Research Article

Theoretical Investigation of Oxazine 170 Perchlorate Doped Polymeric Optical Fiber Amplifier

Piotr Miluski,1 Marcin Kochanowicz,1 Jacek Źmójda,1 and Dominik Dorosz2

1Department of Power Engineering, Photonics and Lighting Technology, Białystok University of Technology, Białystok, Poland
2Department of Silicate Chemistry, AGH University of Science and Technology, Kraków, Poland

Correspondence should be addressed to Piotr Miluski; p.miluski@pb.edu.pl

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Optical signal amplification in the waveguiding structure of optical fibers can be used for optical telecommunication systems and new light sources constructions. Organic dyes doped materials are interesting for new applications in polymeric optical fibers technology due to their benefits (efficient fluorescence, high absorption cross section, and easy processing). This article presents a numerical simulation of gain in poly(methyl methacrylate) optical fiber doped by Oxazine 170 Perchlorate. The calculated gain characteristic for the used dye molar concentration (0.2⋅10^{-6}–1.4⋅10^{-6}) and pump power (1–10 kW) is presented. The fabricated fluorescent polymeric optical fiber is also shown. The presented analysis can be used for optical amplifier construction based on dye-doped polymeric optical fiber (POF).

1. Introduction

Organic electronics have become an alternative for inorganic based devices. The high quantum efficiency of organic fluorophores is useful in numerous optical applications: sensors, light sources, lasers, and amplifiers [1–10]. The high quantum yield of fluorescence was reported for laser organic dyes (xanthenes, oxazines, 7-aminocoumarins) [11]. Their structural properties allow incorporation directly into poly(methyl methacrylate) (PMMA) which is commonly used in polymer optical fiber technology. The spectroscopic properties of 7-(diethylamino)coumarin, Oxazine 170 Perchlorate, and codoped Perylene-Rhodamine 6G fibers were previously investigated [12–15]. Optical transmission can be easily obtained for PMMA attenuation optical windows of 465, 525, 565, and 650 nm. The lowest attenuation of the PMMA core POF is approximately 100 dB/km [16–18]. Much higher losses are observed for the infrared radiation spectrum. The high numerical aperture, the good optical transmission in the visible spectrum range, and the excellent mechanical and processing properties yield numerous constructions of optical fiber amplifiers and lasers based on PMMA matrix. Solvent-free doping technique is especially desired in the polymeric fiber drawing technology. The impurities and solvent residues cause technological problems during the drawing process of polymeric fibers [16]. There are known luminescent organic and inorganic complexes in polymeric optical fiber technology. However, the absorption and emission cross sections of organic dyes are typically significantly higher than those observed in lanthanide ions, which are well known for their narrow absorption bands. Although the absorption cross section luminescence efficiency of lanthanides can be improved using organic ligands and energy transfer (antenna effect), the chelate molecules luminescence is quenched by PMMA nonradiative transitions and efficient luminescence can be observed only for triplet state europium (Eu3+) and terbium (Tb3+) complexes [19–26]. In such circumstances, organic dyes are frequently used in polymer optical fiber technology. The step and gradient refractive index profile and Rhodamine B, Rhodamine 6G, and Oxazine 4 optical amplifiers were presented [27–30]. The possibility of light amplification in organic dyes doped fibers is especially important in terms of compact devices fabrication as the absorption cross section is much higher than in rare earth ions. A recently developed semiconductor laser source in the visible range spectrum offers new applications in short VIS spectrum range for...
optical signal amplification. The oxazines seem to be excellent candidates for this region due to the high absorption and emission cross section and direct PMMA doping possibility. Oxazine chromophore can be obtained by substitution of the xanthenes central carbon atom by nitrogen which, as a consequence, shifts the luminescence spectrum to a longer wavelength (ca. 80 nm) [11]. The article presents a theoretical investigation of gain in polymeric optical fibers doped by Oxazine 170.

2. Theoretical Background

The fluorescence of organic dyes is widely used in laser technology of wavelength converters (typically in the solvent-dye mixture). New amplification possibilities appearing since fluorescent dyes were successfully used for polymeric optical fiber core doping (step or gradient refractive index profile). This idea can be easily applied to rigid polymer optical fibers. Some specific advantages (e.g., limited fluorescence self-quenching at low dye concentration) can be obtained using long affecting length in the waveguiding structure of the optical fiber. The coherent optical radiation (at a wavelength near the fluorescence maximum wavelength) can be amplified upon the excited state population which can be obtained by one-end or side excitation condition. Due to the fast depopulation of the excited state (lifetime typically few ns), amplification can be obtained only for the pulsed operating regime. The energy level scheme can be described as double wide energy bands as presented in Figure 1. The main excitation transition occurs from the ground (1) to a high energy excited state (3) but nonradiative transitions deplete higher energy levels ((3) → (2)) and radiative emission occurs mostly from the lowest energy excited level (2).

