Research Article

Determining the Critical Slip Surface of Three-Dimensional Soil Slopes from the Stress Fields Solved Using the Finite Element Method

Yu-chuan Yang, 1 Hui-ge Xing, 2 Xing-guo Yang, 3 and Jia-wen Zhou 1

1 State Key Laboratory of Hydraulics and Mountain River Engineering, Sichuan University, Chengdu 610065, China
2 College of Architecture and Environment, Sichuan University, Chengdu 610065, China
3 College of Water Resources and Hydropower, Sichuan University, Chengdu 610065, China

Correspondence should be addressed to Jia-wen Zhou; jwzhou@scu.edu.cn

Received 8 December 2015; Revised 5 February 2016; Accepted 7 February 2016

Academic Editor: Manuel Pastor

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The slope stability problem is an important issue for the safety of human beings and structures. The stability analysis of the three-dimensional (3D) slope is essential to prevent landslides, but the most important and difficult problem is how to determine the 3D critical slip surface with the minimum factor of safety in earth slopes. Basing on the slope stress field with the finite element method, a stability analysis method is proposed to determine the critical slip surface and the corresponding safety factor of 3D soil slopes. Spherical and ellipsoidal slipsurfaces are considered through the analysis. The moment equilibrium is used to compute the safety factor combined with the Mohr-Coulomb criteria and the limit equilibrium principle. Some assumptions are introduced to reduce the search range of center points and the radius of spheres or ellipsoids. The proposed method is validated by a classical 3D benchmark soil slope. Simulated results indicate that the safety factor of the benchmark slope is 2.14 using the spherical slip surface and 2.19 using the ellipsoidal slip surface, which is close to the results of previous methods. The simulated results indicate that the proposed method can be used for the stability analysis of a 3D soil slope.

1. Introduction

Landsides are a common worldwide geological disaster that can cause heavy casualties and huge economic losses [1–3]. The slope is not only an important environment of human existence but also an important part of engineering construction. Slope instability has been called one of the three major geological disasters, along with earthquakes and volcanoes [4]. The slope instability problem is closely associated with safety and economic benefits; as a result, slope stability analysis has a very important practical significance and economic value. A great deal of accumulated experience has been obtained on slope stability analysis, which is based on limit equilibrium theory [5–7]. Limit equilibrium method is the most popular method in assessing slope stability [8, 9]; however, this method cannot provide the relationship of internal stress and strain in rock or soil slopes, and they do not always provide unique factors of safety owing to the inherent assumptions of limit equilibrium analyses [10]. Currently, finite element method is widely used in slope stability analysis because the method can calculate the stress and strain based on the nonlinear constitutive relation of rock and soil mass [2, 11, 12]. However, this method cannot consider both the stress and moment equilibrium [13]. Although the strength reduction method can determine the failure zone and the safety factor [2, 14, 15], it is difficult to link the finite element calculation results with the traditional safety factor of the slope.

Currently, many engineers still adopt two-dimensional (2D) analysis methods due to the various limitations of the 3D slope stability analysis [6]. The three-dimensional (3D) slope is often simplified as a 2D slope problem because the above methods are not convenient for use in the direct 3D slope stability analysis [16, 17]. The most commonly used method in practical engineering to analyze the 3D slope stability is to consider each profile as a 2D slope [18]. Finally, the safety factor of the slope can be calculated by
the weighted average of each profile; however, the method often introduces some errors. At present, various existing computational methods have different accuracies in determining the critical slip surface and the corresponding safety factor [2, 19]. Cheng et al. introduced a practical way in using NURBS surface and ellipsoidal surface to simulate a three-dimensional sliding surface [20]. Ahangar-Asr et al. proposed a three-dimensional approach in conjunction with genetic algorithm (GA) to investigate the effect of earthquake force inclination on the minimum safety factor of slope and the shape and direction of the corresponding failure surface [21]. Hajiazizi and Tavana determined three-dimensional nonspherical critical slip surface in earth slopes using an optimization method to obtain the nonspherical critical slip surface, which is more consistent with the actual slip surface in nature by using the three-dimensional alternating variable local gradient [15]. According to the above references, the safety factor using 3D analysis methods is higher than that from the corresponding 2D analysis; that is, the 3D analysis provides a more economic slope design method [20].

