Research Article

Range-Angle-Dependent Beamforming by Frequency Diverse Array Antenna

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This paper proposes a range-angle-dependent beamforming for frequency diverse array (FDA) antenna systems. Unlike conventional phased-array antenna, the FDA antenna employs a small amount of frequency increment compared to the carrier frequency across the array elements. The use of frequency increment generates an antenna pattern that is a function of range, time, and angle. The range-angle-dependent beamforming allows the FDA antenna to transmit energy over a desired range or angle. This provides a potential to suppress range-dependent clutter and interference which is not accessible for conventional phased-array systems. In this paper, a FDA radar signal model is formed and the range-angle-dependent beamforming performance is examined by analyzing the transmit/receive beampatterns and the output signal-to-interference-plus-noise ratio (SINR) performance. Extensive simulation examples and results are provided.

1. Introduction

Phased-array antennas have been widely used in many modern communication, radar, and navigation systems [1–3]. They offer a directional gain which is useful for detecting/tracking weak targets in the radar look direction while suppressing strong sidelobe interferences from other directions. By controlling the linear phase progression across elements, the beam can be steered to the desired direction precisely. However, a limitation of the phased-array antenna is that the beam steering is fixed in an angle for all the ranges. This limits the system performance to mitigate non-desirable range-dependent signal sources and thus degrading its ability to discern targets of interests from background noise or interference [4]. Moreover, if we want to focus the antenna beams on the directions with different ranges, multiple antennas or a multibeam antenna must be required [5–7].

Recently, a flexible beam scanning array named frequency diverse array (FDA) was proposed in [8]. The most important difference of FDA antenna from a conventional phased-array antenna is that a small amount of frequency increment compared to the carrier frequency is used across the array elements, instead of a linear phase shift like the phased array. Note that the FDA radar discussed in this paper is different from the general multiple-input multiple-output (MIMO) radar with frequency diversity where orthogonal waveforms are employed in each antenna element [9–13]. Here, the same coherent waveform is radiated from each antenna element. The use of frequency increment in FDA generates an antenna pattern that is a function of range, time, and angle [14–17].

The FDA could be used to fulfill multiple mission requirements. It was recognized in [8] that the apparent beam steering angle can be outside of real space. This provides the system designer with an increased design freedom and subsequently additional capability. It was suggested in [18] that by exploiting the multiple degrees of freedom, including space, time, frequency, and modulation, and by partitioning and combining the multidimensional space,
the formed FDA radar can serve multiple missions simultaneously. Two patents have been issued [19, 20], which discussed the increased degrees of freedom. In [21], the continuous beam scanning feature is examined by simulation examples. In [22], the FDA was investigated from a simulation and design perspective, along with a low-cost FDA design.

In [23–25], the application of FDA in synthetic aperture radar (SAR) was investigated. The concept was to increase the angular extent of the measure scene by exploiting the bending-beam phenomenology, in order to decrease the time of the imaging platform in the scene. However, they will reject the received signals that are not frequency-matched to the transmit signals. One FDA bistatic radar system was introduced in [26, 27], which could have applications in low-probability-of-intercept (LPI) radars and limiting returns from undesirable range cells. A concept by merging the waveform diverse MIMO and FDA to increase the degrees of freedom of an antenna array was proposed in [28]. Additional study was presented in [17, 29, 30] to exploit the range-dependent characteristics and the periodic nature of the beampatterns. Although not completely associated with FDA, the phased MIMO proposed in [31] developed a flexible antenna array.

In summary, FDA provides additional degrees of freedom to efficiently gather, and therefore potentially use, scene information. However, current research undermines potential FDA capability, and much further work should be carried out. For example, the FDA apparent scan angle is not equal to the nominal scan angle, which means that precise steering depends on both the range and angle. Consequently, it is insufficient to precisely steer the beam like conventional phased-array antennas.

In this paper, we present a range-angle-dependent beamforming for FDA radar. Different from the papers published in the literature [32, 33], where a large frequency increment is employed to ensure the required waveform orthogonality, a small frequency increment is employed in this paper. The range-angle-dependent data model is formed and the range-angle-dependent beamforming is presented. The system performance is examined by analyzing the transmit-receive beampattern and the output signal-to-interference-plus-noise ratio (SINR) performance.

