sub>1</sub>, D<sub>2</sub>, D<sub>3</sub>, and D<sub>4</sub>, determine the best alternative. Subjective weights are as follows: (a) construction and operation capability (C<sub>1</sub>); (b) risk management ability (C<sub>2</sub>); (c) environmental practices (C<sub>3</sub>); (d) business value formation (C<sub>4</sub>). Objective weight: (e) financial capability (C<sub>5</sub>); the importance weights of attributes are shown in Table 3.

Step 2. After meeting the committee with all policy makers, all the policy makers are convinced that the importance and reliability are equal (I<sub>1</sub> = I<sub>2</sub> = I<sub>3</sub> = I<sub>4</sub>).

Step 3. We use linguistic weighting variables and their respective fuzzy numbers to evaluate the importance weight of each attribute. Based on the evaluation value, the fuzzy weight of

personal attributes is calculated by equation. Fuzzy weights and set fuzzy weights of attributes are shown in Table 4.

The AFW stands for set fuzzy weights as shown in Table 5.

Step 4. The fuzzy value of the fuzzy weight is calculated by (4) and the normalized weight of the attribute is calculated by (5). These weights derive the value of the weight vector W = [0.1699; 0.1971; 0.2115; 0.1971, 0.2244].

Step 5. We use linguistic level variables and their respective fuzzy numbers with respect to each subjective criterion (Table 2) to evaluate the fuzzy numbers of the four alternatives and then compute a comprehensive fuzzy score for each selection criterion by (6). The evaluation of decision-makers under subjective evaluation attributes and set evaluation are shown in Table 6.

Step 6. We evaluate the fuzzy financial with various alternatives and objective indicators and then use (11) to calculate the relative objective criteria to select the fuzzy rating, as shown in Table 7.

Step 7. We establish the fuzzy evaluation matrix with the aggregate rating, as shown in Table 8.

Step 8. We obtain the total fuzzy fraction of each position.

The total score in Table 9 shows that the descending order of the three alternatives is A<sub>3</sub> > A<sub>2</sub> > A<sub>1</sub>. Therefore, the committee should recommend that alternative A<sub>3</sub> be selected as the appropriate partner in the four options.

### 6. Conclusions

This paper proposes an effective method to solve the problem of private sector partner selection in fuzzy homogeneous environment. Firstly, we select attributes and identify potential partners. Secondly, we get comprehensive fuzzy evaluation. Thirdly, calculate defuzzification value and choose an

TABLE 5: Fuzzy values of set fuzzy weights and normalized weights of attributes.

Method	Attribute				
	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	C <sub>5</sub>
Calculating fuzzy values	6.6250	7.6875	8.2500	7.6875	8.7500
Normalized weight	0.1699	0.1971	0.2115	0.1971	0.2244

TABLE 6: Evaluation of decision makers under subjective evaluation attributes and set evaluation.

Attribute selection scheme		Evaluation of decision maker				Set evaluation
		D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	
C <sub>1</sub>	A 1	F	B. P & F	B. F& G	F	(22.5, 42.5, 57.5, 77.5)
	A 2	B. F & G	F	G	VG	(50, 70, 77.5, 92.5)
	A 3	B. P & F	G	B. P & F	B. F & G	(22.5, 42.5, 65, 85)
C <sub>2</sub>	A 1	B. P & F	F	P	F	(15, 35, 42.5, 62.5)
	A 2	F	B. F & G	P	F	(22.5, 42.5, 50, 70)
	A 3	B. F & G	G	B. P & F	B. F & G	(30, 50, 72.5, 92.5)
C <sub>3</sub>	A 1	G	G	G	B. F & G	(52.5, 72.5, 80, 100)
	A 2	B. F & G	P	B. F & G	VG	(35, 55, 70, 85)
	A 3	G	B. F & G	B. P & F	F	(30, 50, 65, 85)
C <sub>4</sub>	A 1	G	P	G	B. P & F	(30, 50, 57.5, 77.5)
	A 2	B. F & G	P	G	G	(37.5, 57.5, 65, 85)
	A 3	G	B. F & G	VG	F	(50, 70, 77.5, 92.5)

TABLE 7: Evaluation of decision makers under objective evaluation attributes and set evaluation.

