Research Article

The Effect of Temperature on the Spectral Emission of Plasma Induced in Water

B. Charfi

Département de Préparation Technologique, Institut Préparatoire aux Etudes d’Ingénieurs de Sfax (IPEIS), 3018 Sfax, Tunisia

Correspondence should be addressed to B. Charfi; bilel_charfi@yahoo.com

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A numerical modeling investigation of the spectral emission of laser-induced plasma in MgCl$_2$-NaCl aqueous solution has been presented. A model based on equilibrium equations has been developed for the computation of the plasma composition and excited levels population. Physical interpretation is presented to comment on firstly the evolution of atomic species number densities, and secondly on the population of the excited species emitting MgII and NaI resonant lines for temperatures ranging from 3000 K to 20 000 K. It is shown that MgII line reach a maximum of population on the issuing level, at norm temperature of 13800 K. Whereas, NaI line presents two norm temperatures, evaluated at 3300 K and 11700 K. This splitting of the NaI norm temperature is explained by the low-ionization potential and weak concentration of the sodium atom in this aqueous solution. Thus, the proposed model can be useful to predict the optimal plasma temperature for the detection of given chemical element, which is not easy to reveal experimentally.

1. Introduction

Laser-Induced Breakdown Spectroscopy (LIBS) is identified as the optical emission spectroscopy of the laser-induced plasma [1–3]. LIBS has been acknowledged as a useful tool for the analysis of solid samples. However, for the liquids analysis, the application of such technique was relatively delicate and has been confronted to several drawbacks related to the short lifetime and the poor spectral signal of the plasma induced in liquids [4–8]. In previous work [9], the LIBS sensitivity has been improved by optimization of parameters influencing the spectral emission of the plasma induced on water target. This enhancement has been carried out in a 50 mg/L MgCl$_2$-NaCl mixed solution; particular attention is paid to the spectral emission of MgII (279.55 nm) and NaI (588.99 nm) lines. The intensity of those resonant spectral lines, emitted from the laser-induced plasma on the water sample, is found to be dependent on parameters of LIBS analysis system, such as laser pulse energy and delay time (observing time after firing the laser) [9].

Several studies have been reported on the correlation between the LIBS emission spectra from a water target and LIBS system parameters [5, 9–11]. For example, Adamson et al. [10] observed the dependence of LIBS emission spectra, mainly the hydrogen H-alpha and H-beta emission lines on gate time and laser pulse energy.

Samek et al. [5] reported the effect of delay time on the intensities of the H-alpha, Li, and Na peaks lines when performing LIBS on aqueous samples.

However, relatively few works have been concerned with theoretical approach of the dependence of line intensities emitted from water plasma on the LIBS system parameters; for example, Ahmed and Jaidane [11] simulated the time evolution of lines intensities emitted from Ca, Ca$^+$, Mg, and Mg$^+$ using a simple theoretical approach based on electron-ion recombination. It should be noted that this dependence of lines intensities on the mentioned LIBS system parameters is related, for the most part, to the plasma temperature, since the change of any of the LIBS parameters leads to variation of the plasma temperature.

The work described in this paper is motivated by the desire to gain fundamental knowledge concerning the effect of plasma temperature on Laser-Induced Plasma Spectral Emission (LIPSE), and ultimately to determine the suitable plasma temperature for the detection of a given chemical element.
The first part of this work is devoted to a brief description of assumptions used for the LIPSE study. The second part presents the calculation of the number densities of species considered in the MgCl$_2$-NaCl aqueous solution. In the last part of the paper, results concerning the densities of species emitting MgII and NaI lines are presented as a function of plasma temperature.

2. Theoretical

2.1. Assumptions. The interpretation of LIPSE is a complex task with many unsolved problems. The most important questions concern the ablation mechanisms [12], the chemical reactivity [13, 14], the deviations from equilibrium [12, 14, 15], self-absorption phenomenon [11, 15], and the matrix effect [12, 16].

