

## Research Article

# A Phase Noise Analysis Method for Millimeter-Wave Passive Imager BHU-2D-U Frequency Synthesizer

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Received 3 July 2013; Accepted 13 August 2013

Academic Editors: R. Luzzi and R. Newcomb

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A nontrivial phase noise analysis method is proposed for frequency synthesizer of a passive millimeter-wave synthetic aperture interferometric radiometer (SAIR) imager for concealed weapon detections on human bodies with high imaging rates. The frequency synthesizer provides local oscillator signals for both millimeter-wave front ends and intermediate frequency IQ demodulators for the SAIR system. The influence of synthesizer phase noise in different offset frequency ranges on the visibility phase errors has been systematically investigated with noise requirements drawn, and the integrated RMS phase error could represent uncorrelated phase noise effects in the most critical offset frequency range for visibility error control. An analytical phase noise simulation method is proposed to guide synthesizer design. To conclude, the phase noise effects on SAIR visibility errors have been concretized to noise design requirements, and good agreements have been observed between simulation and measurement results. The frequency synthesizer designed has been successfully in operation in BHU-2D-U system.

## 1. Introduction

Various techniques in the area of concealed weapon detection on human bodies have been developed and widely applied for security checks. Compared with active detection systems, such as the X-ray sensors, the passive SAIR imaging system [1] provides several advantages. It only receives rather than emitting high frequency signals and does not result in human health concerns [2]. Moreover, any concealed hazards, including nonmetallic weapons, can be observed in the obtained image explicitly [3–5].

Visibility error is significant for a SAIR system. Frequency Synthesizer (FS) provides two local oscillators (LO) for mmW front ends and IF IQ demodulators, and its phase noise (PN) contributes to visibility errors. The PN analysis consists of 3 key problems: determining whether mmW or IF LO is the major cause of visibility errors from system-level analysis; finding the offset frequency range (OFR) whose PN is the main contributor of visibility errors and establishes proper SAIR FS phase noise design requirements; finding an accurate PN simulation method to realize FS design and fulfill the requirements.

In Section 2, system configuration and PN system-level modeling are given, and the dominant source of visibility errors from FS is found. In Section 3, this risky PN is separated to three OFRs by visibility error analysis, and SAIR design requirements are proposed. In Section 4, an accurate PN simulation method is given, and FS design is realized. It is found that integrated RMS phase error could represent uncorrelated PN effects that lead to visibility errors. In Section 5, comparisons of simulations and measurements are given. Important conclusions are summarized for FS PN analysis and design of HIR SAIR imager.

## 2. PN System-Level Modeling

A SAIR imager named BHU-2D-U [6] has been developed by Beihang University. It consists of a 48-element U-shaped antenna array, and each receiver channel [7] is composed of a mmW receiver [8] and an IF IQ demodulator. The DSP subsystem computes complex cross-correlations between IF IQ output pairs of all receivers simultaneously, with the results calibrated to form visibility samples, whose IFT

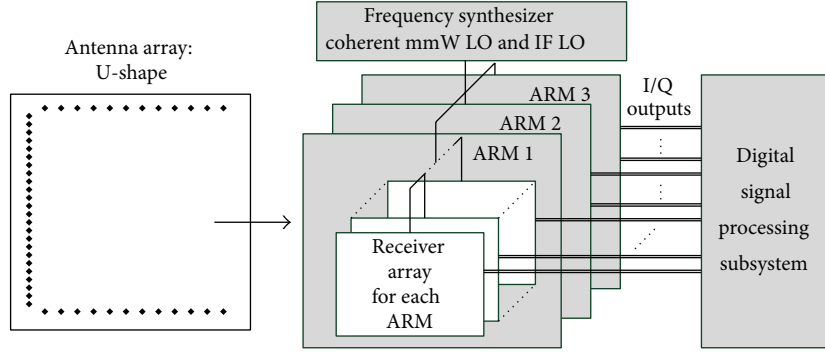


FIGURE 1: System configuration of BHU-2D-U.

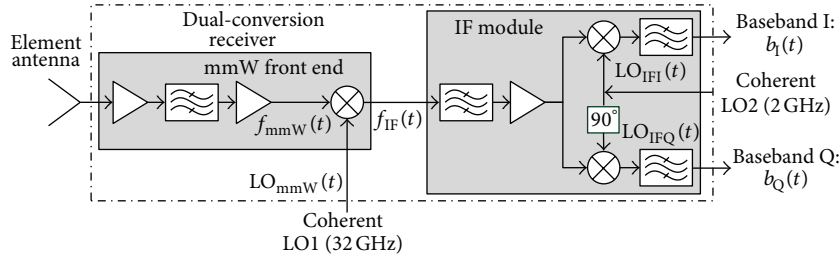


FIGURE 2: Dual-conversion receiver block diagram.