A <sub>i</sub>	capital strength	capital raising	financial ability rating	fuzzy subjective
A <sub>1</sub>	(18, 20, 30, 32)	(15, 15, 15, 15)	(33, 35, 45, 47)	(46.8, 48.9, 62.9, 66.7)
A <sub>2</sub>	(14, 15, 15, 16)	(8, 10, 15, 16)	(22, 25, 30, 32)	(68.8, 73.3, 88, 100)
A <sub>3</sub>	(12, 16, 16, 18)	(10, 10, 10, 10)	(22, 26, 26, 28)	(78.6, 84.6, 84.6, 100)

TABLE 8: Fuzzy evaluation matrix.

A <sub>i</sub>	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	C <sub>5</sub>
A <sub>1</sub>	(22.5, 42.5, 57.5, 77.5)	(15, 35, 42.5, 62.5)	(52.5, 72.5, 80, 100)	(30, 50, 57.5, 77.5)	(46.8, 48.9, 62.9, 66.7)
A <sub>2</sub>	(50, 70, 77.5, 92.5)	(22.5, 42.5, 50, 70)	(35, 55, 70, 85)	(37.5, 57.5, 65, 85)	(68.8, 73.3, 88, 100)
A <sub>3</sub>	(22.5, 42.5, 65, 85)	(30, 50, 72.5, 92.5)	(30, 50, 65, 85)	(50, 70, 77.5, 92.5)	(78.6, 84.6, 84.6, 100)

TABLE 9: The scores obtained.

Attribute		
A <sub>1</sub>	fuzzy number	(34.36, 50.28, 60.51, 76.87)
	Calculating fuzzy values	55.51
A 2	fuzzy number	(43.10, 59.68, 70.39, 86.68)
	Calculating fuzzy values	64.96
A 3	fuzzy number	(43.57, 60.43, 73.34, 91.32)
	Calculating fuzzy values	67.17

alternative plan. Finally, an example is given to demonstrate the rationality of the algorithm.

The method proposed in this paper has three main contributions and advantages. First, when considering the attributes of distribution center location, it is divided into subjective and objective attributes. The traditional FRS based on the combination of SAW and FST can be extended to

the location selection of homogeneous/heterogeneous group decision domain in fuzzy environment. Second, the method proposed in this paper allows FMADM to accommodate linguistic terms represented by fuzzy numbers. This helps to create a decision-making process, which is more realistic than the existing system. Third, the method proposed in this paper uses simplified ranking of fuzzy numbers rather than complex programs, so the calculation speed is faster. This method provides a flexible method for decision-makers to choose any FMADM.

There is a great space for improvement in the selection of private sector partners. Researchers need to do further researches.

### Data Availability

The data used to support the findings of this study are available within the paper.

## Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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## References

