Research Article

Characterization of the Pore Filling of Solid State Dye Sensitized Solar Cells with Photoinduced Absorption Spectroscopy

Carol Olson, Dirk Veldman, Klaas Bakker, and Frank Lenzmann

Solar Energy, Energy Research Centre of the Netherlands (ECN), Westerduinweg 3, 1755 LE Petten, The Netherlands

Correspondence should be addressed to Carol Olson, olson@ecn.nl

Received 15 October 2010; Revised 26 April 2011; Accepted 16 May 2011

Academic Editor: Dinko Chakarov

Copyright © 2011 Carol Olson et al. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Near steady-state photoinduced absorption (PIA) and UV-Vis absorption spectroscopy are used to characterize the pore filling of spiro-MeOTAD (2,2',7,7'-tetrakis-(N,N-di-p-methoxyphenylamine)9,9'-spirobifluorene) into the nanoparticulate TiO2 electrode of a solid-state dye-sensitized solar cell (ssDSC). The volumetric ratio of filled to unfilled pore volumes, as well as the optical signature of interacting chemical species, that is, the hole-transfer yield (HTY), are investigated. PIA spectroscopy is used to measure the HTY, relative to the amount of spiro-MeOTAD present, without needing to determine the extinction coefficients of the dye and spiro-MeOTAD cation species. The Beer-Lambert law is used to relate the relative PIA signal to the penetration length of the hole-conductor in the TiO2 film. For the sample thickness range of 1.3–5 μm investigated here, the optimum characteristic penetration length is determined to be 3.1±0.46 μm, which is compared to 1.4 μm for the 200 mg mL−1 concentration of spiro-MeOTAD conventionally used. Therefore, doubling the effective penetration of spiro-MeOTAD is necessary to functionalize all the dye molecules in a ssDSC.

1. Introduction

First generation dye sensitized solar cells (DSCs) are composed of a high surface area nanoparticulate TiO2 electrode, onto which a ruthenium dye, such as the Z907 dye (cis-RuLL(2SCN)2 (L = 4,4'-dicarboxylic acid-2,2'-bipyridine, L' = 4,4'-dimethyl-2,2'-bipyridine), [1, 2] is adsorbed, immersed in a liquid electrolyte, typically containing an I−/I3− redox couple, which conducts holes to a platinum counter electrode [3]. In the next generation of dye cells, however, replacement of the liquid electrolyte with a solid electrolyte is desirable. The liquid electrolyte presents sealing and module production challenges, especially because the I−/I3− redox couple is corrosive to metals such as Ag, the grid metal, and degradation products from the electrolyte block the activity of the Pt cathode [4]. The most widely investigated and successful [5] solid-state electrolyte material to date is the molecular hole-transporting spiro-MeOTAD [6, 7] but other possibilities for iodine-free electrolytes [8], including inorganic and polymeric hole-transporting materials, have also been investigated.

The infiltration of a solid into a nanoporous electrode emerged as a challenging problem from the start [6, 7] and has remained [9–11] so in the making of ssDSCs. The primary characterization tool to date has been scanning electron microscopy (SEM) [10]. In the best cases, SEM images roughly indicate the homogeneity of the spiro-MeOTAD/TiO2 composite at the exposed surface. Unlike transient absorption spectroscopy (TAS), it cannot quantitatively measure the percentage of dye molecules that are in effective contact with the hole transporter and therefore are regenerated, that is, the hole transfer yield (HTY). TAS optically identifies the signal of an oxidized species and quantifies it by use of the extinction coefficient.

TAS has been used to observe the kinetics of various electron transfer processes in the DSC [12–14] and to compare the HTY of various hole-conducting materials to spiro-MeOTAD [15]. However, it has not been possible
to isolate the separate absorption contributions from the charged dye and the spiro-MeOTAD in an assembled ssDSC within the spectral range of 500–1000 nm [16]. By comparing TAS results of both sides of a ssDSC sample, a concentration gradient in the filling of the spiro-MeOTAD is generally not observed, except for very low concentrations of spiro-MeOTAD or very thick TiO 2 films [15, 17, 18]. The strong absorption of the oxidized spiro-MeOTAD was unambiguously identified in the IR region, when TAS measurements were taken between 600–1500 nm [18].