The remaining sections are organized as follows. The FDA is briefly introduced in Section 2. The range-angle-dependent beamforming is presented in Section 3, along with the SINR analysis. Next, extensive numerical simulation examples and results are provided in Section 4. Finally, Section 5 concludes this paper with a short discussion of future work.

2. FDA Radar System and Signal Model

In conventional phased arrays, it is assumed that the waveform radiated by the array elements is identical, excluding the current amplitude and current phase. Differently, the FDA elements can be either excited with the same waveform or different types of waveforms. Consider a collocated FDA radar system with \( M \) transmit elements and \( N \) receive elements. For simplicity and without loss of generality, here we assume that the waveform radiated from each antenna element is identical but with a frequency increment of \( \Delta f \) Hz as shown in Figure 1. That is, the radiated frequency from each element is

\[
f_m = f_0 + (i - 1) \cdot \Delta f, \quad m = 1, 2, 3, \ldots, M,
\]

where \( f_0 \) is the radar operating carrier frequency. The signal transmitted at the \( m \)th element can be represented by

\[
\phi_m(t) = \exp\{j2\pi f_m t\}. \tag{2}
\]

The signal delayed to a target can then be expressed as

\[
s_m(t) = \exp\left\{j2\pi f_m \left( t - \frac{R_m}{c_0} \right) \right\}, \tag{3}
\]

with

\[
R_m = R_0 - m d \sin \theta,
\]

where \( c_0 \) is the speed of light, \( d \) is the element spacing, and \( \theta \) is the direction angle. The reference point is \((0, 0)\) and a far-field approximation is assumed. If we steer the beam to the angle \( \hat{\theta} \) and range \( \hat{R}_0 \) with the transmit beam weighting factor, we get the following:

\[
w_{T_m}(t) = \exp\left\{j2\pi f_m \left( \frac{\hat{R}_0}{c_0} - \frac{m d \sin \hat{\theta}}{c_0} \right) \right\}. \tag{5}
\]

This weighting function is used to achieve the maximum directional gain in the desired direction angle \( \hat{\theta} \) and range \( \hat{R}_0 \).

The transmit signal seen by the point target is given by

\[
s_T(t) = \sum_{m=0}^{M-1} \exp\left\{j2\pi f_m \left( t - \frac{R_m}{c_0} + \frac{m d \sin \theta_0}{c_0} \right) \right\}
\times \exp\left\{j2\pi f_m \left( \frac{\hat{R}_0}{c_0} - \frac{m d \sin \hat{\theta}_0}{c_0} \right) \right\}
\approx \exp\{j\phi_0\} \frac{\sin(\omega_f M \left( t - \left( (R_0 - \hat{R}_0) / c_0 \right) + \phi_0 \right))}{\sin(\omega_f \left( t - \left( (R_0 - \hat{R}_0) / c_0 \right) + \phi_0 \right))}, \tag{6}
\]

\[
\sin(\omega_f \left( t - \left( (R_0 - \hat{R}_0) / c_0 \right) + \phi_0 \right))
\]
Figure 2: Comparative beampattern between FDA and conventional phased array with $\Delta f = 15$ kHz.

Figure 3: The frequency increment-dependent beam steering angle.

where $B$ denotes $(\sin \theta_0 - \sin \hat{\theta}_0)$.

$$x_n(t) = \sum_{m=0}^{M-1} \exp \left\{ j2\pi f_m \left( t - \frac{2R_0}{c_0} + \frac{md \sin \theta_0}{c_0} \right) \right\}$$

$$\cdot \exp \left\{ j2\pi f_m \left( \frac{\hat{R}_0}{c_0} - \frac{md \sin \hat{\theta}_0}{c_0} \right) \right\}$$

$$\approx \sum_{m=0}^{M-1} \exp \left\{ j2\pi f_m \left( t - \frac{2R_0}{c_0} + \frac{\hat{R}_0}{c_0} + \frac{mdB}{c_0} + \frac{md \sin \theta_0}{c_0} \right) \right\},$$

(7)

where

$$\omega_f = \pi \Delta f$$

$$\phi_0 = \pi \frac{d}{\lambda_0}$$

$$\lambda_0 = \frac{c_0}{f_0}.$$

(8)

The phase term $\exp \{j\Phi_0\}$ is associated with the geometry of the setup.