TABLE 1: BHU-2D-U general specifications.

Parameter	Specification
Center frequency	34 GHz
Geometry of antenna array	U Shape
Field of view	20° (Horizontal) 36° (Vertical)
Temperature sensitivity	1~3 K
Effective distance	2.5~5 m
Range resolution	6.5 cm at 3 m
System bandwidth	200 MHz

generate the brightness temperature of the field of view. Key parameters of BHU-2D-U are summarized in Table 1, and its simplified block diagram is shown in Figure 1 [6].

A 32 GHz mmW LO and a 2 GHz IF demodulator LO are required for BHU-2D-U. Figure 2 gives the double side-band dual-conversion receiver structure [6]. As Ku and higher frequency multipliers are easy to be integrated in the mmW front end, 8 GHz output is selected for FS. Both LO come from the same reference TCXO for coherency. Power divider networks are designed at 2 and 4 GHz for lower loss. The preliminary FS design is shown in Figure 3.

Though previous SAIR researches have given that coherent FS PN has negligible effects on visibility, different receiver channels do produce uncorrelated PN [9] which generates

visibility errors. Therefore, it is crucial to concretize PN requirements by system-level modeling and find the dominant PN contributor LO.

**2.1. System-Level PN Modeling.** The aim of system-level PN modeling is to concretize PN effects in the visibility errors. Firstly, it is assumed that phase terms of all signals are constant without phase noise effects. Let  $f_{mmW}(t)$ ,  $LO_{mmW}(t)$ ,  $f_{IF}(t)$ ,  $LO_{IFI}(t)$ , and  $LO_{IFQ}(t)$  be the narrow-band mmW received signal and mmW mixer LO, IF downconverted signal, and IF I/Q demodulator LOs, as shown in Figure 2. They are given as

$$\begin{aligned}
 f_{mmW}(t) &= A_{mmW} \cos(\omega_{mmW}t + \theta_{mmW}), \\
 LO_{mmW}(t) &= A_{LO1} \cos(\omega_{LO1}t + \theta_{LO1}), \\
 LO_{IFI}(t) &= A_{LO2} \cos(\omega_{LO2}t + \theta_{LO2}), \\
 LO_{IFQ}(t) &= A_{LO2} \cos(\omega_{LO2}t + \theta_{LO2} + 90^\circ),
 \end{aligned} \tag{1}$$

where  $A_i$  and  $\theta_i$  are given as the amplitude and phase terms for each signal, and subscripts LO1 and LO2 represent the first and second LO.  $f_{IF}(t)$  and  $b_i(t)$  are given as

$$\begin{aligned}
 f_{IF}(t) &= K_1 f_{mmW}(t) LO_{mmW}(t), \\
 b_{I,Q}(t) &= K_2 f_{IF}(t) LO_{IFI,Q}(t),
 \end{aligned} \tag{2}$$

where  $K_{1,2}$  refers to the conversion loss of the mmW and IF mixer. As the mmW mixer is single side band and the IF I/Q

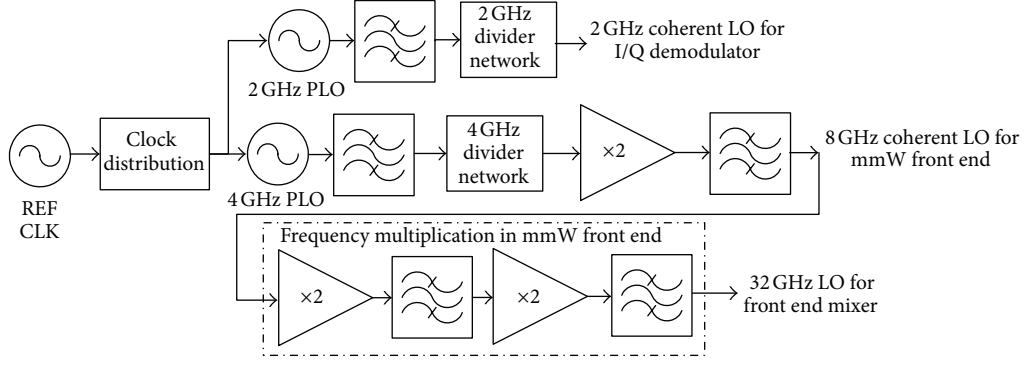


FIGURE 3: Preliminary FS design block diagram.

