Research Article

A New Approach to Weapon-Target Assignment in Cooperative Air Combat

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A new approach to solving weapon-target assignment (WTA) problem is proposed in this paper. Firstly, relative superiority that lays the foundation for assignment is calculated based on the combat power energy of the fighters. Based on the relative superiority, WTA problem is formulated. Afterwards, a hybrid algorithm consisting of improved artificial fish swarm algorithm (AFSA) and improved harmony search (HS) is introduced and furthermore applied to solve the assignment formulation. Finally, the proposed approach is validated by eight representative benchmark functions and two concrete cooperative air combat examples. The results show that the approach proposed in this paper achieves good performances in solving WTA problem in cooperative air combat.

1. Introduction

Weapon-target assignment (WTA) refers to an assignment of defensive weapons to engage or counter identified threats. The primary concern is minimizing the total expected survivability of the targets [1, 2]. Weapons are assigned to threats based on the detection outcomes within previous stages. Considering the short time of air combat, the problem must be solved as close to real time as possible. Another characteristic is quality of the derived solution, which causes critical effects on the following combat deployment [3].

WTA is regarded as a crucial part in operation; therefore the achievements on that are rich. In the matter of problem formulation, multiple factors such as relative distance, relative angle, and relative velocity are taken into consideration. In domain of algorithms, several sophisticated search and heuristic algorithms have been proposed, such as genetic algorithms [4–7], simulated annealing [8], discrete particle swarm optimizations [9–12], permutation and tabu search heuristics [13], and other algorithms [14–16].

Concerned with the characteristics and developing tendency about air combat, an approach to WTA in cooperative air combat is proposed in this paper. Within the approach,

relative superiority between fighters and targets, acting as the foundation of the formulation, is calculated in terms of combat power potential, and a hybrid algorithm combined with improved artificial fish swarm algorithm with improved harmony search for solving the formulation is introduced.

The concept of combat power potential is firstly introduced by Zhou et al. [17]. As described in [17], air combat space can be seen as a potential consisting of infinite points and each point is under effect by fighters. The effect, generated by fighters and equipment carried by them, is quantitatively defined as potential energy called combat power potential energy. Combat power potential energy reflects the impact on each point inside the air combat space by fighters.

The artificial fish swarm algorithm (AFSA) simulating the behavior of a fish inside water was proposed by Li et al. [18] and has already been applied in engineering contexts [19–24]. The main artificial fish behaviors are random, chasing, swarming, and searching, which allows the algorithm to act better in global searching but poor in local searching.

Harmony search, mimicking the improvisation process of music players, is originated by Geem et al. [25]. The HS performs excellently in quality of the solutions but with low search speed and is strongly dependent on initial solution.

This paper is organized as follows: In Section 2, the formulation of WTA is introduced. The design of hybrid algorithm is studied in Section 3. Section 4 presents the results of simulation. Section 5 concludes the paperpagebreak

2. WTA Problem Formulation

2.1. Analysis on Relative Superiority. Superiority relation acts as the critical ingredient in WTA formulation. In this paper, superiority relation is formulated in accordance with the descending velocity of combat power potential energy possessed by one side towards the other side.

2.1.1. Combat Power Potential Energy Model of Fighter. Due to the limitation on pages, combat power potential energy of fighter can be calculated by model of which in [26].

2.1.2. Calculation on Descending Velocity. We get to know from the potential theory that potential energy will be descending while distance is getting larger. As a kind of potential, combat power potential has the same characteristics, which means combat power potential energy generated by fighters descends with more restriction, such as distance limits and angle limits. For calculating descending velocity, gradient is introduced in the paper. Assuming a function described as $f = f(P)$, $P = (x, y, z)$, then gradient of function f in point P can be defined as

$$\text{grad } f(P) = \nabla f = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z} \right). \quad (1)$$

It is known from [26] that combat power potential energy of fighter is a function with regard to coordinates of fighters and targets (x, y, z, x_T, y_T, z_T) . Calculate the gradient of e depicted in [26] on x_T, y_T, z_T and then we can get

$$\begin{aligned} \frac{\partial e(x_T, y_T, z_T)}{\partial x_T} &= \frac{\partial e_D(x_T, y_T, z_T)}{\partial x_T} (\omega_1 e_W(x_T, y_T, z_T) \\ &\quad + \omega_2 e_E(x_T, y_T, z_T)) + e_D(x_T, y_T, z_T) \\ &\quad \cdot \left(\omega_1 \frac{\partial e_W(x_T, y_T, z_T)}{\partial x_T} + \omega_2 \frac{\partial e_E(x_T, y_T, z_T)}{\partial x_T} \right), \\ \frac{\partial e(x_T, y_T, z_T)}{\partial y_T} &= \frac{\partial e_D(x_T, y_T, z_T)}{\partial y_T} (\omega_1 e_W(x_T, y_T, z_T) \\ &\quad + \omega_2 e_E(x_T, y_T, z_T)) + e_D(x_T, y_T, z_T) \\ &\quad \cdot \left(\omega_1 \frac{\partial e_W(x_T, y_T, z_T)}{\partial y_T} + \omega_2 \frac{\partial e_E(x_T, y_T, z_T)}{\partial y_T} \right), \\ \frac{\partial e(x_T, y_T, z_T)}{\partial z_T} &= \frac{\partial e_D(x_T, y_T, z_T)}{\partial z_T} (\omega_1 e_W(x_T, y_T, z_T) \\ &\quad + \omega_2 e_E(x_T, y_T, z_T)) + e_D(x_T, y_T, z_T) \\ &\quad \cdot \left(\omega_1 \frac{\partial e_W(x_T, y_T, z_T)}{\partial z_T} + \omega_2 \frac{\partial e_E(x_T, y_T, z_T)}{\partial z_T} \right). \end{aligned} \quad (2)$$

Take $\partial e(x_T, y_T, z_T)/\partial x_T$, for instance; through further derivation, we will obtain

$$\begin{aligned} &\frac{\partial e(x_T, y_T, z_T)}{\partial x_T} \\ &= \frac{\partial (\ln(1 + A_{DR}(x_T, y_T, z_T) + A_{DIR}(x_T, y_T, z_T)))}{\partial x_T} \\ &\quad \cdot (\omega_1 \ln(1 + A_M(x_T, y_T, z_T)) \\ &\quad + \omega_2 \ln(1 + A_{DIS}(x_T, y_T, z_T))) \\ &\quad + \ln(1 + A_{DR}(x_T, y_T, z_T) + A_{DIR}(x_T, y_T, z_T)) \\ &\quad \cdot \left(\omega_1 \frac{\partial (\ln(1 + A_M(x_T, y_T, z_T)))}{\partial x_T} \right. \\ &\quad \left. + \omega_2 \frac{\partial (\ln(1 + A_{DIS}(x_T, y_T, z_T)))}{\partial x_T} \right). \end{aligned} \quad (3)$$