\( \tau_v \) (lifetime of level (3)) is significantly shorter than fluorescence lifetime \( \tau \), and the three-level system can be simplified to a two-level system. Knowing the molar extinction coefficient \( \varepsilon(\lambda) \), the absorption cross section can be calculated by

\[
\sigma^a(\lambda) = 3.8 \times 10^{-21} \cdot \varepsilon(\lambda) .
\]

\( \sigma^a_p \) and \( \sigma^e_s \) are absorption and emission cross sections at the signal wavelength. The layout of the optical fiber amplifier system for the one-end excitation method is presented in Figure 2.

The relationship \( \tau_v \ll \tau \) gives some simplification of the mathematical problem description. In such circumstances, the level (3) charge density is

\[
N_3(t, z) \equiv 0.
\]

The total charge densities expression is given by

\[
N_T = N_1(t, z) + N_2(t, z) ,
\]

where \( N_T, N_1, \) and \( N_2 \) are total, ground, and excited state charge densities, respectively.

The steady-state, time-dependent rate equations can be expressed as [27]

\[
\frac{\partial N_2(t, z, r)}{\partial t} = \frac{2\pi \cdot \sigma^a_p \cdot N_1(t, z) \cdot I_p(t, z)}{h \nu_p} \cdot \eta - \frac{N_2(t, z)}{\tau} - 2\pi \cdot \frac{\sigma^e_s \cdot N_2(t, z) - \sigma^a_s \cdot N_1(t, z) \cdot I_s(t, z)}{h \nu_s} \cdot \eta
\]

(4)

\[
\frac{\partial I_p(t, z, r)}{\partial t} = 2\pi \cdot \frac{\sigma^a_p \cdot N_1(t, z) \cdot I_p(t, z) \cdot \eta}{h \nu_p}
\]

\[
\frac{\partial I_s(t, z)}{\partial t} = -2\pi \cdot \frac{\sigma^e_s \cdot N_2(t, z) \cdot I_s(t, z)}{h \nu_s} \cdot \eta,
\]

where \( I_p(t, z) \) and \( I_s(t, z) \) represent the pump and the signal power densities, \( \nu_p \) and \( \nu_s \) are frequencies for the pump and the signal wavelength, \( h \) is Planck’s constant (6.626 \times 10^{-34} J \cdot s), and \( z \) is the direction of radiation propagation. \( \eta \) is the overlap integral of pump radiation distribution and dye concentration profile [27]:

\[
\eta = \int_{a_0}^{a_0} \Theta(r) \Psi(r) r dr,
\]

(5)

where \( \Theta(r) \) and \( \Psi(r) \) are dye and excitation radiation distributions and \( a_0 \) is the dye profile radius. For the step profile of dye distribution, the function \( \Theta(r) \) will be constant in the integral boundary, and in consequence \( \eta \) will be a fixed value and is independent of the pump distribution. The dye and pump distributions used in the calculation are presented in Figure 3.
In the steady-state conditions at a constant excited state population, the signal and pump intensities can be calculated using [27]

\[
\frac{\partial I_s(z,r)}{\partial z} = \eta \left( \frac{\sigma_s^0 / h \nu_p}{\sigma_p^0 / h \nu_s} \right) I_p(z) + \frac{\sigma_s^0}{\tau} I_s(z) N_t - k_s I_s(z),
\]

\[
\frac{\partial I_p(z,r)}{\partial z} = -\frac{\left( \frac{\sigma_p^0 / h \nu_s}{\sigma_p^0 / h \nu_p} \right) I_p(z) + \sigma_s^0 / \tau}{1 / \tau \eta} I_s(z) N_t - k_p I_p(z),
\]

where \( k_p \) and \( k_s \) are attenuations estimated for pump and signal wavelength. The signal gain versus fiber length can be obtained using

\[
g(z) = 10 \log \left( \frac{I_s(z)}{I_s(z = 0)} \right).\]

3. Oxazine 170 Perchlorate Optical Fiber Amplifier

Oxazine 170 was chosen to calculate the optical gain possibility in polymeric optical fiber structures. Poly(methyl methacrylate) was chosen as the host material. Using the Oxazine 170 dye, the maximum of emission (645 nm) corresponds to the most interesting transmission window for PMMA core fiber (650 nm) since low-cost laser diode sources and highly sensitive silicon-based photodiodes are commercially available for this spectrum range [32, 33].

The Oxazine 170 Perchlorate main absorption band is situated at 614 nm since the emission spectrum appeared at 641 nm as presented in Figure 4. The chosen parameters of the investigated dye-doped PMMA step-index amplifier are presented in Table 1.

The optical fiber amplifier parameters were calculated using steady-state time-independent equations ((6)-(7)). The simulations were carried out by varying the most important parameters in terms of signal amplification possibility using Runge-Kutta method and Matlab computational software. The simulation step \( (dz = 0.1 \cdot 10^{-3} \text{ m}) \) was chosen to obtain convergent high accuracy results and short simulation time (less than 30 s on a quad-core CPU, 2.5 GHz, 4 GB RAM).

