Research Article

A New Methodology for Multiscale Myocardial Deformation and Strain Analysis Based on Tagging MRI

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Myocardial deformation and strain can be investigated using suitably encoded cine MRI that admits disambiguation of material motion. Practical limitations currently restrict the analysis to in-plane motion in cross-sections of the heart (2D + time), but the proposed method readily generalizes to 3D + time. We propose a new, promising methodology, which departs from a multiscale algorithm that exploits local scale selection so as to obtain a robust estimate for the velocity gradient tensor field. Time evolution of the deformation tensor is governed by a first-order ordinary differential equation, which is completely determined by this velocity gradient tensor field. We solve this matrix-ODE analytically and present results obtained from healthy volunteers as well as from patient data. The proposed method requires only off-the-shelf algorithms and is readily applicable to planar or volumetric tagging MRI sampled on arbitrary coordinate grids.

1. Introduction

Cine MRI, combined with (C)SPAMM (Complementary SPAtial Modulation of Magnetization) encoding technology [1–4], admits disambiguation of local tissue motion, thus enabling the extraction of myocardial deformation and strain [5], which are known to correlate with cardiac pathologies. In particular, Götte et al. found that strain is more accurate than geometry in discriminating dysfunctional from functional myocardium [6]. Deformation and strain can be operationalized in various ways, either without explicit a priori regularization, or through exploitation of sparse constraints combined with interpolation and/or regularization [5, 7–33]. Possible encodings are (DENSE) Displacement ENCoding with Stimulated Echoes, cf. Aletras et al. [2], and (HARP) HAmonic Phase, cf. Osman et al. [20, 21]. Tagging-based methods using HARP technology form our point of departure, compare with Figure 1 for an illustration.

Given a dense motion field within the myocardium, our aim is to devise an operational procedure for direct extraction of myocardial deformation and strain. By “direct” we mean that we seek to obviate sophisticated preprocessing steps, such as segmentation of, or interpolation between tag lines, and finite element methods explicitly coupled to the tagging pattern. Although such sophisticated “indirect” procedures exist and have been proven powerful, they require specific algorithmics that is neither trivially implemented nor readily available. Instead we aim for a multiscale, optimally conditioned, intrinsically parallelizable, linear algorithm for obtaining deformation (and thus strain) in analytically closed form. Optimal conditioning is achieved by exploitation of the scale degree of freedom in the definition of spatiotemporal differential image structure. In addition we aim to minimize the number of extrinsic control parameters. We believe that the parsimony of our method facilitates applicability and optimization, since only off-the-shelf algorithms (linear filtering and inversion of
linear systems) are needed in our computation of myocardial deformation and strain.

Our approach is as follows. To begin with, the velocity gradient tensor field, which is the prerequisite for the model we present in this paper, is obtained using the multiscale motion extraction algorithm for scalar image sequences proposed by Florack et al. [12]. This algorithm is adapted to the situation of tagging MRI data [10, 13]. Slick encoding proposed by Florack et al. [12]. This algorithm is adapted motion extraction algorithm for scalar image sequences we present in this paper, is obtained using the multiscale gradient tensor field, which is the prerequisite for the model extraction algorithm used to provide the input velocity gradient tensor field, loc. cit.) Some experimental results are given in Section 3 to demonstrate the feasibility of our approach.

Section 4 concludes our work with a summary and briefly sketches work in progress.

Data acquisition details for the scans used in this paper are given in the appendix.

2. Theory

2.1. Deformation. The velocity gradient tensor, with components $L^a_{\beta}$ relative to a coordinate frame, relates the rate of change of a momentary infinitesimal line element $dx^a$ to the line element $dx^\beta$ itself. (One can either view $dx^a$ as the $a$-component of an “infinitesimal vector” attached to a fiducial material point in Euclidean space and representing a directed material line element, that is, an “infinitesimal” number—or as the $a$th element of a local covector frame, depending on engineering or mathematical mind set.) From $d\dot{x}^a = dv^a$ it follows, using the chain rule, that

$$d\dot{x}^a = L^a_{\beta} dx^\beta$$

(1)

(The Einstein summation convention applied here will be used henceforth.) The numbers $L^a_{\beta}$ constitute a matrix $L$ with row and column index $a, \beta$. To get an estimate of this tensor field we have applied the algorithm of Florack et al. and van Assen et al., solving a linear system of algebraic equations enforcing optimal conditioning through scale selection. The reader is referred to the literature for details [10, 12, 13].