The signal received by the $n$th element is given by (7). Similarly, using the receive beam weighting factor:

$$w_{Rn}(t) = \exp \left\{ j2\pi f_n \left( \frac{\hat{R}_0}{c_0} - \frac{nd \sin \hat{\theta}_0}{c_0} \right) \right\},$$

(9)

we can get

$$y_n(t) \approx \exp \{j\Phi_1\}$$

$$\times \frac{\sin \left( \omega_f M \left( t - \left( \frac{2(R_0 - \hat{R}_0)}{c_0} \right) \right) + 2\phi_0 M B \right)}{\sin \left( \omega_f \left( t - \left( \frac{2(R_0 - \hat{R}_0)}{c_0} \right) \right) \right) + 2\phi_0 B},$$

(10)

where $\exp \{j\Phi_1\}$ is the phase factors associated with the geometry of the setup. It can be noted that the periodicity of the pattern is halved in range, given that the elapsed time is now a two-way concern.

In the following, we make a summary on the FDA characteristics ($M = N = 15$, $f_0 = 10$ GHz, and $d = \lambda/2$ are assumed in the simulations):

(1) if the frequency offset $\Delta f$ is fixed, the beam direction will vary as a function of the range (see Figure 2), that is, it is a range-dependent beam;

(2) if the range is fixed, the beam direction will vary as a function of $\Delta f$. This means that the FDA also is a frequency-offset-dependent beam as shown in Figure 3;
from the first and (i.e., \(\Delta f = 0\)), the corresponding FDA is just a conventional uniform linear array (ULA)-phased array.

3. Range-Angle-Dependent Beamforming

3.1. Transmit/Receive Steering Vector. Consider a given target at far field, the phase of the signal transmitted by the first element is

\[
\psi_1 = \frac{2\pi f_1}{c_0} r, \quad (11)
\]

\[
a_\phi(\theta, r) = \left[ 1 e^{-j((2\pi f_0 d \sin \theta \sin \phi) + (2\pi M - 1)\Delta f \cdot d \sin \theta \sin \phi/c_0)} \quad \ldots \quad e^{-j((2\pi f_0 (M - 1)\Delta f \cdot r/c_0) \quad (2\pi M - 1)\Delta f \cdot r/c_0))} \right]^T
\]

\[
\approx \left[ 1 e^{-j((2\pi f_0 d \sin \theta \sin \phi) \quad \ldots \quad e^{-j((2\pi f_0 d \sin \theta \sin \phi) \quad (2\pi M - 1)\Delta f \cdot r/c_0))} \right]^T
\]

\[
= 1 e^{-j((2\pi f_0 d \sin \theta \sin \phi) \quad \ldots \quad e^{-j((2\pi f_0 d \sin \theta \sin \phi) \quad (2\pi M - 1)\Delta f \cdot r/c_0))} \right]^T \odot \left[ 1 e^{j((2\pi M - 1)\Delta f \cdot r/c_0) \quad \ldots \quad e^{j((2\pi M - 1)\Delta f \cdot r/c_0))} \right]^T
\]

\[
= a_\theta(\theta) \odot a_r(r).
\]

The phase difference between the signals coming from the first and second elements can then be expressed as

\[
\Delta \psi_1 = \psi_2 - \psi_1 = -\frac{2\pi f_0 d \sin \theta}{c_0} - \frac{2\pi \cdot \Delta f \cdot d \sin \theta}{c_0} + \frac{2\pi \cdot \Delta f \cdot r}{c_0}. \quad (14)
\]

Similarly, the phase difference between the signals coming from the first and \((m-1)\)th elements can be expressed as

\[
\Delta \psi_{m-1} = -\frac{2\pi f_0 (m-1) d \sin \theta}{c_0} + \frac{2\pi (m-1) \Delta f \cdot r}{c_0} - \frac{2\pi \cdot (m-1)^2 \Delta f \cdot d \sin \theta}{c_0}. \quad (15)
\]

The first term is simply the conventional array factor seen frequently in array theory. The second term is of importance because it shows that the radiation pattern of the array depends on the range and frequency increment. Note that the FDA is different from conventional frequency scanning arrays. Frequency-scanned arrays uses the frequency increment as a function of time for all elements, while the FDA uses the frequency increment as a function of the elements.

where \(r\) is the distance between the first element and the observed point target. Similarly, for the second element we have

\[
\psi_2 = \frac{2\pi f_2}{c_0} (r - d \sin \theta) = \frac{2\pi (f_1 + \Delta f)}{c_0} (r - d \sin \theta), \quad (12)
\]

\[
\[
\[
\]