In this paper, a 3D slope stability analysis method, combined with the finite element method and the limit equilibrium principle, is proposed to determine the critical slip surface and the corresponding safety factor of 3D soil slopes. Some assumptions are introduced to reduce the search range of the center points and the radius of spheres or ellipsoids. And the proposed method is validated by a classical benchmark slope and compared with other conventional 3D slope stability analysis methods. Some useful conclusions are presented in this paper.

2. Method

In this section, according to the rotational failure in 3D soil slopes, the stress field of the 3D soil slope is calculated using the finite element method. The safety factor of a certain slip surface can be determined by using the elastic-perfectly plastic soil model, the Mohr-Coulomb criteria, and the limit equilibrium principle. And the spherical and ellipsoidal slip surfaces are used to determine the critical slip surface.

2.1. 3D Slope Stability. Landslides (or slope failure) often pose a great threat to human beings and/or manmade structures. Figure 1(a) shows a landslide that occurred in the soil slope at the Zhaotong City, Yunnan, Southwest China, which is a typical form of rotational failure in soils. Rational assessment of the slope stability using analytical methods is very important for the hazard prevention and mitigation of landslides. According to the stability analysis of 3D soil slopes, two key issues should be determined: (a) the location of the critical slip surface and (b) the corresponding safety factor of this critical slip surface.

As shown in Figure 1(b), for the rotational sliding in soil slopes, the form of the slip surface is complicated and is influenced by the geological conditions; however, the critical slip surface can be assumed to be a spherical surface or ellipsoidal surface, which can explain most conditions of the actual landslide characteristics in soil slopes. Furthermore, this assumption can ensure the feasibility of determining the safety factor of the critical slip surface.

2.2. Stress Field of a Slope. The stress field of a slope under natural conditions can be simulated by different numerical methods. A commonly used method for determining the stress field of a slope is the finite element method [13]. Figure 2(a) shows the vertical stress distribution of a 3D soil slope solved using the finite element method. A potential slip surface is located behind the stress field of the 3D slope; this surface is the critical slip surface of the slope and must be determined. As shown in Figure 2(a), the slope elements are cut by a spherical surface or an ellipsoidal surface, with several different elements interacting with the cutting surface, and the slip surface is composed of a group of elements. Figure 2(b) shows the stress distribution of a slip surface element in one representative element.

As shown in Figure 2(b), the principal stresses $\sigma_1$, $\sigma_3$, and $\sigma_2$ of the representative element can be determined via numerical simulation, assuming that the area of the slip surface $S$ is $dA$ and the total stress on the slip surface $S$ is $p_1$:

$$p_1 = \sqrt{\sigma_1^2 + \tau_1^2}, \quad (1)$$
where $\sigma_i$ and $\tau_i$ are the normal stress and shear stress on the slip surface, respectively.

According to force equilibrium analysis, the total stress, $p_i$, can be divided into three parts along the axis directions of $X$, $Y$, and $Z$:

$$
\begin{align*}
p_i(x) &= \sigma_3 \cos \alpha, \\
p_i(y) &= \sigma_2 \cos \beta, \\
p_i(z) &= \sigma_1 \cos \gamma,
\end{align*}
$$

where $\alpha$, $\beta$, and $\gamma$ are the angles between the normal direction of the slip surface $S$ and the axis directions of $X$, $Y$, and $Z$, respectively. The relationship between these three angles is given by

$$
(\cos \alpha)^2 + (\cos \beta)^2 + (\cos \gamma)^2 = 1.
$$

The normal stress and total stress on the slip surface can be determined as follows:

$$
\begin{align*}
\sigma_i &= p_i(x) \cos \alpha + p_i(y) \cos \beta + p_i(z) \cos \gamma \\
&= \sigma_3 (\cos \alpha)^2 + \sigma_2 (\cos \beta)^2 + \sigma_1 (\cos \gamma)^2, \\
p_i &= \sqrt{\sigma_3^2 (\cos \alpha)^2 + \sigma_2^2 (\cos \beta)^2 + \sigma_1^2 (\cos \gamma)^2}.
\end{align*}
$$

