Research Article

On the Cross Correlation Properties of MIMO Wideband Channels under Nonisotropic Propagation Conditions

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Wideband (WB) and ultrawideband (UWB) systems combined with multiple-input multiple-output (MIMO) technology increase both the systems performances and the complexity of the channel models required to evaluate their capabilities. Because in real scenarios waves propagate nonisotropically, the accuracy of the channel model is increased if nonisotropic propagation is considered. The channel bandwidth is the key term in the evaluation process of these systems because large bandwidths introduce frequency selectivity, a unique phenomenon of WB and UWB systems with more complexity in the latter case. This is due to the fact that, unlike WB technology in which the propagating signal is the only affected parameter by the frequency selectivity, in the UWB case, this phenomenon also affects the antenna propagation pattern (APP). In this paper, we developed a novel channel model based on the statistical analysis of two-dimensional cross correlation functions (CCFs) of WB/UWB MIMO nonisotropic channels. A mathematical solution to assess the frequency selective behavior of the UWB APP is also presented. The CCF reveals how the power spectral density (PSD) of the channel is influenced by bandwidth, nonisotropic propagation, and APP.

1. Introduction

The design of high quality wideband (WB) and ultrawideband (UWB) multiple-input multiple-output (MIMO) wireless systems requires the development of two-dimensional (2D) space-time-frequency (STF) channel models along with the evolution from narrowband (NB) to WB/UWB transmissions. This evolution from NB to WB/UWB MIMO channels brings new and more complex propagation phenomena involving the following open questions.

1. What are the main propagation phenomena that appear in a 2D propagation scenario when the channel bandwidth increases?
2. In a 2D scenario, how does the influence of the antenna propagation pattern (APP) on NB channels differ from the influence of the APP on WB/UWB channels characteristics?
3. Is a 2D channel model developed for the study of WB channels adequate for the analysis of UWB channels?

An exhaustive approach to characterize WB/UWB MIMO channels and to answer the questions enumerated above is to statistically analyze the behavior of their space-time-frequency (STF) channel transfer functions (CTFs). We propose a model for both WB and UWB MIMO channels based on two-dimensional (2D) STF cross correlation function (CCF) between the CTFs of two subchannels of a multicarrier (orthogonal frequency division multiplexing, OFDM) channel. A subchannel represents the connection between two antennas, one at the base station (BS) and the other at the mobile station (MS), which transmit/receive the signal at specific time and frequency.

The calculation of the CCF for WB/UWB MIMO channels has attracted the attention of several researchers, for example, [1–5]. Ma and Pätzold extended an NB MIMO channel model to a version adequate for WB channels analysis. The main improvement made to extend the applicability of the NB model was to add the elements which introduce the frequency selectivity caused by the propagation channel. This model presents the 2D CCF derived only for isotropic propagation.
Pätzold and Hogstad developed a WB MIMO channel model with temporal, spatial, and frequency correlation properties. This model presents the 2D CCF derived for both isotropic and nonisotropic propagation assuming a specific geometry of scatterers around receiver [2]. Saleh and Valenzuela (S-V) developed one of the first UWB channel models which was proposed to reproduce the multipath effect of indoor environments. Using S-V results, Zou et al. determined a CCF expression of multiband OFDM-UWB discrete-time base-band channel impulse response [3, 4]. Abdi and Kaveh propose an ST-CCF for a MIMO frequency nonselective Rician fading channel, assuming a one ring of scatterers model around the MS [5]. This model is as an example of an outdoor environment, where the von-Mises probability density function (PDF) is suggested to model the nonisotropic propagation environment around the user.

As a summary, our literature review shows that the general approach is to develop channel models for WB transmissions separated from the channel models for UWB communications. Another trend is to include the effects of the propagation environment (waves clustering, frequency selectivity) and to ignore the frequency selective behavior of the antenna patterns. Because UWB systems were mainly developed for indoor applications the research in the field of UWB outdoor channel modeling was not a priority [6–8]. From the literature review, it was also observed that most of the MIMO-CCF models are based on a specific geometry for scatterers distribution around MS to characterize the nonisotropic propagation.

Lately, UWB technology in combination with MIMO systems finds more and more interest in areas such as location tracking application for outdoor emergency services [9, 10], location tracking and sensor applications for mobile outdoor users [11], and medical [12] and electronic warfare applications [13]. Even more, some research results [14–16] proved that a joint radar and wireless communication system would constitute a unique platform for future intelligent environmental sensing and ad hoc communication networks, in terms of both spectrum efficiency and cost effectiveness. This evolution regarding the use of UWB systems in outdoor environments, as radar or communication system, has led to the formulation of specific requirements aiming at investigating the influence of outdoor propagation on UWB mobile systems [17, 18].

The model proposed in this paper describes the CCF between two subchannels of an outdoor WB/UWB MIMO channel employing directional and omnidirectional antennas and in the presence of nonisotropic wave propagation in 2D space. Instead of assuming a specific geometry for scatterers in space (models based on specific geometries of scatterers in the space are just able to predict the behavior of that particular propagation scenario), we used specific mathematical relationships between the physical parameters of the wireless channel along with appropriate assumptions on their PDFs to derive a channel model based on the CCF of outdoor WB and UWB MIMO channels. This model is an extension of a 2D NB channel model [19]. The evolution through systems with (ultra)wide bandwidths implies new propagation effects that make the NB model inappropriate for WB/UWB transmissions. In order to extend the NB channel model to a version adequate for WB/UWB channels analysis, the mathematical structure of the model needs to be updated with the elements which characterize the new propagation phenomena (represented by channel frequency selectivity, waves clustering) and with the elements which define the performances of the new systems (represented by operating bandwidth, frequency selectivity of the antenna). We represent the nonisotropic scatterers by the Fourier series expansion (FSE) of the PDF of the propagating directions. We also consider the effect of directional and omnidirectional antenna element patterns by the FSE of the APPs. The expression of the CCF turns out to be a composition of linear expansions of Bessel functions of the first kind. Fourier analysis of the derived CCF is used to determine the power spectral density (PSD) of WB and UWB channels in a stationary scenario. The mathematical set-up of the stationary scenario transforms the MIMO channel into a multiple-input single-output (MISO) channel to be analyzed as a special case. The contribution in this 2D-CCF model is fourfold.

