Research Article

Partially Transparent Jaumann-Like Absorber Applied to a Curved Structure

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A Jaumann absorber with its metal backing replaced with a combined low-pass and polarizer FSS is investigated with respect to its absorption and its polarization-dependent low-frequency transparency properties. This structure is applied to an idealized curved wing-front end, and its monostatic radar cross-section is determined. The FSS-Jaumann structure preserves an absorption similar to the planar Jaumann absorber in the higher frequency interval and enables a partial transparency in the $TE_z$ polarization at 1 GHz. In addition, once the structure is applied to the wing-front end, a significant reduction in two-dimensional radar cross-section for both the $TM_z$ and $TE_z$ polarization over 2–16 GHz is observed. A sensitivity analysis shows that the resistivity of the inner resistive layer has a large impact on the 1 GHz transmission.

1. Introduction

This paper is a second step towards a design of a curved absorber at high frequencies with a polarization-sensitive transparent window at low frequencies. The structure is intended to be applied to the front end of an aircraft wing. The first step was achieved in [1] where it was shown that a Jaumann-similar absorber could be used to efficiently reduce the monostatic radar cross-section (RCS). This reduction persists over $\pm 20^\circ$ angular interval around the forward direction of an idealized airplane wing. Our long-term goal is to design a curved antenna radome with absorbing properties with low monostatic RCS at high frequencies and a transparent polarization-sensitive antenna window at low frequencies. The purpose of this paper is to investigate the absorption and transparency properties of a Jaumann absorber when the back-metal layer is replaced with a low-pass frequency-selective surface (FSS). The aim is to preserve or improve the absorption properties and at the same time to obtain radome transparency of the surface while keeping low RCS of the structure.

A common problem in electromagnetic design is to add frequency-dependent properties (here absorption, transparency) to a complicated, for example, a curved structure. An example of such a complication is to, for example, investigate a large bandwidth frequency response of a layered structure by varying/optimizing layer thickness or periodic structures design. For planar surfaces, a unit-cell approach allows such an investigation with comparable short calculation time to evaluate many different designs towards approaching an optimum. A similar investigation for this case with its broken alignment between the unit cell that is now curved and the planar incoming wave makes a similar investigation considerably slower due to its larger electromagnetic size. It is known that applying a planar Jaumann absorber to a curved surface results in a certain performance loss [2], which can partly be compensated for on certain generic shapes like cylinders [3]. The design process of Jaumann-similar structure, for both the planar and cylindrical geometries, suffers from multiple local minimums in cost functions aiming to reduce their overall monostatic RCS behavior. Similar to, for example, [4], we address this challenge by first separating the design structure into several subfunction parts each optimized towards a “good” solution. Secondly, these partial designs are used as a starting point to fine-tune a global structure. It is shown in [1] that there are large similarities in the resonant frequency and absorption level between the planar
design and design on a surface with moderate curvature. This allows us here to use a planar model to investigate the possibility of adding a low-frequency transparency window to the structure by replacing a back-metal surface with a low-pass FSS, which is subsequently applied to a wing-front end to evaluate how this affects its scattering properties.

The concept of a combined curved absorber with transparent window is not unique; in this paper, we combine a Jaumann absorber with a low-pass gangbuster-like FSS combined with a polarizer to add transparency in one polarization to a curved surface. Somewhat surprisingly we have not found any paper in the literature about this subject. The different subparts of the design are however well known, and a brief review of these is given here: the Salisbury screen [5], or the quarter wavelength absorber, which consists of a resistive sheet on top of a quarter wavelength thick dielectric spacer placed on a metal plane. It has a fairly narrow absorption bandwidth, which can be extended by adding additional resistive sheets and spacers; such a construction is commonly called a Jaumann absorber which is rather well known, see, for example, [1, 13]. The Jaumann absorber has been extensively used to reduce RCS for the last half century. However, absorbers on non-planar surfaces have considerably fewer references [1–3], each of these references was discussed above. Frequency-selective surfaces have been used to improve the absorption bandwidth-thickness efficiency of planar, see, for example, [8–11], where a periodic lossy FSS is used as a replacement of the resistive sheets. Another more extensively studied area is frequency-selective surfaces used as pass/stop band filters for a variety of polarizations, a review for planar surfaces, and a range of elements can be found in, for example, [4, 12].