Snaith et al. [18] proposed that the amount of spiro-MeOTAD in the pores of the TiO 2 is equal to the concentration of spiro-MeOTAD of the starting solution, c, plus an amount from the wet overlayer, resulting from the spin-coating, which is driven into the film by a concentration gradient setup during the process of evaporation. They defined a “filling fraction,” F, as the ratio of the thickness of the spiro-MeOTAD, \( t_{\text{spiro}} \), divided by the equivalent thickness of the pores, equation (1a), where \( t_{\text{spiro}} \) depends on the thickness of the wet overlayer of spiro-MeOTAD solution, \( t_{\text{WET}} \), the final dry spiro-MeOTAD “overlayer” thickness, \( t_{\text{OL}} \), the thickness of the TiO 2 film, \( t_{\text{TiO}_2} \), and the porosity of the titania, \( p \).

\[
F = \frac{t_{\text{spiro}}}{t_{\text{WET}}}, \quad (1a)
\]

\[
t_{\text{spiro}} = c^* \left( t_{\text{WET}} + (p * t_{\text{TiO}_2}) \right) - t_{\text{OL}}, \quad (1b)
\]

\( t_{\text{WET}} \) is determined by spin-coating various concentrations of the spiro-MeOTAD onto flat substrates. After drying, the film thicknesses were measured with the SEM and the volume of the dry spiro-MeOTAD film was calculated. The wet volume results from dividing the dry volume of the spiro-MeOTAD by the % volume that the spiro-MeOTAD occupies in the starting solution (calculated from the density and the starting concentration). The focus is on the change in spun wet film thickness due to the change in solute concentration, \( c^* \). Solution effects are not considered here. Ding et al. [19] tested (1a) and (1b) with various characterization techniques, and they were the first to largely validate Snaith’s equation by quantifying the spiro-MeOTAD desorbed out of the ssDSC, with UV-Vis absorption measurements.

In this work, we analyze the volume-based filling fraction by comparing calculated and experimental spiro-MeOTAD sample masses. From this analysis, an empirical correction factor is proposed to bring the filling fraction to more closely reflect the actual mass infiltrated into the pores. Observation of the filling fraction is complementary to the information gained with TAS, that is, the fraction of dye molecules that are (not) being regenerated by the spiro-MeOTAD.

We propose a method of using photoinduced absorption spectroscopy (PIA) to relatively determine the dye regeneration yield of an ssDSC, and we show its relationship to the filling fraction. After identifying the separate spectral contribution of the oxidized solid spiro-MeOTAD in a blend with phenyl-C71-butyric-acid-methyl ester ([70]PCBM) on TiO 2, we examine the PIA spectra of ssDSCs with various filling fractions. We demonstrate that a single PIA measurement of a ssDSC at two different wavelengths can be used as a relative measure for the dye regeneration yield.

2. Experimental

2.1. Sample Preparation. The SnO 2:F coated glass substrates were cleaned with Extran MA01, sodium hydroxide solution and ethanol and sintered at 450°C for 1 hour. The substrates were then coated with a compact layer of TiO 2 by aerosol spray pyrolysis deposition, at 0.9 bar and ~470°C, of titanium (IV) isopropoxide (1.56 g, Aldrich 97%), acetyl acetone (2.3 g), and ethanol (113.3 g). A total of 5 layers were coated 80–100 nm of flat compact TiO 2 after sintering at 570°C for 30 min. TiO 2 paste (Dyesol screenprint paste DSR 18R-T, 3 g) was diluted with ethanol (3 mL) for 4 micron thick films this paste was further diluted with ethanol for thinner films, and was doctor bladed onto the substrates. They were then dried (20 min at 80°C) and sintered at a rate of 900°C/h until 450°C where they remained for 30 minutes. After the substrates were cooled down to approximately 40°C they were immersed in aqueous TiCl 4 solution (40 mM), kept at 70°C for 30 min, and subsequently rinsed with deionized water and ethanol. They were sintered again at 450°C for 30 minutes. Directly out of the oven, the TiO 2 films were sensitized overnight in a solution of Z907 Dyesol DNH2 (0.28 mM) in a 1:1 mixture of CH 3 CN : tBuOH, and subsequently rinsed with CH 3 CN. The spiro-MeOTAD solution (Merck SHT-263) was dissolved overnight at 70°C in chlorobenzene at concentrations of 25, 45, 90, 180, and 200 mg mL⁻¹. Before spin-coating, TBP (0.1 μL per mg spiro-MeOTAD) and Li-FSI solution (175 mg/mL Li-FSI in Acetonitrile; 0.21 μL per mg spiro-MeOTAD) was added to this solution. The solution was heated again to 70°C and then was spin-coated (180 μL or 20 μL/cm²) onto the TiO 2 films that had been heated on a hotplate for 90 seconds at 70°C. Spin-coating was done with a Laurell Technologies Corp. spin coater (Model WS-400B-6NPP/LITE) programmed to wait 1 minute, accelerate to 2300 rpm for 30 sec, and decelerate to 800 rpm for 30 seconds. After the spiro-MeOTAD was applied, 100 nm thick gold contacts were thermally evaporated on top of the spiro-MeOTAD overlayer with a rate of 0.15 nm/s at a pressure of 1 × 10⁻⁶ mbar.

The spectra of the dye alone was obtained from a TiO 2 film sensitized with Z907 dye as described above but without spin-coating and gold evaporation.

