A Rapid Transfer Alignment Method for SINS Based on the Added Backward-Forward SINS Resolution and Data Fusion

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Two viewpoints are given: (1) initial alignment of strapdown inertial navigation system (SINS) can be fulfilled with a set of inertial sensor data; (2) estimation time for sensor errors can be shortened by repeated data fusion on the added backward-forward SINS resolution results and the external reference data. Based on the above viewpoints, aiming to estimate gyro bias in a shortened time, a rapid transfer alignment method, without any changes for Kalman filter, is introduced. In this method, inertial sensor data and reference data in one reference data update cycle are stored, and one backward and one forward SINS resolutions are executed. Meanwhile, data fusion is executed when the corresponding resolution ends. With the added backward-forward SINS resolution, in the above mentioned update cycle, the estimating operations for gyro bias are added twice, and the estimation time for it is shortened. In the ship swinging condition, with the “velocity plus yaw” matching, the effectiveness of this method is proved by the simulation.

1. Introduction

Transfer alignment is a rapid and effective initial alignment method, which is widely used for inertial navigation systems (INSs) in ships and planes. For the quick response requirement of weapon systems, rapidity is always the main aim of the initial alignment. In 1989, a fast transfer alignment method was presented by Kain and Cloutier, in which alignment can be fulfilled in 10 s, and 1 mrad accuracy can be got with swinging movement and “velocity plus attitude” matching [1]. Based on reference 1, a prefilter was added before the Kalman filter by Spalding [2]. Together with the former, the calculation amount was reduced and alignment time was shortened. And in this method, 1 mrad accuracy was reached within 6 s, when the update frequency of reference data was 1 Hz. Aviation transfer alignment experiments on Apache helicopter and F-16 fighter were conducted by Shortelle and Graham, respectively [3–5], and the test results indicated that, when the update frequency was 12.5 Hz, the alignment time could be reduced to 5 s and the accuracy could reach 1 mrad, with “velocity plus attitude” matching and Wing-Rock tactical action.

In the above references, the rapidity of initial alignment was studied, while the estimation for inertial sensor errors was not taken into account or not given sufficient attention. To those strapdown INSs, which are composed of low or medium accuracy initial sensors, sensor errors will decrease navigation accuracy greatly, due to the great drift of gyros after the long time storage [6]. So, it is certain that navigation accuracy will be improved if the sensor errors are estimated in the transfer alignment process. But the observability degree of each state variable in a Kalman filter for transfer alignment relies on the information matching method and the motion of carrier [7, 8]. With swinging movement and “velocity plus attitude” matching, an effective estimation for sensor errors cannot be completed within 10 s for it usually lasts for several minutes [9].

In this paper, after transfer alignment process in ship between the master INS (MINS) and slave INS has been studied, a faster transfer alignment method is introduced, in which the estimation for gyro bias can be fulfilled in a shorter time. In ship, the accuracy of platform INS (PINS) is usually several magnitudes higher than that of strapdown INS. The PINS is used as MINS while the strapdown INS
is used as slave INS, and the navigation parameters from MINS are used as reference data. In the paper, the slave INS and strapdown INS are both abbreviated as SINS. In the integration of M/S INS, flexure deformation is a key factor which will determine transfer alignment accuracy [10]. In this paper, "velocity plus yaw" matching method is chosen due to the fact that the "attitude" matching method is easily suffered by flexure deformation [11, 12], while "velocity" matching method can ensure the rapidity and accuracy of estimation for horizontal misalignment angles [8]. According to the analysis based on piece-wise constant systems (PWCS) linear theory [7], with the excitation of the wave swinging, the velocity errors, misalignment angles, and gyro bias are the observable parameters [13], but, unfortunately, the estimation for gyro bias is a time-consuming process which usually lasts for several minutes.

