Research Article

Statistical Analysis of Ratio of Random Variables and Its Application in Performance Analysis of Multihop Wireless Transmissions

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The distributions of random variables are of interest in many areas of science. In this paper, the probability density function (PDF) and cumulative distribution function (CDF) of ratio of products of two random variables and random variable are derived. Random variables are described with Rayleigh, Nakagami- m , Weibull, and α - μ distributions. An application of obtained results in performance analysis of multihop wireless communication systems in different transmission environments described in detail. The proposed mathematical analysis is also complemented by various graphically presented numerical results.

1. Introduction

The distribution of the ratio of random variables is of interest in statistical analysis in biological and physical sciences, econometrics, and ranking and selection [1]. It has been studied by several authors [2–5]. The ratio of random variables is also of interest in analysing wireless communication systems [6–9]. In wireless communication systems, one of problems is fading caused by multipath propagation. When a received signal experiences fading during transmission, signal envelope fluctuates over time [10]. There is a very wide range of statistical models for describing the statistical behaviour of signal envelope where accuracy and veracity depend on communication scenario and propagation environment. The most frequently applied models in the open technical literature are Rayleigh, Nakagami- m , Weibull, and α - μ . In addition to fading, the wireless transmission can be also subjected

to shadowing which is the result of large obstacles and deviations in terrain profile between transmitter and receiver. In such composite environments, signal envelope can be modelled with product of two random variables [11, 12]. A fundamental requirement in planning wireless communication systems, besides providing specified quality of service (QoS), is to ensure high system capacity. Cochannel interference (CCI) is a result of frequency reuse which is essential in increasing system capacity [13].

In the areas of deployment, connectivity, and capacity, multihop systems have a number of advantages over traditional communication networks. Relaying techniques enable network connectivity where traditional architectures are impractical due to location constraints and can be applied to cellular, wireless local area networks (WLANs) and hybrid networks. The performance analysis of multihop wireless communication systems operating in fading channels has been an important field of research in the past few years [14–17].

The main contribution of this paper is the derivation of useful closed-form expressions for the probability density function (PDF) and cumulative distribution function (CDF) of ratio of product of two random variables and random variable. Among the rest, these expressions can be used as general theoretical tool in the performance analysis of wireless communication systems since the product of random variables in nominator can represent signal envelope which suffers from fading and shadowing while the random variable in denominator can represent CCI envelope. Therefore, the ratio of such random variables is signal-to-interference ratio (SIR). Rayleigh, Nakagami- m , Weibull, and α - μ distributions are included in our analysis to enable wide range of use of results presented in the paper, that is, to model different transmission environments. Capitalizing on closed-form expressions derived in the paper in the terms of Meijer G functions, the outage probability of multihop system, as an important and widely accepted performance measure, is determined and discussed.

2. Statistics of Ratio of Products of Two Random Variables and Random Variable

In this section, statistical analysis of ratio of products of two random variables and random variable, $\lambda = xz/y$, is presented. For derivation of the corresponding PDF of λ , we have to obtain the PDF of products of two random variables, $t = xz$, using the following equation:

$$p_t(t) = \int_0^\infty |J| p_x\left(\frac{t}{z}\right) p_z(z) dz, \quad (2.1)$$

where $|J|$ is the Jacobian transformation given by $|J| = |dx/dt| = 1/z$. Using similar procedure, the PDF of λ can be derived as

$$p_\lambda(\lambda) = \int_0^\infty |J| p_t(\lambda y) p_y(y) dy, \quad (2.2)$$

where $|J| = |dt/d\lambda| = y$.

Cumulative distribution function can be obtained by definition as

$$F_\lambda(\lambda) = \int_0^\lambda p_\lambda(\lambda) d\lambda. \quad (2.3)$$

First, we present different distributions describing statistical behaviour of variables x, y , and z .

(a) Rayleigh Distribution

In the case of Rayleigh distribution, the PDFs of random variables are given by

$$\begin{aligned} p_x(x) &= \frac{2}{\Omega_x} x e^{-x^2/\Omega_x}, \\ p_y(y) &= \frac{2}{\Omega_y} y e^{-y^2/\Omega_y}, \\ p_z(z) &= \frac{2}{\Omega_z} z e^{-z^2/\Omega_z}, \end{aligned} \quad (2.4)$$

where $\Omega_x = \varepsilon\langle x^2 \rangle$, $\Omega_y = \varepsilon\langle y^2 \rangle$, $\Omega_z = \varepsilon\langle z^2 \rangle$, and $\varepsilon\langle \cdot \rangle$ denotes expectation.