demodulator is double side band, the phase terms of  $b_1(t)$  and  $b_Q(t)$  can be given as

$$\begin{aligned}\theta_{b_1}(t) &= \theta_{\text{mmW}} - \theta_{\text{LO1}} \pm \theta_{\text{LO2}}, \\ \theta_{b_Q}(t) &= \theta_{\text{mmW}} - \theta_{\text{LO1}} \pm (\theta_{\text{LO2}} + 90^\circ).\end{aligned}\quad (3)$$

From (3), the phase terms of IF I/Q demodulator output signals are constants. However, PN is always present in a realizable LO, whose phase term can be given by

$$\theta_{\text{LO}}(t) = \theta_{\text{LO}} + \theta_n(t), \quad (4)$$

where  $\theta_{\text{LO}}(t)$  is the phase,  $\theta_{\text{LO}}$  is the definitive phase, and  $\theta_n(t)$  is the time-variant phase drift caused by PN. In SAIR signal processing, the visibility function sample  $V_{ij}$  is obtained by cross-correlations between any I/Q output signals calculated in the UV domain (antenna separation by wavelength), and it is proportional to the expectation of the cross-correlation of  $b_i(t)$  and  $b_j(t)$  ( $i$  and  $j$  refer to any I/Q demodulated signal, and  $i$  can be equal to  $j$ ) [1]:

$$\begin{aligned}V_{ij} &= E[b_i(t)b_j^*(t)] = E[A_{b_i(t)}A_{b_j(t)}^*]E[e^{j(\theta_{b_i(t)} - \theta_{b_j(t)})}] \\ &= E[A_{b_i(t)}A_{b_j(t)}^*]E[e^{j(\text{CPM}_{\text{II,IQ}}(t))}],\end{aligned}\quad (5)$$

where  $E[\cdot]$  is the expectation operator and  $*$  denotes conjugated signal;  $A_{b_{i,j}(t)}$  and  $\theta_{b_i}(t)$  are the amplitude and phase of baseband output signal pairs. A new parameter called channel phase mismatch (CPM) is defined for I-I and I-Q cases in (6) as (the same for QQ and QI):

$$\begin{aligned}\text{CPM}_{\text{II}}(t) &= \Delta\theta_{\text{mmW}} + \Delta\theta_{\text{LO1}} \pm \Delta\theta_{\text{LO2}}, \\ \text{CPM}_{\text{IQ}}(t) &= \Delta\theta_{\text{mmW}} + \Delta\theta_{\text{LO1}} \pm (\Delta\theta_{\text{LO2}} - 90^\circ),\end{aligned}\quad (6)$$

where  $\Delta$  refers to the phase difference between channel pairs. CPM is thus the combination of phase difference of mmW received signal  $\Delta\theta_{\text{mmW}}$ , mmW mixer LO  $\Delta\theta_{\text{LO1}}$  and IF IQ demodulator LO phase mismatches  $\Delta\theta_{\text{LO2}}$ , and  $\Delta\theta_{\text{mmW}}$  can be calibrated by point source method.  $\Delta\theta_{\text{LO1}}$ , and  $\Delta\theta_{\text{LO2}}$  could be replaced by (4) as phase mismatches:

$$\Delta\theta_{\text{LO1,2}}(t) = \Delta\theta_{\text{LO1,2}} + \Delta\theta_{n1,2}(t), \quad (7)$$

where  $\Delta\theta_{\text{LO}}$  is definitive and can also be calibrated, but  $\Delta\theta_n(t)$  cannot. Correlated PN is  $\Delta\theta_n(t) = 0$ , whereas uncorrelated PN is  $\Delta\theta_n(t) \neq 0$ . The visibility phase error of (5) could be simplified by calibration as:

$$\begin{aligned}E[e^{j(\text{CPM}_{\text{II,IQ}}(t))}] &= E[e^{j(\Delta\theta_{\text{mmW}} + \Delta\theta_{\text{LO1}} \pm \Delta\theta_{\text{LO2}})}] \\ &\xrightarrow{\text{calibration}} E[e^{j(\Delta\theta_{n1}(t) \pm \Delta\theta_{n2}(t))}],\end{aligned}\quad (8)$$

where  $\Delta\theta_{n1,2}(t)$  represents the uncorrelated PN in mmW LOs and IF I/Q demodulator LOs, respectively. In the imaging calculation, phase error expectation of (8) is integrated in time domain and produces error in the imaging results. This integration is given as

$$E[e^{j(\Delta\theta_{n1}(t) + \Delta\theta_{n2}(t))}] = \frac{1}{\tau_s} \int_0^{\tau_s} e^{j(\Delta\theta_{n1}(t) + \Delta\theta_{n2}(t))} dt, \quad (9)$$

where  $\tau_s$  is the single image integration time (SIIT). It is clear that  $\tau_s$  is significant for phase noise analysis and is treated later.