The rest of the paper consists of Section 2 describing the design goals and constraints at our numerical model. A low-pass FSS is designed in Section 3. This designed FSS surface is integrated with the Jaumann absorber by replacing its metal-back layer in Section 4. The section ends with a fine-tuning of the Jaumann parameters. A brief sensitivity analysis of the resulting planar structure is done in Section 5. In Section 6 is the designed structure applied to the wing front. The paper ends with conclusions and bibliography.

2. Design Goals and Restrictions

An infinitely extended cylinder with idealized wing cross-section is shown in Figure 1. The combined FSS absorber is applied to the front-end part. To emphasize the scattering properties of the applied absorbing/transparency structure, we further reduce the electromagnetic model to include only the 15% forward part of the wing. This front-end part is well approximated by the corresponding part of an ellipse with major and minor radius of 400 mm and 49.4 mm, respectively. The resulting 15% structure is extended with a short block with a smooth transition from the elasticity curvature to horizontal (x-direction) and embedded in a PML layer to reduce back-end scattering. For a detailed discussion of the model and its implementation in Ansoft HFSS 11, see [1, 13]. The applied structure is periodic in the z-direction. By utilizing a periodic (master/slave) boundary conditions, this allowed the final scattering structure to consist of a 6.8 mm thick (z-direction) slice.

The frequency interval of interest here is 1–16 GHz. For TMz-polarized incoming waves (see Figure 1), the structure should reduce the monostatic RCS levels to below a metal wing RCS level over the entire frequency interval. Similar RCS reductions are required for incoming waves with frequencies between 2 and 16 GHz in the TEz polarization. In addition, the structure should be as transparent as possible to waves with TEz polarization at 1 GHz. The long-term goal is to protect an antenna radiating TEz-polarized waves at 1 GHz. Such an antenna and its protecting structure will interact, and the radiation performance of the antenna, such as the level of polarization purity, increases its side lobe level, and transmission losses may be degraded, see, for example, [14, 15]. All such considerations are beyond the scope of the present paper, since the antenna element is not yet determined. Starting from a concept-proved Jaumann absorber design [1], we replace its main wave-blocking feature, the metal-back plate, with an FSS surface. The design of such an FSS is the subject of the next section.

3. A Gangbuster-Similar Low-Pass Frequency-Selective Surface

To create a polarization-selective transparency window starting from a Jaumann absorber design, we note that its main blocking feature is the back-metal layer. Replacing the metal back with a suitable chosen FSS has the possibility to introduce transparency in one polarization at 1 GHz. However, the function of the Jaumann absorber strongly depends on the back metal for its function at its desired
resonance frequency. To preserve as much of the back-metal properties as possible, and to introduce the desired separate scattering behavior of incoming TMz/TEz waves, suggests that the choice of planar FSS structures should be in alignment with the polarizations for normal-incident waves. The frequency filter properties are strongly dependent on the patch type, its geometry, and size of the corresponding unit cell. A further limitation on the unit-cell requirement in our case is that the resulting design should be compatible with a one-direction periodicity requirement along the axis of the cylinder. A starting design for such a low-pass FSS compatible with the polarization requirements is an array of metal-patch dipoles from a family of low-pass frequency-selective surfaces called gangbusters [4, 16]. To include the desired high-reflection behavior of the TMz polarization, we combine such a gangbuster FSS with a periodic polarizer. A gangbuster FSS consists of straight dipoles arrayed in line with a small interdipole spacing, each line of dipoles is slightly displaced to the neighboring line, resulting in a nonrectangular unit cell. The gangbuster family has a low-pass behavior and for higher frequencies shows a wide-band high-reflection behavior; the family members mainly differ in size of the bandwidth of the low-pass region. To obtain a rectangular compatible unit cell, required for the simulation of a unit slice of the cylinder we modify a gangbuster of the “type 2” family (see [4]) to an equal-sides triangular lattice arrangement. We name the resulting triangular structure a gangbuster-like FSS, see Figure 2(a).