Nevertheless, the description of LIPSE phenomenon can be simplified by making certain hypothesis [17, 18]. For this work the following assumptions have to be considered.

1. Conventionally, LIBS measurements are made in the microsecond time scale, that is, when the LIBS plasma is under recombination conditions. In the microsecond regime of the plasma lifetime, typical values of electron number density $n_e$, and plasma temperature $T$, range in the interval $10^{15} < n_e < 10^{18}$ cm$^{-3}$ and $3000 < T < 20000$ K [10, 14, 15]. The study presented in this paper is limited to this temperature range $3000–20000$ K.

2. The reported $n_e$ and $T$ ranges are considered sufficient to create plasma satisfying LTE (Local Thermodynamic Equilibrium) conditions, [10, 14, 15, 18, 19]. Under this LTE hypothesis, the plasma is considered to be sufficiently dilute that particles are independent and indistinguishable, allowing a Boltzmann statistical description and the application of Dalton’s law for partial pressures [16, 18–20].

3. For the temperature range considered in this study, the plasma induced in MgCl$_2$-NaCl solution, is supposed to be composed of the following species: electrons (e$^-$), H, H$^+$, O, O$^+$, Na, Na$^+$, Mg, Mg$^+$, Mg$^{++}$, Cl, Cl$^+$, H$_2$O, O$_2$, OH, and H$_2$. Species with elevated ionization energy ($E_i > 20$ eV) have not been taken into account; indeed, their existence require excessively high temperatures (out of our range of interest).

4. The laser-induced plasma is supposed to be homogeneous. It is well known that plasmas present a spatial distribution of their parameters. This plasma inhomogeneity yields to a self absorption of resonant spectral lines. Solving a model for those inhomogeneous plasmas could be very complicated. However for a water-plasma at the end of its cooling process and within a short observation window, spatial gradients have a lower influence on the plasma parameters. Thus the homogeneity of the plasma and optical thinness are assumed, that is, the reabsorption effect is neglected for the plasma induced on the liquid surface.

5. The laser-induced plasma is treated as a closed system, where matter conservation and electrical neutrality are assumed. Of course this assumption is suspect but it is made in this work to simplify the problem.

2.2. LTE-Model. Considering the above assumptions, the intensity $I_{nl}$ of given spectral line emitted from the laser-induced plasma, corresponding to a transition from an upper excited level $m$ to a lower excited level $l$ is given by [15, 16]

$$I_{nl} = F \cdot A_{ml} n_m \cdot h \nu_{nl},$$

(1)

where $F$ is an experimental factor which depends on the probing volume of the plasma and the spectral response of the detection system, $A_{ml}$ is the transition probability from level $m$ to $l$, $n_m$ is the number density of atoms on the upper excited level $m$, $h$ is the Planck’s constant, and $\nu_{nl}$ is the frequency of the transition.

As the laser-induced plasma satisfied the local thermodynamic equilibrium (LTE), levels populations obey the Boltzmann statistic, that is, the population $n_m(T)$ of an upper excited level $m$ is related to the total number density $n(T)$ by the Boltzmann equation [18]:

$$n_m(T) = \frac{n(T)}{U(T)} \cdot g_m \exp \left( \frac{E_m}{kT} \right),$$

(2)

$g_m$ is the statistical weight of the excited level $m$, $E_m$ is the corresponding energy, and $k$ is Boltzmann’s constant.

$U(T)$ is the partition function of the corresponding specie, its value, is well tabulated in [19, 21].

In this work, the partition functions have been computed using NIST energy level data [21]; then the obtained values are verified with those reported by Drawin and Felenbok [19].

It should be noted that the relevant partition functions are those calculated by using only observed levels. This is a crude approximation because it neglects the existence of many other levels. However, in general, partition function varied slightly over low-temperature range.