The sample with a blend of [70]PCBM and spiro-MeOTAD on TiO 2 was made using [70]PCBM ([6,6]-phenyl C71-butyric acid methyl ester, Solenne B.V., used as received, 6.9 g) and dissolved at 70°C in chlorobenzene (100 μL). After the [70]PCBM was fully dissolved, a solution (100 μL of 180 mg mL⁻¹ spiro-MeOTAD in chlorobenzene) was added. This [70]PCBM/spiro solution was then spin-coated as described above on a TCO substrate coated with 80 nm of compact TiO 2.

The total thickness (TiO 2 + spiro MeOTAD overlayer) of the ssDSC was measured using a Dektak Profiler after
a scratch with a scalpel was made in the nonactive region between the gold contacts.

2.2. IV Measurements. Current-voltage measurements of the ssDSC were performed using a continuous solar simulator (Wacom) with a 5 kW Xe lamp (Type WXS-300S-50). The measurements were performed at STC (Standard Test Conditions: 1000 W m$^{-2}$, 25°C and AM1.5 spectrum, inclusive of a spectral mismatch correction, designed for the liquid DSC with Z907, utilizing a monocrystalline silicon solar cell with KG3 filter (Fraunhofer ISE RS-ID 2)) using a home-made measurement system which included a Keithley 2400 Source meter. The mismatch factor was not tailored to the ssDSC. Our experience with Z907 informs us of an error of about 5%.

2.3. Desorption Measurements. UV-Vis spectra were taken using a HP 8453 spectrometer and cuvettes from Hellma type 117.100-QS. The area of the cut samples was determined with the aid of a computerized optical microscope (Leica MZ7.5 Microsystems). Desorption of the samples was done in a closed flask filled with a known volume of chlorobenzene for 1 hour.

2.4. Density of Spiro-MeOTAD. A quartz cuvette with an opening of 4 $\times$ 10 mm was filled to the rim with water to determine the total inner volume of the cuvette. The volume was calculated by subtracting the weight of the full cuvette with that of the empty cuvette. To determine the volume of spiro-MeOTAD, this procedure was done on both an empty cuvette and a cuvette containing spiro-MeOTAD. After the volume of the empty cuvette was determined, the cuvette was filled with a 200 mg/mL spiro solution and heated to 70°C for 24 hours to evaporate the chlorobenzene. The weight of the spiro-MeOTAD was then determined by subtracting the weight of the cuvette before and after it was filled with spiro MeOTAD.

2.5. Photoinduced Absorption. Near steady-state photoinduced absorption spectra were recorded between 0.5 and 2.5 eV by excitation at 458 (2.71 eV) or 514 nm (2.41 eV) with a mechanically modulated (275 Hz) continuous wave argon ion laser pump beam and by measuring the change in transmission of a tungsten-halogen probe beam through the sample ($\Delta T$) with a phase sensitive lock-in amplifier after dispersion with a monochromator and detection using Si, InGaAs, and cooled InSb detectors. The pump power was typically 50 mW with a beam diameter of 2 mm. The signal intensity ($\Delta T T^{-1}$) was corrected for the photoluminescence, which was recorded in a separate experiment. Samples were measured in ambient atmosphere (290 K). The error is estimated to be <5%, but depends on the signal intensity and the transmission of the sample. Any error in the overlap of the beams is cancelled out by dividing the signals taken at different wavelengths.

3. Results and Discussion

3.1. SEM Characterization and Filling Fraction Analysis. A typical example of an ssDSC cross-section is shown in Figure 1. The SnO$_2$:F layer on the conducting glass is clearly visible. The degree of the penetration of the spiro-MeOTAD into the TiO$_2$ is visually often not apparent and the composite often appears as a monolithic layer. The spiro-MeOTAD overlayer however is evident and measurable in the SEM image. ssDSC cross-sections showing a range of overlayer thicknesses are shown in Figure 2. The images A and B in Figure 2 have relatively thick spiro-MeOTAD overlayers, with visible striations apparently produced in the spin-coating process step. While the upper edge in Image C of Figure 2 is smooth, it is not resolvable whether there is a continuous spiro-MeOTAD overlayer or not. The existence of this layer was only deduced by the electrical measurements described below. The topmost edge of the sample in Image D appears to have a rougher surface, with particles clearly visible, indicating that there is no overlayer present, or that the overlayer may be shortened by the particles sticking up.

In order to calculate the filling fraction in (1a) and (1b), the thicknesses of the spiro-MeOTAD overlayer and of the TiO$_2$ film were measured by SEM. The porosity was taken to be 68% [19], which is typical for unsensitized TiO$_2$ films. The influences on the porosity due to sample variation, the presence of the dye, double layer or solvation effects, were not taken into account here. The focus is to identify the influential parameters and the trends observed in the pore filling due to the variation of spiro-MeOTAD concentration. Figure 3 shows the range of filling fractions, as calculated using (1a) and (1b), plotted as a function of the concentration of spiro-MeOTAD in solution, for the ssDSC samples in this study. The relationship of $t_{\text{NET}}$ to the spiro-MeOTAD concentration is plotted in Figure 4(a).

