Research Article

Adaptive Real-Time Estimation on Road Disturbances Properties Considering Load Variation via Vehicle Vertical Dynamics

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Vehicle dynamics are directly dependent on tire-road contact forces and torques which are themselves dependent on the wheels’ load and tire-road friction characteristics. An acquisition of the road disturbance property is essential for the enhancement of vehicle suspension control systems. This paper focuses on designing an adaptive real-time road profile estimation observer considering load variation via vehicle vertical dynamics. Firstly, a road profile estimator based on a linear Kalman filter is proposed, which has great advantages on vehicle online control. Secondly, to minimize the estimation errors, an online identification system based on the Recursive Least-Squares Estimation is applied to estimate sprung mass, which is used to refresh the system matrix of the adaptive observer to improve the road estimation efficiency. Last, for mining road category from the estimated various road profile sequences, a road categorizer considering road frequency and amplitude simultaneously is approached and its efficiency is validated via numerical simulations, in which the road condition is categorized into six special ranges, and this road detection strategy can provide the suspension control system with a better compromise for the vehicle ride comfort, handling, and safety performance.

1. Introduction

The road properties have significant impact on vehicle performance because vehicle dynamics are directly dependent on tire-road contact forces and torques. Road roughness is a broad term that incorporates everything from potholes and cracks to the random deviations that exist in a profile. The analysis and estimation of a road surface are hot and challenging topics, and the researches related to road disturbances have been presented, which can be classified into three categories: road measurement, road modeling, and road estimation. Each of these categories is reviewed briefly in the sequel.

Road Measurement. It mainly focuses on measuring the road profile accurately for road serviceability, survey, and road maintenance. There are primarily three methods in use internationally. The first category consists of profilometers and profilographs [1–4]. These are manually directed and/or trailer towed mechanisms that directly contact the pavement under evaluation, such as the longitudinal profile analyser (LPA). The second category is inertial profilers such as the Mays Meter [5] and the GMP (general motor profilometer) [6], in which a vehicle mounted accelerometer is applied to collect data while traveling at normal speed conditions. González et al. also developed a road roughness estimator by the use of acceleration measurement [7]. Furthermore, Ngwangwa et al. reconstructed road defects and road roughness classification using vehicle responses with artificial neural networks simulation [8]. The third category, equipped with a laser (ultrasonic) transceiver [9], is more accurate but very expensive.
Road Modeling. It mainly focuses on providing road input source to the virtual vehicle simulation system or the Four-Post Test Rig for vehicle ride analysis. In 1970s, the PSD (power spectral density) function was used by Whitehouse and Archard [10] and Shinozuka and Jan [11] to investigate the road roughness. In 1993, Cebon proposed a method based on the IFFT (inverse fast fourier transform) to discretize PSD, which is a simple, fast, and convenient tool for generating road surfaces [12,13]. In 1995, the contemporary international standard ISO 8608 [14] dealt with road roughness assumes, due to classification of roads into different classes according to their unevenness, equal intensity of road unevenness in the whole range of wavelengths and a general form of the fitted PSD were given. A method based on linear filtering (autoregressive and moving average method or ARMA modelling) was proposed by Yoshimura in 1998 [14], which has a smaller calculation, and a faster simulation speed, but its precision is not very well. Pazooki et al. [15], in 2007, summarized different stochastic models of parallel road tracks and evaluated their accuracy by comparing the difference of the measured parallel tracks and the synthetic parallel tracks. In 2012, Hassan and Evans [16] developed a comprehensive off-road vehicle ride dynamics model considering a random roughness model of the two parallel tracks.

