

Research Article

Waypoint Position Optimization for Accurate Ground-Based Arrival Time Control of Aircraft

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In the ground-based arrival time control operation, the measurement of the arrival time error and the speed advisory to cancel it are performed at specific waypoint(s). It is generally recognized that the arrival time accuracy depends on the accuracy of trajectory prediction and control and the availability of information about the aircraft intent. Additionally, the position of the waypoint also determines the arrival time accuracy. Therefore, in this study, the feasibility of waypoint position optimization to improve the arrival time accuracy of aircraft controlled by ground-based speed advisory and its effectiveness are discussed. The models of flight time uncertainty and the arrival time control window were developed using the actual track and numerical weather forecast data. An optimization problem was formulated that defined the arrival time uncertainty at the terminal point as the objective function and numerically solved using sequential quadratic programming. Through numerical investigations, the feasibility of the waypoint position optimization and its effectiveness were clearly demonstrated in comparison with uniform arrangement cases. It was also clarified that the advantage of the multiple waypoint application was enhanced when larger arrival time control windows were available.

1. Introduction

In future air traffic plans [1–3], civil aviation authorities plan to introduce a time-based operation to manage the increase of air transportation demand. Arrival management (AMAN) is recognized as one of the promising applications of a time-based operation. In the original AMAN concept [4, 5], aircraft descend from the cruise altitude to reach the merging point placed near an airport, for example, the runway threshold, and the waypoint at an intermediate altitude at each aircraft’s required time to achieve efficient time separation. The required time to arrive at the merging point is determined by air traffic controllers (ATCs) based on the estimated time of arrival (ETA) of aircraft in the same traffic stream. Aircraft equipped with required time of arrival (RTA) functionality can satisfy this using the airborne control [6]. However, not all aircraft are equipped with RTA functionality, and, in particular, fewer aircraft are equipped with it for descent trajectories [6]. For an aircraft incapable of the RTA functionality on a descent trajectory, it is necessary for the ground controllers to estimate its arrival time from its state and indicate the airspeed to satisfy the required time to arrive for an appropriate separation from the preceding aircraft. Additionally, as an increase of unmanned air systems is expected [7, 8], it is possible that the need for ground-based trajectory management will increase.

Numerous studies concerning ground-based trajectory management have been devoted to clarifying its feasibility [9–15] and improvement of operability [16–19], efficiency [20, 21], and accuracy [22–24]. Among the studies on accuracy improvement, the improvement of wind prediction accuracy [22, 24] and ground use of flight intent [23] have often been the focus. Despite the fact that the position of the waypoints used to measure the time to arrive and determine the flight speed to satisfy the required time are also expected to affect the arrival time accuracy, conventional waypoints have been applied in the aforementioned past studies. Although the application of multiple waypoints has been introduced to improve the arrival time accuracy [14], only conventional waypoints have been used. Even in a recent study on the application of the ground-based speed advisory [25], the waypoints were evenly spaced. Thus, no studies have been
conducted on the optimum positions of the waypoints to improve the accuracy of ground-based arrival time control.

In this study, we aim to clarify the feasibility of waypoint position optimization to improve the arrival time accuracy of ground-based arrival time control. For this purpose, the uncertainty model of the ground-based trajectory prediction is derived using actual operation data and weather forecast data. Additionally, the arrival time control window models using the speed advisory are also derived. Through numerical analysis using these models, the feasibility of the optimum waypoint position and its effectiveness are investigated. The waypoint optimization is extended for the application of multiple waypoints, and its effectiveness is clarified.

Flight trajectories to Tokyo from the westward direction are particularly focused on in this study because they represent the heaviest traffic in Japan. The descent trajectory under consideration is shown in Figure 1. Aircraft continuously descend from the initial point at an altitude of 30,000 ft to the terminal point placed 120 km away at an altitude of 15,000 ft. This trajectory was determined to imitate the flight path angle of the actual descent trajectories toward Tokyo presented in the next section. The following sequence of the arrival time control operation is considered: (1) before departure, the pilot enters the descent route parameters including the optimized positions of waypoints into the Flight Management System; (2) before arriving at the initial point, the pilot is provided with a constant indicated airspeed (IAS) by the ATC to satisfy the required time to arrival at the terminal point; (3) at the moment of passing through the waypoints, the flight time error is measured and the ATC newly calculates a constant IAS to meet the indicated required time to arrive; and (4) the pilot receives the calculated IAS and immediately adjusts the IAS to the received IAS using Mode Control Panel.