Tissue deformation can be described by a map $f : M \rightarrow N : x(X, t_0) \rightarrow x(X, t)$, in which $x(X, t)$ denotes the spatial position of a material point at time $t$, with reference position $X = x(X, t_0)$ at time $t_0$ (Lagrange picture). Domain $M$ and codomain $N$ are copies of the deformable tissue medium (a subset of $\mathbb{R}^n$) at times $t_0$, respectively, $t \geq t_0$. We fix $t_0$ so as to correspond to end-diastole. (During the diastolic phase the heart relaxes and is refilled with blood. It is followed by the
systolic phase, in which the heart contracts. It is this phase that traditionally receives most attention by cardiologists.)

The associated differential map,

$$f_s \equiv df : TM_x \rightarrow TN_x : v \mapsto f_s(v) = \gamma^t \nabla f_s,$$

relative to a basis \(\{e_i\}\) of \(TN_x\), provides a local linearization of tissue deformation, that is, the deformation tensor. Here \(TM_x\) is the tangent space of \(M\) at the fiducial point \(x = x(X,t_0)\), and \(TN_x\) that of \(N\) at the \(f\)-mapped point \(x = x(X,t)\). The matrix \(F(t,t_0)\) of this linear map relative to the local coordinate charts \([x^a, N]\) and \([X^i, M]\) is given by the Jacobian

$$F^a_i = \frac{\partial x^a}{\partial X^i}.$$

By virtue of the chain rule, the relation between deformation and velocity gradient tensors, (1) and (3) is given by the first-order ODE [35]

$$\dot{F} = L_F,$$

subject to an initial condition, namely, \(F(t = t_0, t_0) = I\).

Equivalently,

$$F(t, t_0) = I + \int_{t_0}^t L(s) F(s, t_0) \, ds.$$

Only for stationary flows, that is, \(L(t) = L_0\) pointwise constant, this initial value problem admits a trivial solution \(F(t, t_0) = \exp((t - t_0)L_0)\). (For the sake of simplicity the spatial dependency of all field entities is suppressed in the notation.) However, we do not have stationarity, and so we must proceed more carefully.

Equation (5) induces an expansion known as the matricant, compare with Gantmacher [35]:

$$F(t, t_0) = I + \int_{t_0}^t L(r) \, dr + \int_{t_0}^t L(r) \int_{t_0}^r L(s) \, ds \, dr + \cdots.$$

The matricant has the following property:

$$F(t, t_0) = F(t, t_1)F(t_1, t_0) \quad (0 < t_1 < t).$$

It follows that, if we split the interval \([t_0, t]\) into \(n\) parts by using intermediate points \(t_1, \ldots, t_n\) separated by \(\Delta t_k = t_k - t_{k-1}\) \((k = 1, \ldots, n)\), with \(t_0 = t_1\),

$$F(t, t_0) = F(t, t_n) \cdots F(t_1, t_0),$$

with \(t_0 < t_1 < \cdots < t_{n-1} < t_n = t\).

For an infinitesimally narrow time interval \([t_{k-1}, t_k]\) we have by approximation

$$F(t_k, t_{k-1}) = I + L(t^*_k) \Delta t_k + \text{higher order terms in } \Delta t_k,$$

in which \(t^*_k\) is any point satisfying \(t_{k-1} \leq t^*_k \leq t_k\). Equations (8) and (9) give rise to a representation in terms of a so-called multiplicative integral [35]:

$$F(t, t_0) = \int_{t_0}^t \left(1 + L(r) \, dr \right)$$

$$\overset{\text{def}}{=} \lim_{\Delta t_k \rightarrow 0} \left(1 + L(t^*_k) \Delta t_k \right) \cdots \left(1 + L(t^*_1) \Delta t_1 \right).$$

One recognizes the multiplicative counterpart of the Riemann sum approximation for ordinary (additive) integrals. One can show that this is identical to

$$F(t, t_0) = \int_{t_0}^t \exp(L(r) \, dr)$$

$$\overset{\text{def}}{=} \lim_{\Delta t_k \rightarrow 0} \exp(L(t^*_k) \Delta t_k) \cdots \exp(L(t^*_1) \Delta t_1).$$

Several properties of the deformation tensor are manifested in this representation. For instance, for square matrices \(A, B\), one has

(i) \(\det AB = \det A \det B\),

(ii) \(\det(I + \epsilon A) = 1 + \epsilon \text{ trace } A + O(\epsilon^2)\),

(iii) \(\det A = \text{ trace } A\).

