Research Article

Experimental Investigation of Wave Velocity-Permeability Model for Granite Subjected to Different Temperature Processing

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Understanding the change of permeability of rocks before and after heating is of great significance for exploitation of hydrocarbon resources and disposal of nuclear waste. The rock permeability under high temperature cannot be measured with most of the existing methods. In this paper, quality, wave velocity, and permeability of granite specimen from Maluanshan tunnel are measured after high temperature processing. Quality and wave velocity of granite decrease and permeability of granite increases with increasing temperature. Using porosity as the medium, a new wave velocity-permeability model is established with modified wave velocity-porosity formula and Kozeny-Carman formula. Under some given wave velocities and corresponding permeabilities through experiment, the permeabilities at different temperatures and wave velocities can be obtained. By comparing the experimental and the theoretical results, the proposed formulas are verified. In addition, a sensitivity analysis is performed to examine the effect of particle size, wave velocities in rock matrix, and pore fluid on permeability: permeability increases with increasing particle size, wave velocities in rock matrix, and pore fluid; the higher the rock wave velocity, the lower the effect of wave velocities in rock matrix and pore fluid on permeability.

1. Introduction

Permeability is a physical parameter to measure the ability of a porous material to allow fluids to pass through it. There are various methods to measure the permeability, such as steady-state method, transient pulse method [1], and oscillating pore pressure method [2]. The existing methods require strict conditions and the measurement is time consuming. Thus, for exploitation of hydrocarbon resources and disposal of nuclear waste, it is of great importance to simplify the permeability measurement under extreme conditions (high temperature and high pressure).

Acoustic testing technique is one of the most effective tools to study the earth interior. Through acoustic testing technique, some characteristics can be obtained in rock, such as porosity, destiny, saturation, fluid type, pressure, temperature, and geometrical characteristics of cracks [3]. Based on experiments, some researchers found that ultrasonic velocity is more sensitive to porosity. Nara and Kaneko [4] used the P wave velocity to analyze the propagation of cracks in granite under different temperatures and humidity. They found that the propagation of cracks caused by stress corrosion can be monitored by P wave velocity well. Wave velocity is more sensitive to the change of rock mesostructure. Kuila et al. [5] investigated the ultrasonic velocity response of well-characterised low porosity shales from the Officer Basin in Western Australia to both isotropic and anisotropic stress fields and evaluated the velocity response to the changing stress field. The results indicate the magnitude and orientation of the stress anisotropy with respect to the shale microfabric have a significant impact on the velocity response to changing stress fields. Qiao and Zhao [6] obtained accurate P wave and S wave velocity data at pressures up to 180 MPa on different core samples of sandstone in dry, water, and oil-saturated conditions from the Yanchang oilfield. The differences among the wave velocities...
in various conditions are mainly caused by the different rock microstructures.

Some researchers also developed empirical wave velocity-porosity formulas. Wyllie et al. [7–9] found the monotone function between wave velocity and porosity. Raymer et al. [10] improved Wyllie’s formula and proposed wave velocity-porosity formula is an expression of divided function. The relationship between wave velocity and porosity in low porosity rocks is obviously different than the one in high porosity rocks.

Carman [11] proposed a formula to estimate permeability of porous media with some general parameters, such as porosity, superficial area, and particle size. Based on Carman’s research, Coussy [12] proposed a more common form of Kozeny-Carman formula. Above research results indicate that permeability of rock is connected with porosity.

Rock permeability under high temperature usually needs to be measured for the engineering purposes such as coal gasification and nuclear waste disposal. With increasing temperature, permeability increases owing to the increase in number and size of pores and cracks. Scholars have researched the effects of temperature on rock properties from different aspects, such as breakage mesomechanism [13–16], mechanical property [17–20], acoustic property [21–23], and permeability [22–25]. Few experimental equipments can measure the permeability directly at high temperature (above 150°C). But the wave velocity measurement at high temperature can be obtained easily now. If the relationship between wave velocity and permeability can be established, the permeability of rock at high temperature can be obtained from wave velocity measurement.