According to (1), to understand the dependence of line intensity on the plasma temperature, the evolution of excited level population $n_m(T)$ as function of temperature should be investigated, which require the determination of the corresponding specie density $n(T)$, as shown in (2).

In this model, assuming the LTE state of the laser-induced plasma, a system of equations with species densities as unknowns could be formed by Dalton, matter conservation, and Saha and Guildberg-Waage equations. This equilibrium model based on the LTE assumption is referred to, as the LTE-model.

3. Results and Discussion

3.1. Plasma Composition. Adopting the LTE-model, a code is written in Maple language for the numerical computation of the plasma composition. The “solve” Maple command is used for solving the system of equations.
The system is initialized by an approached value of the electron density at the starting calculation point, then equations system is solved and a new value for $n_e$ is calculated.

This code has been adapted to calculate the composition of equilibrium plasma of 50 mg/L MgCl$_2$-NaCl aqueous solution at atmospheric pressure, for given temperature.

To corroborate our calculation, species number densities calculated with this numerical code for water-alkaline salt plasma are compared with previous published data in [17], the model reproduces with satisfactory accuracy results reported by Hannachi et al. It is also interesting to make comparison with experimental data from literature, but to our knowledge, there are no available experimental measurements for species number densities of plasma induced in aqueous solution.

Results presented in Figure 1 illustrate densities of elemental species considered in the equilibrium plasma of 50 mg/L MgCl$_2$-NaCl aqueous solution at atmospheric pressure, for temperatures ranging from 3000 to 20 000 K.

Figure 1 shows a progressive disappearance of neutral species with increased temperature. In parallel, densities of charged species (H$^+$, O$^+$, and Cl$^+$) grow up exponentially; for example, density of H$^+$ ion, $n_{H^+}$ ($T$) gain two orders of magnitudes from 6000 K to 12 000 K. In this temperature range, the intensive ionization of major species leads to an increase of the electron density; this excess of electron density favors the recombination process of Na$^+$ ions, due to the low-ionization potential of sodium. This process of Na$^+$ recombination compensate the sodium ionization process, which explain the flat curve of sodium density noted between 6000 K and 12 000 K.

After reaching maximal values, charged species densities follow a slight decrease, for example, H$^+$ density stays nearly constant around 17 000 K, with $n_{H^+}(T) \sim 10^{17}$ cm$^{-3}$, then it decrease slightly from 19 000 K. This weak decrease is interpreted with the Dalton’s law. Since the total pressure of the plasma is supposed to be invariable, the temperature increase must be accompanied with a reduction of the total number of species which promote recombination process, and consequently decrease the charged species density.

Concerning the electrons density $n_e$, three regions can be distinguished. At low plasma temperature ($T$ < 4000 K), the electrons density can be identified by Na$^+$ density: $n_e \sim n_{Na^+}$; indeed, sodium presents the lowest ionization energy (5.1 eV), thus, for low temperature the sodium ionization is nearly the sole source of electrons. In the temperature range 4000–5000 K, the neutrality is affected by the production of the Mg$^{++}$ ions, and the evolution of $n_e$ follow the evolution of Mg$^{++}$ density. For temperature higher than 5000 K, $n_e$ keeps a profile intimately adjacent to $n_{H^+}$; the neutrality is assured by hydrogen ion H$^+$; this is evident, since hydrogen, which has the highest ionization energy (13.6 eV), is the major element in the solution. At 17 000 K, the plasma reaches the saturation of electrons, with electron number density around $10^{17}$ cm$^{-3}$. Beyond 17 000 K, the electron density undergoes a slight decrease. In fact, at such elevated temperature the plasma is saturated of ionized species, and the electron density $n_e$ reaches higher values; therefore, Le Chatelier’s principle suggests that equilibrium is displaced towards the reduction of those species by recombination process.

