

Research Article

A Protection Method Based on Feature Cosine and Differential Scheme for Microgrid

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The fault current level of microgrid is different between islanded mode and grid connected mode. This situation degrades the performance of traditional overcurrent protection schemes. Hence, this paper proposes a protection method based on feature cosine and differential scheme. Firstly, feature cosine is proposed; it employs ellipse equation and minimum least squares to quantify the united behavior about voltage and current. Secondly, fault current direction and feature cosine are analyzed when fault occurs at different locations of a typical microgrid, and then the difference of feature cosine between faulty and healthy section locations is obtained. Thirdly, based on feature cosine and differential scheme, the differential direction is defined and utilized to detect faulty section location. Lastly, various time domain simulation case studies, including different microgrid operation modes, grounding resistances, faulty types, faulty section locations, and noise influence, are conducted and demonstrate that the proposed protection has high accuracy.

1. Introduction

Due to climate concern, technological advancements, and government incentives, microgrids are emerging as a lowmedium voltage energy network which include various types of distributed generation (DG) such as solar, wind, and geothermal [1, 2]. Some advantages of the presence of microgrids include reduction of power delivery loss, reduced greenhouse gases, and enhancement of power reliability.

However, the emergence of microgrids involves a lot of technical challenges, e.g., voltage and frequency control, stability problems, power quality, and so on, because microgrid operation, control, and protection are typically different from those of traditional power networks [3–5]. One of the major issues in microgrid is the microgrid protection. Different reasons responsible for this are as follows: (i) power flow may become bidirectional when DGs are integrated into the microgrid; (ii) fault current levels may be limited to 2~3 times the inverter-rated current; (iii) the microgrid may connect or

disconnect DGs; (iv) the microgrid has two operation modes including islanded and grid connected modes; (v) zero and negative sequence currents cannot be neglected in normal conditions since single- and three-phase unbalanced loads are embedded into microgrids.

At present, scholars have proposed various methods to protect microgrids. Reference [6] proposes a three-stage approach to microgrid protection including offline analyses, online calculation, and real-time protection, which is based on establishing dynamic security model in microgrid. Reference [7] employs hysteresis control and maximum current RMS control to limit the fault current; it can make fault current have a percentage of fifth harmonic which is utilized to build protection strategy, but this method is only suitable for islanded microgrid. Reference [8] investigates protection issues related to LV microgrids and elaborates LV microgrid protection concepts comprehensively. Voltage and frequency relays are used as a point of common coupling relay, and directional overcurrent (DOC) relay is utilized for feeder



FIGURE 1: Elliptical behavior of a phase in a bus for different situations. (a) Elliptical behavior of a phase in a bus for different values of ϕ and (b) elliptical behavior of a phase in a bus for different values of I_0 .

protection. DOC takes a long time to operate. Besides, with its operation, all of the feeder elements should be tripped. In [9, 10], sequence components, e.g., positive and negative sequence components, are employed to design the protection, but it can make relay coordination become more complex because of multiple settings. Reference [11] has proposed a novel fault location method based on the maximum oscillation magnitude of the transient voltage signal, but this method does not consider the three-phase microgrid. The dq wavelet packet transform-based digital protection has been implemented to investigate several transient disturbances occurring in different parts of the microgrid system [12]; it suffers a problem about choosing suitable wavelet basis functions. Two time-frequency-based differential schemes, which can avoid the selection of wavelet basis functions, are presented for microgrid protection; one is the Hilbert-Huang transform [13], and the other is the generalized Stransform [14]. In these two works, how to find effective threshold is necessary. This problem can be avoided by some statistical classifiers; for instance, [15, 16] have used the threephase voltage amplitude, voltage total harmonic distortions, and other 19 electrical features to build classifiers including Decision Tree and Naive Bayes, to detect fault and achieve protection; [17] has utilized combined wavelet transform and decision tree to detect and classify the fault; however, the protection strategies in [15, 16] are only designed for islanded microgrid, and the unbalanced loads situation is not considered in [17]. Reference [18] presents a data-mining-based intelligent differential protection scheme for the microgrid, but it uses 7 feature components, for example, the differential rate-of-change of frequency, the differential reactive power change with time and so on, but the shortcoming of this method is that it has much data needed to solve including many feature components and high sampling rates. This problem can also be found in [15-17].

Thus, compared with other differential methods, the contributions of this paper are as follows:

(1) This paper extracts the fault feature through solving the parameters of ellipse equation based on the current and voltage fault component. It can only use 5 sampling points to determine the parameters of ellipse which are employed to acquire polarity relationship between the busbar voltage and current.

(2) As for detection criteria, this paper uses ± 1 to define the feature direction of busbar. It can decrease the difficulty of communication and avoid threshold selection for different operation modes of microgrid.

The rest of this paper is organized as follows. Section 2 employs ellipse equation and minimum least squares to acquire feature cosine to describe the united behavior about voltage and current. The microgrid structure and the reason why the feature cosine can be used are shown in Section 3. Section 4 discusses the change of feature cosine when fault occurs at different locations. Section 5 presents how to use the feature cosine to obtain the differential feature direction to detect faulty section location. Section 6 shows the performance of proposed method including different microgrid operation modes, grounding resistances, and faulty section locations. Moreover, the condition of unbalanced loads is taken into consideration.