For losing the burden of calculation, $A_{DR}(x_T, y_T, z_T)$, $A_{DIR}(x_T, y_T, z_T)$, $A_M(x_T, y_T, z_T)$, $A_{DIS}(x_T, y_T, z_T)$ are simplified as $A_{DR}(x_T, y_T, z_T) = C_1/r(x_T, y_T, z_T)$, $A_{DIR}(x_T, y_T, z_T) = C_2/r(x_T, y_T, z_T)$, $A_M(x_T, y_T, z_T) = C_3/r(x_T, y_T, z_T)$, $A_{DIS}(x_T, y_T, z_T) = C_4/r(x_T, y_T, z_T)$, where $r(x_T, y_T, z_T) = \sqrt{(x_A - x_T)^2 + (y_A - y_T)^2 + (z_A - z_T)^2}$. Substitute simplified $A_{DR}(x_T, y_T, z_T)$, $A_{DIR}(x_T, y_T, z_T)$, $A_M(x_T, y_T, z_T)$, $A_{DIS}(x_T, y_T, z_T)$ into (3); we will derive

$$\begin{aligned} &\frac{\partial e(x_T, y_T, z_T)}{\partial x_T} \\ &= \frac{\partial (\ln(1 + C_1/r(x_T, y_T, z_T) + C_2/r(x_T, y_T, z_T)))}{\partial x_T} \\ &\quad \cdot \left(\omega_1 \ln \left(1 + \frac{C_3}{r(x_T, y_T, z_T)} \right) + \omega_2 \right. \\ &\quad \cdot \ln \left(1 + \frac{C_4}{r(x_T, y_T, z_T)} \right) \left. + \ln \left(1 + \frac{C_1}{r(x_T, y_T, z_T)} \right) \right. \\ &\quad \left. + \frac{C_2}{r(x_T, y_T, z_T)} \right) \\ &\quad \cdot \left(\omega_1 \frac{\partial (\ln(1 + C_3/r(x_T, y_T, z_T)))}{\partial x_T} \right. \\ &\quad \left. + \omega_2 \frac{\partial (\ln(1 + C_4/r(x_T, y_T, z_T)))}{\partial x_T} \right) \end{aligned}$$

$$\begin{aligned}
&= \frac{\partial (\ln(1 + C_1/r(x_T, y_T, z_T) + C_2/r(x_T, y_T, z_T)))}{\partial r(x_T, y_T, z_T)} \\
&\cdot \frac{\partial r(x_T, y_T, z_T)}{\partial x_T} \cdot \left(\omega_1 \ln \left(1 + \frac{C_3}{r(x_T, y_T, z_T)} \right) \right. \\
&+ \omega_2 \ln \left(1 + \frac{C_4}{r(x_T, y_T, z_T)} \right) \Bigg) + \ln \left(1 \right. \\
&+ \frac{C_1}{r(x_T, y_T, z_T)} + \frac{C_2}{r(x_T, y_T, z_T)} \Bigg) \cdot \left(\omega_1 \right. \\
&\cdot \frac{\partial (\ln(1 + C_3/r(x_T, y_T, z_T)))}{\partial r(x_T, y_T, z_T)} \cdot \frac{\partial r(x_T, y_T, z_T)}{\partial x_T} \\
&+ \omega_2 \cdot \frac{\partial (\ln(1 + C_4/r(x_T, y_T, z_T)))}{\partial r(x_T, y_T, z_T)} \\
&\cdot \frac{\partial r(x_T, y_T, z_T)}{\partial x_T} \Bigg) = \left(\frac{r(x_T, y_T, z_T)}{r(x_T, y_T, z_T) + C_1 + C_2} \right. \\
&\cdot \left. - \frac{C_1 + C_2}{r^2(x_T, y_T, z_T)} \cdot \frac{2(x_A - x_T)}{2r(x_T, y_T, z_T)} \cdot -1 \right) \cdot \left(\omega_1 \right. \\
&\cdot \ln \left(1 + \frac{C_3}{r(x_T, y_T, z_T)} \right) + \omega_2 \\
&\cdot \ln \left(1 + \frac{C_4}{r(x_T, y_T, z_T)} \right) \Bigg) + \ln \left(1 + \frac{C_1}{r(x_T, y_T, z_T)} \right. \\
&+ \frac{C_2}{r(x_T, y_T, z_T)} \Bigg) \cdot \left(\omega_1 \cdot \left(\frac{r(x_T, y_T, z_T)}{r(x_T, y_T, z_T) + C_3} \right. \right. \\
&\cdot \left. \left. - \frac{C_3}{r^2(x_T, y_T, z_T)} \cdot \frac{2(x_A - x_T)}{2r(x_T, y_T, z_T)} \cdot -1 \right) + \omega_2 \right. \\
&\cdot \left(\frac{r(x_T, y_T, z_T)}{r(x_T, y_T, z_T) + C_4} \cdot - \frac{C_4}{r^2(x_T, y_T, z_T)} \right. \\
&\cdot \left. \left. \frac{2(x_A - x_T)}{2r(x_T, y_T, z_T)} \cdot -1 \right) \right) \\
&= \frac{(x_A - x_T) \cdot (C_1 + C_2)}{(r(x_T, y_T, z_T) + C_1 + C_2) \cdot r^2(x_T, y_T, z_T)} \cdot \left(\omega_1 \right. \\
&\cdot \ln \left(1 + \frac{C_3}{r(x_T, y_T, z_T)} \right) + \omega_2 \\
&\cdot \ln \left(1 + \frac{C_4}{r(x_T, y_T, z_T)} \right) \Bigg) + \ln \left(1 \right. \\
&+ \frac{C_1 + C_2}{r(x_T, y_T, z_T)} \Bigg) \cdot \left(\omega_1 \right.
\end{aligned}$$

$$\begin{aligned}
&\cdot \frac{(x_A - x_T) \cdot C_3}{(r(x_T, y_T, z_T) + C_3) \cdot r^2(x_T, y_T, z_T)} + \omega_2 \\
&\cdot \left(\frac{(x_A - x_T) \cdot C_4}{(r(x_T, y_T, z_T) + C_4) \cdot r^2(x_T, y_T, z_T)} \right) \Bigg).
\end{aligned}$$

(4)

