Research Article

An Adaptive Nonlinear Extended State Observer for the Sensorless Speed Control of a PMSM

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Received 13 December 2014; Accepted 5 March 2015

Academic Editor: Andrzej Swierniak

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This paper presents a sensorless speed control strategy for a permanent-magnet synchronous motor (PMSM) based on an adaptive nonlinear extended state observer (ANLESO). In this paper, an extended state observer (ESO), which takes back-EMF (back electromotive force) as an extended state, is used to estimate the rotor position and the rotor speed because of its simpler structure and higher accuracy. Both linear ESO (LESO) and nonlinear ESO (NLESO) are considered to estimate the back-EMF of PMSM, and NLESO is finally implemented due to its obvious advantage in convergence. The convergence characteristics of the estimation error of the observer are analyzed by the Lyapunov theory. In order to take both stability and steady-state error into consideration, an adaptive NLESO is proposed, which adaptively adjusts the parameters of NLESO to a compromised value. The performance of the proposed method was demonstrated by simulations and experiments.

1. Introduction

In recent years, permanent-magnet synchronous motors have increasingly gained lots of applications due to their high efficiency, high dynamic response, and high torque to current ratio [1, 2]. Compared to DC motors, PMSMs are superior in robustness and overload capability and they do not need mechanical commutation. As the fast switch components and digital signal processors become economical, PMSMs are widely used as an alternative for energy saving applications. Besides, some countries have kept using low-cost induction motors due to their simple structure and easiness in manufacturing. However, induction motors are less efficient than PMSMs in terms of performance [3, 4].

PMSM drives require a position sensor with high resolution to achieve an efficient vector control, such as a shaft encoder or a resolver. Unfortunately, these sensors are expensive and have a limited lifetime. Besides, the size of the motor assembly will become larger. Therefore, many sensorless control methods have been developed to eliminate these mechanical sensors. In particular in some extreme environments where position sensors may work abnormally,

sensorless control methods are more robust than those using position sensors [4].

By means of injecting high frequency signal into motor, the impedance difference caused by magnetic saturation, which contains the information about the rotor position, can be calculated [5]. However, injecting high frequency signal brings noise and torque ripples. Because of good standstill performance, the method is usually used within low-speed range [6, 7]. The extended Kalman filter (EKF) was also employed for rotor speed and position estimation due to its good dynamic performance and strong antijamming capability [8]. Algorithm complexity and large calculating quantity are disadvantages of EKF, which limits its practical application. Neural network technology has a good advantage in terms of parameter identification and it has been used in sensorless control system by many scholars [9]. In these papers, the rotor position is identified online by neural network. However, the method needs a long computation time and brings great burden on the digital signal processing, which gives rise to choke points in applications. Zhang and Li proposed the model reference adaptive scheme (MRAS) to implement a sensorless control system. The idea of MRAS

is to build a reference model of the PMSM system without containing unknown parameters and to obtain the difference between the reference model outputs and actual system outputs. Next, an appropriate adaptive law will be designed to adjust parameters of reference model in real time according to the difference [10]. But the accuracy of this method depends on the designed reference model, which may prohibit the convergence of the system. Moreover, in [11, 12], the flux linkage is used as state variable and is estimated directly. Some authors used a sliding mode observer (SMO) approach [6, 13–16]. The structure of SMO is simple and convenient to be used in practical applications. Unfortunately, the estimation accuracy of SMO would be affected by chattering.

The extended state observer (ESO) first proposed by Huang and Han in [17] is the key step of the active disturbance rejection control (ADRC) that is taking off as a technology after numerous successful applications in engineering. ESO has simple structure and it is able to estimate unmodeled dynamics accurately in many cases. In terms of ADRC, a class of nonlinear ESOs is designed to estimate the sum of both the states and external disturbances [18]. After that, Gao proposed a class of linear ESOs (LESO) and provided guidance on how to choose the optimal parameters in the controller design. In this way, the number of parameters to be configured is reduced [19]. At present, ESO is mainly used in control system to estimate disturbances and to compensate them via a feed-forward cancellation technique [20–22]. Besides, ESO can be extended to multi-input–multi-output systems as well [22].