2. Feature Cosine of One Phase in a Bus

2.1. Mathematical Background. The voltage and current signals in one phase of a bus at time *t* can be written as

$$u(t) = U_0 \sin(\omega t) \tag{1}$$

$$i(t) = I_0 \sin(\omega t - \phi) \tag{2}$$

where the angle ϕ is the delay between i(t) and u(t). U_0 and I_0 are the peak values of u(t) and i(t), respectively. ω is the angular velocity, $\omega = 2\pi f$. In China system, f = 50 Hz. $\cos(\phi)$ is defined as the feature cosine.

As for a bus, Figure 1 shows the united behavior of the voltage and current sine signals for one phase at different conditions. This behavior can be modeled using a conic section mathematical equation or, more specifically, the equation of the ellipse.

By applying (5), the Cartesian form for the equation of the bus ellipse is defined as (4) [19].

$$\sin^2(\omega t) + \cos^2(\omega t) = 1 \tag{3}$$

$$x^{2}(t) - 2\cos(\phi) x(t) y(t) + y^{2}(t) - \sin^{2}(\phi) = 0$$
 (4)

$$x(t) = \frac{u(t)}{U_0} = \sin(\omega t)$$
(5)

$$y(t) = \frac{i(t)}{I_0} = \sin(\omega t - \phi)$$
(6)

The equation of the ellipse, for any value of U_0 and I_0 , is given by

$$I_0^2 u^2(t) - 2U_0 I_0 \cos(\phi) u(t) i(t) + U_0^2 i^2(t) - U_0^2 I_0^2 \sin^2(\phi) = 0$$
(7)

Hence, as for a bus, using the geometric properties of (7) can monitor the behavior of voltage and current signals for each phase and identify the moment when potential faults have occurred; besides, this paper proposes that the parameters of the ellipse can be seen as an index to indicate the faulty section location, which is elaborated in the following sections.

2.2. Feature Cosine. According to [20], an ellipse section defined in \mathbb{R}^2 represents a set of points whose coordinates satisfy the general equation (8), the form of (8) is equivalent to (7), and (8) can be seen as a fitting model to obtain the parameters of (7).

$$ax^{2} + bxy + cy^{2} + dx + ey + f = 0$$
 (8)

with the parameters *a* or *b* or $c \neq 0$.

Then, (7) and (8) can both be rewritten in matrix form as

$$f(\mathbf{x}) = \mathbf{\alpha}\mathbf{x} + 1 \tag{9}$$

$$a = [a \ b \ c \ d \ e]$$
$$x = [x_1 \ x_2 \ x_3 \ x_4 \ x_5]^{\mathrm{T}} = [x^2 \ xy \ y^2 \ x \ y]^{\mathrm{T}} (10)$$
$$= [u^2(t) \ u(t)i(t) \ i^2(t) \ u(t) \ i(t)]^{\mathrm{T}}$$

Based on the minimum least squares, a cost function J_a can be written as

$$J_{a}(a, \cdots, e) = \frac{1}{2} \sum_{i=1}^{n} \left[f(\mathbf{x}_{i}) - 0 \right]^{2}$$
(11)

Hence, the parameters estimation problem is transformed into a simpler problem of finding a local minimizer for J_a ; this problem can be solved by Levenberg-Marquardt algorithm, and it is described in [16, 17].

Lastly, the parameters of equation (7) can be obtained from Levenberg-Marquardt algorithm.

$$\boldsymbol{a} = \boldsymbol{a}^* = \begin{bmatrix} a^* & b^* & c^* & d^* & e^* \end{bmatrix}$$
(12)

And the feature cosine $\cos(\phi)$ can be shown in (13), $\cos(\phi)$ can represent the phase relation between the voltage and current, and it is mentioned that $\cos(\phi)$ for each phase is a constant even in the condition of unbalanced loads if a microgrid operates normally. $\cos(\phi)$ is the index mentioned in Section 2.1. Section 3 will illustrate why $\cos(\phi)$ can be employed to detect microgrid faulty location.

$$\cos\left(\phi\right) = -\frac{b^*}{\left(2\sqrt{a^*}\cdot\sqrt{c^*}\right)}\tag{13}$$

3. Feature Cosine Utilization Reason

3.1. Microgrid Topology. A modified microgrid based on the topology of CERTS microgrid model [21] is shown in Figure 2(a) and established in Matlab/Simulink. This microgrid is a part of the power distribution system, and it is connected to the utility grid using a transformer 0.4/10kV. Each distributed generation (DG) is controlled by improved droop controller [22, 23]. Table 1 shows each load capacity. The system parameters are given: the power electronic device is the IGBT; the capacities of DGs are all 80kVA; switch frequency is 6kHz; the DC voltage is 800V; Line: resistance and inductance are 0.642 Ω /km and 0.083H/km; the length of Line 1, Line 2, and Line 3 are 0.3km, 0.2km, and 0.5km, respectively.

3.2. Reason. The fault current-limiting strategy is applied for each DG according to [24, 25]. For example, when the microgrid occurs, three-line-ground (LLLG) fault or single-line-ground (LG) fault at 0.2s, whose faulty location is Line 2 of Figures 2(a), 2(b), and 2(c), shows that the fault current-limiting strategy, after 0.21s, can effectively limit each DG fault current into 2 times of the rated current; besides, this strategy can restrain the harmonics and make the frequency of output current and voltage equal to 50Hz. This is the reason why this paper can use the feature cosine to detect the faulty section.

4. The Analysis of Microgrid Fault Feature

4.1. Fault at Line 1. Based on the analysis method from [26], this paper focuses on the current direction. When short-circuit fault occurs at Line 1 of Figure 2(a), B_1 , B_2 , B_3 , B_4 , and B_5 are bus. Taking B_1 and B_2 as an example, Figure 3 shows the current direction of B_1 and B_2 , which is suitable for the islanded mode and grid connected mode.