**2.2. Dominant Uncorrelated PN LO.** Based on the analysis above, it is necessary to determine whether  $\Delta\theta_{\text{LO1}}$  or  $\Delta\theta_{\text{LO2}}$  is the dominant uncorrelated PN source. As in Figure 3, compared with the IF LO which is generated by the 2 GHz PLO, the mmW LO is multiplied from 4 GHz once to 8 GHz and then twice in the mmW front ends to 32 GHz; hence, the number of components for mmW mixer LO is greater than for IF LO. Hence the uncorrelated PN in each mmW mixer LO is higher than for IF LO, and mmW LO is the dominant uncorrelated PN source.

### 3. PN OFR Separation and Requirement Analysis

As mmW LO is the dominant uncorrelated PN source and PN simulation and analysis are mostly performed in frequency domain, a suitable OFR guideline for PN analysis is required to define PN requirements over different OFRs. Synthesizer output PN could be further represented by

$$\theta_n(t) = A_n \cos(\omega_m t + \psi_n), \quad (10)$$

where PN is given by random amplitude  $A_n$ , offset angular frequency  $\omega_m = 2\pi f_m$ , and random phase term  $\psi_n$ . Therefore, the OFRs should be defined by  $\tau_s$  and  $f_m$ .

**3.1. OFR Separation and FS PN Requirements.** The phase error expectation is performed in the time domain from 0 to  $\tau_s$ , but PN is usually analyzed in the frequency domain. By Fourier Transform, the OFR separations are given by relations between correlation frequency  $f_s = 1/\tau_s$  and PN modulation frequency  $f_m$  (offset frequency from carrier). A PN separation guideline is proposed for the three OFR separations.

- (1)  $f_m \gg f_s$ . This range could be interpreted as  $f_m > 100 f_s$  (far offset frequency range (FOFR)). Offset frequency  $f_m$  is far from the actual correlation region. Phase errors caused by uncorrelated PN in this range are negligible.
- (2)  $f_m < f_s$  (very near offset frequency range (VNOFR)). The correlations of visibility functions actually take place in this region, and uncorrelated PN could cause huge visibility errors. By (9), it is necessary to give limits on phase mismatch and temperature drifts instead of PN:

$$\begin{aligned} \Delta\phi_{LOi} - \Delta\phi_{OLj} &< 1 \text{ deg}, \\ \Delta\phi_{LOi} - \Delta\phi_{OLj} &< 0.5 \text{ deg / } ^\circ\text{C}, \end{aligned} \quad (11)$$

where  $\Delta\phi_{LOi,j}$  refers to the phase mismatch between different receiver pairs for the same LO.

- (3)  $f_s < f_m < 100 f_s$ . This range is named as middle offset frequency range (MOFR). The PN variations in this region are apparent, and they degrade phase matches in VNOFR by uncorrelated PN between receiver pairs. Therefore, stringent PN simulations and phase error simulations are required. As PN changes rapidly, integrated RMS phase error [10–12] is applied to limit PN for both 4 and 8 GHz LOs in this range:

$$\begin{aligned} \text{PhEr}_{\text{RMS},4\text{ GHz}} &= \sqrt{2 \times \int_{f_s}^{100f_s} \text{PN}(f) df} < 1.3 \text{ deg}, \\ \text{PhEr}_{\text{RMS},8\text{ GHz}} &= \sqrt{2 \times \int_{f_s}^{100f_s} \text{PN}(f) df} < 2.4 \text{ deg}, \end{aligned} \quad (12)$$

where the coefficient 2 refers to double side-band PN integration, and this threshold is more stringent than MIRAS (1 deg for single side-band LO) [9]. Now  $\tau_s$  is required to concretize OFR separations.