1. It includes the main propagation phenomena that appear in 2D WB/UWB MIMO outdoor scenarios and permits the evaluation of combined effects of channel bandwidth, nonisotropic scattering, APP (omnidirectional or directional), and the array interelement distance on the CCF of WB and UWB MIMO channels.

2. This model can be used for the analysis of both WB and UWB propagation channels. The key to apply a model for the analysis of both types of channels is to use the appropriate expressions for APPs. Since WB APP is not frequency selective, the relative bandwidth being a small fraction of the central frequency and the UWB APP is frequency selective and different antenna patterns expressions for these two types of systems should be used. In this paper we propose mathematical expression for UWB APP.

3. It accurately reflects the influence of the MS direction (and speed) on the spectral characteristics of WB and UWB channels.

4. It gives mathematical expressions to evaluate the channel power spectrum of WB and UWB wireless channels.

In [20] a three-dimensional (3D) version of this model was presented. The difference between 2D and 3D versions of the proposed model consists of APP and nonisotropic propagation representations. In the case of the 2D model the APP and the propagation environment are represented depending on azimuth angle spread (AAS). The 3D version of the model represents these two elements as a function of both AAS and elevation angle spread (EAS). From the obtained results it was observed that the 2D model provides a good representation of how the frequency selectivity affects the signal spectrum. A 2D model for most propagation environments is more eligible when we get closer to the ground because a propagation environment behaves similar.
to a 2D environment. Another advantage is that such model represents the propagation environment fairly accurately, with minimum complexity and difficulty. The model presented in this paper is an extension of the conference paper presented in [21]. There are significant differences between the results presented in [21] and the content of the current work, where both the CCF and the PSD are derived and evaluated for WB/UWB MIMO channels while [21] describes only the PSD of WB/UWB systems in a stationary case for MISO channels. The latter paper is mostly about PSD, the derivation process of the CCF (which is the root of the PSD) was not presented, and the model cannot be extended to be used in other scenarios (e.g., indoor propagation, MIMO channels). This statement is also valid for [20] which does not contain the derivation process of the three-dimensional CCF. In the present work are provided details regarding the calculation of the moment generating functions (MGFs- \( \Phi_{r,T} \)) of the delay profile \((r,T)\) and details regarding the calculation of the number of Fourier series coefficients (FSCs) for different PDFs of the AAS necessary to approximate Laplace and von-Mises distributions and how they are further involved in assessing the CCF. Since in [20, 21] CCF was not derived and graphically represented this connection between FSCs, APP, distribution of the propagation environment and CCF behavior cannot be established.

The rest of this paper is organized as follows: in Section 2, the notations and the parameters included in the 2D WB/UWB channels model are described; in Section 3, the WB/UWB CCF expression is derived and is numerically evaluated. In Section 4, the Fourier analysis of the CCF which results in the PSD of the WB and UWB channels is presented; in Section 5, conclusions are presented.

2. Two-Dimensional Wideband/UWB MIMO Model Description

In this section, we describe the propagation scenario, the notations used throughout this paper, and the elements (accompanied by their mathematical expressions) introduced in the structure of the CTF valid for WB and UWB channels. We also emphasize the differences which exist between WB and UWB channel models and how these differences are included in our model.

By definition, a channel is considered WB if the fractional bandwidth \((B_f)\) (the ratio of bandwidth at –10 dB points to center frequency) is \(1\% < B_f \leq 20\%\) while UWB channels are characterized by \(20\% < B_f \leq 200\%\) [22–24]. For both, WB and UWB scenarios, we consider a moving MS with a constant speed vector \(V\) (m/sec) and a fixed BS in a 2D nonisotropic propagation environment. The resulting CTF is determined by the \(p\)th transmitting antenna element at the BS side, the propagation environment, and the \(m\)th receiving antenna element at the MS. CTF description is based on two categories of elements: (C1) elements assigned to the communication system, which are the system bandwidth and APPs at the BS and at the MS, and (C2) elements assigned to the wireless channel represented by nonisotropic propagation, frequency selectivity, and clustering phenomenon.

Both categories of elements enumerated above changed their mathematical representation once with the evolution from NB to WB and UWB channels as it is presented in the following lines.

(C1) The APPs of the \(p\)th and \(m\)th antenna of the BS and the MS array, \(G_p^B(\Theta^B, \omega)\), \(G_m^M(\Theta^M, \omega)\), give the response of the antenna in terms of the propagation directions, \(\Theta\), and frequency, \(\omega\). These functions implicitly include the effect of mutual coupling caused by the neighboring antenna elements. Are all periodic functions of \(2\pi\), where \(\Theta^B\) and \(\Theta^M\) are unity vectors which represent a propagation direction (DOD or DOA) at BS or MS, respectively. We assume that the DOA (to the receiver) and the DOD (from the transmitter) are independent. Therefore, we represent them by their FSCs as follows:

\[
G(\Theta; \omega) = \sum_{k=-\infty}^{\infty} G_k e^{jk\Theta}, \quad G_k = \frac{1}{2\pi} \int_{-\pi}^{\pi} G(\Theta; \omega) e^{-jk\Theta} d\Theta.
\]