When DGs supply power for downstream load shown in Figure 3(a), phase ϕ_1 and ϕ_2 are shown in (14); this is because loads in microgrid are generally inductive loads.

$$\phi_{1} = \arg\left(\dot{U}_{1}\right) - \arg\left(\dot{I}_{1}\right) > 0^{\circ}$$

$$\phi_{2} = \arg\left(\dot{U}_{2}\right) - \arg\left(\dot{I}_{2}\right) > 0^{\circ}$$
(14)

where \dot{U}_1 and \dot{U}_2 are the voltage of B_1 and B_2 . \dot{I}_1 and \dot{I}_2 are the current of B_1 and B_2 . $\arg(\dot{U}_1)$ means the voltage phase of B_1 . $\arg(\dot{I}_1)$ means the current phase of B_1 .



FIGURE 2: Single line diagram and fault current of microgrid. (a) Single line diagram; (b) fault current by DG1 at LLLG; (c) fault current by DG2 at LG.



FIGURE 3: The current direction of B_1 and B_2 when fault occurs at Line 1. (a) DGs supply power for downstream load; (b) DGs supply power for upstream load.





FIGURE 4: The current direction of B₁ and B₂ when fault occurs at Line 2. (a) DGs supply power for downstream load; (b) DGs supply power for upstream load.

After fault, because the grounding impedance of fault point is obviously less than the load impedance [22], as for current direction, B_1 and B_2 are both from bus to fault point. Moreover, the voltage phases of B_1 and B_2 are not changed. Based on this, (15) and (16) can be expressed and present that $\cos(\phi_1^f)$ is positive and $\cos(\phi_2^f)$ is negative when the fault occurs at Line 1.

$$\phi_{1}^{f} = \arg\left(\dot{U}_{1}^{f}\right) - \arg\left(\dot{I}_{1}^{f}\right) \approx \arg\left(\dot{U}_{1}\right) - \arg\left(\dot{I}_{1}\right)$$

$$> 0^{\circ}$$

$$\phi_{2}^{f} = \arg\left(\dot{U}_{2}^{f}\right) - \arg\left(\dot{I}_{2}^{f}\right)$$

$$\approx \arg\left(\dot{U}_{2}\right) - \arg\left(\dot{I}_{2}\right) - 180^{\circ} < -90^{\circ}$$

$$s\left(\phi_{1}^{f}\right) \approx \cos\left(\arg\left(\dot{U}_{1}\right) - \arg\left(\dot{I}_{1}\right)\right) > 0$$

$$s\left(\phi_{2}^{f}\right) \approx \cos\left(\arg\left(\dot{U}_{2}\right) - \arg\left(\dot{I}_{2}\right) - 180^{\circ}\right) < 0$$
(16)

where ϕ_1^f and (ϕ_2^f) are the postfault phase of B₁ and B₂.

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When the DGs supply power for upstream load, the current directions at B₁ and B₂ are shown in Figure 3(b). Through analyzing, when the fault occurs at Line 1, $\cos(\phi_1^{\rm f})$ is positive and $\cos(\phi_2^{\rm f})$ is negative.

4.2. Fault at Line 2. When the fault occurs at Line 2 of Figure 2(a), the current direction of B_1 and B_2 is shown in Figure 4.

When the DGs supply power for downstream loads shown in Figure 4(a) and the fault occurs at Line 2, the current directions, the current directions of B₁ and B₂ are both from bus to fault point because the load impedance is bigger than the grounding impedance [22]. $\cos(\phi_1^f)$ and $\cos(\phi_2^f)$ can be shown in

$$\cos\left(\phi_{1}^{f}\right) \approx \cos\left(\arg\left(\dot{U}_{1}\right) - \arg\left(\dot{I}_{1}\right)\right) > 0$$

$$\cos\left(\phi_{2}^{f}\right) \approx \cos\left(\arg\left(\dot{U}_{2}\right) - \arg\left(\dot{I}_{2}\right)\right) > 0$$
(17)

Similarly, if the DGs supply power for downstream load shown in Figure 4(b), $\cos(\phi_1^f)$ and $\cos(\phi_2^f)$ are both positive when fault occurs at Line 2.

4.3. Fault at Line 3. The current direction of B_1 and B_2 is shown in Figure 5 when the fault occurs at Line 3 of Figure 2(a). There are two situations as follows because the distance is relatively far from fault point to B_2 .

(I) The grounding impedance is relatively small; that is, the effect of fault point on B_2 is serious. And the current direction of B_1 and B_2 will be both from bus to fault point; these directions are opposite to that in prefault and are shown



FIGURE 5: The current direction of B_1 and B_2 when fault occurs at Line 3. (a) DGs supply power for downstream load when the effect is serious; (b) DGs supply power for downstream load when the effect is mild; (c) DGs supply power for upstream load.

in Figure 5(a). (18) shows their feature cosine; they are both negative.

$$\cos\left(\phi_{1}^{\mathrm{f}}\right) \approx \cos\left(\arg\left(\dot{U}_{1}\right) - \arg\left(\dot{I}_{1}\right) - 180^{\circ}\right) < 0$$

$$\cos\left(\phi_{2}^{\mathrm{f}}\right) \approx \cos\left(\arg\left(\dot{U}_{2}\right) - \arg\left(\dot{I}_{2}\right) - 180^{\circ}\right) < 0$$
(18)

(II) When the effect of fault point on B_2 is mild, the current direction of B_1 and B_2 can be maintained; these are same as that in prefault shown in Figure 5(b). The $\cos(\phi_1^f)$ and $\cos(\phi_2^f)$ are both positive.