In this paper, a sensorless speed control scheme for a PMSM based on an ANLESO is proposed. ESO is applied to estimate the rotor position and rotor speed of PMSM for the first time. The information of the rotor position and the rotor speed of PMSM can be calculated by estimating the back-EMF. For this reason, the estimation accuracy of back-EMF affects the accuracy of the position and speed directly. ESO usually treats all the external disturbances and/or system uncertainties as the “total disturbance” and extends it as an additional state variable [16]. Therefore, system states and unknown parts of system can be estimated by ESO in the meantime without knowing the model of the unknown parts (the derivative of the unknown parts). In this scheme, back-EMF is the unknown part of the system and it would be treated as an additional state variable to be estimated. Back-EMF contains the information of the rotor position and speed that cannot be obtained without sensor. For this reason, back-EMF cannot be modeled directly. As mentioned previously, ESO would treat back-EMF as “disturbance” and estimate the back-EMF accurately without knowing its model. By means of Lyapunov stability analysis, an adaptive control scheme is adopted to balance stability and steady-state error. The adaptive control scheme could adaptively adjust the parameters of ESO to a compromised value, and the steady-state error will converge to a minimum on the premise of system stable. Compared to other sensorless control methods, ANLESO has simpler structure, smaller chattering, and higher accuracy.

The state equations of the stator current in a stator-fixed reference frame and the back-EMF for each phase in the fixed frame of the PMSM are discussed in Section 2. In Section 3,

an adaptive nonlinear extended state observer for the sensorless control scheme is designed and discussed. Section 4 gives the simulation results and Experimental results. Finally, conclusions and suggestions for future improvements are given in Section 5.

2. Mathematical Model

The voltages in the three phases can be transformed into the synchronous coordinates in the two phases for vector control. The state equations of the stator current, written in a stator-fixed reference frame ($\alpha\beta$), take the following form [23]:

$$\frac{di_\alpha}{dt} = -\frac{R}{L}i_\alpha - \frac{1}{L}e_\alpha + \frac{1}{L}V_\alpha, \quad (1)$$

$$\frac{di_\beta}{dt} = -\frac{R}{L}i_\beta - \frac{1}{L}e_\beta + \frac{1}{L}V_\beta, \quad (2)$$

where $i_{\alpha,\beta}$, $e_{\alpha,\beta}$, and $V_{\alpha,\beta}$ represent the current, electromotive force, and voltage for each phase, respectively. R and L represent the stator resistance and inductance, respectively.

The back EMF for each phase can be represented in the fixed frame as

$$\begin{aligned} e_\alpha &= -K_E\omega_r \sin \theta, \\ e_\beta &= K_E\omega_r \cos \theta, \end{aligned} \quad (3)$$

where K_E , ω_r , and θ represent the magnetic flux of the PM, the electric angular velocity, and the rotor angle, respectively.

3. Proposed Adaptive Nonlinear ESO

In the sensorless control system, the back-EMF e_α , e_β are usually figured out by the information of control signals V_α , V_β and output currents i_α , i_β . In other words, from the system formulated by (1) and (2), e_α and e_β can be treated as the unknown parts of the system. Thus, the back-EMF would be extended as additional state variables. In this section, linear ESO and nonlinear ESO are described, respectively. For LESO, the bounded-input bounded-output (BIBO) stability can be reached. For NLESO, a Lyapunov stability analysis is shown. At last, an adaptive control scheme is designed in order to improve the estimated accuracy.

The block diagram of the sensorless control system for PMSM is shown in Figure 1. The space vector pulse width modulation (SVPWM) algorithm is used as modulation strategy to generate a sinusoidal current of the stator. To control the PMSM, the three-phase coordinates need to be transformed into dq synchronous coordinates by Clarke transformation and Park transformation. An ADC (analog to digital converter) module is used to detect phase current and bus voltage. The proportional-integral (PI) control is used in speed loop and current loop. All the sensorless control algorithms are simulated by MatLab and executed on a DSP chip.

3.1. Linear ESO. Note that this system is symmetric, and we only need to design an observer to estimate e_α (the structure

Proof. The goal is to prove that there exists a positive definite energy function whose derivative is always made negative. The following energy function is chosen [24]:

$$\begin{aligned}
 V(e_1, e_2) &= A|e_1|^{3/2} - Be_1e_2 + Ce_2^2 \\
 &= A|e_1|^{-1/2} \left[\left(e_1 - \frac{B|e_1|^{1/2}}{2A}e_2 \right)^2 - \frac{B^2|e_1|}{4A^2}e_2^2 \right] + Ce_2^2 \\
 &= A|e_1|^{-1/2} \left(e_1 - \frac{B|e_1|^{1/2}}{2A}e_2 \right)^2 + \left(C - \frac{B^2|e_1|^{1/2}}{4A} \right) e_2^2,
 \end{aligned} \quad (14)$$

where A , B , and C are the parameters to be determined. Suitable A , B , and C need to be chosen to let the energy function meet the Lyapunov stability theorem.