Road Estimation. It mainly focuses on providing real-time rough road estimation for vehicle online control system. Since road input directly affects vehicle vertical suspension dynamics, the availability of suspension sensors such as accelerometer and suspension deflection sensor provide an excellent opportunity for road input estimation. Fialho and Balas developed a road adaptive active suspension using linear parameter varying gain-scheduling [17], in which the road estimation results are applied to the suspension control system to achieve a better balance between ride and handling performance. A new simultaneous input and state estimation algorithm were developed based on the idea of achieving minimum mean square error and minimum error variance [18]. Two stable SISF algorithms were developed based on the minimum variance unbiased estimation technique [19]. A Takagi-Sugeno Fuzzy observer was built for estimating both vehicle dynamics and road geometry [20]. Vehicle sideslip and roll parameters are estimated in presence of the road bank angle and the road curvature as unknown inputs. But it is still not completely ready to be tested in experimental studies since the vehicle speed, parameters variations, and sensor noise are not considered. If the systems are subject to parameter uncertainties, the approaches proposed in [21–23] can be employed. Our previous study [24, 25] also shows the great potential in the enhancement of suspension performance by adopting road estimation in the suspension control system, even though the road estimation algorithm is very simple (just using the statistic value of the accelerometer or suspension deflection sensor measurement to classify the road). Recently, a real-time estimation method based on Kalman filter is proposed to estimate the road profile, and experimental results show the accuracy and the potential of the estimation process [26]. But in this research, the vehicle sprung mass change due to vehicle load variation is not considered, which may attenuate the robustness. Imine and Delanne developed a sliding mode observer to estimate the road profiles, which is hard for real-time implementation since a 16 degrees of freedom (DOF) full car model is too complex to be applied online [27, 28].

This paper focuses on developing a road estimation system for an online vehicle control system, which is limited by some important practical requirements. It should, for instance, be:

- **simple** enough to run in real time despite onboard processing limitations;
- **reliable** enough to operate successfully despite instrumentation failures;
- **robust** to variations in vehicle dynamics;
- **fast** enough to detect the road input changes when a car is driven on road;
- **easy** to incorporate into a control strategy.

With these requirements in mind, the objective of this research has three steps: (1) to develop a road estimator for satisfying the above 5 practical requirements; (2) to obtain vehicle sprung mass online to minimize the road profile estimation errors; (3) and to classify the estimated road profile into several categories according to the main control strategy. The proposed method uses measurements from available sensors: accelerometers and suspension deflection sensors. For simplicity reasons, a quarter-car vehicle model is considered. The estimation process consisting of three blocks is shown in Figure 1. The first block serves to calculate vehicle sprung mass online from sensor measurements, while the second block contains a Kalman filter that uses the result of the first block as a system parameter adjustor in order to improve robustness of the road estimation system. The third block serves to categorize the estimated road profile elevation into specific types.

The rest of the paper is organized as follows. Section 2 describes a road input state estimator based on a linear Kalman filter. Section 3 presents an online sprung mass estimator based on the Recursive Least-Squares Estimation. In Section 4, a novel road categorizer is proposed, and it is validated via numerical simulations. And, the paper is concluded in Section 5.

2. Road Profile Estimator

2.1. 2-DOF Quarter-Car Model. To implement the Kalman filter method, a suitable vehicle model must be developed. In order to describe the vertical dynamics of a vehicle which runs on an uneven road with a constant speed, a 2-DOF quarter-car model is represented in Figure 2. The quarter-car model does not consider the pitch and roll motions. Despite its simplicity, it captures the most basic feature of the vertical model of the vehicle [29]. We assume that wheels are rolling...
where $a_1$ and $a_2$ are constant real numbers. The modified quarter car has to be stable in order to provide useful result; this implies that the real parts of the eigenvalues associated with (4) have to be negative, and consequently $x_r$ converges to zero based on the selection of the constants $a_1$ and $a_2$. However, since $x_r$ represents the road profile input, it should contain as much road input information as possible. In other words, $x_r$ should be damped as slowly as possible, which will affect the stability of (4). Therefore, there is a trade-off between system stability and road input information integrity. In this paper, $a_1$ and $a_2$ are set to 20, which are close to two times of the quarter-car tire hop frequency, is sufficient to keep (4) stable [30]. The quarter car state equations can be written as follows:

$$
x_{k+1} = A_k x_k + v_k,
$$

$$
y_k = H_k x_k + \omega_k,
$$

where $x_k = (x_{1,k} \ x_{2,k} \ x_{3,k} \ x_{4,k} \ x_{5,k} \ x_{6,k})^T$ is a state vector; $y_k = ((x_{1,k} - x_{3,k}) x_{1,k} \ \dot{x}_{1,k})^T$ is an observer vector, where $x_{1,k} - x_{3,k}$ is a suspension deflection measured by sensor; $x_{1,k}$ is a vehicle body position calculated by a twice numerical integration (trapezoidal method) of the filtered vertical acceleration signal; $\dot{x}_{1,k}$ is a filtered vertical acceleration. $v_k$ and $\omega_k$ are the process and measurement noise vector, respectively, assumed to be white, zero mean, and uncorrelated.

Evolution and observation constant matrices are given as

$$
A = E + \Delta t \begin{pmatrix}
0 & 1 & 0 & 0 & 0 & 0 \\
-K_t & C_s & K_t & 0 & 0 & 0 \\
-M & -M & M & -C_s & 0 & 0 \\
0 & 0 & 0 & 1 & 0 & 0 \\
-K_s & C_s & K_s + K_u & -C_s & K_u & 0 \\
0 & 0 & 0 & -M & M & 0 \\
0 & 0 & 0 & 0 & 0 & -20 \\
0 & 0 & 0 & 0 & 0 & -20
\end{pmatrix},
$$

$$
H = \begin{pmatrix}
1 & 0 & -1 & 0 & 0 & 0 \\
-K_t & C_s & K_t & C_s & 0 & 0 \\
1 & 0 & 0 & 0 & 0 & 0
\end{pmatrix},
$$

without slip or contact loss. Equations (1) and (2) represent the vehicle body and the wheel motion, respectively:

\[ m\ddot{x}_u - C_s (\dot{x}_s - \dot{x}_u) - K_s (x_s - x_u) + K_t (x_u - x_r) = 0, \]

\[ M\ddot{x}_s + C_s (\dot{x}_s - \dot{x}_u) + K_s (x_s - x_u) = 0, \]

where $M$ and $m$ are, respectively, the sprung mass and the unsprung mass of a quarter car, $K_s$ represents the suspension stiffness, $K_t$ represents the tire vertical stiffness, $C_s$ is the damper damping coefficient, $x_s$ is the sprung mass position, $x_u$ is the unsprung mass position, and $x_r$ is the road input.

2.2. Kalman Filter for Road Input Estimation. The road input $x_r$ is an estimated signal and it should be a part of the system states. Hence, in this paper, state variables for the quarter car are presented as follows:

\[ x_1 = x_s, \quad x_2 = \dot{x}_s, \quad x_3 = x_u, \]

\[ x_4 = \dot{x}_u, \quad x_5 = x_r, \quad x_6 = \dot{x}_r. \]

And the road roughness profile applied in the estimation observer satisfies the following equation [30]:

\[ \ddot{x}_r + a_2 \dot{x}_r + a_1 x_r = 0, \]
where $E$ is the identity matrix and $\Delta t$ is the sampling period. And it is easy to verify that the observability matrix $O$ is full rank:

$$O = (H \ H G \ H G^2 \ H G^3 \ H G^4 \ H G^5)^T. \tag{7}$$

A standard Kalman filter formulation is used for the velocity estimation [31, 32]. The time update and measurement update equations of the filter are constructed as follows:

\begin{align*}
\text{time update} & \quad [\tilde{x}]_k = [A] \ [\tilde{x}]_{k-1} + [B] u_{k-1}, \\
[ P^- ]_k &= [A] \ [P]_{k-1} \ [A]^T + [Q], \\
\text{measurement update} & \quad [K]_k = [P^-]_k [H]^T ( [H] \ [P^-]_k [H]^T + [R] )^{-1}, \\
[\tilde{x}]_k &= [\tilde{x}]_{k-1} + [K]_k ( [y]_k - [H] \ [\tilde{x}]_{k-1} ), \\
[ P ]_k &= ([I] - [K]_k [H]) \ [P^-]_k,
\end{align*} \tag{8}

where $Q$ is a process noise covariance matrix, $R$ is a measurement noise covariance matrix, $P$ is an estimation of error covariance matrix, $K$ is a Kalman gain, and $\tilde{x}$ is an estimated state vector. The process and measurement noise variables $\nu_k$ and $\omega_k$ determine how much should the process model and the measurements should be trusted by the filter.