Similarly, if the DGs supply power for upstream load shown in Figure 5(c), there are also two situations according to the effect of fault point on B₂. And $\cos(\phi_1^f)$ and $\cos(\phi_2^f)$ will be both negative in these two situations.

In summary, no matter how the initial current direction changes in bus, $\cos(\phi_1^f)$ is positive and $\cos(\phi_2^f)$ is negative

when the fault occurs at the section between B_1 and B_2 . Moreover, there are two situations when the fault does not occur at the area between B_1 and B_2 : (1) $\cos(\phi_1^f)$ and $\cos(\phi_2^f)$ are both positive and (2) $\cos(\phi_1^f)$ and $\cos(\phi_2^f)$ are both negative. These can be clearly shown in Table 2 where "+" is positive, "-" is negative. The difference of feature cosine can be utilized to detect the faulty section in the next section.

5. Protection Methodology

Firstly, it is mentioned that the relays at the ends of a bus are considered and not at the ends of the line; this is because it can reduce the number of relays being used; however, the circuit breakers need to be installed at the ends of the line for isolating a fault.

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TABLE 2: The direction of feature cosine of B_1 and B_2 .





FIGURE 6: The procedures of this paper's proposed method.

Then, it is presented how to obtain the feature direction (D) of each bus through feature cosine.

Step 1. $u_n^w(t)$, $u_{n+1}^w(t)$, $i_n^w(t)$, and $i_{n+1}^w(t)$ are retrieved at B_n and B_{n+1} , $u_n^w(t)$ and $i_n^w(t)$ are the normalized voltage and current of phase-w of B_n , $u_{n+1}^w(t)$ and $i_{n+1}^w(t)$ are the normalized voltage and current of phase-w of B_{n+1} , w is a or b or c, n is the number of bus, and n is equal to 1, 2 and 4.

Step 2. As for B_n , according to Levenberg-Marquardt algorithm, the parameters of bus ellipse equation α_n^w can be calculated. α_n^w can represent the behavior of voltage and current signals.

$$\boldsymbol{a}_{n}^{w} = \begin{bmatrix} a_{n}^{w} & b_{n}^{w} & c_{n}^{w} & d_{n}^{w} & e_{n}^{w} \end{bmatrix}$$
(19)

Step 3. Similarly, as for B_{n+1} , the parameters of line ellipse equation a_{n+1}^w can be obtained.

$$\boldsymbol{a}_{n+1}^{w} = \begin{bmatrix} a_{n+1}^{w} & b_{n+1}^{w} & c_{n+1}^{w} & d_{n+1}^{w} & e_{n+1}^{w} \end{bmatrix}$$
(20)

Step 4. $\cos(\phi_n^w)$ and $\cos(\phi_{n+1}^w)$ are calculated, $\cos(\phi_n^w)$ and $\cos(\phi_{n+1}^w)$ are the feature cosine of B_n and B_{n+1}.

$$\cos\left(\phi_{n}^{w}\right) = -\frac{b_{n}^{w}}{\left(2\sqrt{a_{n}^{w}}\sqrt{c_{n}^{w}}\right)} \tag{21}$$

$$\cos\left(\phi_{n+1}^{w}\right) = -\frac{b_{n+1}^{w}}{\left(2\sqrt{a_{n+1}^{w}}\sqrt{c_{n+1}^{w}}\right)}$$
(22)

Step 5. D_n^w , D_{n+1}^w , and D_{cn}^w can be obtained by the following equations. D_n^w and D_{n+1}^w , which can show the fault current direction of bus, are the feature direction of B_n and B_{n+1}, and D_{cn}^w is the differential direction.

$$D_{n}^{w} = \begin{cases} 1, & \cos(\phi_{n}^{w}) > 0\\ -1, & \cos(\phi_{n}^{w}) < 0, \end{cases}$$

$$D_{n+1}^{w} = \begin{cases} 1, & \cos(\phi_{n+1}^{w}) > 0\\ -1, & \cos(\phi_{n+1}^{w}) < 0 \end{cases}$$

$$D_{cn}^{w} = D_{n+1}^{w} - D_{n}^{w} \qquad (24)$$

Lastly, if $D_{cn}^{w} < 0$, the section between B_n and B_{n+1} is judged as faulty section; if $D_{cn}^{w} \ge 0$, the section between B_n and B_{n+1} is judged as healthy section. Taking B_1 and B_2 as an example, the procedures of this paper's proposed method can be shown clearly in Figure 6.

6. Simulation Results

In order to prove the effectiveness of the proposed method in this paper, different fault conditions are simulated through Matlab/Simulink for the microgrid shown in Figure 2(a), and conditions for the fault study are explained as follows.

(1) Faulty resistances (R_f): 0.01, 0.1, 0.2, 0.3, 0.5, 1, 5, 10 Ω .