Benson et al. [26, 27] modeled the permeability evolution of microcracked rocks with different void space geometries at elevated pressure and tried to establish the relationship of wave velocity and permeability. With reference to Benson’s work, porosity is used as medium to establish a wave velocity-permeability model in this paper. Wave velocity and permeability of rock will be changed by high temperature processing to prove the new model. The ultimate goal is to measure the rock permeability indirectly by acoustic testing technique to provide practical guidance for exploitation of hydrocarbon resources and disposal of nuclear waste.

2. Wave Velocity-Permeability Model of Granite

An extended form of Kozeny-Carman formula considering matrix grains are spherical is shown as follows:

\[ k = \frac{d^2}{36c} \frac{\varphi^3}{(1-\varphi)^2}, \]

where \( c \) is Kozeny-Carman constant changed with grain shape [28]; \( d \) is particle size; \( \varphi \) is porosity.

Raymer et al. [10] improved Wyllie’s formula:

\[ v = (1-\varphi)^2 v_m + \varphi v_0, \quad \varphi < 37\% \]

\[ \frac{1}{\rho v^2} = \frac{\varphi}{\rho_0 v_0^2} + \frac{1-\varphi}{\rho_m v_m^2}, \quad \varphi > 37\%, \]

where \( \varphi \) is the rock porosity; \( v_0, v_m \), and \( v_0 \) are P wave velocities in the rock, pore fluid, and rock matrix, respectively; \( \rho, \rho_0, \) and \( \rho_m \) are densities of the rock, pore fluid, and rock matrix, respectively.

In this paper granite is with low porosity; only the first part of (2) is needed to calculate the porosity. Furtherly, the porosity measured by liquid saturation method at normal temperature \( T_0 \) is used as initial porosity \( \varphi_0 \) to improve (2).

Equation (2) is used to calculate porosity difference \( \Delta\varphi \) between \( \varphi \) at temperature \( T \) and \( \varphi_0 \) at normal temperature \( T_0 \):

\[ \varphi = \varphi_0 + \Delta\varphi. \]

According to (2),

\[ \Delta\varphi = \frac{m - \sqrt{m^2 + 4v_m \Delta v}}{2v_m}, \]

where \( m = \frac{\sqrt{\varphi_0^2 + 4v_m (\varphi_0 - \varphi)}}{\varphi_0}; \Delta v = v - v_0; v_0 \) is the wave velocity at normal temperature \( T_0 \), m/s.

Combining (3) and (4), the porosity yields

\[ \varphi = \varphi_0 - \frac{m + \sqrt{m^2 + 4v_m (v - \varphi)}}{2v_m}. \]

In heating process, the main change in rock is the change of pore and crack structures resulting in the changes in permeability and wave velocity. Therefore, there is clear correlation between permeability and wave velocity through the medium of porosity. Combining (1) and (5), the wave velocity-permeability model can be established.

Under given initial porosity \( \varphi_0 \) and initial wave velocity \( v_0 \), the relationship between permeability and wave velocity at any temperature yields

\[ k = \alpha \left( \frac{\varphi_0 - \left( m + \sqrt{m^2 + 4v_m (v - \varphi)} \right) / 2v_m}{1 - \varphi_0 + \left( m + \sqrt{m^2 + 4v_m (v - \varphi)} \right) / 2v_m} \right)^3, \]

where \( \alpha = d^2/36c \) and the initial porosity of granite sample in this paper is \( \varphi_0 = 0.66 \). If the rock microstructure under different conditions has a little change, \( \alpha \) is a constant. The value of \( \alpha \) can be obtained with initial porosity and permeability.

Although it is commonly known that wave velocity in rock decreases with increasing temperature, there are no effective models to forecast wave velocity at different temperatures at present. This is because the changing mechanism of rock microstructure with temperature is rather complex. It is hard to establish an effective temperature-wave velocity model. But some acoustic testing technique can be used at
3.3. Test Procedures.

(1) Drying of specimens: since the granite permeability measured in the experiment is very low, N2 is adopted as permeability media. Therefore, the specimens need to be dried before measuring permeability at normal temperature. Granite specimens will be dried at 50°C in vacuum oven. Drying time is over 12 hours until rock quality does not change. Specimens are naturally cooled to normal temperature in oven.