Taking the first element as the reference for the array, the steering vector is given by (13) with \(r\) being the slant range of the first element, where

\[
a_\theta(\theta) = \left[ 1 e^{-j((2\pi f_0 d \sin \theta \sin \phi) \quad \ldots \quad e^{-j((2\pi f_0 d \sin \theta \sin \phi) \quad (2\pi M - 1)\Delta f \cdot r/c_0))} \right],
\]

\[
a_r(r) = \left[ 1 e^{j((2\pi M - 1)\Delta f \cdot r/c_0) \quad \ldots \quad e^{j((2\pi M - 1)\Delta f \cdot r/c_0))} \right]. \quad (16)
\]

Note that, since \(f_0 \gg \Delta f\) and \(r \gg (m-1) d \sin \theta\), in an amplitude sense the approximation is taken by ignoring the second-phase term \(2\pi \cdot (m-1)^2 \Delta f \cdot d \sin \theta/c_0\). The receive steering vector \(a_r(\theta, r)\) can be expressed in an alike manner.

3.2. Transmit/Receive Beamforming. The FDA antenna can form a directional transmit beam that points toward the look direction angle \(\theta_0\) and range \(r_0\). Consider \(s(l)\) with \(l = 1, 2, \ldots, L\) being the number of samples of each transmitted pulse to be the baseband transmitted signal from each element. The baseband equivalent model, in a complex-valued form, of the transmitted signals from the \(M\) transmit elements can be expressed as

\[
a_r(\theta_0, r_0) s(l), \quad (17)
\]

where \(a_r(\theta, r)\) is just the FDA transmit steering vector containing complex-valued elements with unit amplitude and phase determined by the look angle \(\theta\) and range \(r\). The signal seen at a specific location with angle \(\theta\) and range \(r\) is a superposition of the delayed and attenuated version of
the transmitted signals. Suppose the FDA is a narrowband system, the signal seen at that location can then be given by

$$a_t^H (\theta, r_i) a_s^H (\theta, r_0) s(l) = \beta_l s(l),$$

(18)

where the first $a_t(\theta, r_i)$ on the left side is a propagation vector due to propagation effects, and takes the same form of the transmit steering vector. $\beta_l$ is the directional gain in the direction of angle $\theta_l$ and range $r_l$. It follows that the signal seen at the look angle $\theta_0$ and range $r_0$ is given by

$$a_t^H (\theta_0, r_0) a_s^H (\theta_0, r_0) s(l) = \beta_0 s(l),$$

(19)

where $\beta_0 = M$ with $\beta_0$ being the directional gain in the direction of angle $\theta_0$ and range $r_0$. Thus, we can obtain a directional gain of $M$ (the size of the transmit aperture) at the look direction. This is like the well-known property seen at the look angle $\theta_0$ is given by

$$\sigma_{\alpha_l}(\theta_0, r_0) = \sum_{l=1}^{L_0} \alpha_l \beta_l \sigma_{\alpha_l}(\theta, r),$$

(20)

where $\sigma_{\alpha_l}(\theta, r)$ is an $N \times 1$ propagation vector due to the propagation delays from a source to the receive elements, and $n(l)$ is the $N \times 1$ additive white Gaussian noise vector with zero mean and covariance matrix $\Sigma_n^2 I$ with $I$ being an identity matrix. The $a_t(\theta, r)$, similarly defined as the transmit steering vector $a_s(\theta, r)$, is the receive steering vector and

$$y = \frac{\sum_{l=1}^{L_0} x(l)s^H(l)}{\sum_{l=1}^{L_0} |s(l)|^2} \triangleq a_0 u(\theta_0, r_0) + \sum_{l} a_l u(\theta, r) + n,$$

(21)

where the virtual steering vector is

$$u(\theta, r) \triangleq \beta_l \cdot a_t(\theta, r_l).$$

It can be easily proved that $n$ has zero mean and covariance matrix $\Sigma_n^2 I$. Assuming the target/interference complex amplitudes $\alpha_l$ are mutually uncorrelated with zero mean and variance $\sigma^2_l$, the interference-plus-noise covariance matrix can be represented by

$$R_{i+n} = \sum_l \sigma^2_l u(\theta, r_l) u^H(\theta, r_l) + \Sigma_n^2 I.$$ 

(23)

We use the conventional nonadaptive beamforming, which is known to be optimal in the sense that it provides the highest possible output signal-to-noise ratio (SNR) in the background of white Gaussian noise, to derive the expression for transmit/receive beamforming pattern and output SINR performance. For this reason and due to its simplicity, the conventional nonadaptive beamformer has been widely used in antenna array systems [34]. Therefore, we use the conventional nonadaptive beamforming at both the transmit and receive arrays of the FDA radar system and derive expressions for transmit/receive beampattern and output SINR performance.