R _f	Р	$[B_1, B_2, B_3, B_4, B_5]$	Each <i>P</i> result	Final result
	а	[0.954, -0.990, -0.982, -0.859, -0.729]	B ₁ - B ₂	
0.01Ω	b	[0.998, 0.999, 0.999, -1.007, -1.009]	healthy	$B_1 - B_2$
	с	[0.999, 0.999, 0.999, -0.997, -0.995]	healthy	
	а	[0.961, -0.986, -0.978, -0.904, -0.797]	B ₁ - B ₂	
0.1Ω	b	[0.998, 0.998, 0.998, -0.991, -0.987]	healthy	$B_1 - B_2$
	с	[0.998, 0.998, 0.999, -0.992, -0.989]	healthy	
	а	[0.999, -1.000, -0.999, -0.997, -0.997]	B ₁ - B ₂	
0.5Ω	b	[-0.891, -0.894, -0.896, 0.720, 0.699]	healthy	B ₁ - B ₂
	с	[-0.958, -0.960, -0.962, 0.925, 0.919]	healthy	
	а	[0.936, -0.979, -0.960, -0.897, -0.767]	B ₁ - B ₂	
2Ω	b	[0.999, 0.999, 1.000, -0.994, -0.993]	healthy	$B_1 - B_2$
	с	[1.000, 1.000, 1.001, -0.996, -0.994]	healthy	
	а	[0.927, -0.974, -0.952, -0.888, -0.752]	B ₁ - B ₂	
10Ω	b	[0.999, 0.999, 0.999, -0.995, -0.993]	healthy	$B_1 - B_2$
	с	[0.999, 0.999, 1.000, -0.998, -0.997]	healthy	

TABLE 3: The feature cosine of each bus and results with different grounding resistances.

(2) Different faulty types (F_t): single-line-ground (LG), double-line-ground (LLG), line-line (LL), and three-line-ground (LLLG), where LG(a) means the single-line-ground whose faulty phase is phase-a.

(3) Faulty section (F_L): Line 1, Line 2, and Line 3.

(4) Different microgrid operation modes (O_m) : islanded and grid connected mode.

(5) Unbalanced loads: each phase capacity of load is changed.

(6) Noise influence: the signal to noise ratio (SNR) is set as 50db, 20db, and 5db.

6.1. Different Grounding Resistances. When the microgrid shown in Figure 2(a) is operated in islanded mode, LG fault is supposed to happen in Line 1 at t = 0.2s; that is, faulty section is between B₁ and B₂ labelled B₁-B₂. Faulty conditions include that faulty phase is phase-a and grounding resistances are set to 0.01Ω , 0.5Ω , 0.1Ω , 2Ω , and 10Ω , respectively. Then Table 3 gives the feature cosine of each bus and judgment results after implementing this paper's method; *P* is phase sequence.

Take grounding resistance 0.5Ω as an example, Figure 7 gives the voltage and current of B₁ and B₂, and Figure 8 shows the bus ellipses of each phase of B₁ and B₂. Figure 7 illustrates that the faulty phase voltage direction of B₁ is same as that of B₂ and the faulty phase current direction of B₁ is opposite to that of B₂, which is illustrated obviously in Figure 8.

Then, as for phase-a, from Table 3 and this paper's method, the feature cosines from B_1 to B_5 are 0.999, -1.000, -0.999, -0.997, and -0.997, respectively. So, the feature directions from B_1 to B_5 are 1, -1, -1, -1, and -1, respectively; that is, their differential directions are -2, 0, 0, 0, respectively. Similarly, as for phase-b and phase-c, their differential directions are all 0. Hence, the faulty section is between B_1 and B_2 ; this result is consistent with the actual fault. Lastly, from

Table 3 we can find that this paper's method can detect fault part effectively in different grounding resistances.

6.2. Different Faulty Types. When the microgrid is operated in islanded mode, different faulty types, including LG(b), LLG(ab), LL(bc), and LLLG, are supposed to happen in Line 1 at 0.2s with grounding resistance 0.1 Ω ; that is, faulty section is B₁-B₂. Then, Table 4 gives the feature cosine of each bus and judgment results; it shows that the proposed method cannot be influenced by different faulty types.

6.3. Different Faulty Section Locations. The islanded microgrids are simulated at 0.2s with different faulty section locations, including B_1 - B_2 , B_2 - B_3 , and B_4 - B_5 . The fault conditions include fault type LG whose faulty phase is phase-c or phase-a; grounding resistances is 0.3 Ω or 10 Ω . Then, Table 5 illustrates that this paper's method can detect different fault parts. It is mentioned that the feature cosine is consist with the analysis in Section 4.3 when the grounding resistance is 10 Ω and faulty section location is B_4 - B_5 .

6.4. Grid Connected Operation Mode. When the microgrid is operated at grid connected mode, different faults are supposed to happen including different faulty section locations, types, and grounding resistances. Table 6 gives the judgments and shows that this paper's method can detect different faults in grid connected operation mode; besides, the protection scheme cannot be changed compared with islanded mode.

6.5. Unbalanced Loads. In order to prove the effectiveness of proposed method in the condition of the unbalanced loads, the capacity of load L-2 in Figure 2(a) is set as follows: phase-a: the active power and reactive power are 19kW and 8kW; phase-b: the active power and reactive power are 17kW and



FIGURE 7: The voltage and current of B₁ and B₂ when fault occurs at Line 1. (a) B₁ voltage; (b) B₂ voltage; (c) B₁ current; (d) B₂ current.



FIGURE 8: The bus ellipse of B₁ and B₂ for different phases. (a) Phase-a; (b) phase-b; (c) phase-c.

7kW; phase-c: the active power and reactive power are 10kW and 8kW.

When different faults are supposed to happen in the microgrid, Table 7 gives the feature cosine of each bus and judgment results. When faulty condition is that faulty section

location is B_1 - B_2 , grounding resistance is 0.1Ω , operation mode is islanded, and faulty type is LG (a), Figure 9 is the current of B_2 and the bus ellipses of B_1 and B_2 . From Figure 9 and Table 7, this paper method can achieve the faulty section location detection in the condition of the unbalanced loads.