For NB channels, it is assumed that the response of the antenna does not change significantly over the bandwidth since the relative bandwidth is a small fraction of the central frequency [19]. This assumption is also true for WB channels but proved to be false once with the evolution through ultrawide bandwidths. UWB antenna patterns are frequency selective and this characteristic should be considered in the design process of UWB channel models. The radiation pattern depicts the relative strength distribution of the transmitted or received power by the antenna. In [25, page 19] it is suggested that, in order to correctly evaluate the received and the transmitted power of UWB signals, the radiation pattern should be determined across the entire frequency spectrum. This requirement is the consequence of the frequency selectivity phenomenon. Thus, according to the method suggested in [25], depending on the signal bandwidth, we propose two approaches for 2D APP calculation as follows:

(a) for WB signals, APP is calculated depending on the central angular frequency, \(\omega\);

(b) for UWB signals, we calculate APP depending on the central frequency and by integrating \(G(\Theta, \omega)\) across all the frequencies of the transmitted signal.

Table 1 presents the APPs of two WB/UWB antennas. The helical (directional) and rectangular (omnidirectional) antennas are often used for antenna arrays and (ultra)wide bandwidth applications [22].

<table>
<thead>
<tr>
<th>Frequency Bandwidth</th>
<th>Antenna Pattern</th>
</tr>
</thead>
</table>
| \(f_{up}, f_{lw}\) | Upper and lower frequencies of UWB channel bandwidth, parameter \(h\) is proportional with the size of the antenna, and \(G_0\) is the real and positive constant antenna gain that varies for each antenna.

(C2) The nonisotropic propagation is characterized by the nonuniform distribution of the waveforms around the MS and the BS in space. In order to describe a nonisotropic channel the PDF of the propagating directions, known as azimuth angular spread (AAS), can be used. In the proposed model, the PDF of the propagation directions is denoted by \(f^B(\Theta^B)\), at the BS, and \(f^M(\Theta^M)\), at the MS. One candidate for
Table 1: 2D antenna radiation patterns.

<table>
<thead>
<tr>
<th>Antenna type</th>
<th>APP, (G(\Theta, \omega)), (\forall \Theta \in [-\pi, \pi))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Helical antenna</td>
<td>WB (\frac{jG_0 \cdot \omega}{2c} \cdot h \cdot \sin \Theta )</td>
</tr>
<tr>
<td></td>
<td>UWB (\frac{1}{(f_H - f_L)} \int_{f_L}^{f_H} jG_0 \cdot \frac{\omega}{2c} \cdot h \cdot \sin \Theta \cdot d\omega )</td>
</tr>
<tr>
<td>Rectangular antenna</td>
<td>WB (\frac{jG_0 \sin((\omega/2c) \cdot h \cdot \sin \Theta))}{((\omega/2c) \cdot h \cdot \sin \Theta)} )</td>
</tr>
<tr>
<td></td>
<td>UWB (\frac{1}{(f_H - f_L)} \int_{f_L}^{f_H} jG_0 \cdot \frac{\sin((\omega/2c) \cdot h \cdot \sin \Theta))}{((\omega/2c) \cdot h \cdot \sin \Theta)} \cdot d\omega )</td>
</tr>
</tbody>
</table>

Table 2: Nonisotropic AAS and corresponding Fourier series coefficients.

<table>
<thead>
<tr>
<th>PDF, (f_\omega(\Theta), \forall \Theta \in [-\pi, \pi)), (\mathcal{F}_k)</th>
<th>Laplace</th>
<th>(\mathcal{F}_k = \frac{e^{-\zeta \sqrt{2\pi}}}{{\sqrt{2\pi}}^s} e^{-\zeta \sqrt{2\pi} \Theta} )</th>
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In these circumstances, the receiver acts as if there was a single multipath component. Due to the better time resolution of WB and UWB systems, multipath components tend to arrive in clusters, rather than in a continuum as it is common for NB channels. The authors of [28] define a cluster as an accumulation of MPCs with similar time of arrivals and angle of arrival. As a consequence of this phenomenon, the CTF of WB/UWB channels is the summation of the dominant \(I\) paths and \(L\) clusters. In the case of NB channels the CTF appeared to be only the summation of \(I\) paths.

The propagation delay of the \(i\)th path within the \(l\)th cluster between the \(p\)th (at the BS) and \(m\)th (at the MS) antenna elements \(\tau_{pm,i,l}\) is decomposed into three components: one component which represents the delay depending on the distance between BS and MS and other two components which vary as a function of the local coordinates of BS and MS:

\[
\tau_{pm,i,l} = \tau_d - (\tau_{p,d} + \tau_{m,i,l}),
\]

where \((\cdot)^T\) represents the transpose operator, \(\tau_d\) is the delay between local coordinates \(O^B\) or \(O^M\), and \(\tau_{p,d}, \tau_{m,i,l}\) represent the propagation delays from antenna \(a^B_p\) to \(a^M_m\) located in their corresponding coordinates \(O^B\) or \(O^M\). \(T_j\) is the cluster arrival rate and is considered to be constant in time. \(\Theta^{B}_{ij}\) and \(\Theta^{M}_{ij}\) were previously defined.

Frequency Selectivity Phenomenon. This refers to the different attenuation that the signal subbands undergo. In our model, the frequency selectivity of the radio channel is characterized by two components. These components are represented by APP (valid only for UWB channels) and by the term \((\omega_{bw}/\omega)^\eta\). The parameter \(\omega_{bw}\) represents the signal bandwidth \(\omega_{bw} = \omega_{H} - \omega_{L}\); \(\omega_{L}\) and \(\omega_{H}\) are the lower and the upper angular frequencies. \(\eta\) depends on the geometric configuration of the objects which produce the signal's diffraction. The following values can be assigned to \(\eta\): 1 (diffraction by corner or tip), 0.5 (diffraction by axial cylinder face), and 1 (diffraction by broadside of a cylinder) [29]. When modeling NB channels, it was adequate to define the path gain depending on the path time-delay [19]. This is not sufficient for WB/UWB MIMO channels.