2. Track and Weather Data

In this study, the secondary surveillance radar (SSR) Mode S data measured at the ground station in a Tokyo suburb were used for analysis. The following data were provided [26]: clock, aircraft identifier and type, longitude and latitude, pressure altitude, true track angle, ground speed (GS), magnetic heading, true airspeed (TAS), and IAS. Aircraft data within 250 NM from the ground station were provided once every 10 s. The SSR Mode S data acquired from December 1 to 31, 2014, were selected for analysis. The aircraft trajectories toward Tokyo were extracted by limiting the heading angle from 60 to 100 degrees in the area in which the latitude was below N35 deg. As aircraft usually maintain their IAS during descent, the flight segment data with almost constant IAS, where its moving average was below 0.1 kt/s and no continuous acceleration or deceleration longer than 30 s was recorded, were extracted as the typical operation trajectories. Their lateral and vertical paths and the relationship between the IAS and altitude are shown in Figure 2. The total number of extracted trajectories was 3,084.

The wind forecast data were provided as the grid point value of the numerical weather forecast data by the Japan Meteorological Agency [27]. This model was developed to precisely predict the weather around the Japanese territory. The wind vector and temperature data were provided every 3 hours, containing every 0.1 degrees in both longitude and latitude. In the analysis, the wind forecast data were applied using linear interpolation.

3. Flight Time Uncertainty Model

The flight time error arises from the difference between the intent GS and actual GS. The actual GS was provided in SSR Mode S data. However, no information concerning the flight intent was provided. In a time-based operation, the intent GS is determined according to the required arrival time, the intent TAS is determined according to the intent GS and forecast wind speed, and the intent IAS is calculated from the intent TAS. Therefore, in this study, the intent GS was estimated from the IAS recorded in SSR Mode S data and weather forecast data. Because the aircraft in descent phases toward a destination airport was inferred to maintain a constant IAS, as mentioned above, the intent IAS was determined as the average IAS of each trajectory. Then, the intent IAS was translated into the intent TAS using the forecast temperature and pressure [28]. The intent GS was estimated as the sum of the intent TAS and the forecast wind speed in the flight direction. Finally, the flight time error for a certain distance \( D \) was obtained as

\[
T_{err} = T_{act} - T_{int},
\]

where

\[
\int_0^{T_{act}} GS_{act} dt = D
\]

and

\[
\int_0^{T_{act}} GS_{int} dt = D.
\]
<table>
<thead>
<tr>
<th>Distance [km]</th>
<th>Num. of Samples</th>
<th>Mean Dev. [s]</th>
<th>STD [s]</th>
<th>RMS [s]</th>
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<td>151</td>
<td>4.24</td>
<td>20.64</td>
<td>21.00</td>
</tr>
</tbody>
</table>

Distance of 40 km is shown in Figure 6, which shows that the flight time error distribution is mound-shaped and slightly biased. Because the actual data were processed, the mean values could never become exactly zero, even though they were rather small. Therefore, in this study, the RMS value was regarded as the measure of the flight time uncertainty. It is obvious that the RMS value was almost linearly proportional to the flight distance. Its approximate function was obtained as follows:

\[
s(D) = 1.95 \times 10^{-4} D \text{[sec]},
\]

where \(D[m]\) is the flight distance. Thus, the flight time uncertainty model was obtained as a function of the flight distance.
4. Arrival Time Control Window Model