The shear stress on the slip surface can be computed as follows:

$$
\tau_i = \sqrt{p_i^2 - \sigma_i^2}.
$$

The shear resistance on the slip surface $S$ can be determined according to the Mohr-Coulomb criterion:

$$
\tau_i^f = c_i + \sigma_i \tan \varphi_i,
$$

where $c_i$ and $\varphi_i$ are the cohesion and friction angle of the soil, respectively.

If the geometric information and the stress field of one representative element are known, then the shear stress and shear resistance on this slip surface element can be determined.

2.3. Safety Factor of a Certain Slip Surface. For the stability analysis of 3D soil slopes, the determination of the 3D critical slip surface from a series of potential slip surfaces in global optimization is a difficult task, thus making the solution time tremendously long [19]. Currently, spherical shapes are commonly used for the slip surfaces in the 3D slope stability analysis because of the relative lack of difficulty in performing global optimization. However, the nonspherical slip surface is the most general shape that can be considered in the 3D slope stability analysis process [24]. In this paper, both spherical and ellipsoidal (nonspherical) shapes of slip surfaces are considered for the stability analysis of 3D soil slopes. Some assumptions are introduced during the determination of the safety factor for a certain slip surface, and details are shown in Figure 3.

As shown in Figure 3, the sliding directions of the slip surface elements are all parallel to the $XY$ plane. If the determination of the safety factor of a slip surface is regarded as a two-dimensional problem and the total number of slip surface elements is $n$, then the safety factor ($F_s$) of the slip surface can be computed as follows:

$$
F_s = \frac{\tau^f}{\tau} = \frac{\sum_{i=1}^{n} \tau^f_i}{\sum_{i=1}^{n} \tau_i} = \frac{\sum_{i=1}^{n} (c_i + \sigma_i \tan \varphi_i)}{\sum_{i=1}^{n} \tau_i},
$$

where $\tau^f$ and $\tau$ are the total shear resistance and shear stress on the slip surface, respectively, and $c$ and $\varphi$ are the cohesion and friction angle of the slope soil, respectively.

However, the safety factor under 3D conditions is difficult to calculate using (7) because the directions of the shear
4 Mathematical Problems in Engineering

Figure 3: Some assumptions for the slip surface of 3D soil slopes: (a) spherical slip surface and (b) ellipsoidal slip surface.

stress $\tau_i$ and the normal stress $\sigma_i$ are not consistent for each slip surface element. The geometric features of a sphere or an ellipsoid have the same characteristics: a fixed center, where the normal stress $\sigma_i$ for each slip element is pointing to this fixed center and perpendicular to the slip surface. Furthermore, it is assumed that shear stresses are directed consistently with the overall sliding direction, which is all parallel to the XY plane. Next, the safety factor is defined in terms of moment rather than in the terms of shear stress $[10]$, which can be calculated by integrating all of the slip elements; subsequently, the safety factor of a determined slip surface can be calculated as follows:

$$ F_s = \frac{M_R}{M_s} = \frac{\int_S (c I_i + \sigma_i \tan \phi_i) \, ds}{\int_S \tau_i l_i \, ds}. \quad (8) $$

where $M_R$ is the resisting moment, which is related with the shear resistance on the slip surface; $M_s$ is the slip moment, which is related with the shear stress on the slip surface; and $l_i$ is the vertical distance from the center of a spherical or ellipsoid to the surface of each element. If the slip surface is a spherical style, then $l_i$ is equal to the radius of the sphere; however, if the slip surface is an ellipsoidal style, then $l_i$ is related to the size parameters of the ellipsoid.