3.2. I-V Characteristics. The short circuit currents and fill factors are plotted in Figure 4(b) for some samples with spiro-MeOTAD concentrations of 100 and 200 mg mL$^{-1}$. Cells having no overlayer (as for all samples with
25 mg mL$^{-1}$ (spiro-MeOTAD) are short circuited due to the direct connection between the TiO$_2$ electrode and the counter electrode. It is interesting to note, however, that the sample with an overlayer of only $\sim 10$ nm (as shown in Figure 2(c)) performs with roughly the same efficiency as those cells with much thicker overlayers. (See supplementary material available at doi: 10.1155/2011/513089).

3.3. Desorption to Measure Mass. After dissolving the ssDSC in chlorobenzene for 1 hour, the concentration of spiro-MeOTAD was determined using Beer’s law, as pioneered by Ding et al. [19]. The change in UV-vis absorption, at 390 nm, of the desorbed sample was measured spectroscopically and compared to the optical densities, at the same wavelength, of solutions with known spiro-MeOTAD concentrations. Lambert-Beer’s law was experimentally verified to be valid in the range of 25–300 mg mL$^{-1}$.

3.4. Calculated Mass. As an alternative to using the desorption measurements to determine the spiro-MeOTAD mass, the mass was calculated using (2), which involves using three measured parameters: the thicknesses of the TiO$_2$ and the overlayer, $t_{TiO_2}$ and $t_{OL}$, (to express volumes with assumed areas of 1 mm$^2$), and the density, $\rho$; one parameter retrieved from the literature, the porosity, $p$; the parameter of interest, the filling fraction, $F$.

$$\text{spiro$_{calc}$ mass} = ( (t_{TiO_2} \cdot 1 \text{ mm}^2) \cdot p \cdot F + (t_{OL} \cdot 1 \text{ mm}^2)) \cdot \rho.$$  \hspace{1cm} (2)

The calculated mass in the pores is the quantity expressed in (2) minus the second term, that is, the contribution of the overlayer. The density of spiro-MeOTAD was determined to be $1 \pm 0.1$ g/cm$^3$, as detailed in the experiment section.

The observed desorbed mass agrees with the calculated total mass of spiro-MeOTAD (2) at low concentrations, but is significantly lower at higher concentrations (Figure 5). One explanation is that the films infiltrated with higher spiro-MeOTAD concentrations may require a longer desorption time than 1 hour to completely desorb all the spiro-MeOTAD. The desorbed TiO$_2$ films were examined spectroscopically, but were too scattering to give meaningful data. On the other hand, Ding et al. [19] also used desorption times of one hour and confirmed the total desorption of the spiro MeOTAD by XPS. Another possibility that is explored below, is that the calculated mass does not take into account...
the effect of increased viscosity at higher spiro-MeOTAD solution concentrations, which lowers the capillary force to draw the liquid into the oxide matrix (see (6) below).

3.5. Characteristic Penetration Length. By multiplying the filling fraction by the thickness of the TiO₂ film, a characteristic penetration length (CPL) may be determined:

\[
\text{CPL} = F \times t_{\text{TiO₂}}.
\]  

Equation (3) shows that the penetration length is a function of the viscosity of the penetrating solution. The application of this equation requires a determination of the effective radius in the tortuous particulate TiO₂ film, which, for example, has been performed for alumina packed beds [21]. It clearly shows the relationship of viscosity to penetration length and may be the focus of future work in understanding

\[
F^2 = \left( \frac{\gamma \cos \theta}{\eta} \right) r_{\text{eff}} t.
\]  

(6)

This may be useful to estimate the extent of filling of spiro-MeOTAD in the pores of a TiO₂ nanoparticulate film. The penetration of a solution into a wetted capillary, or porous medium, is described by the Lucas-Washburn [20–22] equation, in which \( t \) is the penetration length, \( r_{\text{eff}} \) is the effective hydrodynamic pore radius, \( \gamma \) is the surface tension, \( \eta \) is the viscosity, \( \theta \) is the contact angle, and \( t \) is the time, as given in (4).
and optimizing the infiltration of a hole conductor into a TiO$_2$ film. Understanding the pore filling mechanism reflected by the filling fraction is a key to optimizing the pore filling. References to the CPL in this paper from this point on will refer to the CPL$_{corr}$, which is corrected for the effects of viscosity.

3.6. Photoinduced Absorption Spectroscopy: Relation to Filling Fraction. The photoinduced absorption spectroscopy technique allows optical detection of excited species generated by photoexcitation, such as the oxidized states of the dye, Z907, and the hole conductor, spiro-MeOTAD, in a ssDSC. After injection of the electron by the dye into the conduction band of the TiO$_2$, the dye cation is normally regenerated to its neutral state by an electron from the spiro-MeOTAD after a period ranging from less than ps to greater than ns [6]. In the absence of a hole conductor, an electron from the TiO$_2$ recombines with the oxidized dye cation after a period of hundreds of microseconds [2], during which the absorption spectrum of the oxidized dye may be observed.