**3.2.  $\tau_s$  (SIIT) Derivation by Security Imaging  $\Delta T$ .** As HIR is required by security imaging, video rate imaging with very short SIIT is preferred, but SIIT is limited by the least temperature sensitivity required for effective hazard identification, which is given by [1]

$$\Delta T \approx \frac{1}{\eta} \frac{T_A + T_R}{\sqrt{B\tau_{st}/2.46}} \frac{\alpha_W}{\alpha_F} \alpha_{LO} \sqrt{N_V}, \quad (13)$$

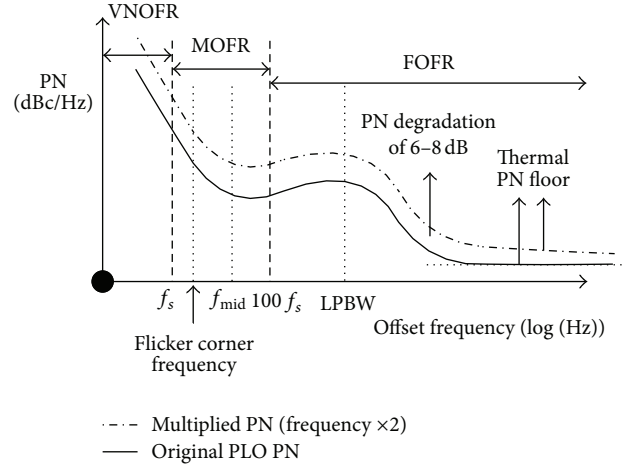


FIGURE 4: OFR separation for FS PN analysis (closed-loop PLO).

where  $\eta$  is element antenna efficiency (0.65 of Bode horn);  $T_A$  (300 K) and  $T_R$  (400 K) are antenna and receiver noise temperatures;  $\alpha_W$  is the window factor (0.53 for hamming window);  $\alpha_F$  is the filter factor (1.19 for gauss prediction);  $N_V$  is the sampling point number for rectangular visibility function ( $49 \times 25 = 1225$ );  $B$  is system bandwidth of 200 MHz [13]. The least brightness temperature discrepancy for hazards and human body is 3 K, in which  $\Delta T$  must be less than [6].

The total integration time ( $\tau_{st}$ ) is related to the dynamic high imaging rate (HIR) application condition of security imaging. If a person goes through a 2.5 m effective imaging distance with an average walking speed of 1.4 m/s, the dwell time is about 1.8 s.  $\tau_{st}$  should be within 1 s for 10 images (0.1 s for each image).  $0.5 \tau_{st}$  corresponds to a sensitivity of 2.63 K, which leaves some margin from 3 K limit. Thus, the  $0.05 \text{ s } \tau_s$  (minimum SIIT) is used for OFR separation.

## 4. PN Simulation Method

Based on the analysis above, a typical OFR separation is shown in Figure 4. It is important to simulate PN in each OFR to obtain an accurate PN curve and estimate whether the requirements of (12) are realized. The method is given for a single-loop PLO FS design (the most common and cost-effective method), and PN simulation for frequency multiplication is also proposed.

Two important parameters in single-loop PLO PN simulation are the flicker corner frequency ( $f_{\text{flicker}}$ ) and loop bandwidth (LPBW).  $f_{\text{flicker}}$  is the flicker noise transition frequency of the reference oscillator and determined by its output stage component. A high-Q and low flicker corner, low PN silicon bipolar TCXO is preferred [14, 15] (our TCXO flicker corner is 80 Hz [16]). LPBW controls the dynamic and noise traits of the loop as well as spur attenuation and is usually set from tens to hundreds of kHz.

**4.1. 4 GHz LO PN Simulation for Each OFR.** Conventional time-consuming PLO PN simulation method [17, 18] is performed by closed-loop transfer function with detailed



loop filter design and PN data from each contributor (TCXO, Phase Frequency Detector (PFD), VCO, and Divider). This method is designed for a quick and accurate simulation of PN specifically for the separated OFRs of BHU-2D-U FS.

- (1) FOFR PN ( $f_m > 2$  kHz). Part of this range is inside LPBW, and the other is outside. PN in the in-LPBW part is mainly caused by reference, PLO chip and frequency divider, while in the other part VCO is the main noise contributor [14].
- (2) VNOFR PN ( $f_m < 20$  Hz). PN in this very near range is caused by reference oscillator noise degraded by  $20 \lg(N)$ ;  $N = f_{RF}/f_{PFD}$  is the multiplier coefficient for integer PLO. For 20 Hz is lower than reference oscillator  $f_{flicker}$ .
- (3) MOFR PN. This region covers both the multiplied reference noise region and the in-LPBW PFD noise region. PN simulation can be further divided into two regions.
  - (a)  $20 \text{ Hz} < f_m \leq f_{flicker} = 80 \text{ Hz}$ . PN in this region is mostly dominated by the degraded reference PN. Reference PN can be given by the modified Leeson Model [19, 20] as