$\partial e(x_T, y_T, z_T)/\partial y_T$ and $\partial e(x_T, y_T, z_T)/\partial z_T$ are yielded in the same way as follows:

$$\begin{aligned}
&\frac{\partial e(x_T, y_T, z_T)}{\partial y_T} \\
&= \frac{(y_A - y_T) \cdot (C_1 + C_2)}{(r(x_T, y_T, z_T) + C_1 + C_2) \cdot r^2(x_T, y_T, z_T)} \cdot \left(\omega_1 \right. \\
&\cdot \ln \left(1 + \frac{C_3}{r(x_T, y_T, z_T)} \right) + \omega_2 \\
&\cdot \ln \left(1 + \frac{C_4}{r(x_T, y_T, z_T)} \right) \Bigg) + \ln \left(1 \right. \\
&+ \frac{C_1 + C_2}{r(x_T, y_T, z_T)} \Bigg) \cdot \left(\omega_1 \right. \\
&\cdot \frac{(y_A - y_T) \cdot C_3}{(r(x_T, y_T, z_T) + C_3) \cdot r^2(x_T, y_T, z_T)} + \omega_2 \\
&\cdot \left(\frac{(y_A - y_T) \cdot C_4}{(r(x_T, y_T, z_T) + C_4) \cdot r^2(x_T, y_T, z_T)} \right) \Bigg),
\end{aligned}$$

(5)

$$\begin{aligned}
&\frac{\partial e(x_T, y_T, z_T)}{\partial z_T} \\
&= \frac{(z_A - z_T) \cdot (C_1 + C_2)}{(r(x_T, y_T, z_T) + C_1 + C_2) \cdot r^2(x_T, y_T, z_T)} \cdot \left(\omega_1 \right. \\
&\cdot \ln \left(1 + \frac{C_3}{r(x_T, y_T, z_T)} \right) \\
&+ \omega_2 \ln \left(1 + \frac{C_4}{r(x_T, y_T, z_T)} \right) \Bigg) + \ln \left(1 \right. \\
&+ \frac{C_1 + C_2}{r(x_T, y_T, z_T)} \Bigg) \cdot \left(\omega_1 \right. \\
&\cdot \frac{(z_A - z_T) \cdot C_3}{(r(x_T, y_T, z_T) + C_3) \cdot r^2(x_T, y_T, z_T)} + \omega_2 \\
&\cdot \left(\frac{(z_A - z_T) \cdot C_4}{(r(x_T, y_T, z_T) + C_4) \cdot r^2(x_T, y_T, z_T)} \right) \Bigg).
\end{aligned}$$

Descending velocity of fighter A in direction of target T is got in the light of definition of gradient:

$$v_{d(x_A, y_A, z_A)}(x_T, y_T, z_T) = |\text{grad}(e(x_T, y_T, z_T))| = \sqrt{\left(\frac{\partial e(x_T, y_T, z_T)}{\partial x_T}\right)^2 + \left(\frac{\partial e(x_T, y_T, z_T)}{\partial y_T}\right)^2 + \left(\frac{\partial e(x_T, y_T, z_T)}{\partial z_T}\right)^2}. \quad (6)$$

Similarly, descending velocity of target T in direction of fighter A is given as

$$v_{d(x_T, y_T, z_T)}(x_A, y_A, z_A) = |\text{grad}(e(x_A, y_A, z_A))| = \sqrt{\left(\frac{\partial e(x_A, y_A, z_A)}{\partial x_A}\right)^2 + \left(\frac{\partial e(x_A, y_A, z_A)}{\partial y_A}\right)^2 + \left(\frac{\partial e(x_A, y_A, z_A)}{\partial z_A}\right)^2}. \quad (7)$$

2.1.3. Calculation on Relative Superiority. Calculation on relative superiority of fighter i with respect to target j is expressed as

$$p_{ij} = \frac{v_{d(x_{A_i}, y_{A_i}, z_{A_i})}(x_{T_j}, y_{T_j}, z_{T_j})}{v_{d(x_{A_i}, y_{A_i}, z_{A_i})}(x_{T_j}, y_{T_j}, z_{T_j}) + v_{d(x_{T_j}, y_{T_j}, z_{T_j})}(x_{A_i}, y_{A_i}, z_{A_i})}, \quad (8)$$

where $v_{d(x_{A_i}, y_{A_i}, z_{A_i})}(x_{T_j}, y_{T_j}, z_{T_j})$ is the descending velocity of fighter i in direction to location of target j and $v_{d(x_{T_j}, y_{T_j}, z_{T_j})}(x_{A_i}, y_{A_i}, z_{A_i})$ is the descending velocity of target j in direction to location of fighter i .

2.2. WTA Formulation. In the paper, the problem is formulated as a combinatorial optimization problem, with the objective of minimizing the total lethality of the targets. The fundamental problem variable is relative superiority p_{ij} .

Consider the assignment problem of m fighters to n targets: let $p_{ij} \in [0, 1]$ be the relative superiority, where $i \in \{1, 2, \dots, m\}$ and $j \in \{1, 2, \dots, n\}$. The WTA is formulated as follows:

$$\begin{aligned} J = \min & \sum_{j=1}^n \left(\prod_{i=1}^m (1 - p_{ij})^{x_{ij}} \right) \\ \text{s.t.} & \sum_{i=1}^m x_{ij} \geq 1, \\ & \sum_{j=1}^n x_{ij} \leq 1, \end{aligned} \quad (9)$$

where x_{ij} is the decision value indicating if fighter i is assigned to target j ; $x_{ij} = 1$ if fighter i is assigned to target j and $x_{ij} = 0$ if fighter i is not assigned to target j .

In the above formulation, we minimize the sum of the weighted cumulative probabilities of threat lethality while

ensuring that all constraints are satisfied. Two constraints, respectively, denote that each target must be assigned by one fighter and each fighter can be assigned to one target at most.

3. A Hybrid Algorithm for the Problem

3.1. Improvements on AFSA. To improve the performance of the algorithm, several modifications were introduced into the AFSA, including initialization, visual and movement strategy, and leap behavior. Concrete implementations are presented below.

3.1.1. Initialization. Initial solution causes crucial influences on convergence performance of the algorithm. The initial solution is randomly generated in the most existed study, by which it is difficult to get solution of high quality. Therefore a hybrid initialization method involving chaos, information entropy, and opposition-based learning methods is proposed and described in Figure 1.

Assume that there are p artificial fish in the swarm, each of which has q variables. X_{rs} denotes the variable s within fish r , $r \in \{1, \dots, p\}$, $s \in \{1, \dots, q\}$. The pseudocode for two algorithms in Figure 1 is described in Algorithms 1 and 2.

3.1.2. Pseudo-Parallel Evolution. In the late period of search, artificial fish will move more slowly and be misled to local optimums. A pseudo-parallel evolution strategy dividing the artificial fish swarm into multiple subswarms is introduced for solving the problem. Each subswarm executes search for optimum independently and exchanges the optimal solution with others at every iteration to maintain the search space and prevent prematurity.