When spiro-MeOTAD perfectly infiltrates the sensitized TiO$_2$ film and regenerates the dye, the photoinduced absorption features of the oxidized dye are replaced with that of oxidized spiro-MeOTAD [6, 7, 15, 17, 18]. In the extended visible spectral range (400–1000 nm), many signals may overlap due to contributions of the oxidized dye (absorption and bleaching bands) [23], electrons in TiO$_2$ [24, 25], and oxidized spiro-MeOTAD [18]. This confluence of signals in the visible region makes it very difficult to analyze spectra. Even when the separate spectral features of the oxidized dye and spiro-MeOTAD are known, near steady state photoinduced absorption spectra in the spectral range of 400–1000 nm cannot always be fitted with a linear addition of the independent oxidized dye or hole-conductor, because the electron density of the TiO$_2$ surface may lead to spectral shifts in the ground state absorption of dyes and thereby to additional spectral variations near the bleaching band [17]. Alternatively, the observation window may be extended to the near infrared region of the spectrum, where
oxidized spiro-MeOTAD shows a broad absorption band and the oxidized ruthenium dyes do not absorb. This strategy was used by Snaith et al. in a qualitative analysis of their photoinduced absorption spectra [18].

The PIA spectrum of only the dye Z907 on TiO₂ reveals a positive ΔTT⁻¹ signal (i.e., bleaching) with a maximum at 515 nm, and a negative signal (i.e., absorption) peaking between 750–800 nm. (Figure 6(a)). The spectral shape is very similar to that reported for TiO₂ films sensitized with the well-studied and structurally similar dyes N₃ (cis-Ru(dcbpy)₂(NCS)₂) [12–14, 26] and N719 (its bis-deprotonated analog) [27]. Therefore, we can safely attribute the positive signal to the bleaching band of Z907 and the negative signal to the absorption band of oxidized Z907. Additionally, a weak absorption tail of electrons in TiO₂⁻ is present in the visible to near infrared region [24, 25].

Although steady-state spectra of chemically oxidized spiro-MeOTAD in solution [28, 29], as well as spectroelectrochemical studies [29] of spiro-MeOTAD in TiO₂ films are available, spectral near steady-state PIA features of optically oxidized spiro-MeOTAD in the solid state may provide slightly different absorption features. Therefore [70]PCBM was used as a photosensitizer to generate a photoinduced absorption spectrum (Figure 6(a)) of oxidized spiro-MeOTAD in a solid composite blend with [70]PCBM on TiO₂ and in the absence of dye Z907. [70]PCBM is used because it can be photoexcited and accept electrons from spiro-MeOTAD [29–31], as a result of its strong ground state absorption in the visible region and strong electron accepting properties [32]. The PIA spectrum of the [70]PCBM:spiro-MeOTAD mixture in TiO₂ reveals two absorption bands in the visible region at ca. 515 nm (2.41 eV) and 700 nm (1.68 eV), and one in the near infrared at 1500 nm (0.83 eV) as shown in Figure 6(a). These three bands are attributed to oxidized spiro-MeOTAD, because of good agreement with previously reported spectra that were obtained by stepwise chemical oxidation [28, 29] or in spectroelectrochemical studies [29, 33]. In dichloromethane solution, Struijk found two absorption bands in the visible, a strong band at 521 nm and a less intense band at 678 nm, and one in the near infrared, at 1514 nm, after stepwise chemical oxidation [28]. A 5–25 nm shift is typically observed when comparing the spectra of a photoactive species in solution to one in the solid state and is due to molecular interaction with the local environment.

Having established the separate contributions of oxidized Z907 and spiro-MeOTAD, it is possible to analyze PIA spectra of TiO₂ films containing both Z907 and spiro-MeOTAD. For ssDSCs, the PIA spectrum strongly changes with increasing spiro-MeOTAD concentration from 25 to 180 mg mL⁻¹ (Figure 6(b)). For the lowest concentration, the absorption maximum at 780 nm and the presence of a bleaching band below 600 nm (Figure 6(b)) are signatures of oxidized Z907. Contributions of oxidized spiro-MeOTAD are visible from the band at 1450 nm, and from its absorption between 550 and 800 nm. This latter absorption peak overlaps with the bleaching band of the dye and thereby causes an altered form of the positive ΔTT⁻¹ band below 600 nm, as compared to the dyed film without spiro-MeOTAD (Figure 6(a)). For the highest concentration of spiro-MeOTAD the absorption maxima of the bands are 515, 730, and 1450 nm, in good correspondence to the spectrum obtained for the film using [70]PCBM as photosensitizer. This indicates that at the highest concentration, the major part of the dye is regenerated by spiro-MeOTAD. However, comparison of the spectrum of the ssDSC, with 180 mg mL⁻¹ spiro-MeOTAD, with that of the spiro-MeOTAD/PCBM blend (Figure 6(c)) shows that even for the highest concentration of spiro-MeOTAD (triangles), there is still some oxidized dye present (visible by the bleaching band at 565 nm and the additional absorption around 750 nm). Furthermore, the additional absorption in the region 850–1200 nm may be explained with the absorption of free electrons in TiO₂ [24].