Clustering Phenomenon. NB systems receive most of the multipath components (MPCs) within the symbol duration. The isotropic propagation environment can be mathematically represented in a similar way, using the following expression of the FSC: \(\mathcal{F}_k = 2\pi f(n) / f(n)\). Von-Mises distributions are specific to WB/UWB MIMO channels.

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where the frequency selectivity phenomenon influences the gain of the channel. In the ray based propagation models which can be applied to signals transmitted at high frequency ranges, like WB and UWB signals, it can be assumed that one propagation path has DOA and time of arrival that does not depend on frequency but has a frequency dependent complex path gain. In our model the path gain of the $i$th path within the $l$th cluster which propagates from the $p$th antenna to the $m$th antenna is expressed as the extension of Friis’ transmission formula $g_{pm} = 1/2\omega_2 r_2$.

When putting together the elements described in (C1) and (C2), the CTF of WB and UWB channels results in the following expression:

$$h_{pm}(t,\omega) = \left(\frac{\omega_{bw}}{\omega}\right)^\eta \sum_{l=1}^L \sum_{i=1}^I G_B^p(\Theta^{\eta}_{il};\omega) \times G_M^m(\Theta^{\eta}_{il};\omega) g_{pm,il} e^{j(\phi_{il}-\omega_2 t_2-\omega_1 t_1)}.$$  \hspace{1cm} (4)

The resulting CTF is represented by the double summation of clusters, $l$, and of the propagation waveforms, $i$, over a maximum number of clusters, $L$, and paths, $I$. Within each cluster (path) the signal reaches the receiver with a response described by the PDFs of some random variables. These random variables are phase, delay, DOD, and DOA. In the resulting CTF each $l$ cluster and implicitly each $i$ waveform is associated with a path attenuation gain, $g_{pm,il}$, a path phase shift, $\phi_{il}$, and a time-varying delay, $\tau_{pm,il}(t) \equiv \tau_{pm,il} + (t/c) V^T \Theta^{\eta}_{il}$. The Doppler shift, of the $i$th received wave within the $l$th cluster, is represented by $\overline{\omega_{il}} = \omega(c) V^T \Theta^{\eta}_{il}$ where $V$ and $c$ are the MS velocity vector and the speed of light, respectively.

### 3. Two-Dimensional Cross Correlation

#### Function of WB/UWB MIMO Channels

The CCF expression of the CTFs, $h_{pm}(t_1,\omega_1)$ and $h_{qn}(t_2,\omega_2)$, of two arbitrary subchannels of a MIMO channel is the result of the following definition:

$$R_{pm,qn}(t_1,t_2,\omega_1,\omega_2) \equiv E\left[h_{pm}(t_1,\omega_1) h_{qn}^*(t_2,\omega_2)\right].$$  \hspace{1cm} (5)

In the CCF expression there are three dimensions: space, two pairs of antenna elements ($p,m,q,n$), time ($t_1,t_2$), and central frequencies ($\omega_1,\omega_2$). According to these three dimensions, we call it STF-CCF. The expectation operation is performed over all introduced random variables. In the presence of enough number of multipaths by invoking the central limit theorem the CTF can be considered a Gaussian random process. Therefore, the above second-order statistics fully characterize statistical behavior of the channel. By replacing (4) with (5), the CCF results in the following expression:

$$R_{pm,qn}(t_1,t_2,\omega_1,\omega_2) = \left(\frac{\omega_{bw1}\omega_{bw2}}{\omega_1\omega_2}\right)^\eta \times \sum_{l=1}^L \sum_{i=1}^I \left\{ E\left[G_B^p(\Theta^{\eta}_{il};\omega_1) G_M^m(\Theta^{\eta}_{il};\omega_1) \times g_{pm,il} \times g_{qn,il} e^{-j\omega_1 \tau_{pm,il} - j\omega_2 \tau_{qn,il}(t_1)}ight]ight. \times E\left[G_B^q(\Theta^{\eta}_{il};\omega_2) G_M^n(\Theta^{\eta}_{il};\omega_2) \times e^{j(\phi_{il}-\omega_1 t_1 - \omega_2 t_2)}ight] \times \left. E\left[G_B^q(\Theta^{\eta}_{il};\omega_2) G_M^n(\Theta^{\eta}_{il};\omega_2) \times e^{j(\phi_{il}-\omega_1 t_1 - \omega_2 t_2)}\right]\right\}.$$  \hspace{1cm} (6)

Regrouping dependent and independent random variables and using the elements described in (C1) and (C2) we obtain

$$R_{pm,qn}(t_1,t_2,\omega_1,\omega_2) = \left(\frac{\omega_{bw1}\omega_{bw2}}{\omega_1\omega_2}\right)^\eta \times \left\{ \sum_{l=1}^L \sum_{i=1}^I \left\{ \left(\tau_{il} \tau_{il}^{-1}\right)^{-1} \times E\left[e^{j(\omega_2 \tau_{il} - \omega_1 \tau_{il} + (\omega_1 t_1 - \omega_2 t_2))}\right] \times E\left[e^{j\phi_{il} - \phi_{il}}\right] \times E\left[G_B^p(\Theta^{\eta}_{il};\omega_1) G_B^q(\Theta^{\eta}_{il};\omega_2) \times e^{j((\omega_1/c) \Theta^{\eta}_{il} - (\omega_2/c) \Theta^{\eta}_{il})}\right] \times E\left[G_M^m(\Theta^{\eta}_{il};\omega_1) G_M^M(\Theta^{\eta}_{il};\omega_2) \times e^{j((\omega_1/c) \Theta^{\eta}_{il} - (\omega_2/c) \Theta^{\eta}_{il})}\right]\right\}.\left(7\right)$$

Equations (8)-(14) present the calculation methodology of the expectations in (7). We present the calculation methodology at the MS side but one should note that the same calculation procedure is valid for the BS side. The calculation of this equation is performed for two cases.