Based on the IAS distribution shown in Figure 3, it was supposed that the maximum and minimum operational IASs were 320 kt and 230 kt in this study. The arrival time also depends on the tailwind speed. In this study, the mean deviation and STD of the tailwind speed were analyzed, and the average and faster/slower tailwind cases were considered in the numerical investigations. The mean deviation and STD of the tailwind for every 1,000 ft of altitude are summarized in Figure 7. To evaluate the flight time between the initial and terminal points while maintaining the constant IAS of 230 kt or 320 kt, the GS was calculated as the sum of the tailwind and TAS translated from the IAS using the average temperature and pressure. The flight time profile of the cases of 230 kt IAS and 320 kt IAS are shown in Figure 8. The difference between the flight times of these trajectories can be regarded as the arrival time control window. In this study, the nominal trajectory was supposed to have the same reducible and extensible times to arrive at the terminal point. In the average wind case, the arrival time control window, equal to half the difference between the reducible and extensible times, became approximately 60 s to arrive at the terminal starting from the initial point. When the tailwind was slower or faster than the average value, the arrival time control window became larger or smaller, respectively. The arrival
time control window became a function of the flight distance, which was numerically obtained as follows for the cases with the average and \( \pm 2\sigma \) wind:

\[
t^{\text{ext}}(D) = t^{\text{red}}(D) = \begin{cases} 
1.03 \times 10^{-9}D^2 + 5.44 \times 10^{-4}D & \text{average wind} \\
9.97 \times 10^{-10}D^2 + 4.10 \times 10^{-4}D & \text{\( \pm 2\sigma \) wind} \\
9.25 \times 10^{-10}D^2 + 3.20 \times 10^{-4}D & \text{+2\sigma wind} 
\end{cases}
\] (5)

These functions are also shown in Figure 9.

5. Feasibility of Waypoint Position Optimization

To clarify the feasibility of waypoint optimization, the introduction of only one waypoint was considered, and the flight time uncertainty at the terminal point was evaluated by changing its position. For clarity in the investigation, it was assumed that deceleration and acceleration occurred instantaneously and that the flight time error followed a normal distribution based on the central limit theorem.

As was demonstrated in the previous section, the flight time uncertainty increased in proportion to the flight distance. The distribution of the flight time error at the waypoint became like that shown in Figure 10(a). In this case, the aircraft could cancel the flight time error between the arrival time control window before arriving at the terminal point and the flight time error distribution reduced to become like that shown in Figure 10(b). Simultaneously, the flight time uncertainty shown in Figure 10(c) again increased in proportion to the distance to the terminal point. Then the flight time uncertainty was obtained as the sum of the STDs of these distributions. The flight time error distribution at the terminal point is shown in Figure 10(d). Thus, it is possible to estimate the arrival time uncertainty at the terminal point using the models of the flight time uncertainty and arrival time control window.

As was expected from the above example, the arrival time uncertainty at the terminal point became the function of the metering waypoint position. Provided that the flight time followed a normal distribution, the STD of the arrival time at the terminal point was calculated as follows:

\[
STD_{\text{terminal}} = \left( \int_{-\infty}^{0} t^2 f(t - t^{\text{ext}}(D_{\text{WP}})) \, dt + \int_{0}^{\infty} t^2 f(t + t^{\text{red}}(D_{\text{WP}})) \, dt \right)^{1/2} + \sigma(D_{\text{terminal}} - D_{\text{WP}}),
\] (6)

where

\[
f(t) = \frac{1}{\sqrt{2\pi} \sigma} \exp\left(-\frac{t^2}{2\sigma^2}\right),
\] (7)

and \( D_{\text{WP}} \) and \( D_{\text{terminal}} \) are the positions of the waypoint and terminal point, respectively.

The behaviors of the STD at the terminal point in the cases of the average and \( +2\sigma \) and \( -2\sigma \) wind are summarized in Figure 11. It was found that the optimum waypoint position became slightly closer to the terminal point from the middle position of 60 km. It was also found that the optimum waypoint position became closer to the terminal point, and the optimum accuracy became better as the arrival time control window became larger. It is considered that it is more preferable for the arrival time control with a smaller control window to cancel the flight time error at the earlier position where its STD is still sufficiently small for the small control window. By contrast, when the control window was larger, the optimum waypoint position became later to minimize the flight distance to increase the flight time error uncertainty. Thus, the feasibility of waypoint optimization for arrival time accuracy improvement has been clearly demonstrated. However, its effectiveness seems only a little better compared with the case of the middle waypoint placement.
6. Position Optimization of Multiple Waypoints