Figure 1 shows the region of validity of the LTE assumption. In fact, the lower limit of electron density for which the plasma satisfies the LTE condition has been estimated to $10^{16}$ cm$^{-3}$ [9, 10]. According to Figure 1, the region of validity of LTE corresponds with temperature higher than 9000 K.

![Figure 1: Species densities as function of temperature, for plasma of MgCl$_2$-NaCl solution concentrated at 50 mg/L, at atmospheric pressure under thermal equilibrium](image-url)
3.2. Number Densities of Emitting Species. The spectroscopic analysis of LIBS spectrum obtained from water sample shows that only resonance emission lines, corresponding with lower energy excited states, exhibit well-resolved lines [5, 9]. This is due to the rapid water-plasma cooling; in fact plasma emission lifetimes are usually very short under such hydrated environment.

The most intense resonance lines, recorded in the LIBS spectrum of the MgCl$_2$-NaCl aqueous solution, are MgII (279 nm) and NaI (588 nm) lines [9]. Table 1 provides the energy levels, transition probabilities, and electronic configuration of those resonance lines.

Table 1 shows that MgII and NaI lines are emitted, respectively, from the magnesium-ionized species in the Mg(3p) excited state, and the sodium neutral specie in its Na(3p) excited state.

Applying the Boltzmann law equation (2), densities of those emitting excited species have been calculated from total densities of corresponding species which are already obtained by the LTE-model.

3.2.1. Population of Excited Level Mg(3p). Figure 2 present the emitting-atom densities at the excited level Mg(3p) of the spectral lines MgII(279 nm), as function of temperature, at atmospheric pressure in the plasma of MgCl$_2$-NaCl solution concentrated at 50 mg/L.

This figure shows that MgII spectral line reaches a maximum of upper-level population, at so-called norm temperature, $T^*$ [18, 23], assessed to 13800 K. The notion of norm temperature explains the competition between two processes promoted by the increase of temperature, namely, the excitation and the ionization. The excitation is a factor of population, contrarily, the ionization constitutes a factor of impoverishment for the emitting level.

A more detailed explanation is given by Boltzmann equation Equation (2) shows that the number of atoms on the superior level $n_m(T)$ is essentially a product of two temperature functions, $n(T)$ and $\exp(-E_k/kT)$. The partition function varies slightly at the considered range temperature. For low temperatures, the ionization process is so weak, thus the total atoms density $n(T)$ kept a constant value, and by the steep increase of the exponential function, the number of atoms in the superior level increases with the temperature. For high temperatures, the exponential term approaches unity; but, owing to the intensification of ionization process, the total atoms density $n(T)$ decrease with the temperature and it follows a reduction of atoms on the superior level. This change of emitting-atoms densities trend shows that for a spectral line, there is a maximum of population at a certain temperature $T^*$.

3.2.2. Population of Excited Level Na(3p). Figure 3 presents the number density on the emitting level Na(3p), of the sodium line NaI, as function of plasma temperature, at atmospheric pressure in the plasma of MgCl$_2$-NaCl solution concentrated at 50 mg/L.

Unlike the MgII spectral line, NaI line presents two maxima of upper-level population, at norm temperatures of 3300 and 11700 K. It should be noted that NaI norm temperatures are both lower than that of MgII.

<table>
<thead>
<tr>
<th>Element</th>
<th>$\lambda$ (nm)</th>
<th>Transition</th>
<th>$E_1$ (eV)</th>
<th>$E_2$ (eV)</th>
<th>$A_{21}$ ($10^8 s^{-1}$)</th>
<th>$g_1$</th>
<th>$g_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mg</td>
<td>279.55</td>
<td>3s$^2$S-3p$^2$P</td>
<td></td>
<td>0</td>
<td>4.43</td>
<td>2.68</td>
<td>2</td>
</tr>
<tr>
<td>Na</td>
<td>588.99</td>
<td>3s$^2$S-3p$^2$P</td>
<td></td>
<td>0</td>
<td>2.104</td>
<td>6.28</td>
<td>2</td>
</tr>
</tbody>
</table>
The curve of number density of Na(3p)-excited atoms as a function of temperature (Figure 3), can be interpreted as follows.