In order to guarantee that $V(e_1, e_2)$ is positively definite, the following rules need to be followed:

$$(R1) \ A > 0$$

$$(R2) \ C > B^2|e_1|^{1/2}/4A > 0.$$

Since $|e_1|^{1/2}$ is bounded, (R2) always can be satisfied by choosing a suitable C .

Calculate the partial derivative of $V(e_1, e_2)$ as follows:

$$\begin{aligned}
 \frac{\partial V}{\partial e_1} &= \frac{3}{2}A|e_1|^{1/2} \text{sign}(e_1) - Be_2, \\
 \frac{\partial V}{\partial e_2} &= -Be_1 + 2Ce_2.
 \end{aligned} \quad (15)$$

The derivative of the energy function is as follows:

$$\dot{V} = \frac{\partial V}{\partial e_1} \dot{e}_1 + \frac{\partial V}{\partial e_2} \dot{e}_2. \quad (16)$$

By substituting (15) into (16), $\dot{V}$ can be given as

$$\begin{aligned}
 \dot{V} &= \left(\frac{3}{2}A|e_1|^{1/2} \text{sign}(e_1) - Be_2 \right) \left(-\left(\frac{R}{L} + \beta_1 \right) e_1 + \frac{1}{L}e_2 \right) \\
 &\quad + (-Be_1 + 2Ce_2) \left(-h - \beta_2|e_1|^{1/2} \text{sign}(e_1) \right).
 \end{aligned} \quad (17)$$

From (17), the following expression can be deduced:

$$\begin{aligned}
 \dot{V} &= \left(\frac{3}{2} \frac{A}{L} - 2C\beta_2 + B \left(\frac{R}{L} + \beta_1 \right) |e_1|^{1/2} \right) \\
 &\quad \cdot |e_1|^{-1/4} |e_1|^{3/4} \text{sign}(e_1) e_2 \\
 &\quad - \frac{B}{L} e_2^2 - \left(\frac{3}{2} A \left(\frac{R}{L} + \beta_1 \right) - B\beta_2 \right) |e_1|^{2(3/4)} \\
 &\quad + (Bhe_1 - 2che_2).
 \end{aligned} \quad (18)$$

Assume that

$$\begin{aligned}
 X &= \frac{3}{2}A \left(\frac{R}{L} + \beta_1 \right) - B\beta_2, \\
 Y &= \left(\frac{3}{2} \frac{A}{L} - 2C\beta_2 + B \left(\frac{R}{L} + \beta_1 \right) |e_1|^{1/2} \right) |e_1|^{-1/4}, \\
 Z &= \frac{B}{L}.
 \end{aligned} \quad (19)$$

Equation (18) can be rewritten as

$$\begin{aligned}
 \dot{V} &= -X|e_1|^{2(3/4)} + Y|e_1|^{3/4} \text{sign}(e_1) e_2 \\
 &\quad - Ze_2^2 - (-Bhe_1 + 2Che_2) \\
 &= V_1 - V_2,
 \end{aligned} \quad (20)$$

where $V_1 = -X|e_1|^{2(3/4)} + Y|e_1|^{3/4} \text{sign}(e_1) e_2 - Ze_2^2$ is a quadratic function with regard to $|e_1|^{3/4} \text{sign}(e_1)$ and e_2 . $V_2 = (-Bhe_1 + 2Che_2)$ is a plane function with regard to e_1 and e_2 . A necessary and sufficient condition for the positively definite property of the quadratic function V_1 can be obtained:

$$\textcircled{1} \ X > 0$$

$$\textcircled{2} \ Z > 0$$

$$\textcircled{3} \ Y^2 - 4XZ < 0.$$

From $\textcircled{1}$ we have

$$(R3) \ (3/2)A(R/L + \beta_1) > B\beta_2.$$

From $\textcircled{2}$ we have

$$(R4) \ B/L > 0, \text{ which means } B > 0.$$

Then, from $\textcircled{3}$ we can derive that

$$\begin{aligned}
 &\left(\frac{3}{2} \frac{A}{L} - 2C\beta_2 + B \left(\frac{R}{L} + \beta_1 \right) |e_1|^{1/2} \right)^2 |e_1|^{-1/2} \\
 &< 4 \frac{B}{L} \left(\frac{3}{2} A \left(\frac{R}{L} + \beta_1 \right) - B\beta_2 \right).
 \end{aligned} \quad (21)$$