2.4. Determination of the Critical Slip Surface. During the process of determining the critical slip surface, the number of calculation steps is high because of the numerous potential slip surfaces; as a result, some assumptions and optimization algorithms should be introduced. The spherical slip surface can be described with the following equation:

$$ (x - x_0)^2 + (y - y_0)^2 + (z - z_0)^2 = r^2, \quad (9) $$

where $(x_0, y_0, z_0)$ are the coordinate values of center point of a sphere and $r$ is the radius of the sphere.

However, for the ellipsoidal slip surface, the description equation can expressed as follows:

$$ \frac{(x - x_0)^2}{a^2} + \frac{(y - y_0)^2}{b^2} + \frac{(z - z_0)^2}{c^2} = 1, \quad (10) $$

where $(x_0, y_0, z_0)$ are the coordinate values of the center point for an ellipsoidal shape and $a$, $b$, and $c$ are the radii in $X$, $Y$, and $Z$ directions, respectively.

According to (9), there are four uncertain parameters $(x_0, y_0, z_0, r)$ to determine for the spherical slip surfaces. The soil slope is cut by several different spheres and forms several slip surfaces, which have the corresponding safety factor. The slip surface with the minimum safety factor is the critical one. Figure 4 shows a 3D slope cut via a sphere from a different perspective.

As shown in Figure 4, for the spherical slip surface, fortunately, the sphere rotated in any direction has no effect on the shape of slip surface. However, for the ellipsoidal slip surface, nine uncertain parameters should be determined: $x_0$, $y_0$, $z_0$, $a$, $b$, $c$, $\alpha$, $\beta$, and $\gamma$, where $\alpha$, $\beta$, and $\gamma$ are the rotation angles of the ellipsoid surface around the axis directions $X$, $Y$, and $Z$, respectively. The increasing number of uncertain parameters will lead to an exponential increase in the computational burden. Figure 5 shows a 3D slope cut by an ellipsoid from different perspectives.

To reduce the number of calculations, the following assumptions are introduced. First, the semimajor axis of the ellipsoidal is parallel to the slope (as shown in Figure 5(a), where OP is assumed parallel to MN) and there are no rotations around the directions X and Y. As a result, only one rotation angle exists, where $\alpha$ and $\beta$ are equal to 0 and $\gamma$ is equal to the inclination of slope. With this assumption, the number of uncertain parameters is reduced to six. Furthermore, it is assumed that a relationship exists among the radius parameters of the ellipsoid; here, the assumption for the relationship among $a$, $b$, and $c$ presented by Zhao et al.
Figure 4: A 3D slope is cut by a sphere: (a) side view and (b) top view.

Figure 5: A 3D slope is cut by an ellipsoidal: (a) side view and (b) top view.

is used that parameter \( a \) is the maximum value and the value of \( b \) is less than \( c \) [25].

Furthermore, determining the appropriate center coordinate and search range of the sphere or ellipsoid embedded in the three-dimensional slope is a problem [15]. To reduce the number of calculations, the center points are limited in one plane [13, 26], which is the same as the two-dimensional problem. According to the symmetry soil slopes, the center points are located in the vertical plane across midpoint \( A \) of the slope (details shown in Figure 6).

As shown in Figure 6, the center points are located in the rectangle \( ABCD \), and the coordinate \( Z \) is a constant. In this manner, the appropriate search domain can effectively reduce the number of calculations. For a determined geometry of 3D soil slopes, the search range of the center points can be further reduced. The optimization for the search range of the center points can simplify the calculation and improve the computing speed [15]. Figure 7 shows the further optimization assumption for the search range of the center points.