F _t	Р	$[B_1, B_2, B_3, B_4, B_5]$	Each P result	Final result
IC	а	[1.003, 1.003, 1.003, -1.008, -1.012]	healthy	
LG (b)	b	[0.928, -0.915, -0.871, -1.100, -1.084]	B_1-B_2	$B_1 - B_2$
	с	[1.002, 1.002, 1.002, -0.991, -0.9867]	$B_1 - B_2$	
UC	а	[0.957, -0.946, -0.915, -0.994, -0.970]	B_1-B_2	
(ab)	b	[0.672, -0.508, -0.380, -0.829, -0.614]	$B_1 - B_2$	$B_1 - B_2$
	с	[0.998, 0.997, 0.997, 1.004, 1.006]	healthy	
TT	а	[0.401, 0.631, 0.715, 0.113, 0.897]	healthy	
(bc)	b	[0.953, -0.941, -0.958, -0.977, -0.900]	$B_1 - B_2$	$B_1 - B_2$
(,	с	[0.956, -0.943, -0.957, -0.978, -0.909]	$B_1 - B_2$	
	а	[0.836, -0.636, -0.473, -0.949, -0.869]	B_1-B_2	
LLL	b	[0.609, -0.696, -0.497, -0.852, -0.642]	$B_1 - B_2$	$B_1 - B_2$
	с	[0.999, -0.866, -0.770, -1.040, -1.010]	$B_1 - B_2$	

TABLE 4: The feature cosine of each bus and judgment results with different faulty types.

TABLE 5: The feature cosine of each bus and judgment results in different faulty section locations.

$egin{array}{ccc} F_{\mathrm{t}} & & \ R_{\mathrm{f}} & \ F_{\mathrm{L}} & & \ \end{array}$	Р	$[B_1, B_2, B_3, B_4, B_5]$	Each <i>P</i> result	Final result
LG(c)	а	[0.998, 0.999, 0.999, -0.988, -0.985]	healthy	
0.3Ω	b	[0.998, 0.999, 0.999, -0.990, -0.987]	healthy	$B_1 - B_2$
B ₁ -B ₂	С	[0.883, -0.940, -0.906, -0.797, -0.656]	$B_1 - B_2$	
LG(c)	a	[0.985, 0.990, 0.992, -0.972, -0.963]	healthy	
0.3Ω	b	[0.988, 0.992, 0.993, -0.974, -0.965]	healthy	$B_2 - B_3$
B ₂ -B ₃	С	[0.766, 0.922, -0.979, -0.739, -0.627]	$B_2 - B_3$	
LG(c)	a	[-0.821, -0.806, -0.796, 0.835, 0.850]	healthy	
0.3Ω	b	[-0.847, -0.833, -0.825, 0.847, 0.861]	healthy	B_4-B_5
B ₄ -B ₅	С	[-0.618, -0.472, -0.374, 0.866, -0.9461]	B_4-B_5	
LG(a)	а	[0.909, -0.956, -0.922, -0.525, -0.345]	B_1-B_2	
10Ω	b	[0.998, 0.998, 0.998, -0.996, -0.994]	healthy	B_1-B_2
B ₁ -B ₂	С	[0.999, 1.000, 1.000, -0.993, -0.992]	healthy	
LG(a)	а	[0.544, 0.780, -0.993, -0.486, -0.324]	B_2-B_3	
10Ω	b	[0.993, 0.995, 0.996, -0.985, -0.980]	healthy	B_2-B_3
B ₂ -B ₃	С	[0.994, 0.996, 0.997, -0.992, -0.989]	healthy	
LG(a)	а	[-0.210, -0.105, -0.034, 0.795, -0.985]	B_4-B_5	
10Ω	b	[-0.923, -0.909, -0.899, 0.942, 0.953]	healthy	B_4-B_5
B ₄ -B ₅	С	[-0.922, -0.910, -0.899, 0.931, 0.939]	healthy	

6.6. Noise Influence. In fact, the elliptical representation of the behavior of both voltage and current signals should consider the existence of the noise, which is inherent in the processes of generation, transmission, or even disturbances related to digital recorders. Hence, in order to implement the proposed method effectively, the wavelet denoising method is employed [27]. It is embedded in Step 1 of Section 5.

When different faults with different SNR including 50db and 5db are supposed to happen in the microgrid, Table 8 shows that this paper method after adding wavelet denoising method can detect faulty section locations in different SNR including 50db and 5db. *6.7. Looped Microgrid.* When different faults are supposed to happen in the looped microgrid shown in Figure 10, Table 9 gives the feature cosine of each bus and judgment results. From Table 9, we can know that this paper method can achieve the faulty section location detection in different faulty conditions for looped microgrid.