(2) Permeability measurement: pulse decay method is used to measure the permeability in this experiment. The dried specimens are weighed. Under conditions of axial stress 0.5 MPa, confining pressure 5 MPa, N2 is injected to saturate the specimens. The pore pressure of one side of specimen remains unchanged while the other side is reduced. The permeability at this condition can be obtained from the osmotic pressure difference between two sides over treating time using

\[ k = \mu \beta V \left( \frac{\ln(\Delta P_i/\Delta P_f)}{2 \Delta t (A/L)} \right), \]  

where \( \mu \) is coefficient of kinetic viscosity, Pa·s; \( \beta \) is coefficient of volume compressibility, Pa⁻¹; \( V \) is volume of pressure vessel, m³; \( \Delta P_i \) is initial osmotic pressure difference, Pa; \( \Delta P_f \) is final osmotic pressure difference, Pa; \( \Delta t \) is testing time, s; \( A \) is initial sectional area of specimen, m²; \( L \) is initial length of specimen, m.

As an example, the permeability of 3# specimen at 200°C is calculated in Figure 3. According to Brace’s advice [1], the first 2 minutes of data at nonsteady seepage stage needs to be abandoned. The choice of points A and B is arbitrary. The nitrogen coefficient of kinetic viscosity is \( \mu = 1.78 \times 10^{-7} \) Pa·s, the nitrogen coefficient of volume compressibility at this state is \( \beta = 2.01 \times 10^{-6} \) Pa⁻¹; \( V = 5 \times 10^{-6} \) m³, the initial osmotic pressure difference is \( \Delta P_i = 4.072 \times 10^5 \) Pa, the final osmotic pressure difference is \( \Delta P_f = 3.967 \times 10^5 \) Pa, the testing time is \( \Delta t = 900 \) s, the initial specimen sectional area is \( A = 2.501 \times 10^{-3} \) m², and the initial specimen length is \( L = 0.10014 \) m. According to (7), the permeability of 3# specimen at 200°C can be obtained \( k = 1.32 \times 10^{-9} \) m².

(3) Wave velocity anisotropy measurement: P and S wave velocities of specimens are measured by ultrasonic probes inside the pressure heads of RTR-1000. Honey is used as coupling agent. Wave velocities are taken with an average of 5 measurements.

(4) High temperature processing: after wave velocity anisotropy measurement, specimens are processed by high temperature stove. Heating rate is maintained at 2°C/min. When the temperature reaches 100°C, the specimens are kept at a uniform temperature for 3 hours and then are naturally cooled to normal temperature in stove.

(5) Repeat steps (2), (3), and (4), and the heat treatment temperature reaches 150°C, 200°C, 250°C, 300°C, 350°C, 400°C, 450°C, 500°C, 550°C, 600°C, 650°C, and 700°C successively.

The mass, permeability, and wave velocity of all specimens are measured directly after different heat treatment temperatures.

### Table I: The basic parameters of granite specimens.

<table>
<thead>
<tr>
<th>Specimen number</th>
<th>Height (mm)</th>
<th>Diameter (mm)</th>
<th>Mass (g)</th>
<th>Density (g/cm³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>99.92</td>
<td>50</td>
<td>509.84</td>
<td>2.60</td>
</tr>
<tr>
<td>2</td>
<td>100.25</td>
<td>50.11</td>
<td>511.40</td>
<td>2.59</td>
</tr>
<tr>
<td>3</td>
<td>100.14</td>
<td>50.01</td>
<td>510.91</td>
<td>2.60</td>
</tr>
</tbody>
</table>

![Figure 1: Core specimens.](image-url)
4. Experimental Results and Analysis

4.1. Thermogravimetric Analysis. In the experimental process, the rock mass was measured after every heat treatment. It was found that, with increasing temperature, the granite mass decreases continuously, as shown in Figure 4. The change of rock mass with temperature relates to the escape of water in rock such as gravity water, bound water, and constitutional water. Figure 5 is the change curve of mass and mass variable with temperature. The great mass change after 200°C, 500°C, and 700°C high temperature processing corresponds to the escape of water. However, due to the low granite permeability, water cannot escape at immediate escape temperatures. Escape of water can result in the increase of rock porosity and permeability. Suppose the volume of rock is unchanged before and after heating, cumulative increment of porosity caused by water escape can be shown in Figure 6.