Then, the following expression can be obtained

$$\begin{aligned}
 &\left(\frac{3}{2} \frac{A}{L} - 2C\beta_2 + B \left(\frac{R}{L} + \beta_1 \right) |e_1|^{1/2} \right) \\
 &< 2 \sqrt{\frac{B}{L} \left(\frac{3}{2} A \left(\frac{R}{L} + \beta_1 \right) - B\beta_2 \right)} |e_1|^{1/4}.
 \end{aligned} \quad (22)$$

Assume that

$$\begin{aligned}
 a &= B \left(\frac{R}{L} + \beta_1 \right), \\
 b &= \sqrt{\frac{B}{L} \left(\frac{3}{2} A \left(\frac{R}{L} + \beta_1 \right) - B\beta_2 \right)}, \\
 c &= \frac{3}{2} \frac{A}{L} - 2C\beta_2, \\
 x &= |e_1|^{1/4}.
 \end{aligned} \quad (23)$$

Equation (22) can be rewritten as

$$c + ax^2 < 2bx. \quad (24)$$

It can be verified that there exists some meaningful x satisfying inequation (24) and meeting the rules (R1)~(R4) if and only if the following conditions are satisfied:

$$\left(\frac{R}{L} + \beta_1\right) > 0, \quad \beta_2 > 0. \quad (25)$$

Therefore, $a = B(R/L + \beta_1) > 0$, and inequation (24) denotes a parabola going upwards. Due to the existence of some meaningful x satisfying inequation (24), the vertex of the parabola must be negative:

$$b^2 - ac > 0. \quad (26)$$

Hence,

$$\frac{B}{L} \left(\frac{3}{2} A \left(\frac{R}{L} + \beta_1 \right) - B\beta_2 \right) - B \left(\frac{R}{L} + \beta_1 \right) \left(\frac{3}{2} \frac{A}{L} - 2C\beta_2 \right) > 0$$

$$\begin{aligned} B\beta_2 \left(2C \left(\frac{R}{L} + \beta_1 \right) - \frac{B}{L} \right) &> 0 \\ 2C \left(\frac{R}{L} + \beta_1 \right) &> \frac{B}{L}. \end{aligned} \quad (27)$$

Inequality (26) is established between the two real roots $x = (b \pm \sqrt{b^2 - ac})/a$ of the quadratic equation $ax^2 - 2bx + c = 0$. In order to separate the two roots as far as possible and make the smaller one very small, a very large B needs to be selected, which makes $B\beta_2 \gg 0$, and the choice of parameter C is required to ensure $2C(R/L + \beta_1) - B/L > 0$. Finally, choose appropriate A to make parameters B and C satisfy rules (R1)~(R4). In this way, V_1 will be a negative definite function with variable e_1 in a very wide range and arbitrary e_2 . Meanwhile, the area in which $\dot{V} = V_1 - V_2$ does not satisfy negative conditions (the area $\dot{V} > 0$) is the part above the intersecting line of the quadratic function V_1 and the plane function V_2 .

The value of e_1 in the intersecting line is the same order as $e_1 = (Bh/X)^2$ which is the root of the following equation:

$$Bhe_1 = X |e_1|^{2(3/4)}. \quad (28)$$

Since X is the same order as $B\beta_2$, the value of e_1 in the intersecting line is the same order as $(h/\beta_2)^2$. Therefore, a large enough β_2 can guarantee that e_1 is stable in a very wide range. The larger β_2 we set, the smaller the unstable boundary of e_1 , and then it will result in a better convergence.