To deal with the contradiction between the rapidity of alignment and time consumption of gyro bias estimation, two viewpoints are put forward by analyzing the alignment process of SINS. Firstly, different from that in PINS, the direct corresponding relationship between inertial sensor data and misalignment angles in SINS is severed by the mathematical platform. Thus, we can adjust the calculated mathematical platform $n'$ constantly to speed up the initial alignment by the repeated SINS resolution with the same set of sensor data. Secondly, analysis indicates that, with a Kalman filter, a new estimation for state vector will be provided. With close-loop correction, new initial navigation parameters and new compensation parameters for gyro bias will be produced for the next navigation period, and with the above new ones, new navigation results will be generated even built on the same set of sensor data. So with the repeatedly data fusion of the added backward-forward SINS resolution results and the external reference data, the estimation time for sensor error will be shortened. With the above two viewpoints, a rapid transfer alignment method based on the added backward-forward SINS resolution is designed. In this paper, the transfer alignment model based on "velocity plus yaw" matching method is choosen due to the fact that the "attitude" matching method is easily suffered by flexure deformation, while "velocity" matching method can ensure the rapidity and accuracy of estimation for horizontal misalignment angles. In this paper, "velocity plus yaw" matching method is choosen due to the fact that the "attitude" matching method is easily suffered by flexure deformation, while "velocity" matching method can ensure the rapidity and accuracy of estimation for horizontal misalignment angles.

This thesis is constructed as follows. In Section 2, the transfer alignment model based on "velocity plus yaw" matching is built, and the reasons why the observability degree of gyro bias is low are analyzed. In Section 3, after the alignment process of INS is studied and compared, a possible way to increase SINS alignment speed is introduced, and the backward-forward SINS resolution is designed. In Section 4, the transfer alignment model based on the added backward-forward resolution is also designed in detail. And in Section 5, the effectiveness of this method is proved by simulation. Finally, some conclusions are given.

2. Transfer Alignment Model Based on "Velocity Plus Yaw" Matching Method

2.1. System Equation. Choose velocity errors, misalignment angles, and gyro bias as the state vector of the system,

$$
X = [\delta V_E \delta V_N \phi_E \phi_N \epsilon_x \epsilon_y \epsilon_z]^T,
$$

where $\delta V_E$ and $\delta V_N$ are east and north velocity errors, respectively, $\phi_E$, $\phi_N$, and $\phi_Y$ are misalignment angles of pitch, roll, and yaw, respectively, $\epsilon_x$, $\epsilon_y$, and $\epsilon_z$ are gyro bias along $x$, $y$, and $z$ axes. To ships which sail on the sea, the height and upward velocity can be set as zero.

The system state equation can be constructed as

$$
\dot{X}(t) = A(t)X(t) + W(t),
$$

where $A(t)$ is the state matrix and $W(t)$ is the system noise matrix. With the system vector, velocity error, and misalignment angle equations, the state matrix $A(t)$ can be expressed as

$$
A(t) = \begin{bmatrix}
\frac{V_N}{R} \tan L & 2\omega_i \sin L + \frac{V_E}{R} \tan L & 0 & -f_U & f_N & 0 & 0 & 0 \\
-\left(2\omega_i \sin L + \frac{V_E}{R} \tan L\right) & 0 & f_U & 0 & -f_E & 0 & 0 & 0 \\
0 & -\frac{1}{R} & 0 & \omega_i \sin L + \frac{V_E}{R} \tan L & -\left(\omega_i \cos L + \frac{V_E}{R}\right) & -T_{11} & -T_{12} & -T_{13} \\
\frac{1}{R} & 0 & -\left(\omega_i \sin L + \frac{V_E}{R} \tan L\right) & 0 & -\frac{V_N}{R} & -T_{21} & -T_{22} & -T_{23} \\
\frac{1}{R} \tan L & 0 & \omega_i \cos L + \frac{V_E}{R} & \frac{V_N}{R} & 0 & -T_{31} & -T_{32} & -T_{33} \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
\end{bmatrix}
$$
where \( V_E \) and \( V_N \) are the east and north velocity respectively, \( \omega_E \) and \( R \) are the rotational angular rate and radius of the Earth, \( L \) is the latitude of ship position, \( f_E \), \( f_N \), and \( f_I \) denote the projection of the accelerometer measured data \( \mathbf{f} \) in navigation frame \( n \), and \( T_{ij} \) \((i, j = 1, 2, 3)\) are the elements of the direct cosine matrix (DCM) of MINS.