The nonadaptive beamformer weight vector for the uplink beamforming is given by

$$w_i = \frac{a_i(\theta_0, r_0)}{||a_i(\theta_0, r_0)||}.$$ 

(24)

At the receive array, when the nonadaptive beamformer is employed, the receive beamformer weight vector is given by

$$w_r = u(\theta_0, r_0) = M a_s(\theta_0, r_0),$$

(25)

where $\beta_0 = M$ is used. The corresponding normalized FDA transmit/receive beampattern is

$$G(\theta, r) \triangleq \frac{|w^H_r u(\theta, r)|^2}{|w_r^H u(\theta_0, r_0)|^2}$$

$$= \frac{|u^H(\theta_0, r_0) u(\theta, r)|^2}{||u(\theta_0, r_0)||^4}$$

(26)

$$= \left| a_\theta(\theta) \circ a_\theta(r) \right|^2 \left[ a_\theta(\theta_0) \circ a_\theta(r_0) \right]^2$$

$$= \left| a_\theta(\theta) \circ a_\theta(r) \right|^2 \left[ a_\theta(\theta_0) \circ a_\theta(r_0) \right]^2.$$$$\Sigma_n^2 I.$$

It is noticed that, like the phased-array antenna, the FDA antenna has transmit coherent processing gain; however, the FDA directional gain depends on both range and angle, whereas the phased-array directional gain depends only on the range. This range-angle-dependent beam provides a potential to suppress range-dependent interferences and noise which is not available for conventional phased-array radars.

3.3. SINR Analysis. The output SINR of the FDA radar can be evaluated by

$$\text{SINR} \triangleq \frac{|w^H_r u(\theta_0, r_0)|^2}{w^H_r R_{i+n} w_r}$$

$$= \frac{\Sigma_1^2 M^2 N^2}{\sum \sigma_1^2 |a^H_1(\theta_0, r_0) a_1(\theta, r)|^2 + \sigma_1^2 N},$$

(27)

where $\sigma_1^2$ is the variance of the desired target signal. If the target is observed in the background of few weak interferers which are well separated from the target, then the interference-to-noise power can be attributed to the noise term only. In this case, the SINR for the FDA radar simplifies to

$$\text{SINR} \approx \frac{\sigma_1^2 M^2 N}{\sigma_n^2},$$

(28)
which means that the FDA radar is robust to background noise. In contrast, if the target is observed in the background of strong interference, then we can fairly consider the noise power to be negligible as compared to interference power. In such a case, we have

$$\text{SINR} = \frac{\sigma^2 M^2 N^2}{\sum_i \sigma_i^2 |a^H_{\theta_0, r_0} a_\theta(r_i)|^2 |a^H_{\theta_0, r_0} a_r(\theta_i, r_i)|^2},$$

which means that the FDA radar has a robustness against interference. By inspecting (28) and (29) we can conclude that the FDA radar has a range-angle-dependent beamforming robustness against noise and interference. This provides a capability to suppress the range-angle-dependent noise and interference.

4. Simulation Results and Discussions

In our simulations, we assume a ULA of $M = 10$ array elements used for transmitting the baseband waveform and $N = 10$ array elements at the receiving end. Both the transmitting and receiving elements are spaced half a wave length apart from each other. The additive noise is modeled as a complex Gaussian zero mean spatially and temporally white random sequence that has identical variance in the array sensor. In the following, we performed several typical simulation examples assuming the carrier frequency $f_0 = 10$ GHz and $\Delta f = 30$ kHz.