(b) Weibull Distribution

The Weibull random variables are distributed according to

$$\begin{aligned} p_x(x) &= \frac{\beta}{\Omega_x} x^{\beta-1} e^{-x^\beta/\Omega_x}, \\ p_y(y) &= \frac{\beta}{\Omega_y} y^{\beta-1} e^{-y^\beta/\Omega_y}, \\ p_z(z) &= \frac{\beta}{\Omega_z} z^{\beta-1} e^{-z^\beta/\Omega_z}, \end{aligned} \quad (2.5)$$

where $\Omega_x = \varepsilon\langle x^\beta \rangle$, $\Omega_y = \varepsilon\langle y^\beta \rangle$, $\Omega_z = \varepsilon\langle z^\beta \rangle$, and β is Weibull parameter (for the special case of $\beta = 2$ Weibull PDFs reduces to Rayleigh PDFs).

(c) Nakagami- m Distribution

The Nakagami- m PDFs are

$$\begin{aligned} p_x(x) &= \frac{2m_x^{m_x}}{\Gamma(m_x) \Omega_x^{m_x}} x^{2m_x-1} e^{-m_x x^2/\Omega_x}, \\ p_y(y) &= \frac{2m_y^{m_y}}{\Gamma(m_y) \Omega_y^{m_y}} y^{2m_y-1} e^{-m_y y^2/\Omega_y}, \\ p_z(z) &= \frac{2m_z^{m_z}}{\Gamma(m_z) \Omega_z^{m_z}} z^{2m_z-1} e^{-m_z z^2/\Omega_z}, \end{aligned} \quad (2.6)$$

where $\Omega_x = \varepsilon\langle x^2 \rangle$, $\Omega_y = \varepsilon\langle y^2 \rangle$, $\Omega_z = \varepsilon\langle z^2 \rangle$, $\Gamma(\cdot)$ is gamma function, and m_x, m_y , and m_z are Nakagami- m parameters that range from 0.5 to ∞ . Nakagami- m distribution spans via m parameter through wide range of distributions which includes the one-sided Gaussian distribution ($m = 0.5$) and the Rayleigh distribution ($m = 1$) as special cases.

(d) α - μ Distribution

The α - μ distributed random variables are described with following equations:

$$\begin{aligned} p_x(x) &= \alpha \left(\frac{\mu_x}{\Omega_x} \right)^{\mu_x} \frac{x^{\alpha\mu_x-1}}{\Gamma(\mu_x)} e^{-\mu_x x^\alpha / \Omega_x}, \\ p_y(y) &= \alpha \left(\frac{\mu_y}{\Omega_y} \right)^{\mu_y} \frac{y^{\alpha\mu_y-1}}{\Gamma(\mu_y)} e^{-\mu_y y^\alpha / \Omega_y}, \\ p_z(z) &= \alpha \left(\frac{\mu_z}{\Omega_z} \right)^{\mu_z} \frac{z^{\alpha\mu_z-1}}{\Gamma(\mu_z)} e^{-\mu_z z^\alpha / \Omega_z}, \end{aligned} \quad (2.7)$$

where $\Omega_x = \varepsilon\langle x^\alpha \rangle$, $\Omega_y = \varepsilon\langle y^\alpha \rangle$, $\Omega_z = \varepsilon\langle z^\alpha \rangle$, α is parameter related to the nonlinearity, and μ_x, μ_y , and μ_z are the inverse of the normalized variance of x^α, y^α and z^α , respectively ($\mu_x, \mu_y, \mu_z \geq 0.5$). The α - μ distribution is a general distribution that includes as special cases Nakagami- m distribution for $\alpha = 2$ and Weibull distribution for $\mu = 1$.