2.2. Measurement Equation. The differences of velocity and yaw between MINS and SINS are used as measurement data for data fusion. Then, the measurement vector is as

\[
\mathbf{Z} = [V_E - V_{ME} \ V_N - V_{MN} \ Y_E - Y_{ME}]^T, \tag{4}
\]

where \( V_E, V_N \) and \( Y_E \) are the east, north velocity, and yaw from SINS respectively, \( V_{ME}, V_{MN} \), and \( Y_{ME} \) are from MINS, respectively.

The measurement equation can be constructed as

\[
\mathbf{Z}(t) = \mathbf{H}(t) \mathbf{X}(t) + \mathbf{V}(t), \tag{5}
\]

where \( \mathbf{H}(t) \) is measurement matrix and \( \mathbf{V}(t) \) is measurement noise matrix. According to the relationship between measurement and state vectors, the measurement matrix \( \mathbf{H}(t) \) can be expressed as

\[
\mathbf{H} = \begin{bmatrix}
1 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 0 & 0 \\
0 & 0 & T_{12} T_{32} \over T_{12}^2 + T_{22}^2 & -T_{22} T_{32} \over T_{12}^2 + T_{22}^2 & -1 \\
\end{bmatrix}_{3 \times 3} \tag{6}
\]

2.3. Observability Degree of Each State Variable. After the analysis of the model combined with (2) and (5) by PWCS theory, we can conclude that all of the eight selected variables are observable, but the observability degrees are different from each other [13]. The simulation results in Section 5.2 indicate that the horizontal velocity errors and yaw misalignment converge immediately, that the estimation for horizontal misalignment angles lasts for 10–20 s, and that the estimation for gyro bias lasts for 3–5 min, which means that the degrees of velocity errors and yaw misalignment are the highest, those of horizontal misalignment angles are moderate, and those of gyro bias are the lowest.

The reasons which cause the different degrees of errors are as follows. The gyro bias needs integration to be reflected on misalignment angles, and the horizontal misalignment angles need projection reflected on acceleration. Further integration of acceleration, gyro bias can be reflected on velocity errors. In this process, from gyro bias to velocity errors, integrating operations are needed twice, and from horizontal misalignment angles to velocity errors, only one is needed. When velocity errors and yaw misalignment are selected as components of a measurement vector, there is no doubt that observability degrees of gyro bias are lowest, while those of velocity errors and yaw misalignment are highest, which are determined by the mechanism of transfer alignment. To shorten the estimation time for gyro bias, some other novel ways should be sought.

3. A New Way to Speed Up SINS Alignment

3.1. Analysis of Alignment Process in INS. An accepted viewpoint is that in navigation sensor data is of real-time significance. Based on initial navigation parameters, INS obtains the attitude, velocity, and position by the integration of sensor data. After integration, the sensor data can be discarded.

Take the alignment process of PINS as an example. As shown in Figure I(a), \( n' \) frame denotes the physical platform and \( n \) frame denotes the ideal navigation frame. In PINS, inertial sensors are installed on the physical platform. Inertial sensors measure the ship motion in \( n' \) frame, and navigation resolution is also executed in this frame; however, reference data are from \( n \) frame. Before aligning, misalignment angles between \( n' \) and \( n \) frames will cause the differences between navigation resolution values in \( n' \) frame and reference values in \( n \) frame. Because these differences can reflect the misalignments, transfer alignment can be finished with the model in Section 2. In the alignment process, with the above differences caused by misalignment angles, physical platform can be adjusted to coincide with the ideal frame. In other words, in PINS, sensor data reflect the magnitude of misalignment angle and other errors, and there is direct
relationship between sensor data and misalignment angles, so the sensor data are of real-time significance. And the adjustment for physical platform to get new sensor data is a time-consuming process.

At the same time, in SINS, the alignment method is derived from that of PINS, and so, the alignment must be a time-consuming process for the need of real-time sensor data and the adjustment of platform. But in INS, as far as the process of alignment is concerned, maybe, sensor data is of real-time significance for INS, but not for SINS.