Example 1 (one target and no interference). In the first example, one target of interest is supposed to reflect a plane wave that impinges on the array from direction of angle $\theta_0 = 10^\circ$ and range $r = 10$ km. Figures 4 and 5 show, respectively, the comparative transmit beampattern and overall transmit/receive beampattern when compared to the conventional
the array from direction angle of interest is assumed to reflect a plane wave that impinges on the array. It can be noticed that the FDA has a range-independent beampattern. The range-dependent beampattern which provides local maxima at different slant ranges. In contrast, the conventional phased-array radar has a range-independent beampattern. The range-dependent beampattern offers a potential to suppress range-dependent interferences. Further, suppose that the target of interest is located at an angle $\theta_0 = 90^\circ$ and range $r = 10\text{km}$. Figure 6 shows the overall transmit/receive when compared to a phased array. It can also be noticed that, in this case, the FDA still has a range-dependent beampattern, whereas the phased array has a range-independent beampattern.

Example 2 (one target and two interferences with the same angle but different range). In this example, one target of interest is assumed to reflect a plane wave that impinges on the array from direction angle of $\theta_0 = 0^\circ$ and slant range of $r_0 = 10\text{km}$. Further, suppose there are two interferences located as direction angle of $\theta_1 = \theta_2 = 0^\circ$ and slant ranges of $r_1 = 8\text{km}$ and $r_2 = 11\text{km}$. The target power is fixed to 0 dB, while the interference power is fixed to 40 dB and SNR is fixed to 10 dB. Figure 7 shows the overall transmit/receive beamspace profile cut at the target’s range. It can be noticed that the FDA radar and conventional phased-array radar have the same overall transmit/receive beamspace profile in the angle dimension. However, they have different beamspace profile in the range dimension as shown in Figure 8. The conventional phased-array radar has no resolution capability in the range dimension. In contrast, the FDA radar has a resolution capability in the range dimension. From (10), we know that the corresponding range resolution is determined by [35]

$$\rho_r = \frac{c_0}{2 \cdot M \cdot \Delta f}.$$  

(30)

This resolution can efficiently suppress the range-dependent interferences which cannot be accessible for conventional phased-array radar.

Example 3 (one target and two interferences with different angle but different range). In this example, one target of interest is assumed to reflect a plane wave that impinges on the array from direction angle of $\theta_0 = 0^\circ$ and slant range of $r_0 = 10\text{km}$. Further, suppose that there are two interferences located as direction angle of $\theta_1 = 0^\circ$ and $\theta_2 = 25^\circ$ and slant ranges of $r_1 = 9\text{km}$ and $r_2 = 1\text{km}$. The target power is fixed to 0 dB, while the interference power is fixed to 30 dB and SNR is fixed to 10 dB. Figure 9 shows the overall transmit/receive beamspace profile cut at the target’s range. It can be observed from this figure that the FDA exhibits a null at the location of the powerful interference located at $\theta = 25^\circ$. Figure 10 shows the overall transmit/receive beamspace profile cut at the target’s angle. It can be observed from this figure that the FDA exhibits a null at the location of the powerful interference located.
at $r = 9$ km. Therefore, the FDA enjoys the advantages of range-dependent beamforming capability, which provides a potential to suppress range-dependent interferences.

**Example 4 (SINR analysis).** In this example, we simulated the SINR performance. The output SINR performance is examined by the nonadaptive conventional beamformer. Figure 11 shows the output SINR versus SNR for the FDA and phased-array radars, where the interference-plus-noise ratio (INR) is fixed to 30 dB. It can be noticed that the output SINR for the FDA radar has a much higher SINR as compared to the phased-array radar. This observation agrees with the fact that the FDA radar has more interference and noise robust than the phased-array radar.

5. **Conclusion**

FDA has received much attention in recent years; however, little work about the range-angle-dependent beamforming and the corresponding applications has been published. This paper proposes a range-angle-dependent beamforming for FDA radars. The use of frequency increment generates an antenna pattern that is a function of range, time, and angle. The range-angle-dependent beamforming allows the FDA radar to transmit energy over a desired range or angle. This provides a potential to suppress range-dependent clutter and interference which is not accessible for conventional phased-array radars. In this paper, the FDA radar signal model is formed and the range-angle-dependent beamforming is presented. The beamforming performance is examined by...
analyzing the transmit/receive beampatterns and the output SINR performance. Numerical simulation examples and discussions are also provided. The results show that the FDA radar indeed provides a significantly SINR performance improvement when compared to the conventional phased-array radar. More importantly, the FDA radar provides a range-angle-dependent beampattern which provides promising potentials for suppressing range-angle-dependent interferences and many other advantages. The applications of the range-angle dependent beamforming in modern radars will be further investigated in our subsequent work.

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