Consequently,

$$\det F(t, t_0) = \int_{t_0}^t (1 + \text{ trace } L(r) \, dr) = \int_{t_0}^t \exp(\text{ trace } L(r) \, dr).$$

In particular, a divergence free velocity field (\(\text{div } v = \text{ trace } L = 0\)) preserves volumes: \(\det F(t, t_0) = 1\). Furthermore, \(\exp A \exp B = \exp(A + B)\) if \([A, B] = 0\), whence for a stationary velocity field one obtains \(F(t, t_0) = \exp((t - t_0)L_0)\), as we already noticed. Finally, the multiplicative integral suggests a straightforward numerical approximation, namely by using either (10) or (11) without limiting procedure. In this case the two representations are of course no longer identical. For computational efficiency we have chosen the former, with \(\Delta t_k = \Delta t\) corresponding to the (constant) frame interval of our tagging MRI sequence, and \(t^*_k = k \Delta t\).

2.2. Strain. On the basis of the differential map \(f_s\), (2), and its transpose \(f^*_s\), one defines an intrinsic mapping on \(TM_X\), known as the Lagrangian strain tensor [36],

$$E \equiv \frac{1}{2} \left( f^*_s \circ f_s - \text{ id}_{TM_X} \right) : TM_X$$

$$\rightarrow TM_X \ : v$$

$$\rightarrow E(v) = v^i E^j_i\epsilon_j,$$

relative to a basis \(\{\epsilon_j\}\) of \(TM_X\), with mixed tensor components

$$E^j_i = \frac{1}{2} \left( g^{ij} E^p_i h_{qp} F^q_0 - \delta^j_i \right).$$

Here \(g^{ij}\) are the components of the dual Euclidean metric tensor in domain coordinates \([X^i, M]\), and \(h_{qp}\) are those
pertaining to codomain coordinates \( \{x^a, N\} \). \( E \) vanishes identically if \( f_\alpha \) is an isometry, thus \( E \) captures genuinely nonrigid deformations.

The general coordinate convention, see (14), which admits different bases for deformed and undeformed configurations, is instructive. Although one would normally prefer identical bases, let us consider the case in which the metric components \( h_{ab} \) are those induced from \( g_{ij} \) by the deformation map itself (carry-along). That is, we assume that the coordinate frame for the deformed configuration is just the deformed coordinate frame of the reference configuration. One then expects the Lagrangian strain tensor to be nullified, because everything, including the local configuration. One then expects the Lagrangian strain tensor is just the deformed coordinate frame of the reference configuration. Equation (14) permits us to use whatever bases we may consider convenient. This may be beneficial in certain situations, for example, those that suggest spherical, cylindrical or other coordinate systems depending on the configuration of acquisition data, compare with the phantom study by Young et al. [37], and the desired output representation.

Below we consider a single Cartesian coordinate system for both domain and codomain. (In such a system the representations of the various metric tensors, \( g_{ij} \) and \( h_{ab} \) and their duals, \( g^{ij} \) and \( h^{ab} \), all simplify to identity matrices.) Our analysis is confined to a single short-axis plane, whence \( n = 2 \), that is, we only account for in-plane motion components. The theory trivially generalizes to \( n = 3 \) and non-Cartesian coordinate grids.

3. Experiment

Figure 2 illustrates various scalar fields extracted from the strain tensor field, (13) and (14), by contraction with a pair of local unit vectors, namely radial (\( r \) = radial) and azimuthal (\( c \) = circumferential) basis vectors of the polar coordinate system centered at the midpoint of the region of interest, and those defining the strain tensor’s eigensystem. If \( u, v \in TM_X \) are two such unit vectors, then the local scalar quantity derived from the strain tensor is given by the inner product \((u, E(v)) = (E(u), v) = g_{ij} u^i E^j_\ell v^\ell \). Tensor components are evaluated in Cartesian coordinates.

Figure 3 illustrates temporal evolutions of these quantities spatially averaged over the respective regions of interest, together with their standard deviations. (Thus one should not confuse standard deviations with uncertainties in this plot.) Table 1 shows statistics for three healthy volunteers. Figure 4 shows that strain fields have the potential to detect local pathology.