In SINS, as shown in Figure 1(b), a mathematical platform replaces the physical platform in PINS and inertial sensors are directly installed on the ship. Here, the ship body is named $b$ frame and the mathematical platform is named $n'$ frame. In alignment, the adjusting process of the $n'$ frame is the same with that in PINS, while the difference is that the calculated sensor data in $n'$ frame is the projection of measured sensor data from $b$ frame. Only the projection data in $n'$ frame reflect the misalignment angles between $n'$ and $n$ frames, but sensor data cannot. The calculated and measured sensor data are connected by calculated DCM $C_{bn}^n$. In comparison with that in PINS, the direct relationship between sensor data and misalignment angles is severed by the mathematical platform. Then, the $n'$ frame can be adjusted constantly by the repeated calculation for DCM $C_{bn}^n$ with a same set of sensor data, which means that alignment time can be shortened without too much time to be spent in sampling real-time sensor data.

The above set of data can be seen as that, when the ship keeps an ideal static state and there are no sensor errors, all measured sensor data are equal and can be dealt with as a series of single data. In engineering, because of the errors from sensor and reference data, the update frequency of reference data, and so forth, a set of sensor data and reference data should be used for repeated SINS resolution (added backward-forward resolution) and repeated data fusion to improve the alignment accuracy.

Also, different from PINS, SINS is a digital system, in which there is only numerical data, no mass, spring, and resistance. So the adjustment for mathematical platform can be as fast as lightning.

3.2. Backward-Forward SINS Resolution. The above analysis indicates that the alignment of SINS can be fulfilled with a set of same data, which brings a new problem—the way to use these data.

In SINS, with initial attitude, velocity, and position, the navigation resolution is the real-time updating process for navigation parameters with sensor data by integrated calculation. In this process, ship moves from the origin to the end. In backward-forward SINS resolution, as shown in Figure 2, backward SINS resolution is the process in which ship moves from the end to the origin—a reverse process of normal navigation, and forward resolution is that from the origin to the end—a repeated process of normal navigation. From the basic SINS resolution algorithm, the deduction of backward-forward SINS algorithm is shown as follows.

![Figure 2: The process of backward-forward SINS resolution.](image-url)
all sensor data must be stored. According to the formulas (8), the resolution process can be expressed as follows:

\[
C^n_{b_k-1} = C^n_{b_k} \left( I + T_n \omega^b_{nbk} \right)^{-1} = C^n_{b_k} \left( I - T_n \omega^b_{nbk} \right) C^n_{b_k} \left( I - T_n \omega^b_{nbk-1} \right)
\]

\[
V^n_{b_k-1} = V^n_k - T_k \left( C^n_{b_{k-1} f_{k-1}} - (2 \omega^n_{ek} \omega^n_{ek}) \right) V^n_k + g^n
\]

where \( k \) is reduced from \( n \) to 0. As shown in Figure 2, \( t_m \) is both the starting point in the period \( t_{n1} \sim t_{01} \) and the ending point in the period \( t_{0} \sim t_{n} \). Take the attitude, velocity, and position at \( t_{n} \) as the initial attitude velocity and position at \( t_{n1} \), and the backward resolution can be fully realized. In the period of \( t_{0} \sim t_{n} \) and \( t_{n1} \sim t_{01} \), with the same recursive number \( k \), the ship maintains the same attitude, velocity, and position and maintains the same acceleration but opposite in direction. Some errors are induced by the approximation in formulas (9), and all these errors can be ignored when the resolution cycle is short enough. The simulation in Section 3.2.3 proves that the above approximation is effective.

After the backward resolution, a forward resolution should be made in order for the ship to return from the origin to the end. In the forward resolution, formulas (8) can be used. 

3.2.3. Simulation on Backward-Forward SINS Resolution. The sensor errors are listed in Table 1. And we assume that the ship is in a bad-moderate sea condition [18], and the ship swinging parameters are listed in Table 2. Ship initial attitudes are set as 0, and the ship is assumed without linear motion, and located north latitude 32° and east longitude 118°. Sensor sampling and navigation resolution cycle \( T_n \) is set as 10 ms.