Applying the procedure described at the beginning of this section with the aid of [18, Equations (3.461) and (6.631)], [19], [20, Equation (26)], the PDFs and CDFs of λ in different scenarios can be expressed in terms of Meijer G functions $G_{p,q}^{m,n} \left(Y \left| \begin{smallmatrix} a_1, a_2, \dots, a_p \\ b_1, b_2, \dots, b_q \end{smallmatrix} \right. \right)$ as

(a) Rayleigh Scenario

$$\begin{aligned} p_\lambda(\lambda) &= 2\sqrt{\frac{\Omega_y}{\Omega_x \Omega_z}} G_{1,2}^{2,1} \left(\frac{\Omega_y}{\Omega_x \Omega_z} \lambda^2 \left| \begin{smallmatrix} -\frac{1}{2} \\ \frac{1}{2}, \frac{1}{2} \end{smallmatrix} \right. \right), \\ F_\lambda(\lambda) &= \sqrt{\frac{\Omega_y}{\Omega_x \Omega_z}} \lambda G_{2,3}^{2,2} \left(\frac{\Omega_y}{\Omega_x \Omega_z} \lambda^2 \left| \begin{smallmatrix} -\frac{1}{2}, \frac{1}{2} \\ \frac{1}{2}, \frac{1}{2}, -\frac{1}{2} \end{smallmatrix} \right. \right). \end{aligned} \quad (2.8)$$

(b) Weibull Scenario

$$\begin{aligned} p_\lambda(\lambda) &= \beta \sqrt{\frac{\Omega_y}{\Omega_x \Omega_z}} \lambda^{(\beta/2)-1} G_{1,2}^{2,1} \left(\frac{\Omega_y}{\Omega_x \Omega_z} \lambda^\beta \left| \begin{smallmatrix} -\frac{1}{2} \\ \frac{1}{2}, \frac{1}{2} \end{smallmatrix} \right. \right), \\ F_\lambda(\lambda) &= \sqrt{\frac{\Omega_y}{\Omega_x \Omega_z}} \lambda^{\beta/2} G_{2,3}^{2,2} \left(\frac{\Omega_y}{\Omega_x \Omega_z} \lambda^\beta \left| \begin{smallmatrix} -\frac{1}{2}, \frac{1}{2} \\ \frac{1}{2}, \frac{1}{2}, -\frac{1}{2} \end{smallmatrix} \right. \right). \end{aligned} \quad (2.9)$$

(c) *Nakagami- m Scenario*

$$\begin{aligned}
 p_\lambda(\lambda) &= 2 \left(\frac{m_x m_z}{m_y} \right)^{(1/2)(m_x+m_z-1)} \left(\frac{\Omega_y}{\Omega_x \Omega_z} \right)^{(1/2)(m_x+m_z-1)} \frac{1}{\Gamma(m_x)\Gamma(m_y)\Gamma(m_z)} \lambda^{m_x+m_z-2} \\
 &\quad \times G_{1,2}^{2,1} \left(\frac{m_x m_z}{m_y} \frac{\Omega_y}{\Omega_x \Omega_z} \lambda^2 \left| \begin{array}{c} -\frac{1}{2}(m_x + 2m_y + m_z - 3) \\ \frac{1}{2}(m_z - m_x + 1), \frac{1}{2}(1 - m_z + m_x) \end{array} \right. \right), \\
 F_\lambda(\lambda) &= \left(\frac{m_x m_z}{m_y} \right)^{(1/2)(m_x+m_z-1)} \left(\frac{\Omega_y}{\Omega_x \Omega_z} \right)^{(1/2)(m_x+m_z-1)} \lambda^{m_x+m_z-1} \frac{1}{\Gamma(m_x)\Gamma(m_y)\Gamma(m_z)} \\
 &\quad \times G_{2,3}^{2,2} \left(\frac{m_x m_z}{m_y} \frac{\Omega_y}{\Omega_x \Omega_z} \lambda^2 \left| \begin{array}{c} -\frac{1}{2}(m_x + 2m_y + m_z - 3), \frac{1}{2}(3 - m_x - m_z) \\ \frac{1}{2}(m_z - m_x + 1), \frac{1}{2}(1 - m_z + m_x), -\frac{1}{2}(m_x + m_z - 1) \end{array} \right. \right).
 \end{aligned} \tag{2.10}$$