To combine the polarizer, consisting of long metal patches (vertical gray in Figure 2(a)), with the low-pass FSS metal patches (horizontal black) into one resulting structure, we stack them and embed both into a thin dielectric spacer (white), see Figure 2(b). This kind of embedding of gangbuster has been shown to work well in, for example, [4], with the additional benefit that the metal length becomes somewhat more frequency independent of the outside embedding dielectrics which are part of the Jaumann structure, see next section. Note that the respective FSS layers are not in electrical contact with each other. The gangbuster family “type 2” [4] as well as our design has less than 12 dB reflection at 1 GHz. The resulting design parameters are given in the caption Figure 3.

The scattering performance of the lossless structure given in Figure 2 is shown in Figure 3; it is compared with the slightly better performing gangbuster “type 2” polarizer combination. Notice that the resulting structure reflects the orthogonal polarization, for example, where E-field is parallel to the polarizer and has low-pass characteristics for
the parallel polarization (dipoles parallel with $E$-field). As it is seen in Figure 3, we have obtained a high-reflection behavior for the orthogonal polarization over 1–16 GHz. For the parallel polarization, we have obtained a transparent window at and below 1 GHz with less than 10 dB reflection (the structure is lossless). The frequency response then rapidly reaches towards a high-reflection behavior over frequency band between 3 and 15 GHz, with a normal reflection coefficient above $-4$ dB. The next step is to integrate the design given in Figure 2 with an absorber, which is the subject of the next section.

4. An FSS-Backed Jaumann Absorber

We have now obtained the first step in the design procedure, a frequency/polarization-sensitive structure with a low-frequency “transparent” window and a high-frequency high-reflection behavior, see Figure 3. The next step of the design process is to integrate this FSS structure as a replacement of the metal-back layer of a Jaumann absorber, see Figure 4.

The goal here is to fine-tune the Jaumann parameters (spacer properties, and the resistive layers) to optimize the survival of the 1 GHz TE$_z$ polarization transparency while keeping the absorption properties of the original Jaumann absorber for both the TM$_z$ polarization and for the 2–16 GHz of the TE$_z$ polarization. The lossy resistive layers of the absorber will couple the degree of the TE$_z$ transmission at 1 GHz with the absorbing properties for the same polarization in the 2–16 GHz interval. We find naturally that a high transmission coefficient at low frequencies for the TE$_z$ polarization degrades absorption at high frequencies and vice versa. Thus, the resulting structure will be a compromise between these two desired features. It is clear that incident waves scattering on this inhomogeneous structure containing the FSS surface will result in scattered wave in all directions. However, the small electric size of the unit cell in the computation frequency band, 16 GHz and below, allows only evanescent higher-order Floquet modes. Thus, to tune the absorber properties, we make the approximation that the FSS layers can be replaced with an equivalent admittance response. This admittance is obtained from a numerical HFSS calculations of the reflection coefficient through the relation (see e.g., [17])

$$Y_{\text{FSS}}^{(\parallel \perp)} = \frac{1}{Z_{\text{FSS}}^{(\parallel \perp)}} = Y_0 \frac{1 - \Gamma^{(\parallel \perp)}}{1 + \Gamma^{(\parallel \perp)}}.$$  \hspace{1cm} (1)

Here, $Y_0$ is the intrinsic admittance of the free space and $\Gamma^{(\parallel \perp)}$ is the reflection coefficient corresponding to parallel $\parallel$ or orthogonal $\perp$ polarization respectively, assuming that the cross polarizations is small. This approximation is used for optimization purposes to reach a compromise between transmission and absorption. In order to reach such a compromise we have studied a series of cost-functions as

$$G(f) = \sum_{i=10}^{160} \max(\Gamma^\parallel(f_0 + i\Delta f), -12) - w\Gamma^\parallel(f_0).$$  \hspace{1cm} (2)

Here $f_0 = 1$ GHz and $\Delta f = 0.1$ GHz, $\Gamma^\parallel$ and $\Gamma^\perp$ are the reflection and transmission coefficients, respectively, for the parallel polarization expressed in dB to emphasize the importance of the 1 GHz transmission requirement. The relative weight between the higher frequencies and the transmission coefficient at 1 GHz is controlled by the weight $w$. Notice that the cost function only contains the parallel polarization. This choice of $G$ enables fewer calculations resulting in a faster optimization procedure and the resulting design. The other polarization remains at least as good as the optimized one for frequencies above 3 GHz, see Figure 4.