6.8. Sample Microgrid. When different faults are supposed to happen in the looped microgrid shown in Figure 11, Table 10 gives the feature cosine of each bus and judgment results. From Table 10, we can know that this paper method can

$egin{array}{c} F_{\mathrm{t}} \ R_{\mathrm{f}} \ F_{\mathrm{L}} \end{array}$	Р	$[B_1, B_2, B_3, B_4, B_5]$	Each <i>P</i> result	Final result
LG(a)	а	[0.054, -0.540, -0.271, -0.985, -0.974]	B_1-B_2	
0.01Ω	b	[-0.5926, 1.000, 1.000, 0.4800, 0.340]	healthy	B_1-B_2
$B_1 - B_2$	с	[-0.443, -0.013, 0.842, 0.256, 0.421]	healthy	
LG(b)	а	[0.191, 0.780, 0.901, 0.768, 0.822]	healthy	
0.2Ω	b	[0.507, -0.909, -0.840, -0.984, -0.981]	B_1-B_2	B_1-B_2
B ₁ -B ₂	с	[0.181, 0.764, 0.895, 0.713, 0.782]	healthy	
LLG(ac)	а	[0.107, 0.999, -0.829, -0.656, -0.021]	B ₂ -B ₃	
0.5Ω	b	[0.112, 0.875, 0.940, 0.709, 0.759]	healthy	B_2-B_3
B ₂ -B ₃	с	[0.108, 0.989, -0.839, -0.899, -0.545]	$B_2 - B_3$	
LLG(bc)	а	[-0.559, 0.856, 0.943, -0.005, 0.228]	B ₂ -B ₃	
5Ω	b	[0.649, 0.974, -0.701, -0.967, -0.431]	B_2-B_3	B_2-B_3
B ₂ -B ₃	с	[0.637, 0.973, -0.749, -0.961, 0.307]	healthy	
LLL	а	[-0.948, -0.870, -0.585, 0.053, -0.319]	B_4-B_5	
10Ω	b	[-0.935, -0.843, -0.515, 0.619, -0.302]	B_4-B_5	B_4-B_5
B ₄ -B ₅	с	[-0.987, -0.969, -0.193, 0.575, -0.515]	B_4-B_5	

TABLE 6: The feature cosine of each bus and judgment results in grid connected operation mode.

TABLE 7: The feature cosine of each bus and judgment results in unbalanced loads.

$ \begin{array}{c} F_{\rm t} \\ R_{\rm f} \\ F_{\rm L} \\ O_{\rm m} \end{array} $	Р	$[B_1, B_2, B_3, B_4, B_5]$	Each P result	Final result
LG(a)	a	[-0.999, 0.999, 0.999, 0.995, 0.997]	$B_1 - B_2$	
0.1Ω	b	[0.653, 0.667, 0.675, -0.867, -0.851]	healthy	B -B
B ₁ -B ₂ islanded	c	[0.840, 0.852, 0.859, -0.911, -0.902]	healthy	$D_1 D_2$
LL(ab)	а	[-0.969, -0.834, 0.948, 0.951, 0.984]	B ₂ -B ₃	
0.1Ω	b	[-0.718, -0.043, -0.856, 0.909, 0.931]	healthy	BB.
B ₂ -B ₃ islanded	c	[0.948, 0.949, 0.949, -0.999, -0.998]	B ₂ -B ₃	$D_2 D_3$
LLLG	а	[0.994, 0.999, 1.000, -0.991, 0.985]	B ₄ -B ₅	
0.1Ω	b	[0.936, 0.979, 0.987, -1.021, 1.095]	B_4-B_5	B -B
B ₄ -B ₅ islanded	с	[1.095, 1.023, 1.006, -0.991, 0.966]	B ₄ -B ₅	$D_4^{-}D_5^{-}$
LG(b)	a	[-0.167, -0.191, -0.208, 0.115, 0.109]	healthy	
1Ω	b	[0.999, -0.980, -0.980, -0.137, -0.169]	$B_1 - B_2$	B-B
B ₁ -B ₂ Grid	c	[-0.774, -0.780, -0.785, -0.296, -0.298]	healthy	$D_1 D_2$
LLG(ab)	a	[0.958, 0.735, -0.921, -0.456, -0.557]	B ₂ -B ₃	
1Ω	b	[0.837, 0.341, 0.798, -0.993, -0.997]	healthy	B -B
Grid	C		healthy	$D_2^{-}D_3$
$B_2 - B_3$	C	[-0.900, -0.901, -0.902, 0.988, 0.982]	ilealtily	
LLLG	a	[-0.836, -0.880, -0.899, 0.997, -0.994]	B ₄ -B ₅	
1Ω	b	[-0.840, -0.887, -0.912, 0.993, -1.038]	B_4-B_5	BB-
Grid B4-B5	с	[-0.933, -0.952, -0.964, 0.994, -0.899]	B ₄ -B ₅	$D_4^{-}D_5^{-}$



FIGURE 9: The B_2 current and bus ellipse for B_1 and B_2 ; (a) B_2 current, (b) bus ellipse of three phases.

achieve the faulty section location detection in different faulty conditions for the microgrid whose nodes are with only loads.

7. Discussion

When different faults, including different faulty resistances and faulty section, occur in microgrid at 0.2s, Figure 12 shows the fault current peak value of B_1 whose time length is from 0.21s~0.23s.

It is shown in Figure 10 that the B_1 fault current in grid connected mode is higher compared with the islanded mode; besides, the B_1 fault current decreases for the faults occurring on the lines away from the B_1 . So, as for fault current, there is a difference between grid connected and islanded modes; besides, if the microgrid has unbalanced loads, its fault current for each phase is obviously different. It can be concluded that most commercially used overcurrent relay with a preset threshold to operate in grid connected mode may fail or may take a longer time to operate in islanded mode [2]. Hence, [14] has different thresholds to detect fault when the microgrid is operated in different modes. However, [14] did not consider the condition of unbalanced load and will make the protection scheme more complex. Hence, in this paper, the protection method, which has the same threshold in different operation mode and unbalanced load, is proposed and superior to [14].