Overall, with increasing spiro-MeOTAD concentration, two major spectral changes occur: (1) between 750 and 850 nm the ΔTT⁻¹ signal intensity reduces (relative to the 1450 nm peak) and (2) between 525 and 600 nm the positive (i.e., bleaching) signal turns into a negative (i.e., absorption) signal (Figure 6(b)). With increasing spiro-MeOTAD content, both absorption changes are due to lower contribution of the strong absorption (around 800 nm) and bleaching (around 565 nm) of oxidized Z907, relative to oxidized spiro-MeOTAD. By plotting the absorbance at 565 nm versus that at 825 nm, as in Figure 7(a), a linear relation is found with increasing spiro-MeOTAD concentration, when the spectra is normalized at the spiro-MeOTAD 1450 nm peak. This indicates that the spectral changes are due to the same photoexcited species, which we conclude is the oxidized dye.

Plotting all the data gives a slope of −2.0, but the PIA signal (ΔTT⁻¹) of those samples with the lowest concentration of spiro-MeOTAD are much more scattering than the rest of the samples. They are a bilayer, in which the effective refractive index of one layers is the average of spiro-MeOTAD, TiO₂ and air and the other layer is only an average of TiO₂ and air, and is consistent with other observations of concentration gradients in samples with low concentrations of spiro-MeOTAD [17]. These samples clearly scatter the light differently than a single composite layer of spiro- MeOTAD, TiO₂ and air. Highly scattering samples may dramatically influence the accuracy of the PIA measurement by lowering the magnitude of both ΔT and T⁻¹, introducing a large error in their ratio. When these points are disregarded, the linear fit has a slope of −2.2. A line with a slope of −2.4 is also plotted to show that this slope is also within the accuracy of the measurement and/or the fit. A slope of −2.4 is expected because the ratio of PIA signal intensities at 565 nm to 825 nm for the dye on TiO₂ alone, without spiro-MeOTAD, is −2.4. (Figure 6(a)). The ratio of the dye cation absorption peak at 825 nm, or at 565 nm, to the spiro-MeOTAD cation peak at 1450 may be used to extract the relative dye cation concentration from the absorption spectrum of the ssDSC.

The PIA signal intensities for the 565 nm and 825 nm peaks, relative to the 1450 nm spiro-MeOTAD peak, are plotted as a function of filling fraction in the inset of Figure 7(b). Because the filling fraction is a nondimensional measure of concentration, it has an exponential relationship to the transmitted light intensity, as predicted by the Beer-Lambert law, given in (7), where I is intensity, eᵢ is
the extinction coefficient of species \( i \), \( c_i \) is the concentration of species \( i \) and \( l \) is path length.

\[
\log \left( \frac{I_0}{I} \right) = \sum \epsilon c l
\]

\[
= \epsilon_{\text{dye cation}} c_{\text{dye cation}} l + \epsilon_{\text{spiro MeOTAD}} c_{\text{spiro MeOTAD}} l.
\]

(7)

Normalizing the data at the spiro-MeOTAD peak at 1450 has two effects: (i) the observed signal at the 825 nm peak is now a ratio of the signals at the 825 and 1450 nm peaks and (ii) the expression \( (\epsilon_{1450}^{\text{spiro}} c_{\text{spiro}} + \epsilon_{1450}^{\text{spiro}} c_{\text{spiro}}) \) is set to a magnitude of one. The Beer-Lambert law for the normalized data may be written as shown in (8) and simplified with the introduction of constants for the ratio of the extinction coefficients for the respective peaks, as shown in (9)

\[
\frac{\log (\Delta I)_{825}}{\log (\Delta I)_{1450}} = \frac{\frac{\epsilon_{825}^{\text{spiro}} c_{\text{spiro}} l + \epsilon_{825}^{\text{dye}} c_{\text{dye}} l}{\epsilon_{1450}^{\text{spiro}} c_{\text{spiro}} l}}
\]

(8)

\[
= \frac{\epsilon_{825}^{\text{spiro}}}{\epsilon_{1450}^{\text{spiro}}} + \frac{\epsilon_{825}^{\text{dye}}}{\epsilon_{1450}^{\text{dye}}}.
\]