In the same way, the value of e_2 in the intersecting line is the same order as $e_2 = (2Ch/Z)$ which is the root of the following equation:

$$2Che_2 = Ze_2^2. \quad (29)$$

Consider that $Z = B$, the value of e_1 in the intersecting line is the same order as $(2Ch/B)$. From inequality (21), the inequality $2C(R + L\beta_1)/B > 1$ holds. Therefore, a large enough $(R + L\beta_1)$, by setting β_1 , can guarantee the existence of appropriate B and C to make $|e_2| = |(2Ch/B)|$ small enough. $\square$

FIGURE 2: Flow chart of the algorithm to calculate β_1 .

Remark 1. Obviously, the state error would not actually go to zero but enter, and is contained within, a neighborhood of the origin by this method. Therefore, by means of setting appropriate β_1 and β_2 , the performance required in practical engineering can be achieved.

Remark 2. Using a sigmoid function as the nonlinear function in ESO can reduce chatting in the system [15]. Consider

$$\begin{aligned} \begin{bmatrix} \dot{Z}_1 \\ \dot{Z}_2 \end{bmatrix} &= \begin{bmatrix} -\frac{R}{L} & \frac{1}{L} \\ 0 & 0 \end{bmatrix} \begin{bmatrix} Z_1 \\ Z_2 \end{bmatrix} + \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix} u \\ &+ \begin{bmatrix} -\beta_1 \cdot e_1 \\ -\beta_2 \cdot |e_1| \cdot \text{sigmoid}(e_1) \end{bmatrix}, \end{aligned} \quad (30)$$

where

$$\text{sigmoid}(e_1) = \left(\frac{2}{1 + \exp(-ae_1)} \right) - 1. \quad (31)$$

3.3. Proposed Adaptive Nonlinear ESO. Although a large $(R + L\beta_1)$ will render e_2 stable in a wider range, the steady-state error still has to be considered here. From (13) we know that a large $(R + L\beta_1)$ leads to the increase of e_2 in steady state. The improved method proposed in this paper is to adaptively adjust the parameters of NLESO to a compromised value which takes both stability and steady-state error into consideration.

Rewrite inequality (27) as the following expression:

$$\frac{2C}{B} > \frac{1}{R + L\beta_1}. \quad (32)$$

Thus, the roots of (29) hold the following equality:

$$|e_2| = \frac{2C|h|}{B} > \frac{|h|}{R + L\beta_1}. \quad (33)$$

FIGURE 3: Simulation waveforms of estimated back EMF when speed is 500 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 4: Simulation waveforms of actual and estimated i_α, i_β when speed is 500 r/min and the load torque is 1 Nm. (a) Actual and estimated i_α obtained by the proposed ANLESO. (b) Actual and estimated i_β obtained by the proposed ANLESO. (c) Actual and estimated i_α obtained by the conventional SMO. (d) Actual and estimated i_β obtained by the conventional SMO.

This means that the lower bound of e_2 is larger than $|h|/(R + L\beta_1)$. β_1 is a design parameter, so the size of $R + L\beta_1$ can be changed by means of adjusting β_1 . The main idea of this method is to decrease β_1 gradually to reduce steady-state error and increase β_1 when the system may become unstable. By several iterations, the value of β_1 would approximate the compromised value gradually.

Figure 2 illustrates the algorithm to calculate β_1 , where $0 < \alpha < 1$ and $p > 1$ are adjustment factors. ΔV is the error of command velocity and measured velocity.

3.4. Rotor Position and Speed Estimate. Using the estimated back-EMF obtained by the ANLESO, the position and speed

FIGURE 5: Simulation waveforms of actual and estimated speeds when speed is 500 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 6: Simulation waveforms of actual rotor position, estimated rotor position, and estimated error when speed is 500 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

signals can be calculated easily. According to (3), the rotor speed can be obtained as follows:

$$\hat{\omega}_r = \frac{\sqrt{(\hat{e}_\alpha^2 + \hat{e}_\beta^2)}}{K_E}. \quad (34)$$

Similarly, the rotor position can be deduced from (3) as follows:

$$\hat{\theta} = -\arctan \left[\frac{\hat{e}_\alpha}{\hat{e}_\beta} \right]. \quad (35)$$

4. Simulation and Experimental Results

4.1. Simulation Results. In order to show the high-speed performance of the proposed ANLESO, it is necessary to compare it with the conventional SMO through the Mat-Lab/Simulink programming environment. The parameters of PMSM used in simulation are listed in Table 1.