3.1.3. Artificial Fish Moving Strategy. To improve the search ability of the artificial fish, a moving strategy combining

FIGURE 1: Flow of initialization.

maintaining the self-advantage with absorbing the advantage from others is proposed below:

$$X_r^{\text{gen}+1} = \frac{\text{gen}}{\max \text{gen}} X_r^{\text{gen}} + \frac{\max \text{gen} - \text{gen}}{\max \text{gen}} (X_u^{\text{gen}} - X_r^{\text{gen}}), \quad (10)$$

where gen is the current iteration, $\max \text{gen}$ is the maximum iteration, $X_r^{\text{gen}+1}$, X_r^{gen} are the position of artificial fish r at iteration $\text{gen} + 1$ and gen , respectively, and X_u^{gen} is the position of artificial fish u at gen iteration. The first part, $(\text{gen}/\max \text{gen})X_r^{\text{gen}}$, describes artificial fish keeping the self-superiority; the second part inspired by neighborhood search strategy, $((\max \text{gen} - \text{gen})/\max \text{gen})(X_u^{\text{gen}} - X_r^{\text{gen}})$, indicates the absorbance of advantage from another artificial fish u within visual range.

3.1.4. Self-Adaptive Visual Procedure. Visual, which has been deeply studied, determines the convergence speed and accuracy of AFSA. The modifications on visual have been

proposed by many researches, as given in (11)~(13). Reference [19] proposed an improved visual formulation:

$$\text{visual}^{\text{gen}} = \text{visual}^{\text{gen}-1} \cdot (L_{\text{low}} + (\text{rand} \cdot (L_{\text{high}} - L_{\text{low}}))), \quad (11)$$

where $\text{visual}^{\text{gen}}$ and $\text{visual}^{\text{gen}-1}$ stand for the visual at current iteration gen and previous iteration $\text{gen} - 1$. L_{high} and L_{low} represent the upper and lower bounds of the visual, respectively.

The model utilizes a random number to control the visual change and to ensure the overall trend getting lower, whereas, due to stochastic factors existing during the evolution, it is incapable of precise adjustment to the visual.

Another modification on visual is presented in the following equation [20]:

$$\text{visual}^{\text{gen}} = \text{visual}^{\text{gen}-1} \cdot \frac{|y_{\text{best}} - \bar{y}|}{y_{\text{best}}}, \quad (12)$$

where y_{best} is the global best solution by estimation and $\bar{y}$ is the mean solution.

```

(1) Initialize parameter: Set the maximum chaotic iteration
    number ingen
(2) for  $r = 1 : p$  do
(3) for  $s = 1 : q$  do
(4) for  $o = 1 : ingen$  do
(5)  $ch_{os} = \sin(\pi \cdot ch_{o-1,s})$  % Update the chaotic factor
(6) end for
(7)  $X_{os} = X_{\min,s} + ch_{os}(X_{\max,s} - X_{\min,s})$  % Generate initial
    chaotic solution
(8)  $OX_{os} = X_{\min,s} + X_{\max,s} - X_{rs}$  % Generate initial
    opposition-based learning solution
(9) end for
(10) end for

```

ALGORITHM 1: Initialization based on logistic chaos and opposition-based learning [27, 28].