(9)
$y = 0.5 - 2.2 \times x$

**Figure 7:** (a) $\Delta T T^{-1}$ signal intensities relative to the peak at 1450 nm, for 565 nm ($\Delta T_{565\text{ nm}} / \Delta T_{1450\text{ nm}}$), 75 ($\Delta T_{1450\text{ nm}} / \Delta T_{565\text{ nm}}$), y-axis) compared to 825 nm ($\Delta T_{825\text{ nm}} / \Delta T_{1450\text{ nm}}$), x-axis). The solid line is a linear fit to the data, excluding the highly scattering points at the lowest concentration: $y = -2.2x + 0.5$. The dashed line shows $y = -2.4x + 0.55$. (b) The In(relative PIA signal at 825 nm)/2.3 is plotted against the concentration times length (mol cm$^{-1}$). The spiro-MeOTAD concentrations are 45 ($\uparrow$), 90 (•), and 200 (○) mg mL$^{-1}$; 180 (△) mg mL$^{-1}$; 100 (□) mg mL$^{-1}$; 200 (◇) mg mL$^{-1}$. Inset: $\Delta T T^{-1}$ signal intensity relative to the peak at 1450 nm, for 565 nm ($\Delta T_{565\text{ nm}} / \Delta T_{1450\text{ nm}}$), 75 ($\Delta T_{1450\text{ nm}} / \Delta T_{565\text{ nm}}$), □) and for 565 nm ($\Delta T_{565\text{ nm}} / \Delta T_{1450\text{ nm}}$), ◇) compared to the filling fraction obtained in Section 2.1. The data are fitted with exponential functions: $y = -2 * \exp(-x/0.1) + 1.1$ (solid line) and $-1 * \exp(-x/0.1) + 0.75$.

It is interesting to apply (11) to the PIA data, using the CPL (i.e., $F \ast t_{TiO_2}$) in (12), to calculate the effective extinction coefficient, with units of M$^{-1}$ cm$^{-1}$, of the relative intensity signal at 825 nm, as plotted in Figure 7(b).

**Equation 9**

$$B + A \times \left( \frac{c_{\text{dye}}^{+}}{c_{\text{spiro}}^{+}} \right), \quad \text{where} \quad A \equiv \left( \frac{c_{\text{dye}}^{+}}{c_{\text{spiro}}^{+}} \right)_{1450}, \quad B \equiv \left( \frac{c_{\text{dye}}^{+}}{c_{\text{spiro}}^{+}} \right)_{825}.$$ 

If the extinction coefficients and the concentrations of the dye and spiro MeOTAD cations are known, then (9) is quite useful. But, it is also possible to reformulate (8) so that the normalized PIA signal provides a measure of the dye cation population, relative to the concentration of spiro-MeOTAD present, without knowledge of the respective extinction coefficients or cation concentrations. It is quite evident that the dye cation population, that is, those dyes that are not regenerated by the hole conductor, is related to the concentration of the hole conductor, and so we can let the ratio of the dye cation density to the spiro-cation density be a function of the spiro-MeOTAD concentration, as expressed in (10). Now, a relationship between the normalized PIA signal and the concentration of spiro-MeOTAD can be written using an effective extinction coefficient as shown in (11)

$$\log \left( \frac{\Delta I}_{825} \right) = \log \left( \frac{\Delta I}_{1450} \right) + B + \xi * c_{\text{spiro}} * \frac{1}{l}, \quad (10)$$

**Equation 10**

$$\log \left( \frac{\Delta I}_{825} \right) = \log \left( \frac{\Delta I}_{1450} \right) + B + \xi * c_{\text{spiro}} * \frac{1}{l}, \quad (11)$$

Figure 7(b) shows that the data may be linearly fitted for all concentrations higher than 25 mg mL$^{-1}$. The error bars are based upon the deviation of a group of three measurements, and the line has an intercept of 0.16 ± 0.02 and the slope, −814 ± 120. The slope of this line is the effective extinction coefficient for this system. Here, as in the linear fit of the optical data plotted in Figure 7(a), the data points for the very low concentrations of spiro-MeOTAD were not included in the linear fit. Furthermore, in the event of a bi-layer (TiO$_2$ + spiro-MeOTAD + air | TiO$_2$+ air), the relationship between the spiro-MeOTAD concentrations and the dye and oxidized spirocations, assumed in (10), would break down. Indeed, as the concentration of spiro-MeOTAD approaches zero, so will the concentration of spiro-MeOTAD cation, and the expression for $\xi$ will become undefined and very near to this singularity, the relationship becomes superlinear. Despite these considerations, employing this relationship is useful for interpreting the data in the range of concentrations from 45 mg mL$^{-1}$ up through at least 300 mg mL$^{-1}$.
It is possible to estimate the magnitude of $c \times l$ that is necessary to eliminate the dye cation signal. By extrapolating the linear fit in Figure 7(b) to the case where there is no signal from the dye cation, that is, to $y = 0$, the abscissa, $c \times l$, is equal to $1.71 \times 10^{-4} \pm 2.6 \times 10^{-5}$ M cm, which can be converted to a CPL of $3.1 \pm 0.46 \mu$m using (12). The average (corrected) CPL of the samples with spiro-MeOTAD concentrations of 200 mg mL$^{-1}$ is 1.4. Comparison of these two values shows that a doubling of the characteristic penetration length of spiro MeOTAD is required, than currently achieved, in order to be able to regenerate, and thus functionalize, all the dye molecules in a conventionally sensitized ssDSC.