4.2. Change Rule of Wave Velocity with Temperature. When wave transmits in rock through the matrix and pores, its velocity in matrix is higher than the one in pores. With increasing temperature, wave velocity decreases owing to the increase in number and size of pores and hence the travel path. The change in wave velocity can be an indicator for the development cracks degree in rock. Figure 7 shows that wave velocity decreases with increasing temperature. The wave velocity drops significantly at 300°C and 650°C, indicating that there are large numbers of cracks produced and developed at the two temperatures. Compared with the wave velocity at 300°C, the one at 350°C showed only slight change and possible reverse trend.

4.3. Change Rule of Permeability with Temperature. The permeability increases at high temperature result from the development of pores and cracks and the increase in the rock discharge capacity, as shown in Figure 8. Permeability at
5. Validation of Wave Velocity-Permeability Model

According to (1), if $\alpha$ has no change, the relationship between permeability and porosity function $f(\varphi) = \varphi^3/(1 - \varphi)^2$ is linear. So, porosity function $f(\varphi)$ is used as variable to analyze the relationship between porosity function $f(\varphi)$ and permeability $k$ which is shown in Figure 9.

Under close examination, the relationship between permeability and porosity function is approximatively piecewise linear function. The product of geometrical factor and particle size is various at different stages. It relates to the cracks development degree as well. As an example, the piecewise fit using 3# specimen is demonstrated. Stage 1: 50°C–200°C, large slope indicates quick change in permeability with porosity function. Stage 2: 200°C–400°C, small slope shows a slow change in the permeability with porosity function. Stage 3: 400°C–700°C, slightly higher slope than that at stage 2 is obtained. Figure 10 shows that all data fit with Kozeny-Carman equation to a high degree at every stage. Table 2 shows segmentation fitting results of change rule of permeability with porosity function. Fitting degrees of all the three specimens suggest the segmentation is reasonable.

Table 2 shows that the value of $\alpha$ at stage 1 is larger than the one at stage 2 and stage 3. It indicates that particle size is 700°C increased by several hundred times compared to that at normal temperature.

Figure 4: Change rule of mass with temperature.

Figure 5: Change rule of 1# mass and mass variable with temperature.

Figure 6: Cumulative increment of porosity caused by water escape after different heat treatment temperatures.

Figure 7: Change rule of average wave velocity with temperature.
Table 2: Segmentation fitting results of change rule of permeability with \( f(\varphi) \).

<table>
<thead>
<tr>
<th>Stage</th>
<th>Sample</th>
<th>Fitted curve</th>
<th>( \alpha )</th>
<th>( \beta )</th>
<th>( R^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stage 1</td>
<td>1#</td>
<td>( k = 13979 f(\varphi) + 0.39638 )</td>
<td>13979</td>
<td>0.396</td>
<td>0.881</td>
</tr>
<tr>
<td></td>
<td>2#</td>
<td>( k = 14632 f(\varphi) + 0.05796 )</td>
<td>14632</td>
<td>0.058</td>
<td>0.940</td>
</tr>
<tr>
<td></td>
<td>3#</td>
<td>( k = 16233 f(\varphi) + 0.18146 )</td>
<td>16233</td>
<td>0.181</td>
<td>0.987</td>
</tr>
<tr>
<td>Stage 2</td>
<td>1#</td>
<td>( k = 817 f(\varphi) + 1.33911 )</td>
<td>817</td>
<td>1.339</td>
<td>0.944</td>
</tr>
<tr>
<td></td>
<td>2#</td>
<td>( k = 1042 f(\varphi) + 1.38474 )</td>
<td>1042</td>
<td>1.385</td>
<td>0.925</td>
</tr>
<tr>
<td></td>
<td>3#</td>
<td>( k = 812 f(\varphi) + 1.26588 )</td>
<td>812</td>
<td>1.266</td>
<td>0.998</td>
</tr>
<tr>
<td>Stage 3</td>
<td>1#</td>
<td>( k = 1016 f(\varphi) + 3.37391 )</td>
<td>1016</td>
<td>3.374</td>
<td>0.983</td>
</tr>
<tr>
<td></td>
<td>2#</td>
<td>( k = 1021 f(\varphi) + 4.57822 )</td>
<td>1021</td>
<td>4.578</td>
<td>0.999</td>
</tr>
<tr>
<td></td>
<td>3#</td>
<td>( k = 1097 f(\varphi) + 3.18941 )</td>
<td>1097</td>
<td>3.189</td>
<td>0.996</td>
</tr>
</tbody>
</table>