(d) *α - μ Scenario*

$$\begin{aligned}
 p_\lambda(\lambda) &= \alpha \left(\frac{\mu_x \mu_z}{\mu_y} \right)^{(1/2)(\mu_x+\mu_z-1)} \left(\frac{\Omega_y}{\Omega_x \Omega_z} \right)^{(1/2)(\mu_x+\mu_z-1)} \lambda^{(\alpha/2)(\mu_x+\mu_z-1)-1} \\
 &\quad \times \frac{1}{\Gamma(\mu_x)\Gamma(\mu_y)\Gamma(\mu_z)} G_{1,2}^{2,1} \left(\frac{\mu_x \mu_z}{\mu_y} \frac{\Omega_y}{\Omega_x \Omega_z} \lambda^\alpha \left| \begin{array}{c} -\frac{1}{2}(\mu_x + 2\mu_y + \mu_z - 3) \\ \frac{1}{2}(\mu_z - \mu_x + 1), \frac{1}{2}(1 - \mu_z + \mu_x) \end{array} \right. \right), \\
 F_\lambda(\lambda) &= \left(\frac{\mu_x \mu_z}{\mu_y} \right)^{(1/2)(\mu_x+\mu_z-1)} \left(\frac{\Omega_y}{\Omega_x \Omega_z} \right)^{(1/2)(\mu_x+\mu_z-1)} \lambda^{(\alpha/2)(\mu_x+\mu_z-1)} \frac{1}{\Gamma(\mu_x)\Gamma(\mu_y)\Gamma(\mu_z)} \\
 &\quad \times G_{2,3}^{2,2} \left(\frac{\mu_x \mu_z}{\mu_y} \frac{\Omega_y}{\Omega_x \Omega_z} \lambda^\alpha \left| \begin{array}{c} -\frac{1}{2}(\mu_x + 2\mu_y + \mu_z - 3), \frac{1}{2}(3 - \mu_x - \mu_z) \\ \frac{1}{2}(\mu_z - \mu_x + 1), \frac{1}{2}(1 - \mu_z + \mu_x), -\frac{1}{2}(\mu_x + \mu_z - 1) \end{array} \right. \right).
 \end{aligned} \tag{2.11}$$

The PDFs and CDFs of λ in all considered scenarios are presented in Figures 1, 2, 3 and 4.

3. An Application of Presented Theoretical Results in Wireless Communication Systems: The Performance Analysis of Multihop Systems

Multihop (N -hop) transmission is a technique by which the channel from the source (S) to the destination (D) is split into several, possibly shorter, links using relays (R_i , $i = 1, N-1$), as shown in Figure 5.

Depending on the nature of the radio propagation environment, the statistical behaviour of signal envelope can be described with different distributions. This is reason

Figure 1: PDF and CDF of λ in Rayleigh scenario.

Figure 2: PDF and CDF of λ in Weibull scenario.

why our analysis includes so many statistical models. The Rayleigh model is frequently used to describe multipath fading with no direct line-of-sight (LOS) path [10]. The Weibull distribution exhibits an excellent fit to experimental fading channel measurements, for both indoor [21] and outdoor [22] environments. Also good results are provided in urban environments. The Nakagami- m distribution has gained widespread application in the modelling of physical radio channels since it shows great agreement with experimentally obtained results [23]. Fading severity in Weibull and Nakagami- m environments is described by Weibull parameter β and Nakagami parameter m , respectively. As these parameters increase fading severity decreases. The α - μ distribution is a general fading distribution that can be used to better represent the small-scale variation of the fading signal [24]. Parameter

Figure 3: PDF and CDF of λ in Nakagami- m scenario. Figure 4: PDF and CDF of λ in α - μ scenario.

Figure 5: Multihop transmission.

α is related to the nonlinearity of the environment, while parameter μ is associated to the number of multipath [25].