Simulation results are shown in Figure 3, in which (a), (b), and (c) show the resolution results of pitch, east velocity, and latitude. The dot and solid lines denote the simulation with no sensor error and with sensor error, respectively. The simulation is divided into three stages: firstly, in the \( t_{0} \sim t_{n} \) period, sensor data are measured and stored, normal navigation is resolved, and this period lasts for 1 s; secondly, in the \( t_{n1} \sim t_{01} \) period, backward resolution is run; and finally, in the \( t_{02} \sim t_{n2} \) period, forward resolution is run. In the last two stages, the time consumed is determined by the performance of computer.

In Figure 3, without consideration of calculating the error, the ship can move from the end to the origin and move from origin to end with the backward and forward resolutions, respectively.

But the above processes also indicate that, with only backward or forward or backward-forward SINS resolution, no new information will be generated.

### Table 1: Sensor errors.

<table>
<thead>
<tr>
<th>Gyro bias</th>
<th>Acce bias</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td>Random</td>
</tr>
<tr>
<td>x</td>
<td>0.5°/h</td>
</tr>
<tr>
<td>y</td>
<td>0.5°/h</td>
</tr>
<tr>
<td>z</td>
<td>0.5°/h</td>
</tr>
</tbody>
</table>

### Table 2: Swinging parameters.

<table>
<thead>
<tr>
<th>Pitch</th>
<th>Roll</th>
<th>Yaw</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>10</td>
<td>6</td>
</tr>
</tbody>
</table>

4. Rapid Transfer Alignment Based on the Added Resolution and Data Fusion

The analysis in Section 3.1 indicates that alignment for SINS can be fulfilled with a set of data, and in this section, we combine a Kalman filter with the added backward-forward SINS resolution aiming to shorten the alignment time.

As shown in Figure 4, transfer alignment model based on Kalman filter introduced in Section 2 and a close-loop correction method are used in this rapid transfer alignment algorithm. Close-loop correction means that, after data fusion, the new estimation for velocity errors and misalignment angles will be fed to SINS to revise those corresponding parameters, and new estimation for gyro bias will be set as new compensation value to participate in the following navigation resolutions. In other words, after data fusion, the mathematical platform \( C^n_{b_k} \) will be adjusted. For a ship, the update frequency of the reference data from MINS is lower than that of SINS navigation resolution. \( T_s \) and \( T_n \) are set as update cycle of navigation resolution and reference data, respectively. Also, \( T_n \) is set as the added backward-forward SINS resolution cycle.

Two transfer alignment methods are compared, and the estimation processes of gyro bias are schematically demonstrated in Figure 5, in which (a) and (b) indicate these two methods, respectively, which are all based on the principle as shown in Figure 4. In the first one, the added backward-forward SINS resolution and data fusion are not used, while they are used in the second. In Figure 5, the dot-dashed lines denote the real gyro bias, while the solid line denotes the estimation of gyro bias. With the Kalman filter and matching method introduced in Section 2, the estimation of gyro bias is a slow process which will be convergent towards real gyro bias after a long time.

As shown in Figure 5(a), when the reference data is available, such as at the point \( t_{n} \), data fusion is executed, and a new estimate for the state vector will be produced. With the new estimation for misalignment angles and velocity errors, initial navigation parameters will be reset for the next period, such as \( t_{n1} \sim t_{n2} \), which means that the mathematical platform \( n' \) will be adjusted, and the new compensation value for gyro bias will also be reset. In this method, along with time, data fusion is run only once at every reference data update cycle.
But, as shown in Figure 5(b), in the same reference data update cycle, such as $t_0 \sim t_n$, at the point $t_n$, data fusion will be run, and new estimation will be produced, and so will new initial navigation parameters. And new initial parameters and new compensation value for gyro bias will produce the new navigation parameters at the point $t_{01}$, which are different from those at $t_0$. So, a new estimate will be generated at the point $t_{01}$, which is different from that at $t_0$, because the measurement vectors for the Kalman filter are different at points $t_0$ and $t_{01}$, which is caused by the same reference data but different navigation parameters. Similarly, new information will be got at the point $t_{n2}$, which is different from that at $t_n$. In Figure 5(b), with the added backward-forward SINS resolution and data fusion, the estimating operations for gyro bias and the adjustment for mathematical platform $n'$ will be done with two more times. In the second method, even with same observability degrees as in the first one, the estimation time will be shortened, because the estimation frequency is increased.