**Case I.** The paths are considered similar and this is equivalent to $i_1 = i_2 = i, l_1 = l_2 = l$; some of the random variables in this expression become identical and, by using the Fourier series
expansions for both APPs and AASs, we are able to calculate these expectations either at the BS or at the MS.

Case 2. The paths are considered to be dissimilar. This is equivalent to \( i_1 \neq i_2, l_1 \neq l_2 \); we assume that the DOD or DOA PDFs of different propagation waves are independent of each other; that is, \( \Theta_{i_1l_1}^M \) and \( \Theta_{i_2l_2}^M \) (or \( \Theta_{i_1l_1}^B \) and \( \Theta_{i_2l_2}^B \)) are independent.

(i) The calculation of the first expectation in (7) is carried out as follows:

\[
E \left[ \left( \tau_{i_2l_2} - \tau_{i_1l_1} \right)^{-1} \right] e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_1l_1})} \times e^{j(\omega_2 \tau_{i_2l_2} - \omega_1 \tau_{i_2l_2})}
\]

\[
= \begin{cases} 
\Phi_{\tau}^{-1} \left( j (\omega_2 - \omega_1) \right) & \text{Case 1,} \\
\Phi_{\tau} \left( j (\omega_2 - \omega_1) \right) \times \Phi_{\tau} \left( -j (\omega_2 - \omega_1) \right) & \text{Case 2.}
\end{cases}
\]  

Equation (8)

The elements denoted by \( \Phi_{\tau} \) represent the moment generating functions (MGFs) of the delay profile \((\tau, T)\) evaluated at the difference between two frequencies. \( \Phi_{\tau} \) suggests that channel similarity depends on frequency differences and not on absolute frequencies. The value of this parameter tends to decay when the frequency difference increases. The definition of the MGF of a random variable \( x \) with the PDF \( f_x(x) \) is defined as follows [30, page 415]: \( \Phi_{\tau}(s) = E[e^{j\tau x}] = \int_{-\infty}^{\infty} e^{j\tau x} f_x(x) dx \). The probability densities of the absolute values of delay times of arrival of paths and clusters used to calculate the MGFs are represented by [31]

\[
P_{\tau_1}(T) = \frac{\Lambda^T \lambda^T e^{-\Lambda T}}{T!}, \\
P_{\tau_2}(r) = \frac{\Lambda^T \lambda^T e^{-\Lambda T}}{(I-1)!},
\]

where \( \Lambda \) and \( \lambda \) are the cluster arrival rate and ray arrival rate. The parameter \( 1/\Lambda \) is typically in the range of 10–50 ns, while \( 1/\lambda \) shows wide variations from 0.5 ns in non-line-of-sight (NLOS) situations to more than 5 ns in LOS situations [32].

(ii) The calculation of the second expectation in (7) is performed as follows.

Considering the case of the planar wave propagation, we take into account the phase contribution of surrounding scatterers by a random phase change parameter \( \phi_{\tau} \sim U[-\pi, \pi) \). Since the path phase shifts, \( \phi_{\tau} \), appear in (4) in the form of \( e^{j\phi_{\tau}} \), the correlations of \( e^{j\phi_{\tau}} \) over different paths and clusters, \( E[e^{j(\phi_{i_1l_1} - \phi_{i_2l_2})}] \), have impact on the channel characteristics. We assume that \( E[e^{j(\phi_{i_1l_1} - \phi_{i_2l_2})}] \) can take the following values:

\[
E \left[ e^{j(\Phi_{i_1l_1} - \Phi_{i_2l_2})} \right] = \begin{cases} 
1, & \text{Case 1,} \\
k^2, & \text{Case 2.}
\end{cases}
\]

(iii) The calculation of the third expectation in (7) is based on the following methodology:

Case 1 : 
\[
E \left[ G_m^M \left( \Theta_{i_1l_1}^M; \omega \right) G_n^M \left( \Theta_{i_2l_2}^M; \omega \right) \times e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_2l_2})} \right]
\]

\[
= \int_{-\pi}^{\pi} G_m^M \left( \Theta_{i_1l_1}^M; \omega \right) G_n^M \left( \Theta_{i_2l_2}^M; \omega \right) \\
\times e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_2l_2})} \times e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_2l_2})} d\Theta_{i_1l_1}^M \\
\times e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_2l_2})} \times e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_2l_2})} \\
\times e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_2l_2})} \\
\times e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_2l_2})} \times e^{j(\omega_1 \tau_{i_1l_1} - \omega_2 \tau_{i_2l_2})}
\]

\[
= \sum_{k=0}^{\infty} \left( \mathbb{G}^M_{m,k} \left( \omega_1 \right) \mathbb{G}^M_{n,k} \left( \omega_2 \right) \mathbb{F}_k \right) I_k \left( \frac{|d_{m,n}|}{c} \right),
\]

where \( \mathbb{G}^M_{m,k} \), \( \mathbb{G}^M_{n,k} \), and \( \mathbb{F}_k \) are the FSCs of the APPs (defined in (1)) and the AAS (defined in (2)) in the corresponding coordinate, respectively, \( I_k(u) \) is the \( k \)-th order Bessel function, \( \mathbb{F} \) is the linear convolution, and \( | \cdot | \) is the Euclidean norm.