4. Conclusion and Future Work

We have proposed a novel, simple and robust linear model for extracting myocardial deformation and strain. Material motion and gradient velocity are determined by a multiscale linear system of algebraic equations for the phase images extracted from the tagging MRI data. These phase images are scalars, not densities, and are not hampered by tag fading due to \( T_1 \) relaxation.

We have analytically solved the linear matrix-ODE governing myocardial deformation. By discretizing the closed-form solution we have subsequently solved for the induced Lagrangian strain tensor field, yielding results that are typical for healthy volunteers, compare with Garot et al. [14], and atypical for a patient with a medical history of small infarcts on either side of a deviatory region and...

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Table 1: Spatial average and standard deviation of strains from three healthy volunteers (labels I, II, III) over base, mid, and apex short-axis cross-sectional ROIs at that time frame at which \( E_{\text{max}} \) has attained its maximum in mid-slice (\( t_1 = 16, t_{\text{II}} = 15, t_{\text{III}} = 14 \)). Rows correspond to, from top to bottom, \( E_{\text{cc}}, E_{\text{rI}}, E_{\text{cI}}, E_{\text{max}}, \) and \( E_{\text{min}} \).
Figure 2: Color-coded strain fields in short axis mid-slice cross-sections, time frames 1, 6, 11, 16, 21 (a full heart cycle subtends 42 frames), regularized through Gaussian convolution with spatial scale $\sigma = 1.0$, for one healthy volunteer. First row: Circumferential strain $E_{cc}$. Second row: Radial strain $E_{rr}$. Third row: Shear strain $E_{cr}$. Fourth row: Minimal strain eigenvalue $E_{\text{min}}$. Fifth row: Maximal strain eigenvalue $E_{\text{max}}$.

confirmed by late-enhancement MRI. This demonstrates the feasibility of our method. An advantage of our method is that only off-the-shelf algorithms are needed. This serves clarity, facilitates optimization, and enables implementation on dedicated hardware. The method is applicable in any spatial dimension, does not require conversion to a Cartesian sampling grid, is optimally conditioned due to local scale selection, and is readily adapted to other modalities such as velocity encoding MRI.

Our quantitative results in this feasibility study demand further evaluation so as to reveal their statistical significance and clinical value. Furthermore, experiments based on carefully controlled synthetic or phantom data will allow us to disclose the physical significance and numerical tolerance of the mathematical framework in terms of ground truth deformation properties. Moreover, by virtue of the transparent mathematical theory, it is also possible to assess tolerances on the basis of theoretical error propagation models [38], which
Figure 3: Temporal evolution of scalar strain quantities over the first half of the heart cycle (i.e., mostly systolic) in mid-slice cross-section. Error bars indicate standard deviations over the spatial ROI in each time frame, thus capturing all sources of variation due to (primarily) actual spatial variability, noise, and numerics. Legends explain the various graphs. Notice the strong correlation between the extrinsic (polar system related) and intrinsic (eigensystem related) strains. (In the eigensystem, shear strain vanishes identically.)

Figure 4: Radial (a) and circumferential (b) colour-coded strains in a basal short-axis slice at approximately end-systole for a patient. Red arrows on the left indicate regions where the respective strain values deviate from normal. These regions were confirmed to be static by a cardiologist. The patient's anamnesis mentions small infarcts on either side of these regions. Their locations, indicated by black arrows, are highlighted in late-enhancement MRI.

Appendix

Data Acquisition Details

The short-axis MR tagging image data used in this study were acquired with a Philips Intera 1.5 T scanner from three volunteers (Table 1) and a patient in basal, midventricular, and apical slices. The patient (Figure 4) had a history of severe stenoses, and small infarction areas confirmed with late-enhancement MRI 14 minutes after gadolinium contrast injection. A 2D multishot gradient-echo with Echo
Planar Imaging (EPI factor 9) with breath-holding in end-expiration was used. Scan parameters were: TE 4.4 ms, TR 19 ms, flip angle 10°, field-of-view 300 mm, scan matrix 128, acquisition voxel size $2.34 \times 2.68 \times 8 \text{mm}^3$ reconstructed into $1.17 \times 1.17 \times 8 \text{mm}^3$. Tagline spacing was 8 mm.

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References


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