There is no doubt that the added resolution and data fusion in Figure 5(b) will increase the burden of navigation computer. Though in the last decades, the processing powering of the employed microprocessors has dramatically increased, it is difficult, in some way, to complete a large computation in a relatively short period.

As shown in Figure 6, in this rapid transfer alignment method, three tasks should be completed within one reference data update cycle. (1) Inertial sensor data needs to be sampled and stored and navigation resolution should be run. (2) Reference data needs to be sampled and stored and data fusion should be run. (3) Backward and forward calculations and data fusions should be executed. The first task should be
executed at every navigation update cycle. The last two tasks should be run in the last navigation update cycle of every reference data update cycle, which means that the above three tasks should be finished in $T_s$. Otherwise, the first task in the first navigation cycle of the next reference data cycle will be compromised. It is difficult to finish these three tasks in $T_s$ with a computer of limited performance.

However, this problem can be resolved by the full use of resources of high speed computers with the support of real-time multitasking operation system (RTOS), such as VxWorks. In VxWorks, the above three tasks can be set with different priorities. The first can be run preferentially when Task 2 or Task 3 is being run, which means that the first task of the next reference data cycle can be run preferentially when the idle resources of CPU in the previous cycle. The paper is not involved in the programs in RTOS in detail.

5. Simulation

5.1. Parameters for Simulation. The ship moving parameters are set as in Section 3.2.3. The ideal velocity and yaw of the ship are used as reference data from MINS after white noise is added. The variance of the white noise is set as $\begin{bmatrix} (0.4 \text{ m/s})^2 & (0.4 \text{ m/s})^2 & (0.3^\circ)^2 \end{bmatrix}$. The sensor errors are listed in Table 1.

The parameters for Kalman filter are

$$X_0 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}^T,$$

$$P_0 = \text{diag} \left[ (0.1 \text{ m/s})^2 \quad (0.1 \text{ m/s})^2 \quad (1.5^\circ)^2 \quad (1.5^\circ)^2 \quad (1.5'/\text{h})^2 \quad (1.5'/\text{h})^2 \quad (1.5'/\text{h})^2 \right],$$

$$Q = \text{diag} \left[ (500 \text{ ug})^2 \quad (500 \text{ ug})^2 \quad (0.5^\circ)^2 \quad (0.5^\circ)^2 \quad (0.5^\circ)^2 \quad 0 \quad 0 \quad 0 \right],$$

$$R = \text{diag} \left[ (0.4 \text{ m/s})^2 \quad (0.4 \text{ m/s})^2 \quad (0.3^\circ)^2 \right].$$

5.2. Simulation Results. The simulation lasts for 500s, and the simulation results are stored once per second. The misalignment angle curves are shown in Figure 7. The estimation of velocity error curves are in Figure 8, and the estimation curves of gyro bias in Figure 9. In Figures 7–9, the dot-dash and solid lines denote the simulation results of scheme 1 and scheme 2, respectively. The dotted lines in Figures 7 and 8 are the limit alignment accuracy of misalignment angles and velocity. And the dotted lines in Figure 9 denote the setting value of constant gyro bias.

The curves in Figure 7 show that, either in scheme 1 or scheme 2, misalignment angles can be estimated rapidly and are oscillating in small amplitudes with the swinging frequency of ship. But the tendency of misalignment curves, especially that of roll ones, indicates that estimation speed is slightly higher in scheme 2 than in scheme 1. The statistical data about misalignment angles are shown in Table 3, and the statistical results show that the alignment accuracy of these two schemes is roughly equal after 60 s. The curves in Figure 8 indicate that the estimation speed and accuracy for velocity error are roughly equal in scheme 1 and scheme 2.