### 2.3. Simulation Setup

This paper presents simulations of the quarter-car system as shown in Figure 2 with parameters tabulated in Table 1.

Two types of road inputs were used during experimental and simulation analysis. One input is a trigonal bump with 40 mm height and 400 mm length shown in Figure 3; another input is a random road input modeled based on the inverse Fourier transform as shown in Figure 4.

Figure 5 to Figure 8 show a comparison between the actual and the estimated road profile height. In Figures 5 and 7, the vehicle passes the bump at a constant speed of 15 km/h and 45 km/h, respectively. In Figures 6 and 8, the vehicle runs on a random road, and the speed is 30 km/h and 60 km/h, respectively. The simulation results show that, in the random road input or the low speed bump input condition, the road estimator is very efficient, while in the condition of passing the bump with a relatively high speed, as shown in Figure 7, the estimation result is not very well. This is induced by the road model defined in (4). In fact, the road model applied in the proposed estimation observer should make a compromise between system stability and the integrity of road input information. We want to keep the system stable sacrificing the integrity of road input information in this research. And this strategy decreases the road estimator performance in an impulse input condition. The higher the vehicle speed is, the sharper the road input in time domain will be and the worse the road estimator will be. But its negative effect is acceptable since most drivers will reduce the vehicle speed when they run over a bump.

### 3. Sprung Mass Estimation

The road estimation method presented afore is based on a hypothesis that the vehicle system parameters in Table 1 are known and invariable. But in a real vehicle control system, it is not easy to obtain the sprung mass of the equivalent 2-DOF model, because of the nonlinear properties of the suspension system and the weight distribution variation on
different driving conditions. What is more, the sprung mass varies greatly between empty and full loaded, especially for a commercial vehicle. All these factors will induce a significant sprung mass change and, then, attenuate the efficiency of the road estimation system. As shown in Figure 9, 20% sprung mass error will induce an obvious road estimation error. Consequently, it is necessary to estimate the sprung mass online for improving the efficiency of road estimation.

3.1. Solution Formulation. With setting $y = -K_s(x_s - x_u)$, $\theta = [M, C_s]^T$, and $\psi^T = [\dot{x}_s, \dot{x}_s - \dot{x}_u]$, (2) can be written as

$$y = \psi^T \cdot \theta.$$  

The vehicle sprung mass and suspension damping coefficient are estimated simultaneously via the Recursive Least-Squares Estimation. The Recursive Least-Squares Estimation procedures are given as follows:

$$\hat{\theta}_{N+1} = \hat{\theta}_N + K_{N+1} \left(y_{N+1} - \psi^T_{N+1} \hat{\theta}_N\right),$$  \hspace{1cm} (10)

$$K_{N+1} = \frac{P_N \psi_{N+1}}{1 + \psi_{N+1}^T P_N \psi_{N+1}},$$  \hspace{1cm} (11)

$$P_{N+1} = P_N - \frac{P_N \psi_{N+1} \psi_{N+1}^T P_N}{1 + \psi_{N+1}^T P_N \psi_{N+1}}$$

$$= \left(I - K_{N+1} \psi_{N+1}^T \right) P_N.$$  \hspace{1cm} (12)
where $P$ is a symmetric covariance matrix ($2 \times 2$) and $\theta_0$ is the Least-Squares estimation of $\theta$; the calculation order is described as follows.

Calculate $K_1$ by $\theta_0$ and $P_0$ according to (11) first; then, update the value of $y_1$ and $\psi_1^T$; and then, calculate $\theta_1$ and $P_1$ according to (10) and (12), respectively; last, recursive the mentioned steps in order until the error reaches the standard. As for the initial values, $\theta_0$ and $P_0$, they can be calculated by the Least-Squares Estimation.