High absorption and emission cross section (presented in Table 1) allow efficient amplification in the dye-doped optical fiber amplifier as it is presented in Figure 5. The pump radiation intensity (at wavelength 614 nm) strongly decreases (according to the high absorption of this wavelength by
Table 1: Parameters used for simulation of Ox170 doped optical fiber amplifier (estimated and from [34]).

<table>
<thead>
<tr>
<th>#</th>
<th>Parameter</th>
<th>Oxazine 170 Perchlorate</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$\sigma_p^a$: absorption cross section at the pump wavelength</td>
<td>$3.17 \times 10^{-16} \text{ cm}^2 \text{ at } 615 \text{ nm}$</td>
</tr>
<tr>
<td>2</td>
<td>$\sigma_s^a$: absorption cross section at the signal wavelength</td>
<td>$5.25 \times 10^{-17} \text{ cm}^2 \text{ at } 645 \text{ nm}$</td>
</tr>
<tr>
<td>3</td>
<td>$\sigma_e^s$: emission cross section at the signal wavelength</td>
<td>$4.20 \times 10^{-16} \text{ cm}^2 \text{ at } 645 \text{ nm}$</td>
</tr>
<tr>
<td>4</td>
<td>$\tau$: lifetime of level (2)</td>
<td>$5.1 \text{ ns}$</td>
</tr>
<tr>
<td>5</td>
<td>$\lambda_p$: pump wavelength</td>
<td>$614 \text{ nm}$</td>
</tr>
<tr>
<td>6</td>
<td>$\lambda_s$: signal wavelength</td>
<td>$645 \text{ nm}$</td>
</tr>
<tr>
<td>7</td>
<td>$n$: refractive index</td>
<td>$1.493$</td>
</tr>
<tr>
<td>8</td>
<td>$a_0$: core radius</td>
<td>$0.5 \text{ mm}$</td>
</tr>
<tr>
<td>9</td>
<td>$k_p$: attenuation estimated for pump wavelength</td>
<td>$k_p = 12 \text{ dB/m}$</td>
</tr>
<tr>
<td>10</td>
<td>$k_s$: attenuation estimated for signal wavelength</td>
<td>$k_s = 10 \text{ dB/m}$</td>
</tr>
</tbody>
</table>

Figure 5: Pump (blue) and signal (red) intensity distribution versus fiber length in Oxazine 170 optical fiber amplifier; molar dye concentration: $2 \times 10^{-6}$; pump power: 1kW; signal power: 1W.

Oxazine 170). Excited electrons emit photons (transition from state $(2) \rightarrow (1)$) synchronously with signal photons (at signal wavelength 645 nm). The optimum fiber length in terms of optical fiber amplifier construction is 0.046 m since the signal reaches its maximum.

The gain is strongly dependent on the dye concentration. Increasing the dye concentration results in high gain at a relatively low pump radiation power (Figure 6). Unfortunately, dye concentration has to be limited due to polymeric host doping possibility and fluorescence concentration quenching mechanism. Low concentration increases optimum optical fiber length (0.28 m for molar concentration $0.2 \times 10^{-6}$ versus 0.05 for molar concentration $1.4 \times 10^{-6}$). In fact, polymeric optical fiber amplifier lengths doped by highly fluorescent dyes are limited to few tenths of centimeters.

Assume that, at a low dye concentration, high gain can be obtained by increasing the pump intensity radiation as presented in Figure 7. For pump intensity from 1 kW to 10 kW, the gain increases from 26.8 dB ($z = 0.059$ m) to 36.0 dB ($z = 0.073$ m). The optimum amplification length changes are significantly smaller in comparison with those observed for dye concentration modifications (Figure 7). Moreover, both signals (pump and signal radiation) are attenuated in polymeric optical fiber structures. In such circumstances, the pump power radiation should be relatively high. Although the pulse pump power intensity of an order of kW was successfully used in polymer optical fiber amplifiers and stable gain parameters were obtained, the increase of photostability of fluorophores is one of the main issues considered in polymeric host based optoelectronic devices. Additionally, considering the application of Oxazine 170 doped PMMA fiber amplifier, it was experimentally verified that the fiber drawing process can be applied for fiber production (Figure 8). The fabrication process and measured luminescent properties were presented elsewhere [13].

4. Conclusions

The numerical simulation of gain in polymeric optical fibers doped by Oxazine 170 was presented. The step-index dye profile was used for calculations. The gain characteristic for the used dye molar concentration ($0.2 \times 10^{-6}$/$1.4 \times 10^{-6}$) and pump power (1–10 kW) was presented. A maximum gain of
36.0 dB was obtained for 10 kW and Oxazine 170 dye molar concentration $1.4 \cdot 10^{-4}$. The possibility of polymeric optical fiber fabrication was confirmed. The presented analysis can be used as a primary stage of optical amplifier construction based on Oxazine 170 Perchlorate.

**Conflicts of Interest**

The authors declare that there are no conflicts of interest regarding the publication of this article.

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**References**