As shown in Figure 7, point \( R \) is the midpoint of the straight line \( AM' \), and two auxiliary lines \( RQ'/RQ \) are added, which are perpendicular to \( M'EM'/AM' \), respectively. Regarding to the slope geometry and the potential slip surface, the search range of the center points can be greatly reduced into the range of \( QQ'SS' \). For the soil slopes, when the sliding surface is tangent to the plane \( MEF \) (as shown in Figure 6), the slip surface cuts a small part of the 3D slope, which cannot be the most dangerous slip surface. While the depth of the tangent plane in the slope is greater than \( MR \) with the slip surface, the resistance moment of the slip surface will be relatively large [8]. The radius of the spheres or ellipsoids...
can be limited to a small range [4]. Furthermore, to address the very large number of calculations for the 3D slope, some optimization algorithms can be introduced to improve the computational efficiency [15].

2.5. Calculation Process. The calculation process for determining the critical slip surface of 3D soil slopes from stress field using the finite element method is shown as follows:

1. According to a special 3D soil slope, first, the numerical model of this slope should be established, and then, the finite element method is used to calculate the stress field of this slope by means of gravity loading; here, the Mohr-Coulomb constitutive model for the soils is used during the numerical simulation process.

2. After the completion of numerical simulation, the computing nodes, elements, mechanical parameters, and stress field of the slope are exported to four data files (nodes.txt, elements.txt, parameters.txt, and stress.txt); the four files can be loaded by the VBA (Visual Basic for Applications) programming language.

3. After the main program has loaded the four exported files, that is, nodes.txt, elements.txt, parameters.txt, and stress.txt, to set the search range of the center points, the rotation angle of the ellipsoid, the range of values of the radius, and other initial conditions, including the boundary condition of the slope, can be automatically detected and the shear strength parameters of each element can be found in the file of parameters.txt.

4. After several random slip surfaces are generated under some certain optimization principles, the safety factor of each slip surface can be determined using (8), where the minimum value is the safety factor of the soil slope and the corresponding slip surface is the critical one.

5. After exporting the geometry information of the critical slip surface, the stress field on the critical slip surface can be visualized using various drawing software packages, such as Surfer or Tecplot.

### Table 1: Mechanical parameters of the benchmark soil slope.

<table>
<thead>
<tr>
<th>Soil Layer</th>
<th>$E$ (MPa)</th>
<th>$\nu$</th>
<th>$\gamma$ (g/cm$^3$)</th>
<th>$c$ (kPa)</th>
<th>$\phi$ ($)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Layer 1</td>
<td>500</td>
<td>0.30</td>
<td>1.92</td>
<td>29</td>
<td>20</td>
</tr>
<tr>
<td>Layer 2</td>
<td>200</td>
<td>0.33</td>
<td>1.92</td>
<td>10</td>
<td>0</td>
</tr>
<tr>
<td>Layer 3</td>
<td>500</td>
<td>0.30</td>
<td>1.92</td>
<td>29</td>
<td>20</td>
</tr>
</tbody>
</table>

Note. $E$ is the elastic modulus; $\nu$ is Poisson’s ratio; $\gamma$ is the density; $c$ is the cohesion; and $\phi$ is the friction angle.
meshes are used the elastic-perfectly plastic properties. The secondary calculation process of the slope stress field is carried out by using the Mohr-Coulomb model; this stress field is the input data for slope stability analysis. After the completion of numerical simulation, the computing nodes, elements, mechanical parameters, and stress field of the slope are exported to four data files by using the self-designed secondary development codes for the ABAQUS. Figure 9 shows the stress distribution characteristics of the benchmark slope.

From Figure 9, the benchmark slope is mainly under compressive stress with a low level; because the slope height is at a small scale, the maximum compressive stress of the benchmark slope is in the range of 0 to 0.45 MPa. Furthermore, small tensile stress exists at the slope surface, and stress dislocation appears around weak layer 2. As the potential slip surface cannot be directly determined from the stress field of the 3D slope, some indirect methods should be introduced to determine the critical slip surface and its corresponding safety factor. The following stability analysis results are performed based on these stress field results for the benchmark slope.