3.2. Simulation. Here, the vehicle system model parameters are from Table 1; the road profile defined in Figure 4 is selected as a vertical road input and the vehicle runs with a constant speed of 20 km/h. The estimation result is shown in Figure 10, which demonstrates the estimation result converges at an acceptable region (the error is less than 5%) after 2.5 s and then shows great efficiency after 20 s. Generally, the vehicle load is a constant during a vehicle start-stop period and the convergence time for sprung mass estimation is usually far less than a vehicle start-stop period. The sprung mass estimation is a little bit time-consuming, but it is not a big issue. For example, the original sprung mass is set in normal load condition. The road estimation block will be triggered once the vehicle has been started and the vehicle velocity is greater than 10 km/h; it will obtain the sprung mass (the error is less than 5%) in 2.5 s after the road estimation block is triggered, and the sprung mass will be refreshed. And then the sprung mass will be updated in every 2.5 s until it is stable (the change is less than 1%) or the estimation time is more than 40 s.

4. Road Categorizer

In the previous sections, the road estimator performs very well in a quarter-car system. However, does this estimator have the same performance applied to an actual car online system? It cannot be denied that the estimated result, in an actual car online system, will be worse than expectation due to the effect of wheel radius, wheel contact area, and the noise signals in the control system. What is more, the estimated road profile cannot be applied to the control strategy directly since these road sequences are estimated by postestimation, which produces an unavoidable time delay. However, in many vehicle control systems, such as active/semiactive suspension system, obtaining the primary road category information is effective [33]. Hence, it is necessary to develop a road categorizer to distinguish the road category for the main control strategy. But the most common road classification methods, estimating the road PSD (power spectral density) or the road RMS (root mean square), are not enough effective for an online control system, because these methods need to compute plenty of road height values which will consume a lot of estimation time, and this time lag usually cannot be neglected in a real-time control system.

In fact, most onboard suspension control systems, only require the mainly frequency or amplitude information of road input. In [33, 34], a road-frequency adaptive suspension is proposed, where the road surface is classified by the frequency properties according to the fact that [0–4 Hz] is the car-body frequency region and [4–8 Hz] is the human-body frequency region. [8–12 Hz] is the wheel frequency region and [12–∞ Hz] is the harshness frequency region. Bastow et al. also categorize the road profile into four grades, which defined a very good surface with amplitudes under 5 mm, medium-quality roads with amplitudes less than 13 mm, poor-quality roads with amplitudes less than 25 mm, and off-road with the amplitudes often exceeding 25 mm [35]. However, it is a challenging issue to design a proper filter to avoid some unimportant long waves without any phase delay, as shown in Figure 4; the road waves are not fluctuating along the horizontal plane due to the effect of some long waves.
which has small contribution on the vehicle vertical dynamic; consequently, we should estimate the road input frequency and amplitude avoiding the unimportant long waves. In the other hand, the road categorizer only depending on the road frequency or the road amplitude does not work very well always. And the suspension control strategy should consider the road frequency and amplitude simultaneously in some case, such that a car runs on a road twice with different speed or a car runs on different road (ISO Class A and ISO Class C) with same speed. It will be much better if the road categorizer considers road frequency and amplitude simultaneously. Hence, a novel road categorizing method considering road frequency and amplitude simultaneously is proposed in the following paragraph.

For road frequency estimation, refer to the article [34], a first-order zero-crossing algorithm is applied, with the road velocity state $\dot{x}_r$ being the input, to identify the frequency components of road disturbances. The frequency estimation result of Figure II is shown in Figure I2, and the current estimation value is actually the last circle’s frequency.

As for road amplitude analysis, road velocity state $\dot{x}_r$ does not contain the amplitude information, but the road amplitude estimation only via $x_0$ is very difficult, since some of the significant road waves are not fluctuating along the horizontal plane. As shown in Figure I1, the value of “A” is one of the main amplitudes values, which is the amplitude of the wave with dominant frequency, should be estimated.