The curves in Figure 9 show that, in scheme 2, the estimation curves of gyro bias converge towards the setting values at about 50 s, and the oscillating amplitudes are very small in 100 s, while in scheme 1, 200 s is needed for the convergence of gyro bias, and relatively large oscillations still exist even after 300 s. The statistical mean values shown in Table 4 indicate that, in scheme 2, in the period from 50 s to 100 s, about 96% and 93% and 72% of gyro bias can be estimated along $x$, $y$, and $z$ axes, respectively. And about 99%, 97%, and 78% can be estimated in the period from 100 s to 150 s.

6. Conclusion

Two viewpoints are given in this paper. The first is that, in SINS, mathematical platform cuts off the direct relationship between sensor data and misalignment angles, which means that initial alignment can be fulfilled by the repeatedly resolution on a same set of sensor data. The second is that, with the added backward-forward SINS resolution and repeated data fusion on the corresponding resolution results and the external data, the alignment time can be greatly reduced.
Table 3: Statistical results for misalignment angles.

<table>
<thead>
<tr>
<th>Time</th>
<th>Pitch (mrad)</th>
<th>Mean</th>
<th>Standard variance</th>
<th>Roll (mrad)</th>
<th>Mean</th>
<th>Standard variance</th>
<th>Yaw (mrad)</th>
<th>Mean</th>
<th>Standard variance</th>
</tr>
</thead>
<tbody>
<tr>
<td>1~10s</td>
<td>Scheme 1</td>
<td>−0.8225</td>
<td>1.0610</td>
<td>1.1833</td>
<td>4.9672</td>
<td>−0.9375</td>
<td>1.2756</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Scheme 2</td>
<td>0.4631</td>
<td>1.6724</td>
<td>0.2318</td>
<td>0.7429</td>
<td>−0.3956</td>
<td>1.0700</td>
<td></td>
<td></td>
</tr>
<tr>
<td>11~20s</td>
<td>Scheme 1</td>
<td>−0.2278</td>
<td>0.5136</td>
<td>−0.0705</td>
<td>0.5156</td>
<td>−1.1170</td>
<td>0.7199</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Scheme 2</td>
<td>−0.4993</td>
<td>0.5865</td>
<td>0.4806</td>
<td>0.2647</td>
<td>−0.4755</td>
<td>0.8203</td>
<td></td>
<td></td>
</tr>
<tr>
<td>31~40s</td>
<td>Scheme 1</td>
<td>−0.4776</td>
<td>0.4653</td>
<td>0.9794</td>
<td>0.5194</td>
<td>0.0448</td>
<td>0.9782</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Scheme 2</td>
<td>−0.8563</td>
<td>0.4557</td>
<td>0.4980</td>
<td>0.6148</td>
<td>−0.3609</td>
<td>0.8828</td>
<td></td>
<td></td>
</tr>
<tr>
<td>51~60s</td>
<td>Scheme 1</td>
<td>−0.5430</td>
<td>0.4296</td>
<td>0.5377</td>
<td>0.4614</td>
<td>−0.2183</td>
<td>0.9682</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Scheme 2</td>
<td>−0.7073</td>
<td>0.4854</td>
<td>0.5415</td>
<td>0.5531</td>
<td>0.2041</td>
<td>0.9117</td>
<td></td>
<td></td>
</tr>
<tr>
<td>61~500s</td>
<td>Scheme 1</td>
<td>−0.5075</td>
<td>0.4498</td>
<td>0.4154</td>
<td>0.4852</td>
<td>−0.0877</td>
<td>0.9168</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Scheme 2</td>
<td>−0.6541</td>
<td>0.4505</td>
<td>0.4815</td>
<td>0.4831</td>
<td>0.0709</td>
<td>0.9011</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Limited accuracy</td>
<td>−0.4990</td>
<td>0.4990</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
<td>0.0</td>
</tr>
</tbody>
</table>

Table 4: Statistical results for gyro bias.