Figure 8: Change rule of permeability with temperature.

Figure 9: Change rule of permeability with \( f(\varphi) \).

big at stage 1 and becomes small at stage 2 and stage 3. Thus, this matches the real behavior. Fitting results obtained with both (1) and (6) all show intercepts that should not be from theoretical equation. The intercept should be caused by cracks development. The higher the development degree of cracks is, the bigger the intercept is. Therefore, (6) can be amended as follows:

\[
k = \alpha \left( \frac{\varphi_0 - \left( m + \sqrt{m^2 + 4v_m (v - \varphi_0)} \right) / 2v_m}{1 - \varphi_0 + \left( m + \sqrt{m^2 + 4v_m (v - \varphi_0)} / 2v_m \right)^2} \right)^3 + \beta,
\]

where \( \beta \) is a value related to crack development degree of cracks; \( \alpha \) and \( \beta \) need to be determined by experiments.

Substituting \( \alpha \) and \( \beta \) of Table 2 into (8), the fitting results are compared with experimental data in Figure 11. Given some wave velocities and the corresponding permeabilities through experiments, the other permeabilities at different temperatures and wave velocities can be obtained.

6. Sensitivity Analysis

A wave velocity-permeability model has been established in Section 4. In this section, the sensitivity analysis for some parameters in (8) will be carried out. Particle sizes of different rocks are much different. With sedimentary rock, for example, the range of particle size is from \( 10^{-5} \) mm to \( 10^{2} \) mm. The range of sandstone particle size is mainly from 1/16 mm to 2 mm. The sandstone with smaller particle size from 1/256 mm to 1/16 mm is called siltstone. The range of shale particle size is mainly less than 1/256 mm. Udden-Wentworth scale is the most widely used size grading at present. Then, Krumbein [29] used \( \Phi \) to express the scale as shown in Table 3. Conversion formula: \( d = 2^{-\Phi} \), where \( d \) is particle size, mm. In sensitivity analysis, the values of \( \Phi \) are \(-2, 0, 2, 4, 6, 8, \) and \( 10 \).

P wave velocities of some typical rocks are shown in Table 4 [30]. Therefore, in sensitivity analysis, the values of \( v_m \) are 5000, 6000, 7000, and 8000 m/s.

P wave velocities of some fluids are shown in Table 5 [31]. Therefore, in sensitivity analysis, the values of \( v_l \) are 300, 600, 900, 1200, and 1500 m/s.
Figure 12 shows the effect of particle size on permeability when $v_m = 6000$ m/s and $v_{fl} = 600$ m/s. It clearly indicates that $\Phi$ has great effects on permeability, as shown in Figure 12. The larger $\Phi$ is, the higher the permeability will be.

Figure 13 shows the effect of $v_m$ on permeability when $\Phi = 2$ and $v_{fl} = 600$ m/s. The larger $v_m$ is, the higher the permeability will be. When $v_r$ is bigger, $v_m$ has nearly no effect on permeability. The smaller $v_r$ is, the greater the effect of $v_m$ on permeability will be.

Figure 14 shows the effect of $v_{fl}$ on permeability when $\Phi = 2$ and $v_m = 6000$ m/s. The larger $v_{fl}$ is, the larger the permeability will be. When $v_r$ is larger, $v_{fl}$ has nearly no effect on permeability. The smaller $v_r$ is, the greater the effect of $v_{fl}$ on permeability will be.