3.2. Spherical Slip Surface. First, a potential spherical slip surface is assumed to exist in the 3D benchmark soil slope, and the center of these potential spherical slip surfaces are located in the middle of the width direction, as shown in Figure 10(a). The benchmark slope is cut by these potential spherical slip surfaces.

According to the geometric information of the benchmark slope, the precise search range $QQ'SS'$ for the center point of potential spheres can be determined, as shown in Figure 10(b). The details of the search range of the center points can be gained from Figure 10(b); that is, the center point must be located in the range $QQ'SS'$. As a result, the corresponding radius range of the spheres is from 18.3 m to 29.3 m.

Once the search range of the center points and radius for the spherical slip surfaces are determined, several random
The search of the spherical slip surface is more complicated than the search of the spherical slip surface; for each spherical slip surface, the geometric information and stress distribution of the surface can be computed and the corresponding safety factor can be determined, where the minimum safety factor is the critical slip surface. Figure 11(a) shows the normal stress distribution on the critical slip surface, which is in the range of 6.0 kPa to 145 kPa. The normal stress on the slip surface is related with the stress field of the soil slope and can be used to compute the shear resistance of the slip surface. Figure 11(b) shows the safety factor results of the critical slip surface. From Figure 11(b), the center point of the critical slip surface is "6.1 m, 19.3 m, and 25.0 m" and the radius is 24.5 m. The slip moment and resisting moment are 401.2 kN⋅m and 187.9 kN⋅m, respectively; the corresponding safety factor is 2.135. Comparison of the presented method with previous methods is presented in Table 2 (previous methods are from [8, 17, 22]).

As shown in Table 2, although there is little difference in the shape of spherical slip surface, the safety factor of benchmark soil slope using the presented method is close to those of other methods. The simulated results indicate that the proposed method can be used for the spherical stability analysis of a 3D soil slope.

### Ellipsoidal Slip Surface

The search of the ellipsoidal slip surface is more complicated than the search of the spherical slip surface. Some assumptions are introduced to reduce the number of calculations; Figure 12(a) shows the 3D soil slope cut by an ellipsoid, where the center of these potential ellipsoidal slip surfaces is located at the middle in the width direction.

As shown in Figure 12(a), no rotation angle exists around the axis directions X and Y, but the rotation angle around the axis direction Z is equal to the inclination of the soil slope and the rotation angles (α, β, γ) are "27°, 0°, and 0°", respectively. The initial value of (a, b, c) is set as (20 m, 15 m, and 15 m), respectively; these values are no larger than 25 m. The search range of the center points is the same as the spherical slip surface.

Once the search range of the center points and radius for the ellipsoidal slip surfaces are determined, several random spheres are generated. The slope is cut by these ellipsoids, and the safety factor of these ellipsoidal slip surfaces can be computed, where the minimum one is the critical slip surface. Figure 12(b) shows the safety factor results of the critical slip surface. As shown in Figure 12(b), the center point of the critical slip surface is "8.0 m, 15.1 m, and 25.0 m" and the radius values (a, b, c) are "24.4 m, 11.7 m, and 20.7 m," respectively. The slip moment and resisting moment are 189.1 kN⋅m and 414.6 kN⋅m, respectively; the corresponding safety factor is 2.193. Comparison of the presented method with previous methods is presented in Table 3 (improved simplified Janbu's method [23]).

As presented in Table 3, the safety factor determined using the proposed method is 2.193, which is larger than that of Zhang's result and is also larger than that of the spherical slip surface because the proposed method meets all forces and moment equilibrium conditions based on slope stress field. However, from all of other results and this paper's results, we found that the safety factor of this benchmark slope is in the range of 2.0 to 2.2. The simulated results indicate that the presented method can suit not only the stability analysis of spherical slip surface but also the ellipsoidal slip surface.
Table 3: Comparison of the stability results of the ellipsoidal slip surface for different methods.