$$PN_{ref} (\text{Linear}) = PN_{floor} \left( 1 + \frac{f_c^2}{f_m^2} \right) \left( 1 + \frac{f_{flicker}}{f_m} \right), \quad (14)$$

where  $PN_{floor}$  is the PN floor and  $f_c$  is the corner frequency (20 dB/dec to flat noise floor) [16]. The PN can be given as

$$PN_{PLO} (\text{dBc/Hz}) = PN_{ref} + 20 \lg(N) + PN_{deg}, \quad (15)$$

where  $PN_{deg}$  is a degradation of 3-4 dB by other noise sources. A lower  $N$  and a low PN reference resonators are effective to minimize PN [21]. VCO PN in this region is usually suppressed by 30~40 dB; thus, it is not considered.

- (b)  $80 \text{ Hz} < f_m < 2 \text{ kHz}$ . In this range, PFD, frequency divider, and other noises come in, the multiplied reference noise from (13) is degraded, and the noise slope becomes smaller. Conventional in-LPBW PN simulation method assumes PN remains unchanged from  $f_{flicker}$  to LPBW as

$$PN_{PLO} (\text{dBc/Hz}) = PN_{floor} (1 \text{ Hz}) + 10 \lg(f_{PFD}) + 20 \lg(N). \quad (16)$$

There are two obvious drawbacks. Firstly, PN in this region is not constant; secondly, PFD frequency specified in the datasheet cannot be applied in every design. A modified method introduces a new mean frequency  $f_{mid}$  ( $f_{mid} = \sqrt{f_{flicker} \times \text{LPBW}}$ ), with its PN calculated by

$$PN_{f_{mid}} (\text{dBc/Hz}) = PN_{floor} (1 \text{ Hz}) + 10 \lg\left(\frac{f_{PFD}}{f_{PFD,G}}\right) + 10 \lg(f_{PFD}) + 20 \lg(N), \quad (17)$$

where  $PN_{floor}(1 \text{ Hz})$  is the normalized 1 Hz PN floor at a specified PFD frequency ( $f_{PFD,G}$ ) from datasheet, and  $f_{PFD}$  is the actual PFD. A negative slope of about -13 dB/dec is employed between  $f_{flicker}$  and  $f_{mid}$ . A noise peaking of 3~5 dB is always present between  $f_{mid}$  and LPBW. Therefore, PN can be simulated by  $f_{flicker}$ , the negative slope and LPBW.

**4.2. Multiplier Output PN Simulation.** Once the 4 GHz PN has been simulated, the PN of 8 GHz, 16 GHz and 32 GHz can be proposed by

$$PN_{MUL} (\text{dBc/Hz}) = PN_{PLO} + 20 \lg\left(\frac{f_{MUL}}{f_{PLO}}\right) + PN_{deg}, \quad (18)$$

where  $PN_{MUL}$  is the output PN of frequency multiplier, and  $f_{MUL}$  and  $f_{PLO}$  represent multiplier output and PLO output frequency, respectively.  $PN_{deg}$  is the PN degradation coefficient of 1~2 dB due to power noise. The degradation of PN for each multiplied frequency is 6~8 dB. The parameters used in the above method are shown in Figure 4 with only upper side-band PN depicted.

## 5. Results and Discussions

**5.1. Synthesizer Design.** The design of FS PLO is performed with reference to the PN simulation method above. As FOFR PN is negligible and its main PN contributor is VCO, a PLO chip with an on-chip VCO is preferred, which is lower in cost than multichip designs. From MOFR discussions, large PFD frequency is preferred (also smaller  $N$ ); thus, a chip with a larger PFD frequency is preferred [22~24]. Other loop parameters such as -65 dBc spur control, LPBW, and phase margin are required. A common rule for LPBW is 1/10~1/20 of PFD frequency [25]. A narrow LPBW trades lock time for steeper attenuation on PN and spurs but may cause in-LPBW PN to rise [26]. 40 kHz and 100 kHz are set for LPBW from MOFR PN control and spur requirements (limited to -65 dBc for 8 GHz). The common rule of phase margin is 30~55 deg, and 45 deg is a balanced choice between oscillatory and sluggish loops [27]. A 3rd-order loop filter is designed on known methods [22, 28].

**5.2. PN, RMS Phase Error Simulations and Test Results.** PN profiles are simulated by the above methods and also measured [29] (Figure 5). Simulation and measurement results are given in Tables 2 and 3 and Figure 6.