In the sequel, a novel road amplitude estimation method is proposed as shown in Figure I1, where, $T_1$, $T_2$, and $T_3$, used to detect each complete cycle, are the three attached times when first-order zero-crossing of the road velocity sequence happens; $y_1$, $y_2$, and $y_3$ are the three road height values in the times $T_1$, $T_2$, $T_3$, respectively. Then the road amplitude “A” can be simply calculated as (13), where $T_1$, $T_3$ are used to detect the troughs of a circle and $T_2$ used to detect the peak of a circles are the distance between the point $(T_2, y_2)$ to the
Table 2: Suspension mode selection based on road condition.

<table>
<thead>
<tr>
<th>Range</th>
<th>Driving condition</th>
<th>Suspension control objective</th>
</tr>
</thead>
<tbody>
<tr>
<td>I and II</td>
<td>Good road surface with medium or low speed, mostly on an urban driving condition</td>
<td>Improve the vehicle ride performance</td>
</tr>
<tr>
<td>III</td>
<td>Expressway driving condition</td>
<td>Improve the road holding</td>
</tr>
<tr>
<td>IV</td>
<td>Bad road with low speed</td>
<td>Limit the low frequency body motion</td>
</tr>
<tr>
<td>V and VI</td>
<td>Poor-quality road surface with medium-high speed and the impulse road input</td>
<td>Attenuate the impact feeling</td>
</tr>
</tbody>
</table>

The amplitude estimation result is shown in Figure 13; even though the algorithm is running in real time, the estimation result still has a complete cycle time lag.

As road frequency and amplitude estimation can be achieved, a road categorizer special for a semiactive suspension control system can be designed, as shown in Figure 14. A certain type of road can be detected by judging the amplitude and frequency of the estimated road profile into the specific range (I–VI), where the suggestion values of $A_{\text{low}}$, $F_{\text{low}}$, and $F_{\text{high}}$ are 10 mm, 4 Hz, and 8 Hz, respectively. The suspension mode selection based on the road condition in specific range (I–VI) is detailed in Table 2. Ranges I and II are the medium-low frequency and low amplitude areas, corresponding to good road surface with medium-low speed, mostly on an urban driving condition. In this case, the suspension system should be turned to soft mode to improve the vehicle ride performance. Range III is the high frequency and low amplitude area, corresponding to the expressway driving condition, in which more attention should be paid to the tire deflection, and a relative hard mode suspension system should be regulated to achieve better road holding for driving safety. Range IV is the low frequency and high amplitude area corresponding to a bad road with low speed, which is very common for an off-road. In this condition, limiting the low frequency body motion should be a key objective. Ranges V and VI correspond to poor-quality road surface with medium-high speed and the impulse road input. In these cases, the suspension system should be adjusted to attenuate the impact feeling.

5. Conclusions

An acquisition of road disturbances property is essential for the enhancement of suspensions control systems. This paper presented a method to estimate the road profile elevation based on Kalman filter. To minimize the estimation errors, an online identification system based on Recursive Least-Squares Estimation is adopted to estimate sprung mass in real time, which is applied to refresh the system matrix of the adaptive observer. And a novel road categorizer considering road frequency and amplitude simultaneously is approached to classify various road profile sequence for suspension control system. The main conclusions are as follows.

(1) A road profile estimator based on linear Kalman filter is proposed, which has great advantages on practical online vehicle control.

(2) An online sprung mass estimator is proposed, which demonstrates the estimation result converges at an acceptable region (the error is less than 5%) after 2.5 s and then shows great efficiency after 20 s. With this online sprung mass estimator, the accuracy road estimation result can be improved greatly.

(3) A novel road amplitude estimation method is proposed. And the road condition is categorized into six special ranges according to the road frequency and amplitude estimation result simultaneously, which can provide the suspension control system with a better trade-off for the ride comfort, handling, and safety performance.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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