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(1) Set the critical entropy  $H_0$ 
(2)  $H = 0$ 
(3) while  $H < H_0$ 
(4)   for  $r = 1 : p$ 
(5)     for  $t = r + 1 : p$ 
(6)       for  $s = 1 : q$ 
(7)          $X_{ts} = X_{\min,s} + \text{rand} \cdot (X_{\max,s} - X_{\min,s})$ 
(8)          $P_{rt}^s = 1 - |X_{rs} - X_{ts}| / (A_s^{\max} - A_s^{\min})$  % Difference ratio
            Between  $X_{rs}$  and  $X_{ts}$ ,  $A_s^{\max}$  and  $A_s^{\min}$  are the maximum
            and minimum value of the variable  $s$  respectively
(9)          $H_s = \sum_{r=1}^p \sum_{t=2}^p (-P_{rt}^s \log P_{rt}^s)$  % Entropy of variable  $s$  in
            artificial fish swarm
(10)         $H = (1/q) \sum_{s=1}^q H_s$  % Entropy of the whole swarm
(11)      end for
(12)    end for
(13)  end for
(14) end while

```

ALGORITHM 2: Initialization based on information entropy [29].

In accordance with (12), the mean solution is getting closer to the global best solution by estimation. During the approach to the optimal solution, difference between the current mean solution and the optimal one decreases, as well as the visual scope. However, y_{best} is hard to estimate, which easily causes the algorithm to fall into local optimal or poor performance in convergence.

Reference [21] proposed another kind of improvement on visual:

$$\text{visual}^{\text{gen}} = \begin{cases} \left(\beta - \frac{\text{gen}}{N} \right) \cdot \text{visual}^{\text{fixed}} & \\ \alpha \cdot \text{visual}^{\text{gen}-1}, & \alpha = \left(\frac{\text{visual}^N}{\text{visual}^1} \right)^{1/N}, \end{cases} \quad (13)$$

where N is the maximum iteration, visual^1 is the initial value, visual^N is the previously set value at the last iteration, $\text{visual}^{\text{fixed}}$ is a fixed value, and β is a constant number.

In initial iterations, the visual varies in accordance with the upper formulation for ensuring good performance in convergence speed and global searching, thereafter changing by means of the next one for better convergence accuracy. But there are two deficiencies that existed; the switch condition from the upper formulation to the one below is not quite clear and the visual at the last iteration is not easy to obtain.

The main purpose is to ensure the artificial fish searching with larger visual within initial iterations and with smaller visual afterwards, although the modified means are quite different such as (11) to (13). Whereas the above improvements on visual are insufficient for the research on the algorithm falling into the local optimum, therefore a modified visual model concerned with iteration and convergence speed is constructed as follows:

$$\text{visual}_r^{\text{gen}} = \begin{cases} \max \left\{ \text{visual} \cdot |D_r(\text{gen}) - D_r(\text{gen} - 1)| \cdot e^{-30(\text{gen}/\max \text{gen})^S}, 1 \right\}, & D_r(\text{gen}) - D_r(\text{gen} - 1) \neq 0, \\ \text{visual} \cdot |D_r(\text{gen} - \text{gen}') - D_r(\text{gen} - \text{gen}' - 1)| \cdot e^{-30(\text{gen}/\max \text{gen})^S}, & D_r(\text{gen}) - D_r(\text{gen} - 1) = 0, \end{cases} \quad (14)$$

where gen' measures the iterations at which the optimal solution stays unchanged, visual is the initial visual, $D_r(\text{gen}_{\text{last}})$ is the solution at the last iteration before $D_r(\text{gen}) - D_r(\text{gen} - 1) = 0$, $D_r(\text{gen}_{\text{last}} - 1)$ is the solution at the previous iteration before gen_{last} , and S is a constant number that could be 1, 3, 5, 10.

From (14) we can see that adjustment in visual changes one dimension at least and gets smaller as $D_r(\text{gen}) - D_r(\text{gen} - 1)$ decreases, which helps improve the accuracy of the solutions. When $D_r(\text{gen}) - D_r(\text{gen} - 1) = 0$, the visual obtained by (14) will get larger, by which artificial fish are capable of escaping from local optimal regions.

3.1.5. Improvements on Leap Behavior. For preventing the artificial fish from converging to local optimal solutions, leap behavior forcing the artificial fish to change its location is adopted in certain references [22, 23]. In this paper, artificial fish executes leap behavior when the optimal solution stands still after one iteration. Meanwhile, it is thought that the higher the number of iterations at which optimal solution stagnates is, the higher the extent the optimal solution varies and the higher the probability of leap behavior execution is. Accordingly, improvements on leap behavior probability and leap behavior strategy are designed as follows.

The leap behavior is modified as outlined in (15):

$$X_r^{\text{gen}+1} = X_r^{\text{gen}} + \text{visual}_r^{\text{gen}} \cdot \lambda \cdot \text{rand}, \quad (15)$$

where λ is a bool vector; the quantity of 1 in vector is obtained from

$$\theta = \max \left\{ 1, q - q \cdot \text{round} \left(e^{-30(\text{gen}'/\text{gen})^s} \cdot \frac{D_r(\text{gen} - \text{gen}')}{D_r(\text{gen})} \right) \right\}. \quad (16)$$

Equation (16) makes it certain that one dimension at least, q dimension at most in location of artificial fish r , changes by leap behavior at each iteration. The bigger $D_r(\text{gen} - \text{gen}')/D_r(\text{gen})$ and gen'/gen are, the more dimension changes. By this way, leap behavior is able to adjust the location of artificial fish dynamically and to achieve the goal of avoiding premature convergence.

3.2. Improvement on HS. In this article, improvements on HS contains two domains: harmony memory consideration rate and new harmony generating strategy.

3.2.1. Improvements on Harmony Memory Consideration Rate. Modifications on harmony memory consideration rate have been studied in many researches [30, 31]. Through the reference, it can be concluded that harmony memory consideration rate should be given a small value to increase the diversity of the harmony memory and global search

when solutions differ greatly. On the other hand, when the solutions are relatively resembled, harmony memory consideration rate should be raised for performing search more accurately and reducing the time for searching. In this paper, it is considered that iteration has effect on harmony memory consideration rate as solution does; particularly harmony memory consideration rate is supposed to increase gradually at final iterations for acting better in global search. The harmony memory consideration rate is formulated from the perspectives of current iteration and deviations between harmony vectors as follows:

$$\text{HMCR}(\text{gen}) = \frac{E_{\min}(\text{gen})}{E_{\max}(\text{gen})} e^{\text{gen}/\max \text{gen}-1}, \quad (17)$$