<table>
<thead>
<tr>
<th>Methods</th>
<th>Safety factor</th>
<th>Radius (m)</th>
<th>Center point (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zhang's result [23]</td>
<td>2.096</td>
<td>$a = 46, b = c = 24.4$</td>
<td>(0.0, 36.6, 27.4)</td>
</tr>
<tr>
<td>Presented method</td>
<td>2.193</td>
<td>$a = 24.4, b = 11.7, c = 20.7$</td>
<td>(8.0, 15.1, 25.0)</td>
</tr>
</tbody>
</table>

Figure 12: Stability analysis result of the benchmark slope using an ellipsoidal slip surface: (a) slope cut by a sphere and (b) safety factor result of the critical slip surface.

4. Discussion and Conclusion

In geotechnical engineering, the slope stability problem is an important issue for construction safety and long-term operation. Because many theoretical issues remain not fully resolved, the mechanics of the slope instability should continue to be studied [27–29]. The finite element method is the most widely used method for slope stability analysis [4]. However, the critical slip surface and the corresponding safety factor cannot be determined directly based on the stress field and displacement field of the slope; thus, an indirect method should be introduced to solve this problem, such as the strength reduction method [13, 28]. However, this method requires iterative calculations and limits the node unbalanced force, which inevitably results in the calculating efficiency not high. In this paper, a stability analysis method was proposed to determine the critical slip surface of 3D soils slopes from the stress field with the finite element method. Spherical and ellipsoidal slip surfaces are considered for the 3D soil slopes. And the safety factor of the slip surface is computed based on Mohr-Coulomb criteria and limit equilibrium principle.

A classical benchmark soil slope is used to verify the proposed stability analysis method for 3D soil slopes. The simulated results indicate that, for the spherical slip surface, the slip moment and resisting moment are 187.9 kN·m and 401.2 kN·m, respectively, and the corresponding safety factor is 2.135, which is close to the value of the previous three different methods considered [8, 17, 22]. For the ellipsoidal slip surface, the slip moment and resisting moment are 189.1 kN·m and 414.6 kN·m, respectively; the corresponding safety factor is 2.193, which is close to Zhang's result [23]. From all of the previous results and this paper's results, the safety factor of this benchmark slope is in the range of 2.0 to 2.2.

The proposed method can resolve some limitations of the existing 3D methods that are based on the limit equilibrium approach. For the limit equilibrium approach, the method cannot consider the internal stress field of the slope, and many assumptions are necessary considered for the slices of slope soils. Besides, the traditional finite element method cannot directly determine the critical slip surface of slope and calculate the corresponding safety factor. The organic combination of the FEM with the limit equilibrium principle can fully account for soil deformation and the influence of elastoplastic stress adjustment on the slope stability. That means the proposed method can determine the critical slip surface via mathematical programming using the stress field of the slope as the input. Based on the FEM and limit equilibrium principle, the slope transfers the element interaction force by itself. When a critical state is reached, the element nodes appear failure. The proposed method can not only determine the location of critical slip surface but also can calculate the corresponding safety factor of the 3D soil slopes. Furthermore, it makes good use of geometric combination to reduce the search range during the calculation process.

Regarding the proposed method for the stability analysis of a 3D soil slope, some reasonable assumptions were introduced to reduce the search range of the center points and radius. In addition, the definition of the safety factor was relatively unique by using the resisting moment and the slip moment. Combined with the assumption of the sliding
direction, the safety factor is very convenient for the integral solution in the sliding surface. Therefore the proposed method can provide some realistic guidance for the 3D symmetric soil slope stability.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

Acknowledgments

The authors gratefully acknowledge the support of the National Natural Science Foundation of China (51209156), Youth Science and Technology Fund of Sichuan Province (2016JQ0011), and the Science Foundation for Excellent Youth Scholars of Sichuan University (2013SCU04A07).

References