The definition of the linear convolution can be formulated as follows [33, page 155]: given two discrete-time signals, \( x_n \) and \( y_n \), the linear convolution between them is defined as follows: \( z_n \approx x_n \ast y_n = \sum_{k=-\infty}^{\infty} x_k y_{n-k} \).

The vectors and \( d_{m,n}^M \) and \( d_{p,q}^B \) are the separation vectors between two antenna elements at the MS (\( m,n \)) and at the BS (\( p,q \)). Large distances often result in less STF correlation as the Bessel functions asymptotically decrease. The norms of \( d_{m,n}^M \) and \( d_{p,q}^B \) represent shifted distances (between \( \omega_1 a_p^B \) and \( \omega_1 a_q^B \)) at the BS and (between \( \omega_2 (t_2 V + a_m^M) \) and \( \omega_1 (t_1 V + a_m^M) \)) at the MS. Parameters \( d_{c}^M \) contain space, time, and frequency separations between \( h_{pm}(t_1, \omega) \) and \( h_{pn}(t_2, \omega) \). These two vectors, illustrate the impact of the antennas' location (spatial correlation), of the carrier frequencies (frequency correlation), of the time indexes and of the mobile speed on the CCF at BS and MS. The value of the \( d_{m,n}^B \) and \( d_{p,q}^B \) can be determined based on the following equations:

\[
d_{m,n}^M \approx \omega_1 (a_m^M - t_2 V), \\
d_{m,n}^M \approx (\omega_2 t_2 - \omega_1 t_1) V + (\omega_1 a_m^M - \omega_2 a_m^M),
\]

\[
d_{p,q}^B \approx \omega_1 a_p^B, \\
d_{p,q}^B \approx \omega_2 a_q^B, \\
d_{p,q}^B \approx \omega_1 a_p^B - \omega_2 a_q^B.
\]
Similar to the calculation in the first case, for the second case, we have (in MS)

\[
\begin{align*}
\text{Case 2 : } & E \left[ C^M_m \left( \Theta_{1,i_1}, \omega_1 \right) C^M_n \left( \Theta_{2,i_2}, \omega_2 \right) 
\times e^{i (\omega_1 \langle a_{m,i_1} \rangle - \omega_1 i_1 \Theta_{m,i_1} - \omega_2 \langle a_{n,i_2} \rangle + \omega_2 i_2 \Theta_{n,i_2})} \right] \\
&= (2\pi)^2 \\
&\times \left[ \sum_{k=-\infty}^{\infty} k \alpha^2 \text{e}^{ikd_m} \mathcal{C}^M_{m,k} (\omega_1) \otimes \mathcal{F}^M_k \left( \frac{d_M}{c} \right) \right] \\
&\times \left[ \sum_{k=-\infty}^{\infty} f \beta^2 \text{e}^{ikd_n} \mathcal{C}^M_{n,-k} (\omega_2) \otimes \mathcal{F}^M_k \left( \frac{d_N}{c} \right) \right].
\end{align*}
\]

We formulate the CCF including both cases using the derivations presented above:

\[
R_{\text{pm,sn}} \left( t_1, t_2, \omega_1, \omega_2 \right) = \frac{\left( \omega_{m,i_1} \omega_{n,i_2} \right)^y}{\left( \omega_1 \omega_2 \right)^y (4\omega_1 \omega_2)} \\
\times \Phi^{-1} \left( j ~ \left( \omega_1 - \omega_2 \right) \right) \Phi_T \left( j ~ \left( \omega_2 - \omega_1 \right) \right) \\
\times \left\{ \mathcal{W} \left( d_{p,i}^B \mathcal{H}_k^B \right) \times \mathcal{W} \left( d_{m,n}^B \mathcal{H}_k^B \right) \right\} \\
\times \left( \omega_{m,i_1} \omega_{n,i_2} \right)^y \left( 4\omega_1 \omega_2 \right)^y
\]

We evaluate the CCF presented in (14) for the scenario, \( i_2 = i_1 = i_2 = i_1 = i_2 = l \), and \( k^2 = 0 \). The final expression of the CCF obtained in this scenario is presented in

\[
R_{\text{pm,sn}} \left( t_1, t_2, \omega_1, \omega_2 \right) = \frac{\left( \omega_{m,i_1} \omega_{n,i_2} \right)^y}{\left( \omega_1 \omega_2 \right)^y (4\omega_1 \omega_2)} \\
\times \Phi^{-1} \left( j ~ \left( \omega_1 - \omega_2 \right) \right) \Phi_T \left( j ~ \left( \omega_2 - \omega_1 \right) \right) \\
\times \left\{ \mathcal{W} \left( d_{p,i}^B \mathcal{H}_k^B \right) \times \mathcal{W} \left( d_{m,n}^B \mathcal{H}_k^B \right) \right\}
\]

where

\[
\mathcal{W} (d, \mathcal{H}_k) \equiv 2\pi \sum_{k=-\infty}^{\infty} \int_{-\infty}^{\infty} e^{i k d} \mathcal{H}_k (\omega) \left( \frac{|d|}{c} \right) \tau,
\]

\[
\mathcal{H}_k = \mathcal{G}_k (\omega_1) \otimes \mathcal{G}_k^* (\omega_2) \otimes \mathcal{F}_k.
\]

3.1. CCF Numerical Evaluation. Low correlation between received signals is a necessary condition for good MIMO performances. This low correlation is achieved when each antenna provides a unique weighting for each cluster with multipath components. In order to achieve space diversity with MIMO systems, the antennas need to be as compact as possible but also to be able to recover signals with dissimilar multipath fading. An optimal solution may be a low threshold for correlation rather than zero correlation between antennas. Low correlation is often considered when CCF \( < 0.7 \). Correlation values are especially significant in applications where the evaluation of the channel capacity is necessary.