The cost function $G$ is minimized with respect to thicknesses and permittivities of each layer as well as the resistivity in each of the lossy layers (see Figure 4). The cost function $G$ suffers from a number of local minimums catching the used deterministic optimizer of $G$; to work around this problem we have used a range of starting conditions to improve the probability of finding a global optimum. We restricted the optimization domain of the parameters to:

$$\begin{align*}
2.2 \leq & \varepsilon_r1 \leq 6, & 1.4 \leq & \varepsilon_r2 \leq 6, \\
0.6 \leq & R_1Y_1 \leq 5, & 0.6 \leq & R_2Y_0 \leq 5, \\
2 \leq & d_1 \leq 7, & 2 \leq & d_2 \leq 7.
\end{align*}$$  \hspace{1cm} (3)

By varying the coefficient $w$ from 50 to 200, we get an almost linear variation of the $-10$ dB absorption bandwidth from 10.1 GHz to 8.8 GHz, and the corresponding transmitted power at 1 GHz varies from $-4.94$ dB to $-3.8$ dB, respectively. Thus, a more wide-band absorber can be achieved at the cost of a lower transmission at 1 GHz. A fast method to obtain the transmission/reflection coefficients for normal incident waves on a stratified structure is to use wave-splitting and propagation matrices for each layer,

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{Figure4.png}
\caption{The cross-section of the FSS-backed Jaumann absorber.}
\end{figure}
similarly to [18, 19]. The resistive layers were considered to be sufficiently thin, so that they may accurately be accounted for as a generalized boundary condition [19].

The final design, using the homogenized FSS model, was obtained by using the weight \( w = 120 \). The resulting parameters are \( d_1 = 3.0 \, \text{mm}, \, d_2 = 5.7 \, \text{mm}, \, \varepsilon_r_1 = 2.2, \, \varepsilon_r_2 = 1.4, \, R_1 = 414 \, \Omega/\square, \) and \( R_2 = 1260 \, \Omega/\square. \) The corresponding reflection coefficients for the parallel and orthogonal polarizations are shown in Figure 5. The reflection coefficient of an optimized Jaumann absorber with the same total thickness (including the FSS thickness) as the optimized FSS jaumann is also shown in this figure. The Jaumann absorber is optimized with the same cost function as in (2) where the transmission term is eliminated. The resulting parameters for the Jaumann design are \( d_1 = 4.4 \, \text{mm}, \, d_2 = 5.8 \, \text{mm}, \, \varepsilon_r_1 = 2.2, \, \varepsilon_r_2 = 1.4, \, R_1 = 228 \, \Omega/\square, \) and \( R_2 = 459 \, \Omega/\square. \) The approximated design is compared with a full-wave simulation of the resulting structure which is presented by dotted lines for both polarizations. From the full-wave simulation, it is clear that the normal-incident reflection coefficient well agrees with the predicted homogenized result. We also find that the FSS Jaumann design provides desired level absorption over a large part of the frequency band. However, as it is expected, the absorption bandwidth is less than one obtained by an optimized metal-back Jaumann absorber with the same total thickness. It is due to the transparent window at low frequencies and the FSS thickness which is not used for the absorption means but for the transparency. More precisely, the \(-10 \, \text{dB} \) absorption bandwidth for the orthogonal and parallel polarizations is, respectively, reduced 8% and 17% for FSS-backed Jaumann as compared with the above-described optimized Jaumann. However, we can conclude that the metal-back replacement with a combined polarizer and a polarization-sensitive low-pass FSS results in a fair absorber. We are now in the position to investigate the transparency properties.