where $E_{\min}(\text{gen})$, $E_{\max}(\text{gen})$, respectively, represent the best and worst solution in harmony memory at iteration gen . The harmony memory consideration rate in (17) utilizes dynamic mechanism to select the harmony vector under various circumstances. The larger $E_{\min}(\text{gen})/E_{\max}(\text{gen})$ is, the smaller the difference among the harmony vectors in harmony memory is, which indicates that $\text{HMCR}(\text{gen})$ becomes larger to converge to the optimum fastly. Likewise, the larger gen is, the larger $\text{HMCR}(\text{gen})$ is, and the algorithm is able to have a faster convergence to the optimum.

3.2.2. New Harmony Improvisation. New harmony improvisation deciding general performance in optimization is also seen as the key point in modifications on HS. A new method for harmony improvisation in terms of learning strategy is defined in this paper, which is described as follows:

$$u_s^{\text{gen}} = \begin{cases} u_{r_1,s}^{\text{gen}} + \min\{c_1, c_2\} \cdot (u_{\text{best},s}^{\text{gen}} - u_{r_1,s}^{\text{gen}}) + \max\{c_1, c_2\} \cdot (u_{r_2,s}^{\text{gen}} - u_{r_1,s}^{\text{gen}}), & D_{\text{best}}(\text{gen}) - D_{\text{best}}(\text{gen}-1) = 0, \\ u_{r_1,s}^{\text{gen}} + \max\{c_1, c_2\} \cdot (u_{\text{best},s}^{\text{gen}} - u_{r_1,s}^{\text{gen}}) + \min\{c_1, c_2\} \cdot (u_{r_2,s}^{\text{gen}} - u_{r_1,s}^{\text{gen}}), & D_{\text{best}}(\text{gen}) - D_{\text{best}}(\text{gen}-1) \neq 0, \end{cases} \quad (18)$$

where u_s^{gen} is the decision variable s in harmony vector generated at iteration gen , $u_{r_1,s}^{\text{gen}}$, $u_{r_2,s}^{\text{gen}}$, $u_{\text{best},s}^{\text{gen}}$ are the decision variables s in harmony vectors r_1 , r_2 and the optimal harmony vector in harmony memory generated at iteration gen , and c_1 , c_2 are learning coefficients, $0 \leq c_1, c_2 \leq 1$, $c_1 \neq c_2$.

The bigger one between c_1 and c_2 is selected to make sure that the harmony is affected by the neighborhood solution inside the harmony memory and avoid prematurity when $D_{\text{best}}(\text{gen}) - D_{\text{best}}(\text{gen}-1) = 0$. Otherwise, the harmony improvisation is more influenced by the optimal solution, which helps in converging to optimum more quickly.

3.3. Switch Condition

3.3.1. Switch Condition Analysis. Switch condition acting as a key part of the hybrid algorithm causes a great influence on speed and accuracy of convergence. Switch condition is discussed by two aspects as switching iteration and individual standard error of artificial fish.

(1) *Switching Iteration.* Switching iteration is to make the hybrid algorithm switch from improved AFSA to improved HS at a certain iteration, which is obtained by multiple concrete experiments.

(2) *Individual Standard Error of Artificial Fish.* This factor reflects the deviation among artificial fish in the swarm. It should be switched to the HS for the following search while the individual standard error of artificial fish gets smaller, which means the search space gets smaller. The model of individual standard error of artificial fish, with regard to location and fitness value, is proposed as follows.

The standard error of location on artificial fish lse is calculated by

$$lse = \sqrt{\frac{1}{q-1} \sum_{s=1}^q lse_s^2},$$

$$lse_s^2 = \frac{1}{p-1} \sum_{r=1}^p (X_{rs} - \bar{X}_s)^2, \quad (19)$$

where $\bar{X}_s$ is the average location of all artificial fish in dimension s . The artificial fish are of high probability to gather in local optimal region while each fish gets closer, as well as lse being smaller.

The standard error of fitness value on artificial fish fse is calculated by

$$fse = \sqrt{\frac{\sum_{r=1}^p (D_r(\text{gen}) - \bar{D}(\text{gen}))^2}{p-1}}, \quad (20)$$

where $\bar{D}(\text{gen})$ is the average fitness value. Likewise, the artificial fish seems to get trapped in the local optimum area while fitness value of each fish is resembled, as well as fse being smaller.

From the information mentioned above, the individual standard error of artificial fish is derived by

$$\begin{aligned} se &= \varphi_1 \cdot lse + \varphi_2 \cdot fse \\ \text{s.t. } 0 &\leq \varphi_1, \varphi_2 \leq 1 \\ \varphi_1 + \varphi_2 &= 1, \end{aligned} \quad (21)$$

where φ_1, φ_2 , respectively, represent the coefficients about lse and fse . The switch to improved HS should be executed for global optimum if se is smaller than the presented value se_{def} , which means the stand error of fitness value and location fluctuate to a smaller extent; therefore the solution is weak.

3.3.2. Design for Switch Step. For the sake of fast convergence and quality of solutions, it is ruled in this paper that the switch is executed only if any condition is satisfied. Due to the different performances of the algorithms when facing various problems or benchmark functions, it is also regulated that the individual standard error of artificial fish is seen as the prior factor, and the switch flow is given in Figure 2.

It can be seen from Figure 2 that individual standard error of artificial fish is investigated at first; switch is executed if satisfied; otherwise checking whether the algorithm is qualified to switch from the perspective of switching iteration, the switch is carried on if satisfied, or else the algorithm runs back to the improved artificial fish swarm algorithm.

3.4. Flow for Hybrid Algorithm. The concrete flow for the proposed hybrid algorithm is depicted in Figure 3.

4. Simulation Results

4.1. Verification Tests by Benchmark Functions. The algorithms are always tested by benchmark functions. For thoroughly validating the performances of the proposed IAFSA-HIS, other three algorithms including IABHS, IBAFSA, and GDHS are introduced for comparison. Main properties of the

FIGURE 2: Switch flow for algorithm.

selected benchmark functions used in the experiments are shown in Table 1.

Parameters are set as follows: $\text{ingen} = 100$, $H_0 = 0.3$, $S = 5$, $\text{visual} = 1.5$, $\gamma_1 = 0.3$, $\gamma_2 = 0.5$, $c_1 = 0.6$, $c_2 = 0.4$, $\varphi_1 = 0.6$, $\varphi_2 = 0.4$, $\text{max gen} = 100000$, and $n = 30$; for other parameters, refer to [24, 30, 32].

The algorithms were run 100 times independently to catch their stochastic properties and the results are depicted in Table 2 and Figures 4–11.

The parameters Best, Mean, Worst, and Std.dev are the best, mean, worst, and stand error of the optimum on average after 100 running times, where Mean reflects the precision of the results obtained by the algorithms within certain iterations and Std.dev reflects the robustness and stability of the algorithms.