Figure 1: Fourier series coefficients for two AAS PDFs, to approximate Laplace and von-Mises distributions (with orders of nonisotropy \( n = 3, 10 \)) determined to correspond to the real PDFs for the nonisotropic propagation environment.
Figures 2 and 3 depict the effect of the distribution of the nonisotropic propagation environment, the APP (directional, omnidirectional), the antenna spacing, and the carrier frequency offset, $\Delta f = f_2 - f_1$ (where $f_1$ is constant at 5 GHz for WB channels and at 3.1 GHz for UWB channels) on the normalized CCF $|R(t_1, t_2, \omega_1, \omega_2)|^2 / |R(t_1, t_1, \omega_1, \omega_1)|^2$. In the reported figures, the unit for the antenna spacing is half of the highest frequency of the signal bandwidth, $\lambda/2 = c\pi/\omega_H$, where $\omega_H = 2\pi f_H$.

In [22, page 26] measurement results for spatial correlation of UWB MIMO channels with omnidirectional antennas are presented. The measured data show that the spatial correlation is a monotonously decreasing function of the antenna distance. A complete characterization of MIMO UWB channels correlations is provided in [34]. It was stated that, for about 4 cm antenna spacing, the correlation function follows a pattern of the first kind zeroth-order Bessel function with distance. It was also found that a value of 2 cm for antenna spacing is sufficient for CCF $\leq 0.5$. In [35–37] it was stated that the CCF values are higher for directional antennas than for omnidirectional antennas. This is because their beamwidth limits the effective angular spread and their ability to capture multipath signals from all directions. The results, regarding the spatial correlation, presented in Figures 2 and 3, are consistent with the CCF’s behavior described in the mentioned references. In the reported figures the influence of the frequency correlation is also evaluated. It can be observed how CCF decreases as $\Delta f$ increases. This decrease results not only from the Bessel functions (as the central frequencies appear in the Bessel operands) but also from the term produced by the MGF of the delay profile. As the figures show, the CCF is maximum when $\Delta f = 0$ and when there is no separation between the antennas of the MIMO system. CCF also decreases when WB APP is replaced by UWB APP. This is because UWB signals offer a higher degree of diversity owing to their abundant multipaths. In Figure 1 it can be observed that the number of FSCs necessary to approximate Laplace PDF is larger than the number of FSCs necessary to approximate von-Mises distribution. This indicates that a propagation environment described by Laplace PDF is characterized by a higher order of nonisotropy which provides better diversity and lower correlation between MIMO subchannels. The graphical representations of CCF show that the correlation decreases faster when the environment has
Laplacian distribution, for both WB and UWB channels. In [38] the influence of parameters like antenna element spacings, environment parameters, and scattering density, on the spatial correlation properties of multilink MIMO channels, was presented. Based on different propagation phenomena like those previously mentioned new key technical issues in developing and realizing multiinput multioutput technology were presented in [39].

4. Fourier Analysis of the 2D STF-CCF of WB/UWB MIMO Channels

The derived CCF can be used to analyze the power spectral density (PSD) of WB and UWB MIMO channels. PSD gives the distribution of the signal power among various frequencies and also reveals the presence or the absence of repetitive patterns and correlation sequences in the signal process. These structural patterns are useful in a wide range of applications like data forecasting, signal detection and coding, pattern recognition, and radar and decision-making systems. The analyzed PSD corresponds to a multiple-input single-output (MISO) channel which is a particular case of MIMO channel. This analysis corresponds to the stationary scenario when $\omega_1 = \omega_2 = \omega$ and $m = n = 1$. Considering $\Delta d^M = \Delta V + \Delta(t_2 - t_1)$ we get

$$R_{p,q} \left( t_1, t_2, \omega, \omega \right) = \frac{\pi \omega_{p,q}^2}{2 \omega_{p,q}^2 \mathcal{F}^B \left( d_{p,q}^B, \mathcal{R}^B \right)} \times \sum_{k=-\infty}^{\infty} j^k e^{j k \Delta V} \left( \mathcal{X}^M_{1,k} (\omega) \otimes \mathcal{X}^M_{1,k} (\omega) \otimes \mathcal{X}^M_{1,k} \right)$$

where $\mathcal{F}[\cdot]$ denotes the Fourier transform and $T_k(\Lambda) \equiv \cos \left[ k \cos^{-1}(\Lambda) \right]$ is the $k$th-order Chebyshev polynomial.
Figure 4: PSD of WB channels, MS moves in the positive direction of the x-axis ((a), (b)) and y-axis ((c), (d)), two antenna types employed at the MS, nonisotropic propagation (Laplacian or von-Mises distributed), and isotropic environment (uniformly distributed).

function of the first kind [16], page 486], the Fourier transform of the CCF derived for stationary case versus the time-difference index, $\Delta t \doteq t_2 - t_1$, results in the following equation:

$$
R_{p_1,q_1}(\Lambda, \omega) \doteq \int_{-\infty}^{\infty} e^{-j\Lambda \Delta t} R_{Y_{p_1,q_1}}(t_1, t_2, \omega, \omega) \, d\Delta t
$$

$$
= \frac{\omega_{bw}^2}{2\omega_{bw}^2} \mathcal{W} \left( d^M_{y,p}, \mathcal{H}_k^B \right) \frac{\pi c}{|V|}
$$

$$
\times \sum_{k=-\infty}^{\infty} \left[ (e^{jk\xi V} \mathcal{G}_{1,k}^M (\omega) \otimes \mathcal{G}_{1-\kappa}^M (\omega) \otimes \mathcal{F}_k^M )C_k \right],
$$

(19)

where $\mathcal{H}_k^B \doteq \mathcal{G}_{p_k}^B (\omega) \otimes \mathcal{G}_{q_k}^B (\omega) \otimes \mathcal{F}_k^B$ and $\Lambda$ is a frequency variable in the interval $-(\omega/c)|V| < \Lambda < (\omega/c)|V|$. Note that $R_{p_1,q_1}(\Lambda, \omega) = 0$ for all $|\Lambda| \geq (\omega/c)|V|$. We denote $C_k = T_k(c\Lambda/|V|\omega)/\sqrt{1 - (c\Lambda/|V|\omega)^2}$, $T_k(\cdot)$ is the Chebyshev polynomials which form a complete orthogonal set on the interval $-1 \leq u < 1$, with respect to the weighting function $1/\sqrt{1 - u^2}$.