For the well-known power conservation relation for a homogeneous planar structure, see, for example, [20]

\[
P_{\text{loss}} = 1 - |\Gamma|^2 - |T|^2, \tag{4}
\]

where \( \Gamma \) and \( T \) are the reflection and transmission coefficient of the homogenized FSS-backed Jaumann absorber, respectively, and \( P_{\text{loss}} \) is the power loss of the structure, valid for normally incident plane waves of a lossy stratified nonmagnetic structure in free space.

We can now evaluate the level of transparency obtained by the resulting structure. The resistive losses of the structure at 1 GHz are 43% which for this design could be lowered marginally on the expense of the absorption bandwidth. Thus, the FSS-backed Jaumann results in a partial transparency. However, rather large part of the 1 GHz incoming field ends up as heat of the structure. What does this partial transparency imply for the RCS behavior of the curved surface?

![Figure 5: The reflection from the FSS-backed Jaumann absorber for the parallel (solid line) and orthogonal (dashed line) polarizations and the optimized Jaumann absorber with the same thickness (stars line) determined by the wave-splitting model. The full-wave analysis of each polarization is also shown by dotted-line curves.](image)

**Table 1:** Sensitivity analysis of the structure shown in Figure 4. Here, \( |\delta d_i/d_i| \leq 10\%, |\delta R_i/R_i| \leq 10\%, i = 1, 2. \)

<table>
<thead>
<tr>
<th>( \delta d_i/d_i )</th>
<th>( \delta d_2/d_2 )</th>
<th>( \delta R_1/R_1 )</th>
<th>( \delta R_2/R_2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \delta \text{BW/BW} )</td>
<td>&lt; 3.5%</td>
<td>&lt; 0.4%</td>
<td>&lt; 0.5%</td>
</tr>
<tr>
<td>( \delta T^p/T )</td>
<td>&lt; 0.2%</td>
<td>&lt; 0.1%</td>
<td>&lt; 6%</td>
</tr>
</tbody>
</table>

**5. Sensitivity Analysis of the FSS-Backed Jaumann Structure**

In this section, we verify that the resulting design is robust towards small changes in the Jaumann parameters by a one-parameter variation of the design. The two quality evaluation parameters are the absorption bandwidth and the 1 GHz-transparency. Note that the relative thickness/dielectric properties cowork to make an electrical width of the dielectric spacers, thus to account for a combination of dielectric-frequency dependence and possible thickness variations it suffices to consider a range of thicknesses variations. It has been shown in [21] that the basic Jaumann absorbers are moderately insensitive to small changes in designed parameters. The similar response of the admittance representation of the FSS with the full-wave simulation allows us to use the simplified model to evaluate the robustness. Our perturbation study shows that our design is also moderately insensitive to small parameters perturbation. The results of the parameter variations are collected in Table 1.

Note that the largest sensitivity is in the levels of resistivity in \( R_1 \) changing the 1 GHz transmission coefficient with 6%. This indicates that it is necessary to include a low-pass behavior in at least one of the resistive layers. Work in this direction is in progress.
6. FSS-Backed Jaumann Absorber for an Aircraft Wing-Front Profile

The question considered in this section is the following: does the FSS-backed Jaumann structure have an RCS lower than a plain metal wing-front when it is applied to the wing? The structure is applied on an elliptical layer in the wing front end by specifying the coordinates of each metal dipole patch of the FSS on an elliptic layer. Each layer in the FSS-backed Jaumann is mapped into a corresponding dipole patch of the FSS on an elliptic layer. The outer surface of the wing is replaced with the top-resistive layer $R_2$ of the FSS-backed Jaumann design. The dielectric space layer is created by inserting another elliptic surface which is shifted a distance $d$ in the $x$-direction. Each sequential layer of the design is similarly translated. The distance $d$ for each layer is identical with the corresponding thickness of the planar design ($d_1$, $d_2$). This results in that each layer is very similar to the planar Jaumann along the $x$-axis, but the surface normal thickness away from the $x$-axis shrinks, resulting in a shift of frequency for wave of nonnormal incident direction. In [1], this was shown to be beneficial for the RCS reduction behavior for nonnormal incidence. The layer thicknesses are calculated in the optimization process for the planar structure and are equal to 3.0 mm and 5.7 mm, respectively, for inner and outer layers. Similarly, the FSS structure is located inside a similar elliptical layer with maximal thickness of 1.5 mm at the front end. The wires are along $z$-axis, and the dipoles are bent along the elliptical curve of the wing. Thus, the parallel and orthogonal polarizations in the planar structure corresponds to the TE$_z$ and TM$_z$ polarizations in the curved structure with respect to the coordinate system reference shown in Figure 1 and the FSS in Figure 2.