As seen from Table 2 and Figures 4–11, the advantages in terms of best, median, worst, mean, and standard error of IAFSA-HIS are outstanding among the four algorithms in general. Particularly, IAFSA-IHS achieves the theoretical optimum while others fail still the termination in f_6 and f_7 . However, the proposed algorithm performs relatively poor with regard to f_1, f_4, f_5 , especially for f_1 . Compared with GDHS obtaining the theoretical optimum within fewer iterations in f_1 , IAFSA-IHS fails to get the satisfying solution, which seems to fall into the prematurity as IABHS and IBAFSA do.

It can be concluded that IAFSA-IHS exactly performs better on robustness, convergence speed, and precision with the improvements mentioned above synthetically. Taking f_6 , for instance, as a multimodal function, there exist a lot of local optima surrounding the global optimum which easily misguides the algorithm to stay in the local optimum. For solving the problem, GDHS sets HMCR, PAR, bw in dynamical mode, IBAFSA decodes the artificial fish into binary, sets the trial point, and reinitializes the artificial fish

TABLE 1: Benchmark functions.

Function	Equation	Range	Optimum	Property
Sphere	$f_1(x) = \sum_{i=1}^n x_i^2$	$[-100, 100]$	0	Unimodal
Quartic	$f_2(x) = \sum_{i=1}^n ix_i^4 + \text{random}[0, 1]$	$[-1.28, 1.28]$	0	Unimodal
Duadric	$f_3(x) = \sum_{i=1}^n \left(\sum_{j=1}^i x_j \right)^2$	$[-100, 100]$	0	Unimodal
Rosenbrock	$f_4(x) = \sum_{i=1}^{n-1} \left[(x_i - 1)^2 + 100(x_{i+1} - x_i^2)^2 \right]$	$[-30, 30]$	0	Unimodal
Schwefel	$f_5(x) = -\sum_{i=1}^n x_i \sin\left(\sqrt{ x_i }\right)$	$[-500, 500]$	-12569.5	Multimodal
Rastrigin	$f_6(x) = \sum_{i=1}^n \left[x_i^2 - 10(2\pi x_i) + 10 \right]$	$[-5.12, 5.12]$	0	Multimodal
Griewank	$f_7(x) = \frac{1}{4000} \sum_{i=1}^n x_i^2 - \prod_{i=1}^n \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1$	$[-600, 600]$	0	Multimodal
Ackley	$f_8(x) = -20e^{-0.2\sqrt{\frac{1}{n}\sum_{i=1}^n x_i^2}} - e^{\sum_{i=1}^n \cos(2\pi x_i)/n} + e + 20$	$[-30, 30]$	0	Multimodal

FIGURE 3: Flow for the proposed hybrid algorithm.

TABLE 2: Comparison of results with other algorithms.

	IAFSA-IHS	IBAFSA	IABHS	GDHS
f_1				
Best	$3.0303e - 218$	$3.4848e - 100$	$3.8552e - 60$	0
Mean	$3.7514e - 220$	$4.3574e - 99$	$6.8125e - 59$	0
Worst	$9.3558e - 221$	$6.1893e - 97$	$7.2759e - 57$	0
Std.dev	$7.2377e - 218$	$3.5238e - 99$	$8.7153e - 59$	0
f_2				
Best	$4.3659e - 3$	$5.7852e - 2$	$1.5798e - 4$	$8.9654e - 3$
Mean	$5.9283e - 2$	$6.0237e - 2$	$2.0721e - 2$	$9.3571e - 2$
Worst	$1.1135e - 1$	$1.3145e - 1$	$5.3492e - 2$	$7.5883e - 2$
Std.dev	$6.3844e - 2$	$9.3561e - 2$	$8.9443e - 3$	$1.0184e - 2$
f_3				
Best	$6.901e - 3$	$1.8312e + 3$	$5.7163e - 4$	$3.3694e - 2$
Mean	$5.4431e - 2$	$7.5403e + 3$	$6.7303e - 2$	$5.2391e - 1$
Worst	$3.2967e - 1$	$6.5727e + 4$	$8.1835e - 2$	$2.4749e + 0$
Std.dev	$2.3617e - 2$	$5.4329e + 3$	$4.3516e - 3$	$4.7161e - 2$
f_4				
Best	$1.1364e + 1$	$3.5801e + 1$	$1.0075e + 1$	$6.4625e + 1$
Mean	$9.5879e + 1$	$6.0574e + 1$	$9.5855e + 1$	$8.5942e + 1$
Worst	$1.2841e + 2$	$2.9714e + 1$	$3.3575e + 1$	$1.5399e + 2$
Std.dev	$9.9836e + 1$	$3.4769e + 1$	$1.4848e + 1$	$7.6935e + 1$
f_5				
Best	$-1.1821e + 4$	$-1.1108e + 4$	$-1.1753e + 4$	$-1.2024e + 4$
Mean	$-1.1028e + 4$	$-9.9931e + 3$	$-1.0387e + 4$	$-1.1569e + 4$
Worst	$-1.0254e + 4$	$-9.8301e + 3$	$-9.4539e + 3$	$-1.0965e + 4$
Std.dev	$-1.0879e + 4$	$-1.0256e + 4$	$-1.0024e + 4$	$-1.2569e + 4$
f_6				
Best	0	$3.1827e - 4$	$1.9847e - 3$	$4.2084e - 4$
Mean	0	$9.5648e - 4$	$9.0955e - 3$	$1.5682e - 3$
Worst	0	$8.1815e - 3$	$6.5276e - 1$	$3.3524e - 2$
Std.dev	0	$3.1348e - 4$	$6.4596e - 3$	$1.2563e - 3$
f_7				
Best	0	$6.0477e - 10$	$3.2291e - 14$	$7.7708e - 16$
Mean	0	$7.5628e - 9$	$9.2486e - 13$	$6.2967e - 14$
Worst	0	$9.2466e - 8$	$9.7123e - 12$	$9.1222e - 13$
Std.dev	0	$1.3132e - 9$	$2.2486e - 13$	$1.5422e - 14$
f_8				
Best	$4.0107e - 16$	$3.5687e - 15$	$3.0026e - 13$	$1.2627e - 15$
Mean	$7.5975e - 16$	$7.0145e - 15$	$5.2435e - 13$	$3.3275e - 15$
Worst	$3.2354e - 15$	$9.6461e - 14$	$6.4564e - 12$	$9.5619e - 15$
Std.dev	$5.5484e - 16$	$5.5686e - 15$	$1.3967e - 13$	$2.0131e - 15$

FIGURE 4: Sphere.

FIGURE 7: Rosenbrock.

FIGURE 5: Quartic.

FIGURE 8: Schwefel.

FIGURE 6: Duadric.

FIGURE 9: Rastrigin.

swarm regularly, and IABHS introduces the improvisation strategies with consideration of individual as well as dimension and self-adaptively adjusts HMCR, PAR, bw . All of those improvements are aimed at strengthening the convergence

speed and accuracy, just as IAFSA-IHS does by means of the proposed modification in the paper. From the analysis of the result, these improvements indeed have effects as supposed.

FIGURE 10: Griewank.

FIGURE 11: Ackley.

FIGURE 12: Air combat situation.

4.2. Simulation of WTA Problems

4.2.1. Example 1. There is red formation consisting of eight fighters confronting blue formation including six targets. Through calculation by (1)~(8), situation information referring to [17, 33] on both sides is given in Table 3 and Figures 12–14.

Descending velocity of each side with respect to the other side is obtained by (6) and (7) and shown in Tables 4 and 5.

FIGURE 13: Distribution of combat power energy possessed by both formations in vertical plane.

FIGURE 14: Distribution of combat power energy possessed by both formations in horizontal plane.

Relative superiority of red formation with regard to the blue one, p_{ij} , $1 \leq i \leq 8$, $1 \leq j \leq 6$, is derived by (8) and is given in Table 6.

F_i , $1 \leq i \leq 8$, denotes fighter i . T_j , $1 \leq j \leq 6$, is target j . $\text{ingen} = 100$, $H_0 = 0.3$, $S = 5$, $\text{visual} = 8$, $\text{step} = 4$, $c_1 = 0.6$, $c_2 = 0.4$, $\varphi_1 = 0.6$, $\varphi_2 = 0.4$, and $\text{max gen} = 200$; other parameters are set similarly as in verification tests.

Compared with three algorithms mentioned in verification tests, the optimization process containing four algorithms and the final assignment solution is shown in Figure 15 and Table 7.

It is obviously observed from Figure 15 and Table 7 that solution obtained by IAFSA-IHS gets the lowest fitness value but in slower convergence speed. By comparison, the results derived by GDHS, IBAFSA, and IABHS achieve higher fitness value. GDHS only acts better than IABHS, and the result got by IBAFSA is similar to the one got by IAFSA-IHS. It is concluded that the proposed IAFSA-IHS outperforms the others in solving the example.

TABLE 3: Situation information on both sides.

	X/km	Y/km	Z/km	$V_x/(\text{km/h})$	$V_y/(\text{km/h})$	$V_z/(\text{km/h})$	C_1	C_2	C_3	C_4