7. Conclusions

(1) In this paper, porosity is used as medium to establish a wave velocity-permeability model. Through the new model, the permeability of rock at any temperature can be obtained with wave velocity.

(2) Heat treatment is used to change the microstructure of rock to confirm the new model. Mass, wave velocity, and permeability of granite are measured in experiments after high temperature processing: (a) with increasing temperature, the mass of granite decreases continuously. The change of rock mass with temperature was the escape of different forms of water from the rock. The water escape can increase the porosity. (b) The P and S wave velocities of granite decrease with increasing temperature. The wave velocity...
Figure 11: Segmented fitting curve of wave velocity-permeability.

Table 3: Udden-Wentworth scale and $\Phi$.

<table>
<thead>
<tr>
<th>$d$ (mm)</th>
<th>$\Phi$</th>
<th>$d$ (mm)</th>
<th>$\Phi$</th>
</tr>
</thead>
<tbody>
<tr>
<td>256</td>
<td>-8</td>
<td>1/4</td>
<td>2</td>
</tr>
<tr>
<td>128</td>
<td>-7</td>
<td>1/8</td>
<td>3</td>
</tr>
<tr>
<td>64</td>
<td>-6</td>
<td>1/16</td>
<td>4</td>
</tr>
<tr>
<td>32</td>
<td>-5</td>
<td>1/32</td>
<td>5</td>
</tr>
<tr>
<td>16</td>
<td>-4</td>
<td>1/64</td>
<td>6</td>
</tr>
<tr>
<td>8</td>
<td>-3</td>
<td>1/128</td>
<td>7</td>
</tr>
<tr>
<td>4</td>
<td>-2</td>
<td>1/256</td>
<td>8</td>
</tr>
<tr>
<td>2</td>
<td>-1</td>
<td>1/512</td>
<td>9</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>1/1024</td>
<td>10</td>
</tr>
<tr>
<td>1/2</td>
<td>1</td>
<td>1/2048</td>
<td>11</td>
</tr>
</tbody>
</table>

Table 4: P wave velocities of some typical rocks.

<table>
<thead>
<tr>
<th>Lithology</th>
<th>$v_m$ (m/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sandstone</td>
<td>5480~5950</td>
</tr>
<tr>
<td>Limestone</td>
<td>6400~7000</td>
</tr>
<tr>
<td>Dolomite</td>
<td>7000~7925</td>
</tr>
</tbody>
</table>

Table 5: P wave velocity of some fluids.

<table>
<thead>
<tr>
<th>Fluid</th>
<th>$v_m$ (m/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Air</td>
<td>331 (273 K)</td>
</tr>
<tr>
<td>$CO_2$</td>
<td>259 (273 K)</td>
</tr>
<tr>
<td>$CH_4$</td>
<td>430 (273 K)</td>
</tr>
<tr>
<td>$SO_2$</td>
<td>213 (273 K)</td>
</tr>
<tr>
<td>He</td>
<td>965 (273 K)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Fluid</th>
<th>$v_m$ (m/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>1497 (298 K)</td>
</tr>
<tr>
<td>Drilling slurry</td>
<td>1830 (mean value)</td>
</tr>
<tr>
<td>Petroleum</td>
<td>1295 (307 K)</td>
</tr>
<tr>
<td>Gasoline</td>
<td>1250 (307 K)</td>
</tr>
<tr>
<td>Kerosene</td>
<td>1420 (307 K)</td>
</tr>
</tbody>
</table>

drops significantly at 300°C and 650°C and showed only slight change at 350°C. (c) The permeability of granite increases with increasing temperature, and the rate of the permeability increase also rises with temperature. Permeability at 700°C increased by several hundred times than that at normal temperature.

(3) Using modified wave velocity-porosity empirical formula and Kozeny-Carman equation, a new wave velocity-permeability model is established. If some wave velocities and their corresponding permeabilities are known through experiments, we can obtain the other permeabilities at different temperatures and wave velocities by this model.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.
Acknowledgments

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