It is clearly observed from Tables 2 and 3 that the PN simulations are in good agreement with test results. PN in the VNOFR (10 Hz), MOFR (100 and 1 kHz), and FOFR ( $\geq 10$  kHz) all agree well with measurement results. From PN measurements in Figure 6, it is observed that PN degradation due to frequency multiplication also agrees well with the simulations.

The integrated RMS phase error simulations in Tables 4 and 5 are obtained from PN simulations in Tables 2 and 3, and good agreement has been observed with test results.  $PHEr_{RMS,4 \text{ GHz}}$  and  $PHEr_{RMS,8 \text{ GHz}}$  are limited to 1.3 deg and 2.4 deg (double sideband), by which BHU-2D FS PN requirements of (12) are reached.

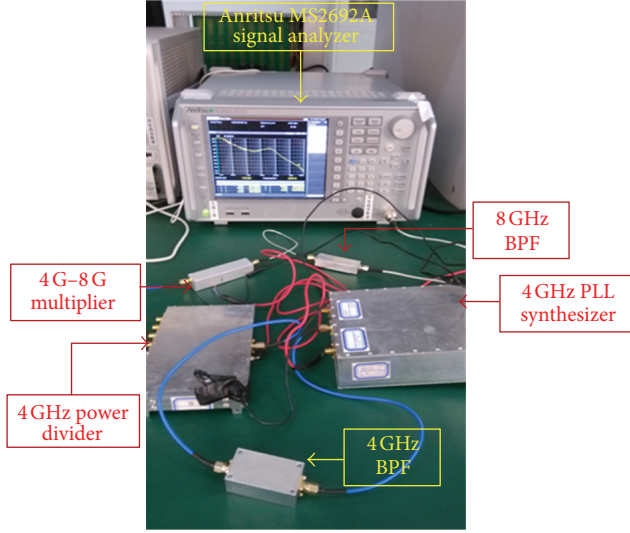


FIGURE 5: 8 GHz phase noise measurement setup.

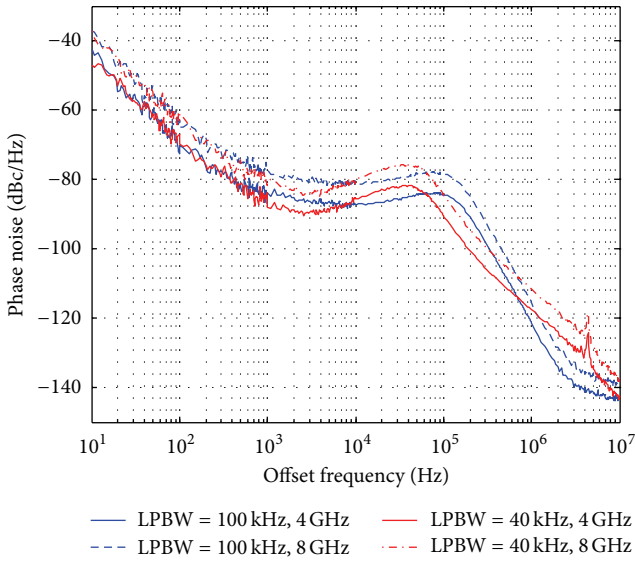


FIGURE 6: Phase noise measurement results.

**5.3. LPBW Discussions for SAIR FS Design.** There are several findings on LPBW from above results. Firstly, as lock time is not specified, LPBW is noncritical for SAIR LOs, and different LPBWs yield similar PN and phase errors in MOFR. In a wider frequency range (10 Hz~10 MHz), wide LPBW does lead to more integrated RMS phase error (13% more, from 6.053–6.842 deg for 8 GHz), but narrow (40 kHz) or wide (100 kHz) LPBW PLO yields nearly identical phase error results in MOFR, with only 2.4% rise from 2.216 deg to 2.268 deg for 8 GHz. As a higher LPBW leads to a smoother PN profile without degradation to design requirements, it is preferred in SAIR FS design.

TABLE 2: Phase noise test results (LPBW = 40 kHz).

Parameter	Offset Freq. (Hz)	Simulation (dBc/Hz)	Measurement (dBc/Hz)
4 GHz phase noise	10	-39.97	-47.00
	100	-69.97	-69.72
	1 K	-85.58	-87.94
	10 K	-92.58	-85.69
	100 K	-95.45	-90.75
	1 M	-120.45	-117.56
8 GHz phase noise	10 M	-146.45	-142.69
	10	-33.98	-37.07
	100	-63.98	-61.02
	1 K	-79.58	-80.65
	10 K	-76.58	-80.16
	100 K	-83.45	-84.87
	1 M	-112.45	-111.54
	10 M	-137.45	-137.68

TABLE 3: Phase noise test results (LPBW = 100 kHz).