Figures 3–6 show the simulation waveforms when the reference speed is changed from zero to 500 r/min and

TABLE 1: The parameters of PMSM.

Parameters	Values
Rated power	1.5 KW
Rated speed	2500 r/min
Input voltage (DC)	310 V
Current	6 A
Stator resistance	1.18 Ω
Stator inductance	53.26 mH
Rotational inertia	1.33×10^{-3} kg·m ²
Flux of permanent magnet	0.0356 Wb
Poles	8

the load torque is 1 Nm. In these figures, part (a) gives the simulation waveforms obtained by the proposed ANLESO and part (b) gives the simulation waveforms obtained by the conventional SMO. Estimated back-EMF, actual and estimated phase currents, actual and estimated rotor speed,

FIGURE 7: Simulation waveforms of estimated back EMF when speed is 2000 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 8: Simulation waveforms of actual and estimated i_α , i_β when speed is 2000 r/min and the load torque is 1 Nm. (a) Actual and estimated i_α obtained by the proposed ANLESO. (b) Actual and estimated i_β obtained by the proposed ANLESO. (c) Actual and estimated i_α obtained by the conventional SMO. (d) Actual and estimated i_β obtained by the conventional SMO.

and actual and estimated rotor position are also shown in these figures.

As can be seen from Figures 3–6, the accuracy of estimation has been greatly improved with the help of proposed ANLESO. Different from the conventional SMO, the back-EMF in Figure 3(a) almost has no chattering. Compared with Figures 4(c) and 4(d), the estimated results of phase

currents in Figures 4(a) and 4(b) are better. Due to the good performance of estimating back-EMF and currents, the chattering phenomenon of the estimated rotor position and speed is reduced, which can be seen from Figures 5(a), 5(b), 6(a), and 6(b). In part (a) of these figures, the estimated speed is almost the same as actual speed; however, the estimated speed in part (b) of these figures exhibits the chattering

FIGURE 9: Simulation waveforms of actual and estimated speeds when speed is 2000 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 10: Simulation waveforms of actual rotor position, estimated rotor position, and estimated error when speed is 2000 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 11: Platform of 1.5 kw PMSM sensorless control system based on DSP.

phenomenon. Besides, it can be seen that the estimated error of the position in part (a) is smaller than that shown in part (b) of these figures.

Figures 7–10 show the two sets of simulation waveforms when the reference speed is changed from zero to 2000 r/min

and the load torque is 1 Nm. In these figures, part (a) gives the simulation waveforms obtained by the proposed ANLESO and part (b) gives the simulation waveforms obtained by the conventional SMO. Estimated back-EMF, actual and estimated phase currents, actual and estimated rotor speed,

FIGURE 12: Operating waveforms of estimated back EMF in steady state when speed is 500 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 13: Operating waveforms of estimated i_α and i_β in steady state when speed is 500 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 14: Operating waveforms of estimated rotor speeds when speed is 500 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

and actual and estimated rotor position are also shown in these figures.

As can be seen from Figures 7–10, when the rotor speed is raised to 2000 r/min, advantages of ANLESO become more apparent than conventional SMO. Comparing the estimated back-EMF in Figures 7(a) and 7(b), we can find that the former has smaller chattering. As a result, the estimation of rotor speed becomes more accurate by ANLESO, which can be seen in Figures 9(a) and 9(b). The waveform forms presented in Figures 10(a) and 10(b) show the estimated rotor position. The position estimation error is reduced and the accuracy of rotor position estimation is improved in Figure 10(a).

4.2. Experimental Results. To further verify the performance of the new SMO for estimating rotor position and speed, an

experimental system has been designed to control the 130SJT-M060D (1.5 kw) sinusoidal PMSM motor made by GSK.

Figure 11 shows a photograph of the sensorless control system. The High Voltage Digital Motor Control Kit, made by TI, is utilized in the system, which contains power modules, switching devices, current and voltage sensing circuit, ADC modules, and PWM DAC (digital to analog converter) modules. A floating-point TMS320F28335 DSP is employed as the digital controller. The current control cycle is 100 μ s and the velocity control cycle is 1 ms. A 2 μ s dead time is chosen for the PWM switching. All of the control variables are monitored in real time by an oscilloscope after they are converted to analog signals through the PWM DACs modules, which use an external low pass filter to generate the waveforms. The motor parameters used in experiment are given in Table 1.