- [1] Y. Peng, J. Zhou, Q. Xu, and X. Wu, "Cost allocation in PPP projects: an analysis based on the theory of "Contracts as reference points"," *Discrete Dynamics in Nature and Society*, Article ID 158765, 6 pages, 2014.
- [2] W. Chen, Z. Yang, and W. Pan, "Port strategic alliance partner selection using grey target model based on error propagation and vertical projection distance," *Journal of Coastal Research*, pp. 797–804, 2015.
- [3] N. Carbonara and R. Pellegrino, "Public-private partnerships for energy efficiency projects: A win-win model to choose the energy performance contracting structure," *Journal of Cleaner Production*, vol. 170, pp. 1064–1075, 2018.
- [4] Y. Wu, L. Li, R. Xu, K. Chen, Y. Hu, and X. Lin, "Risk assessment in straw-based power generation public-private partnership projects in China: A fuzzy synthetic evaluation analysis," *Journal of Cleaner Production*, vol. 161, pp. 977–990, 2017.
- [5] P. Wang, Z. Zhu, and Y. Wang, "A novel hybrid MCDM model combining the SAW, TOPSIS and GRA methods based on experimental design," *Information Sciences*, vol. 345, no. 1, pp. 27–45, 2016.
- [6] P. Liu and S.-M. Chen, "Group Decision Making Based on Heronian Aggregation Operators of Intuitionistic Fuzzy Numbers," *IEEE Transactions on Cybernetics*, 2016.
- [7] J. Yang, Z. Tang, T. Jiao, and A. Malik Muhammad, "Combining AHP and genetic algorithms approaches to modify DRASTIC model to assess groundwater vulnerability: a case study from Jiangnan Plain, China," *Environmental Earth Sciences*, vol. 76, no. 12, 2017.
- [8] W. Li, S. Yu, H. Pei, C. Zhao, and B. Tian, "A hybrid approach based on fuzzy AHP and 2-tuple fuzzy linguistic method for evaluation in-flight service quality," *Journal of Air Transport Management*, vol. 60, pp. 49–64, 2017.
- [9] S. Sindhu, V. Nehra, and S. Luthra, "Investigation of feasibility study of solar farms deployment using hybrid AHP-TOPSIS analysis: Case study of India," *Renewable & Sustainable Energy Reviews*, vol. 73, pp. 496–511, 2017.
- [10] K. E. Weaver, Y. Chen, E. M. Miiller et al., "Examination of Enterococcus faecalis toxin-antitoxin system toxin Fst function utilizing a pheromoneinducible expression vector with tight repression and broad dynamic range," *Journal of Bacteriology*, vol. 199, no. 12, Article ID e00065-17, 2017.
- [11] C. Ruiters and M. P. Matji, "Public-private partnership conceptual framework and models for the funding and financing of water services infrastructure in municipalities from selected provinces in South Africa," *Water SA*, vol. 42, no. 2, pp. 291–305, 2016.
- [12] M. D. Argaw, A. G. Woldegiorgis, D. T. Abate, and M. E. Abebe, "Improved malaria case management in formal private sector through public private partnership in Ethiopia: Retrospective descriptive study," *Malaria Journal*, vol. 15, no. 1, article no. 352, 2016.
- [13] E. B. Barbier, "The Concept of Sustainable Economic Development," *Environmental Conservation*, vol. 14, no. 2, pp. 101–110, 1987.
- [14] C. S. Lim and M. Z. Mohamed, "Criteria of project success: An exploratory re-examination," *International Journal of Project Management*, vol. 17, no. 4, pp. 243–248, 1999.
- [15] S. B. Zhang, Y. Gao, Z. Feng, and W. Z. Sun, "PPP application in infrastructure development in China: institutional analysis and implications," *International Journal of Project Management*, vol. 33, no. 3, pp. 497–509, 2015.
- [16] R. Liang, C. Wu, Z. Sheng, and X. Wang, "Multi-Criterion Two-Sided Matching of Public-Private Partnership Infrastructure Projects: Criteria and Methods," *Sustainability*, vol. 10, no. 4, p. 1178, 2018.
- [17] A. Nesticò, M. Macchiaroli, and O. Pipolo, "Costs and benefits in the recovery of historic buildings: The application of an economic model," *Sustainability*, vol. 7, no. 11, pp. 14661–14676, 2015.
- [18] A. Nestico and F. Sica, "The sustainability of urban renewal projects: a model for economic multi-criteria analysis," *Journal of Property Investment & Finance*, vol. 35, no. 7, pp. 397–409, 2017.
- [19] N. Kshetri, "India's Cybersecurity Landscape: The Roles of the Private Sector and Public-Private Partnership," *IEEE Security & Privacy*, vol. 13, no. 3, pp. 16–23, 2015.
- [20] E. Shakeri and M. Dadpour, "The combination of fuzzy electre and swot to select private sectors in partnership projects Case study of water treatment project in Iran," in *Proceedings of the International Journal of Civil Engineering*, vol. 13, pp. 55–67, 2015.
- [21] S.-Y. Chou, Y.-H. Chang, and C.-Y. Shen, "A fuzzy simple additive weighting system under group decision-making for facility location selection with objective/subjective attributes," *European Journal of Operational Research*, vol. 189, no. 1, pp. 132–145, 2008.
- [22] M. Nei and A. Chakravarti, "Drift variances of FST and GST statistics obtained from a finite number of isolated populations," *Theoretical Population Biology*, vol. 11, no. 3, pp. 307–325, 1977.
- [23] K. E. Holsinger and B. S. Weir, "Genetics in geographically structured populations: Defining, estimating and interpreting FST," *Nature Reviews Genetics*, vol. 10, no. 9, pp. 639–650, 2009.
- [24] J. E. Munoz Garcia, W. Abdel Maksoud, E. Cho et al., "Mechanical and Magnetic Design of the Superferric Dipoles for the Super-FRS of the FAIR Project," *IEEE Transactions on Applied Superconductivity*, vol. 26, no. 4, pp. 1–4, 2016.
- [25] R. H. Pompon, L. Bislick, K. Elliott et al., "Influence of linguistic and nonlinguistic variables on generalization and maintenance following phonomotor treatment for aphasia," *American Journal of Speech-Language Pathology*, vol. 26, no. 4, pp. 1092–1104, 2017.