Numerical simulations using HFSS were used to determine the mono-static RCS of a 6.8 slice “unit-cell” of an infinitely extended cylinder as described in Section 2. The wing is illuminated by an incident plane wave $E^i$ with

$$E^i(x, y) = E_0 \exp[jk_0(x \cos \phi_i + y \sin \phi_i)], \quad (5)$$

where $\phi_i$ is the incident direction here $\phi_i = 0$, and $E_0$ is either

$$E_0 = E_0 \hat{a}_z \quad \text{or} \quad E_0 = E_0 (-\hat{a}_x \sin \phi_i + \hat{a}_y \cos \phi_i), \quad (6)$$

for the TM$_z$/TE$_z$ polarization, respectively. All fields are assumed to have the time dependence $e^{j\omega t}$.

There are now three interesting cases to compare for this wing-front end. The reference case is a plain metal-front end, which the designs are supposed to improve upon, while adding 1 GHz transparency. This is the solid line in Figure 6. The second reference case is the optimized Jaumann absorber described in Section 4 (dashed-dotted curve in Figure 6). Both these reference cases are compared with FSS-backed Jaumann absorber. The dashed curve in the figure shows the performance of the FSS-backed Jaumann absorber. Notice that FSS-backed Jaumann absorber has an overall better performance in both polarizations than the metal-front end. The FSS-backed Jaumann provides a $-10$ dB reduction of 2D RCS over 61% of the frequency band. It is observed that for this polarization the RCS reduction performance of the FSS-backed Jaumann is slightly reduced as compared with the optimized Jaumann absorber.

The $9$ dB improvement in RCS reduction at 1 GHz for the TE$_z$ polarization (Figure 6(b)) for the FSS-backed Jaumann absorber around 1 GHz is clearly due to the transmission of the FSS surface. The cavity behind the FSS-backed Jaumann absorber has been modeled with a perfectly absorbing back wall, and hence all transmitted waves reaching the back wall are absorbed. Such absorption is used as a rough approximation on antenna absorption. The remaining part
of the frequency band for the TE\textsubscript{2} polarization is performing comparably or slightly degraded as compared with the optimized Jaumann absorber. We get a 5 dB reduction over 64\% of frequency band. The absorption performance degradation of the FSS-backed Jaumann with respect to the optimized Jaumann is the cost of low-frequency transparency. It should be noted that both structures have the same total thickness. However, for the FSS-backed Jaumann, part of the thickness is used for the FSS while for the Jaumann all the thickness is used for absorption purpose. Since greater thickness allows higher absorption performance [22], the degradation of the absorption properties of the FSS-backed Jaumann with respect to the optimized Jaumann is expected. Furthermore, for TE\textsubscript{2} polarization, part of this degradation is due to poor reflective properties of the FSS at low frequencies.

7. Conclusion

The investigation of planar absorption and transparency of the designed structure together with its RCS reduction behavior of a wing-front end shows that absorption persists in the presence of a backing FSS replacing the metal layer; a partial transparency is reached but with a high power loss, 43\% at 1 GHz. The RCS reduction behavior of the structure degrades slightly as compared with an optimized Jaumann absorber with the same total thickness, applied to the curved surface. This degradation is due to the partial transparency of the structure at low frequencies. The inner resistive layer is through a perturbation analysis shown to have a large impact on the 1 GHz transparency in the TE\textsubscript{2} polarization. To reduce the transmission losses, a low-pass behavior of the resistive layers is required, and a continued investigation in this direction is in progress.

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