Parameter	Offset Freq. (Hz)	Simulation (dBc/Hz)	Measurement (dBc/Hz)
4 GHz phase noise	10	-39.97	-42.58
	100	-69.97	-68.66
	1 K	-85.79	-86.77
	10 K	-95.98	-94.77
	100 K	-90.98	-90.36
	1 M	-120.45	-117.30
8 GHz phase noise	10 M	-146.45	-142.44
	10	-33.97	-37.96
	100	-63.97	-62.79
	1 K	-79.79	-80.94
	10 K	-89.98	-88.91
	100 K	-83.98	-84.40
	1 M	-112.45	-111.32
	10 M	-137.45	-137.39

TABLE 4: Integrated RMS phase RMS results (LPBW = 40 kHz).

Parameter	Offset Freq. (Hz)	Simulation	Measurement
$PHE_{RMS,4\text{ GHz}}$	20~80	1.098 deg	1.064 deg
	80~2 K	0.448 deg	0.455 deg
	20~2 K	1.170 deg	1.158 deg
	10~10 M	2.875 deg	3.082 deg
$PHE_{RMS,8\text{ GHz}}$	20~80	2.015 deg	1.984 deg
	80~2 K	1.007 deg	0.989 deg
	20~2 K	2.275 deg	2.216 deg
	10~10 M	6.064 deg	6.053 deg

TABLE 5: Integrated RMS phase RMS results (LPBW = 100 kHz).

Parameter	Offset Freq. (Hz)	Simulation	Measurement
$PHEr_{RMS,4\text{ GHz}}$	20~80	0.942 deg	0.957 deg
	80~2 K	0.501 deg	0.515 deg
	20~2 K	1.114 deg	1.086 deg
	10~10 M	3.351 deg	3.469 deg
$PHEr_{RMS,8\text{ GHz}}$	20~80	2.179 deg	2.039 deg
	80~2 K	1.032 deg	1.049 deg
	20~2 K	2.302 deg	2.268 deg
	10~10 M	6.815 deg	6.842 deg

TABLE 6: MIRAS and BHU-2D-U OFR comparison.

Parameter	MIRAS	BHU-2D-U
Integration time	1.2 s	0.05 s
FOFR	>100 Hz	>2 kHz
VNOFR	<1 Hz	<20 Hz
MOFR	1 Hz~100 Hz	20 Hz~2 kHz

## 6. Conclusion

In this paper, PN effects on visibility errors for BHU-2D-U SAIR system have been investigated and concretized to synthesizer PN design requirements from system-level analysis. FS design is given accordingly, and good agreements between simulation and measurement results is observed, with the following conclusions drawn.

For PN OFR separations and requirements, the conclusions are as follows. (1) Due to HIR imaging requirement of BHU-2D-U, OFR separation is different from MIRAS, as shown in Table 6. BHU-2D-U MOFR spreads much further into higher offset frequencies than MIRAS. For MIRAS, the MOFR stays within the flicker noise corner of the reference oscillator, but BHU-2D-U MOFR covers a part of in-LPBW PN that is out of flicker noise region. (2) VNOFR incurred phase error cannot be quantified by PN, and FOFR PN has negligible effects on visibility phase errors. MOFR is the main contributor of uncorrelated PN that can be controlled by FS PN. (3) The PN simulation method is proposed in detail for the newly divided OFRs. The MOFR is further divided by  $f_{\text{flicker}}$ , and PN and integrated RMS phase errors are simulated accurately. Measurement results of integrated RMS phase errors are better than those of MIRAS specifications.

From SAIR FS design perspective, the findings are as follows. (1) As lock time is not important, there is plenty of freedom on LPBW. (2) A slightly higher LPBW leads to smoother in-LPBW PN without noticeable degradation for MOFR phase error requirement of (12). (3) As all interested OFRs are inside LPBW, VCO noise contribution is usually not critical. A low-cost on-chip VCO works well for SAIR synthesizer.

The PN analysis method has been proved to fulfill the specific SAIR phase noise requirements, and the synthesizer designed has been successfully in operation in BHU-2D-U system. Future research works include improvements on

PN and its effects on imaging. These optimizations are also related to system-level improvement plans.

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