A sample may have a filling fraction of 90% but if the 10% of the remaining pore space (i.e., narrow pores) contain a third of the dye molecules then the filling is not optimum. Usually high filling fractions can be only achieved with films not greater than 2–2.5 microns. Thicker films would lead to higher light absorption, higher currents, and higher efficiencies. Indeed, the liquid electrolyte DSC’s are routinely made to be 8–10 microns thick. Equation (6) shows that the penetration depth of the capillary force depends on viscosity, wetting and the pore radius. (We can assume, as did Snaith et al. [18] that the chlorobenzene completely wets the TiO$_2$.) In this case, optimization of the pore filling should address the viscosity of the concentrated spiro-MeOTAD and/or the effective pore radius of the TiO$_2$ film, to optimize the amount of spiro-MeOTAD which can infiltrate into the pores by capillary action.

The PIA measurements in this work were made at a frequency of 275 Hz, very near the crossover point of the two curves in Figure 6(d), at which there is little variation of signal intensity with spiro MeOTAD concentration, and appropriate for a measurement relative to a constant spiro MeOTAD contribution and the analysis used above. However, to quantitatively determine the number of [non]regenerated cations, or the HTY, the extinction coefficients of the two species must be independently known, and the effect of lifetime upon the measurement must be taken into account. The magnitude of the PIA signal is proportional to $g$, the efficiency of generation of the photoinduced species; $I$, the pump intensity; $\tau$, the lifetime of a photoexcitation under steady-state conditions, and $\alpha = (2\nu r s)^{-1}$.

$$-\Delta T \propto \frac{gI_\nu \tau\alpha \tanh \alpha}{(\alpha + \tanh \alpha)}. \quad (13)$$

This equation can be used to detect $\tau$ from chopper frequency-dependent PIA measurements. This results in steady-state lifetimes of $\tau_r = 115 \mu$s for a low spiro-MeOTAD concentration of 45 mg mL$^{-1}$ and to $\tau_r = 995 \mu$s for a four times higher spiro-MeOTAD concentration. Such unequal lifetimes with different hole conductor concentrations complicate quantitative determination of hole transfer yields using near steady-state photoinduced absorption spectra, because the lifetimes are shorter than the period of the chopper (3.6 ms). In this case, an increase in lifetime leads to an increase in PIA intensity. For lifetime-independent and hence more quantitative detection using near-state PIA measurements, much higher frequencies would be required. For example, when measuring at 10 kHz, an increase in lifetime from 0.1 to 1 ms would lead to an increase in PIA intensity as a result of the increased lifetime of only 4%.

This analysis shows that a single PIA measurement at two different wavelengths (825 nm and 1450 nm) can be used as a measure for the hole transfer yield (HTY). Furthermore, this method is more robust than the previous method described by Kroeze et al. [15] In that the quantification may be obtained from a single measurement set, therefore it is not necessary to measure the ssDSC before and after filling with the hole conductor which requires that the light intensities and sample repositioning must be as identical as possible.

4. Conclusions

We prepared ssDSCs with a range of TiO$_2$ thicknesses and filling fractions. The calculated mass based on the filling fraction, as proposed by Snait, was greater than the experimentally desorbed mass. Because the effects of viscosity were observed in the thicknesses of the spiro MeOTAD films spun on flat substrates, a correction factor was proposed for the filling fraction to account for the effects of viscosity in capillary infiltration. According to the Beer-Lambert law, it was shown that PIA signal is related to the filling fraction, and the CPL, through an effective extinction coefficient, which was determined for this material system, allowing the relative dye cation density to be deduced. The optimum value of the CPL, for the sample range of 1.4 to 5 $\mu$m investigated here, was determined to be $3.1 \pm 0.46$ microns which is roughly double the average CPL for the samples used in this study (see supplementary material). This suggests that a solution with a higher concentration of hole conductor and a lower viscosity and/or a greater effective pore radius in the TiO$_2$ film is necessary to minimize the thickness of the overlayer, increase the penetration length of the spiro-MeOTAD and to optimally functionalize all the dye molecules in an ssDSC. In other words, for the solid electrolyte to achieve the same intimate contact with the dye molecules as a liquid electrolyte, the infiltration conditions must be engineered so that a more concentrated solution will enter the pores, either by altering the viscosity of the spiro-MeOTAD solution and/or by altering the pore radii of the TiO$_2$ film.

Acknowledgments

The authors kindly acknowledge Professor Dr. Rene Janssen (TU/e) for allowing us to work with their PIA setup. They are also kindly acknowledge Jan Kroon for helpful discussions. Thanks due to Esther Cobussen for evaporating the gold contacts and to Sjoerd Veenstra for providing the [70]PCBM. Thanks due to G. Boschloo for introducing us to their PIA set-up at Uppsala University. The funding for this work was provided by the Dutch Ministry of Economic Affairs.
References


Submit your manuscripts at http://www.hindawi.com