Information on red formation										
1	40	79	5	662	662	0				
2	44	76	6	662	662	0				
3	48	76	5	662	662	0				
4	50	70	5	662	662	0	361.65	43.59	1973.9	225.82
5	54	66	6	662	662	0				
6	58	66	5	662	662	0				
7	59	60	5	662	662	0				
8	62	56	6	662	662	0				
Information on blue formation										
1	130	170	8	-641	-641	-320				
2	140	160	7	-641	-641	-320				
3	145	155	8	-641	-641	-320	154.99	43.59	1789.7	451.64
4	150	146	8	-641	-641	-320				
5	160	140	7	-641	-641	-320				
6	165	130	8	-641	-641	-320				

TABLE 4: Descending velocity of red formation with regard to blue formation.

	F1	F2	F3	F4	F5	F6	F7	F8
T1	0.0094	0.0094	0.0098	0.0094	0.0093	0.0095	0.0090	0.0088
T2	0.0093	0.0094	0.0098	0.0095	0.0094	0.0098	0.0093	0.0091
T3	0.0092	0.0093	0.0097	0.0094	0.0095	0.0098	0.0093	0.0092
T4	0.0093	0.0095	0.0099	0.0097	0.0098	0.0102	0.0097	0.0096
T5	0.0086	0.0088	0.0092	0.0091	0.0092	0.0096	0.0093	0.0092
T6	0.0085	0.0088	0.0093	0.0091	0.0093	0.0098	0.0095	0.0095

TABLE 5: Descending velocity of blue formation with regard to red formation.

	F1	F2	F3	F4	F5	F6	F7	F8
T1	0.0078	0.0079	0.0082	0.0078	0.0077	0.0080	0.0075	0.0073
T2	0.0077	0.0078	0.0082	0.0079	0.0079	0.0082	0.0077	0.0076
T3	0.0076	0.0078	0.0081	0.0079	0.0079	0.0082	0.0078	0.0077
T4	0.0077	0.0079	0.0083	0.0081	0.0081	0.0085	0.0081	0.0080
T5	0.0071	0.0073	0.0077	0.0075	0.0077	0.0080	0.0077	0.0077
T6	0.0071	0.0073	0.0077	0.0076	0.0078	0.0082	0.0079	0.0079

TABLE 6: Relative superiority of red formation with regard to the blue one.

	F1	F2	F3	F4	F5	F6	F7	F8
T1	0.5455	0.5454	0.5449	0.5455	0.5457	0.5452	0.5461	0.5464
T2	0.5456	0.5454	0.5448	0.5454	0.5454	0.5449	0.5456	0.5459
T3	0.5458	0.5455	0.5449	0.5454	0.5454	0.5448	0.5455	0.5457
T4	0.5457	0.5453	0.5447	0.5450	0.5449	0.5443	0.5450	0.5451
T5	0.5468	0.5464	0.5457	0.5460	0.5457	0.5451	0.5457	0.5457
T6	0.5469	0.5464	0.5457	0.5458	0.5455	0.5449	0.5453	0.5453

TABLE 7: Results of four algorithms.

	F1	F2	F3	F4	F5	F6	F7	F8	Fitness value
GDHS	T6	T1	T3	T4	T5	T2	T4	T1	2.2308
IABHS	T1	T1	T6	T4	T5	T3	T4	T2	2.2315
IBAFSA	T6	T3	T5	T2	T1	T2	T1	T4	2.2299
IAFSA-IHS	T6	T2	T3	T5	T4	T3	T1	T4	2.2298

TABLE 8: Situation information on both sides.

	X/km	Y/km	Z/km	Vx/(km/h)	Vy/(km/h)	Vz/(km/h)	C ₁	C ₂	C ₃
Information on red formation									
1	50	80	5	828	552	138			
2	51	76	6	828	552	138			
3	52	72	5	828	552	138			
4	53	69	6	828	552	138	361.65	43.59	1973.9
5	56	65	6	552	828	138			
6	60	64	5	552	828	138			
7	63	63	6	552	828	138			
8	68	62	5	552	828	138			
Information on blue formation									
1	155	143	7	-402	-768	-283			
2	150	144	7	-402	-768	-283			
3	140	146	8	-402	-768	-283	154.99	43.59	1789.7
4	135	150	7	-768	-402	-283			
5	132	160	8	-768	-402	-283			
6	130	170	8	-768	-402	-283

FIGURE 15: Optimization figure containing four algorithms.

FIGURE 16: Air combat situation.

4.2.2. *Example 2.* To test its performance widely, another situation is chosen in simulation; the situation information is shown in Table 8 and Figures 16–18.

Descending velocity of each side with respect to the other side is gained by (6) and (7) and shown in Tables 9 and 10.

FIGURE 17: Distribution of combat power energy possessed by both formations in vertical plane.

FIGURE 18: Distribution of combat power energy possessed by both formations in horizontal plane.

TABLE 9: Descending velocity of red formation with regard to blue formation.

	F1	F2	F3	F4	F5	F6	F7	F8
T1	0.0104	0.0100	0.0097	0.0095	0.0093	0.0095	0.0096	0.0098
T2	0.0113	0.0110	0.0106	0.0104	0.0102	0.0104	0.0106	0.0109
T3	0.0121	0.0117	0.0114	0.0112	0.0111	0.0114	0.0116	0.0120
T4	0.0118	0.0115	0.0112	0.0110	0.0110	0.0113	0.0115	0.0120
T5	0.0106	0.0104	0.0102	0.0101	0.0100	0.0104	0.0106	0.0111
T6	0.0101	0.0099	0.0097	0.0096	0.0096	0.0099	0.0102	0.0106

TABLE 10: Descending velocity of blue formation with regard to red formation.

	F1	F2	F3	F4	F5	F6	F7	F8
T1	0.0087	0.0084	0.0081	0.0079	0.0078	0.0079	0.0089	0.0082
T2	0.0095	0.0092	0.0089	0.0087	0.0085	0.0088	0.0089	0.0092
T3	0.0102	0.0099	0.0096	0.0094	0.0093	0.0096	0.0098	0.0101
T4	0.0100	0.0097	0.0095	0.0093	0.0092	0.0095	0.0097	0.0101
T5	0.0089	0.0087	0.0086	0.0084	0.0084	0.0087	0.0089	0.0093
T6	0.0084	0.0083	0.0081	0.0080	0.0080	0.0083	0.0085	0.0089

TABLE 11: Relative superiority of red formation with regard to the blue one.

	F1	F2	F3	F4	F5	F6	F7	F8
T1	0.5440	0.5445	0.5450	0.5453	0.5456	0.5453	0.5452	0.5448
T2	0.5428	0.5432	0.5437	0.5440	0.5442	0.5439	0.5437	0.5433
T3	0.5419	0.5423	0.5427	0.5429	0.5431	0.5427	0.5425	0.5420
T4	0.5422	0.5425	0.5429	0.5431	0.5432	0.5428	0.5425	0.5420
T5	0.5437	0.5439	0.5442	0.5444	0.5445	0.5440	0.5437	0.5431
T6	0.5444	0.5447	0.5449	0.5451	0.5451	0.5446	0.5443	0.5437

TABLE 12: Results of four algorithms.

	F1	F2	F3	F4	F5	F6	F7	F8	Fitness value
GDHS	T6	T5	T1	T2	T4	T1	0	T3	2.4894
IABHS	T6	T4	T2	T2	T5	T1	T3	T5	2.2415
IBAFSA	T3	T5	T6	T6	T4	T1	T2	T1	2.2413
IAFSA-IHS	T6	T5	T4	T6	T2	T1	T3	T5	2.2408

Relative superiority of red formation with regard to the blue one, p_{ij} , $1 \leq i \leq 8$, $1 \leq j \leq 6$, is derived by (8) and is given in Table 11.

Parameters remain unchanged as in Example 1, and the result can be seen in Figure 19 and Table 12.

From Figure 19 and Table 12, it is concluded that IAFSA-IHS finds the best solution in highest convergence speed among the four algorithms. Besides, the initial solutions generated by IAFSA-IHS are far better than the ones of others. Among the other three algorithms, IBAFSA performs better in fitness value. IABHS presents a slightly inferior performance than the ones above. GDHS gets the worst results in fitness value as well as in convergence speed. From the example mentioned above, the proposed IAFSA-IHS

FIGURE 19: Optimization figure containing four algorithms.

achieves a general better performance in both simulations that indeed demonstrates the effectiveness of IAFSA-IHS for WTA.

5. Conclusion and Future Works

A new approach to weapon-target assignment in cooperative air combat is proposed. Firstly, assignment model is constructed based on the concept of combat power potential. On the other hand, a hybrid algorithm combining improved AFSA with improved HS is proposed. Finally, the algorithm is tested by eight benchmark functions and two concrete WTA problems in air combat; the results validate the superiority of the proposed approach.

In the future, we will pay more attention to details about the combat power potential energy model of fighter in order to accurately reflect the practical cooperative air combat.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this article.

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