Therefore, any bandlimited CCF (in the interval $-(\omega/c)|V| \leq \Lambda \leq (\omega/c)|V|$) can be expanded in terms of Chebyshev polynomials as shown in (19). The PSD, $R_M^M(\Lambda)$, is the last term in (19) and shows the channel variations caused around or by the MS speed and direction and the impact of
the nonisotropic environment, of the channel bandwidth, and of the APP:

\[ R^M(\Lambda) \triangleq \sum_{k=-\infty}^{\infty} e^{j k \Delta \nu} \left( \mathcal{F}_{\text{WB}}^M(\omega) \otimes \mathcal{F}_{1,k}^M(\omega) \otimes \mathcal{F}_{-k}^M(\omega) \right) C_k. \]  

(20)

In Figures 4 and 5, the PSD of WB and UWB signals is depicted. The presented results illustrate (20) with the influence of the following elements.

(i) The channel bandwidth for WB channels was equal to 200 MHz with the central frequency \( f = 2.5 \) GHz. For UWB channels the results correspond to a bandwidth delimited by \( 3.1 \div 10.6 \) GHz,

(ii) APPs, specific to WB and UWB systems, employed at the MS side (directional and omnidirectional antennas),

(iii) nonisotropic propagation environment around the MS (Laplacian or von-Mises PDFs),

(iv) direction of the MS speed, the positive \( x \)-axis or \( y \)-axis direction.

From the comparative analysis of PSD obtained for WB and UWB channels relevant conclusions can be drawn regarding its distribution in the interval \( -(\omega/c)|V| < \Lambda < (\omega/c)|V| \) as follows.

(i) The PSD fluctuations are more pronounced in the case of UWB channels compared to WB channels. This is
the effect of the frequency selectivity phenomenon whose effects increase with signal frequency and bandwidth. The noticeable increase of frequency selectivity that occurs in the case of UWB channels clearly differentiated them from other channels with narrower bandwidth. This characteristic may be helpful in the identification process of the channel’s type for its bandwidth from its PSD only. In Figures 4(a), 4(b), 5(a), and 5(b) it can be observed that MS movement in the positive direction of the x-axis produces a PSD with larger values at positive \( \Lambda \) than at negative \( \Lambda \). This asymmetry of the PSD is also determined by the Doppler spectrum which concentrates towards positive frequency axis.

(ii) The PSD shape is asymmetrical (Figures 4(a), 4(b), 5(a), and 5(b)) or symmetrical (Figures 4(c), 4(d), 5(c), and 5(d)) as a consequence of the interaction between the beam of the antenna pattern, the direction of the MS speed, and the distribution of the propagation directions around the MS. Figures 4(c), 4(d), 5(c), and 5(d) depict the shape of the PSD which is symmetrically distributed around \( \Lambda = 0 \), because the PDF which characterizes the nonisotropic propagation and the APPs are symmetrical around \( \Theta = 0 \) and are perpendicular towards the speed direction.

For both WB and UWB channels, the maximum Doppler shift is \( (\omega/c)|V| \) (i.e., \( R^M(\Lambda) = 0 \), if \(|\Lambda| \geq (\omega/c)|V|\)).

The obtained results are consistent with those proposed in [19, 37]. In [19] the PSD of a narrowband channel in nonisotropic propagation environment is similar to the PSD shape we obtained for WB channels. Between our results and those presented in [38] there are similarities regarding the U-shape of the PSD but there are also differences determined by parameters specific to channels with large bandwidths, like frequency selectivity, higher central frequency, and APPs typically used for this type of systems. Comparing the PSD shape obtained for WB channels with the PSD obtained for UWB channels and even with the PSD obtained for narrowband channels in [19] we can conclude that the channel bandwidth has a great influence on the channel power spectrum. With the increase of signal bandwidth larger variations can be observed over (because of the increased frequency selectivity) the PSD of UWB channels.

5. Conclusion

In this paper we proposed an outdoor channel model for WB/UWB MIMO systems, with moving receiver, based on the mathematical expression of a 2D STF-CCF. The impact of channel bandwidth, nonisotropic propagation, and omnidirectional and directional antennas on the CCF was evaluated. The increase of the channel bandwidth (from WB to UWB) generated the necessity to develop two approaches for the APPs calculation. The derived CCF appeared to be a combination of linear series expansion of Bessel functions. The coefficients of the CCF expansion are represented by the convolution of the Fourier coefficients of the APPs and the AASs specific to WB and UWB channels. The Fourier transform of the CCF in a stationary scenario showed that the PSD diverges from the U-shaped function, that is, Clarke/Jake model. This deviation depends on the AAS, the employed antennas, and the MS speed direction. The increase of the channel bandwidth also generated a more frequency selective PSD for UWB channels compared to the PSD of WB channels. This information can be useful for applications of signal detection and recognition since the increased frequency selectivity makes the identification of the channel’s type for its bandwidth from its PSD only possible.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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