To investigate the effectiveness of multiple waypoints, it is necessary to formulate a nonlinear optimization problem. The objective function is the STD estimated at the terminal point. This becomes a function of the number and positions of the waypoint expressed as follows:

\[
\min STD_{\text{terminal}}(D_1, D_2, \ldots, D_N),
\]

where the STD obeys the following nonlinear recurrence relation:

\[
STD_{i+1} = \left( \int_{-\infty}^{0} t^2 f_i(t - t^{\text{ext}}(D_{i+1} - D_i)) \, dt + \int_{0}^{\infty} t^2 f_i(t + t^{\text{ext}}(D_{i+1} - D_i)) \, dt \right)^{1/2} + \sigma(D_{i+1} - D_i),
\]

subject to the following constraints:

\[
0 < D_1 < D_2 < \cdots < D_N < D_{\text{terminal}}.
\]

Because the objective function in this formulation is nonlinear, sequential quadratic programming [29] was applied for its optimization analysis, where the multistart method was used to avoid local minimum solutions. The optimization results are summarized in Figure 12, which shows the STD at the terminal point by applying the evenly and optimum placed multiple waypoints with the control windows of the average and -2σ wind conditions. The horizontal axis shows the number of waypoints between the initial and terminal points. It is clear that the optimized placement of the waypoints reduced the STD, and that the STD reduction rate became larger as the number of waypoints increased. It
was also clarified that a larger control window enhanced the accuracy in the optimized waypoint cases, whereas a larger control window rarely contributed to the STD reduction in the evenly placed cases. The even and optimized waypoint placements are summarized in Figure 13. The optimized waypoint was placed backward compared with the even waypoint. To investigate this in detail, the history of the STD is summarized in Figure 14, where the horizontal axis shows the distance and the vertical axis shows the STD at each waypoint. Whereas the STD at the evenly placed waypoints remained almost constant, the optimized waypoints were placed closely in the latter part of the trajectory to minimize the STD at the terminal point despite the fact that the STD in the former part of the trajectory once increased larger than that of the evenly placed waypoints case. These characteristics were enhanced when the arrival time control windows increased.

7. Conclusion

The feasibility of waypoint optimization for the ground-based arrival time control operation and its effectiveness were investigated using flight time uncertainty and arrival time control window models developed using actual track data and weather forecast data. In this study, the STD at the terminal point was considered as the objective function of the optimization. The feasibility and basic characteristics of the waypoint optimization were demonstrated through analysis using one waypoint. To enhance its effectiveness for accuracy improvement at the terminal point, the application of multiple waypoints and the effect of the arrival time control window were numerically investigated. It was clarified that the simultaneous applications of multiple waypoints and the optimization of the waypoint position achieved a significant improvement of arrival time accuracy. It was also clarified that its effectiveness was enhanced when a larger arrival time control window was applied. From this result, it is expected that the waypoint optimization for arrival time accuracy improvement will become more effective when a more accurate trajectory prediction becomes available. Additionally, it is considered that the optimum waypoint placement also depends on the wind condition that determines the arrival time control window. It must be noted that the accuracy of the flight time uncertainty model is essential in this study. Further investigations of the uncertainty model are necessary.

In this fundamental study on waypoint optimization, many assumptions were made, for example, no difference among aircraft types, the trajectory prediction and control error independent of the weather condition, the normal distribution of the flight time error based on the central limit theorem, and instantaneous speed change. Additionally, only the case in which the nominal trajectory had the same reducible and extensible times to arrive at the terminal point was investigated to clarify the fundamental characteristics. For practical use, these assumptions must be mitigated, and various practical cases must be investigated in detail in future work. Although the flight trajectory considered in this study
is just a part of a descent trajectory, because of the limitation of the available track data, the fundamental characteristics found in this study will also be applicable to the entire trajectory. Because the effectiveness of waypoint optimization will be enhanced in longer trajectories, some investigations on its application to cruise trajectories are necessary to demonstrate its worthiness for practical use. Furthermore, the concept of arrival time uncertainty management presented in this study is considered applicable to the time-based operation using RTA functionality, for example, the waypoint placement to minimize the possibility that the arrival time required from the ATC goes out from the ETA window of the RTA functionality.

Conflicts of Interest
The author declares no conflicts of interest.

References