<table>
<thead>
<tr>
<th>Time</th>
<th>Pitch (mrad)</th>
<th>Mean</th>
<th>Standard variance</th>
<th>Roll (mrad)</th>
<th>Mean</th>
<th>Standard variance</th>
<th>Yaw (mrad)</th>
<th>Mean</th>
<th>Standard variance</th>
</tr>
</thead>
<tbody>
<tr>
<td>51~100s</td>
<td>Scheme 1</td>
<td>−0.4139</td>
<td>0.4563</td>
<td>−0.7990</td>
<td>0.9143</td>
<td>0.7591</td>
<td>0.4807</td>
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<tr>
<td></td>
<td>Scheme 2</td>
<td>0.5172</td>
<td>0.0757</td>
<td>0.5335</td>
<td>0.1329</td>
<td>0.6390</td>
<td>0.1588</td>
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<tr>
<td>101~150s</td>
<td>Scheme 1</td>
<td>0.3474</td>
<td>0.2102</td>
<td>−0.3793</td>
<td>0.4709</td>
<td>1.9998</td>
<td>0.3182</td>
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<tr>
<td></td>
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<td>0.5037</td>
<td>0.0505</td>
<td>0.4847</td>
<td>0.0499</td>
<td>0.6072</td>
<td>0.0628</td>
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<tr>
<td>151~200s</td>
<td>Scheme 1</td>
<td>0.5742</td>
<td>0.0632</td>
<td>0.2499</td>
<td>0.1254</td>
<td>0.8496</td>
<td>0.2778</td>
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<td></td>
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<tr>
<td></td>
<td>Scheme 2</td>
<td>0.4943</td>
<td>0.0382</td>
<td>0.4703</td>
<td>0.0284</td>
<td>0.5196</td>
<td>0.0256</td>
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<td></td>
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<tr>
<td>201~250s</td>
<td>Scheme 1</td>
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<td>0.2713</td>
<td>0.0744</td>
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<td>0.0648</td>
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<td></td>
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<tr>
<td></td>
<td>Scheme 2</td>
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<td>0.0224</td>
<td>0.4718</td>
<td>0.0231</td>
<td>0.5255</td>
<td>0.0224</td>
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<tr>
<td>251~300s</td>
<td>Scheme 1</td>
<td>0.5189</td>
<td>0.0344</td>
<td>0.4203</td>
<td>0.0630</td>
<td>0.5292</td>
<td>0.0530</td>
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<tr>
<td></td>
<td>Scheme 2</td>
<td>0.5019</td>
<td>0.0217</td>
<td>0.4752</td>
<td>0.0258</td>
<td>0.5113</td>
<td>0.0236</td>
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<tr>
<td>301~500s</td>
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<td>0.5156</td>
<td>0.0272</td>
<td>0.4122</td>
<td>0.0410</td>
<td>0.5683</td>
<td>0.0412</td>
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</tr>
<tr>
<td></td>
<td>Scheme 2</td>
<td>0.4990</td>
<td>0.0116</td>
<td>0.4823</td>
<td>0.0169</td>
<td>0.5134</td>
<td>0.0129</td>
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<tr>
<td>Setting value</td>
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<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
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</tr>
</tbody>
</table>

With the above two viewpoints: (1) a backward-forward SINS resolution algorithm is designed in detail, and simulation results indicate that a ship can move from the end to the origin with the backward resolution and move from the origin to the end with the forward. (2) A rapid transfer alignment algorithm is also designed in detail, in which the backward-forward resolution and two more operations for the estimation of gyro bias are added in one reference data update cycle. In addition, the correctness of its algorithm is proved by simulation. The simulation result produced with
(1) Sensor data sampling, storing and navigation resolution
(2) Reference data sampling, storing and data fusion
(3) Reverse and forward calculation
∗CPU idle

Figure 6: Calculation process for alignment program.

Figure 7: Estimation curves for misalignment angles.

Figure 8: Estimation curves for velocity errors.

Figure 9: Estimation curves for gyro bias.

the method in this paper indicates that the alignment time is reduced from 300 s to 100 s, compared with that of the transfer alignment method without the added backward-forward SINS resolution and data fusion.

One problem, which may be encountered in engineering applications with this transfer alignment method, is studied, and a possible solution is given in which RTOS is introduced to distribute computer resources coordinately.

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References


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