The product of random variables, $t_i = x_i z_i$, represents signal envelope which suffers from fading and shadowing while the random variable y_i represents CCI envelope at the input of i th terminal ($i = \overline{1, N}$). The random variable $\lambda_i = x_i z_i / y_i$ presents SIR value at the input of i th terminal. Therefore, the mathematical results presented in the previous section can be efficiently used for performance analysis of relayed communication systems in fading environment. Highly important and widely accepted system performance indicator is outage probability defined as probability of having SIR value lower than predetermined threshold λ_0 which defines required QoS. The system failure can occur in sections $S-R_1, R_1-R_2, R_2-R_3, \dots, R_{j-1}-R_j, \dots, R_{N-1}-D$ when some of the values of $\lambda_1, \lambda_2, \lambda_3, \dots, \lambda_j, \dots, \lambda_N$ are below the predetermined threshold λ_0 . The PDF of minimum of λ_i , $\lambda = \min\{\lambda_1, \lambda_2, \dots, \lambda_N\}$, is important for analyzing multihop relayed communication systems in which the source terminal communicates with the destination terminal through a number of relay terminals. It can be obtained based on previous results as

$$p_\lambda(\lambda) = \sum_{n=1}^N p_{\lambda_n}(\lambda) \prod_{\substack{k=1 \\ k \neq n}}^N (1 - F_{\lambda_k}(\lambda)). \quad (3.1)$$

The outage probability of multihop system is defined as

$$P_{\text{out}} = \int_0^{\lambda_0} p_\lambda(\lambda) d\lambda. \quad (3.2)$$

As an illustrative example, the outage probability of dual-hop and triple-hop communication systems can be obtained as

$$\begin{aligned} P_{\text{out}} &= F_{\lambda_1}(\lambda)(1 - F_{\lambda_2}(\lambda)) + F_{\lambda_2}(\lambda)(1 - F_{\lambda_1}(\lambda)) + F_{\lambda_1}(\lambda)F_{\lambda_2}(\lambda), \\ P_{\text{out}} &= F_{\lambda_1}(\lambda)(1 - F_{\lambda_2}(\lambda))(1 - F_{\lambda_3}(\lambda)) + F_{\lambda_2}(\lambda)(1 - F_{\lambda_1}(\lambda))(1 - F_{\lambda_3}(\lambda)) \\ &\quad + F_{\lambda_3}(\lambda)(1 - F_{\lambda_1}(\lambda))(1 - F_{\lambda_2}(\lambda)) + F_{\lambda_1}(\lambda)F_{\lambda_2}(\lambda)(1 - F_{\lambda_3}(\lambda)) \\ &\quad + F_{\lambda_1}(\lambda)F_{\lambda_3}(\lambda)(1 - F_{\lambda_2}(\lambda)) + F_{\lambda_2}(\lambda)F_{\lambda_3}(\lambda)(1 - F_{\lambda_1}(\lambda)) \\ &\quad + F_{\lambda_1}(\lambda)F_{\lambda_2}(\lambda)F_{\lambda_3}(\lambda), \end{aligned} \quad (3.3)$$

respectively. The curves representing PDF of λ and outage probability of multihop (dual-hop and triple-hop) communication system in Weibull fading environment are presented in Figure 6. Without loss of generality, we assumed that the ratios of average powers are equal on all terminals inputs, that is, $\gamma_i = \Omega_{x_i}\Omega_{z_i}/\Omega_{y_i} = \gamma$, $i = \overline{1, N}$. Namely, signal is amplified in terminal so that the ratio of average powers at the input of the next terminal is equal to the ratio of average powers at the input of previous one. It is noticeable that the outage probability is higher for lower values of Weibull parameter, that is, in environment with higher fading severity. Also, having in mind that $\gamma_i = \gamma$, $i = \overline{1, N}$, the higher values of N imply larger distance between the source and destination terminals and higher values of the outage probability.

Figure 6: PDF of $\lambda = \min \{\lambda_1, \lambda_2, \dots, \lambda_N\}$ and outage probability of dual-hop ($N = 2$) and triple-hop ($N = 3$) communication system for different values of γ in Weibull fading environment.

4. Conclusion

The PDF and CDF of ratio of product of two random variables and random variable $\lambda = xz/y = t/y$ have been derived. Rayleigh, Weibull, Nakagami- m , and α - μ statistical models are included in the paper, so that other researchers and engineers could use our results in wide range of scenarios in many areas of science. An application of these results for the wireless communications community has been described. Namely, presented results can help the designers of wireless communication systems to simulate different wireless environments where fading and shadowing affect desired signal and fading affects CCI and readjust system parameters in order to meet the QoS demands. In our future work, we hope to obtain analytical expressions for PDF and CDF of ratio of products of random variables which will have application in analysis of wireless communication systems where both desired signal and CCI are affected by fading and shadowing simultaneously which is realistic scenario in modern urban areas.

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