FIGURE 15: Operating waveforms of rotor position and estimate error when speed is 500 r/min and the load torque is 1 Nm. (a) Actual and estimated rotor position obtained by the proposed ANLESO. (b) Actual and estimated rotor position obtained by the conventional SMO. (c) Estimated error obtained by the proposed ANLESO. (d) Estimated error obtained by the conventional SMO.

FIGURE 16: Operating waveforms of estimated back EMF in steady state when speed is 2000 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 17: Operating waveforms of estimated i_α and i_β in steady state when speed is 2000 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

Figures 12–14 show the operating waveforms when the reference speed is changed from zero to 500 r/min and the load torque is 1 Nm. In these figures, part (a) gives the operating waveforms obtained by the proposed ANLESO and part (b) gives the operating waveforms obtained by the conventional SMO. Estimated back-EMF, estimated phase

currents, and estimated rotor speed are shown in these figures. In Figure 15, actual rotor position, estimated rotor position, and their error are shown.

Figures 12(a) and 13(a) show the experimental results of the proposed ANLESO. Compared to the waveforms obtained by SMO (see part (b) in Figures 12 and 13),

FIGURE 18: Operating waveforms of estimated rotor speeds when speed is 2000 r/min and the load torque is 1 Nm: (a) obtained by the proposed ANLESO and (b) obtained by the conventional SMO.

FIGURE 19: Operating waveforms of rotor position and estimate error when speed is 2000 r/min and the load torque is 1 Nm. (a) Actual and estimated rotor position obtained by the proposed ANLESO. (b) Actual and estimated rotor position obtained by the conventional SMO. (c) Estimated error obtained by the proposed ANLESO. (d) Estimated error obtained by the conventional SMO.

the waveforms of the estimated back-EMF and current shown in Figures 12(a) and 13(a) are more accurate. The waveforms presented in Figures 14(a) and 14(b) show the differences of rotor speed estimated by two kinds of observers. The former speed waveform has less chattering. In other words, ANLESO has higher estimated precision.

Figure 15 shows the experimental results of position response. The estimated error shown in Figure 15(c) is smaller than that in Figure 15(d), which verifies the high precision of ANLESO.

Figures 16–18 show the operating waveforms when the reference speed is changed from zero to 2000 r/min and the load torque is 1 Nm. In these figures, part (a) gives the operating waveforms obtained by the proposed ANLESO and part (b) gives the operating waveforms obtained by the conventional SMO. In these figures, estimated back-EMF, estimated phase currents, and estimated rotor speed are shown. In Figure 19, actual rotor position, estimated rotor position, and their error are shown.

Figures 12–15 show the operating waveforms when the reference speed is changed from zero to 2000 r/min. Figures 12 and 13 provide the operating waveforms obtained by the proposed ANLESO. Figures 14 and 15 show the simulation waveforms obtained by the conventional SMO. In these figures, estimated back-EMF, estimated phase currents, estimated rotor speed, and actual and estimated rotor position are shown.

Figures 16–18 show the experimental results of estimated back-EMF, current and rotor speed when the rotor speed is raised to 2000 r/min. It can be seen that the waveforms in part (a) of these figures have smaller chattering and higher accuracy. In this way, the advantages of ANLESO have been verified.

As shown in Figure 19, when the rotor speed is raised to 2000 r/min, the advantages of ANLESO to estimate rotor position become more apparent than conventional SMO. The estimation error in Figure 19(c) is significantly less than that in Figure 19(d). That is to say, ANLESO has higher accuracy

and smaller chattering when being applied to estimate position than SMO.

5. Conclusions

In this paper, an adaptive nonlinear extended state observer has been designed for the sensorless control of a PMSM. The convergence of this observer has been proved by means of a Lyapunov stability analysis. An adaptive algorithm is adopted to calculate the compromised parameter of ESO in order to take both stability and steady-state error into consideration. The good performance of the proposed sensorless control system was verified by several experimental results. The results show that ANLESO has more advantages than conventional SMO. Compared to conventional SMO, ANLESO has smaller chattering, higher accuracy, and no phase delay.

In future works, we will explore the stability of the ESO under parameter uncertainties in sensorless control system.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

Acknowledgments

This project was supported by the National Natural Science Foundation of China (Grant no. 61304097) and Projects of Major International (Regional) Joint Research Program NSFC (Grant no. 61120106010).

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