At low temperature ($T < 3300$ K), the increase of plasma temperature will serve to populate the excited level (as predicted by the exponential term of the Boltzmann equation). For temperatures ranging from 3300 to 5900 K, the ionization process of sodium becomes dominant and thus, there will be a decrease of sodium density and subsequently the density of sodium atoms on exited state Na(3p) decreases in this temperature range. In the temperature range 5900–11700 K, the ionization of major species in the aqueous solution, specifically hydrogen and oxygen atoms, leads to the increase of the electron density (Figure 1), this overload of electrons in the plasma favors the recombination process of Na$^+$ ions. This explains why the recombination and ionization processes are almost compensated in this temperature range, that is, the sodium density stay nearly constant as shown in Figure 1. As sodium density is roughly invariant in this temperature range (5900–11700 K), owing to the exponential term of the Boltzmann equation, the population of Na(3p) increases with temperature. For temperature higher than 11700 K the ionization dominates again, so the sodium atom density including excited-sodium density decreases with temperature.

Summing up, it seems that, the appearance of two norm temperatures for the NaI line is due, on the one hand to the near to the ground correspondent NaI emitting level and the low-ionization potential of the sodium atom and on the other hand to the low concentration of this species in the aqueous solution.

To make in evidence the effect of sodium concentration on the NaI norm temperatures, the density of excited sodium at Na(3p) state, as function of temperature is represented in Figure 4, for different concentration of sodium in the MgCl$_2$-NaCl aqueous solution.

This figure displays a disappearance of the splitting of NaI norm temperature for higher concentration of sodium. As Na concentration increase, the first maximum of NaI upper level population approaches the second one till both overlap forming only one maximum. The second norm temperature is approximately the same for all aqueous solutions. In fact the second peak of the density of excited sodium is related to the ionization of major species in the aqueous solution, such as hydrogen and oxygen atoms.

4. Conclusion

This work presents a theoretical interpretation for the understanding of the plasma temperature effect on the spectral emission of plasma induced in MgCl$_2$-NaCl aqueous solution. LTE model is carried out to compute the plasma composition and it allowed the estimation of atoms, ions, and electron densities in the laser-induced plasma in the water sample at atmospheric pressure, for temperature ranging from 3000 K to 20000 K. The populations of excited species emitting MgII and NaI lines are also calculated.

The obtained results reveal that MgII line presented a maximum of population on the issuing level, at norm temperature of 13800 K; However, NaI line presents two norm temperatures both lower than the MgII norm temperature. Considering the optically thinness assumption of the laser-induced plasma, the intensity of given spectral line is proportional to the number density of atoms on the upper excited level. Therefore, for better sensibility of the LIBS technique, comparing to the Mg II line, it is recommended to record NaI signal at relatively cold plasma, either by lowering the laser pulse energy, or by detecting the spectral emission at late stage of the plasma lifetime. Moreover, when using common broadband spectrometer systems that measure both lines at once it is suggested that spectrometers should collect light from early in the plasma when it is hot and stay open until it is cold to maximize signal from these two elements.

It should be noted that the numerical model built in this study is not restricted to magnesium and sodium aqueous solutions; it could be applied to any other water-alkaline salt mixture. As seen for magnesium and sodium species, for any other alkaline species such as lithium, calcium, and potassium, the corresponding norm temperature will depend essentially on the ionization potential, upper energy level, and dominance of the considered alkaline species in the aqueous solution.

In this work, it is assumed that the laser-induced plasma is ideal, that is, spatially homogeneous, electrically neutral, optically thin, in local thermodynamic equilibrium (LTE). In reality, not all these conditions may be fulfilled; the effect of departures from plasma ideality is planned for future investigations.

References