8. Conclusion

Based on the geometric representation of one phase in a bus and the analysis of feature cosine of different buses, this paper proposes a protection method to detect the faulty section location using the differential direction. The proposed method uses comprehensively every phase voltage

<i>Р</i> , Р. С	Ρ	$[B_1, B_2, B_3, B_4, B_5]$	Each <i>P</i> result	Final result
Um LG(a) 5.0 P D	۵ م	[0.907, -0.945, -0.909, -0.527, -0.352] [0.999, 0.999, 0.999, -0.995, -0.993]	healthy B ₁ -B ₂	B_1-B_2
B ₁ -B ₂ islanded	C	[0.999, 0.999, 0.999, -0.996, -0.995]	healthy	4
LLG(ab) 1Ω	а Р	[0.535, 0.920, -0.064, -0.899, 0.073] [0.754, 0.939, 0.039, -0.938, -0.726]	B ₂ -B ₃ healthy	я. я.
B ₂ -B ₃ islanded	C	[0.995, 1.000, -1.000, -0.964, -0.940]	B_2 - B_3	57 24
LLLG 50	a D	$\begin{bmatrix} -0.641, 0.450, 0.275, -0.283, 0.377 \\ [-0.967, 0.913, 0.768, -1.000, 0.964] \end{bmatrix}$	B_4 - B_5 B_4 - B_5	B, -B,
B ₄ -B ₅ Grid	C	[0.699, 0.677, 0.647, -0.858, 1.000]	B_4 - B_5	4 5
		(b) SNR=5db		
بت مي ¹ C	Ą	$[B_1, B_2, B_3, B_4, B_5]$	Each <i>P</i> result	Final result
Under December 2017 50	a D	[0.907, -0.945, -0.909, -0.527, -0.352] [0.999, 0.999, 0.999, -0.995, -0.993]	healthy B ₁ -B ₂	4 8
B ₁ -B ₂ islanded	C	[0.999, 0.999, 0.999, -0.996, -0.996]	healthy	22 Ia
LLG(ab) 1Ω	a D	[0.535, 0.920, -0.064, -0.899, 0.073] [0.754, 0.939, -0.100, -0.958, -0.726]	B_2-B_3 healthy	B, -B,
B ₂ -B ₃ islanded	C	[0.995, 1.000, 1.000, -0.974, -0.940]	B_2-B_3	- 7 - 2
LLLG 50	a D	$\begin{bmatrix} -0.643, -0.450, -0.275, 0.283, -0.377 \\ [-0.970, -0.913, -0.768, 1.000, -0.964] \end{bmatrix}$	B_4 - B_5 B_4 - B_5	и и
${ m B_4}$ - ${ m B_5}$ Grid	C	[-0.699, -0.677, -0.647, 0.858, -1.000]	B_4 - B_5	±4 [−] υ5

TABLE 8: The feature cosine of each bus and judgment results in different SNR.

(a) SNR=50db

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TABLE 9: The feature	cosine of each	bus and judg	gment results f	or the loope	d microgrid.
			7		

$ \begin{array}{c} F_{\rm t} \\ R_{\rm f} \\ F_{\rm L} \\ O_{\rm m} \end{array} $	Р	$[B_1, B_2, B_3, B_4, B_5]$	Each P result	Final result
LG(a)	а	[0.965, -0.973, -0.949, -0.790, -0.741]	B ₁ - B ₂	
0.1Ω	b	[-1.102, -1.103, -1.103, -1.098, -1.100]	healthy	B B.
B ₁ -B ₂ islanded	с	[-1.043, -1.044, -1.044, -1.040, -1.041]	healthy	$D_1 D_2$
LLG(ab)	а	[0.932, 0.978, -0.929, 0.958, 0.980]	B ₂ - B ₃	
0.1Ω	b	[0.535, 0.763, -0.500, 0.657, 0.788]	B ₂ - B ₃	B B.
B ₂ -B ₃ islanded	с	[0.997, 0.998, 0.998, 0.997, 0.998]	healthy	22 23
LLLG	a	[-0.906, -0.896, -0.887, 0.691, -0.673]	B ₄ - B ₅	
0.1Ω	b	[-0.654, -0.612, -0.583, 0.561, -0.480]	B ₄ - B ₅	B - B
B ₄ -B ₅ islanded	с	[-1.032, -1.032, -1.031, 0.918, -0.932]	B ₄ - B ₅	D_4 D_5
LG(b)	а	[0.534, -0.953, -0.912, 0.386, 0.939]	B ₁ - B ₂	
1Ω	b	[1.275, 0.767, 0.933, 1.273, 0.933]	healthy	B - B
B ₁ -B ₂ Grid	с	[0.647, 0.764, 0.928, 0.645, 0.928]	healthy	D_1 D_2
LLG(ac)	а	[0.393, 0.935, -0.788, 0.673, 0.938]	B ₂ - B ₃	
1Ω	b	[-0.357, 0.880, 1.007, -0.357, 1.006]	healthy	B - B
Grid	C.	[0.357.0.9530.856.0.724.0.937]	B B	D_2 D_3
B ₂ -B ₃	ť	[0.557, 0.755, -0.650, 0.724, 0.757]	$\mathbf{D}_2^- \mathbf{D}_3$	
LLLG	a	[0.551, 0.746, 0.819, 0.531, -0.831]	B ₄ - B ₅	
1Ω	b	[0.442, 0.588, 0.662, 0.292, -0.503]	B ₄ - B ₅	B ₄ - B ₅
Grid	C	[0 907 1 039 1 067 1 006 -1 051]	B B.	$\nu_4 \nu_5$
B_4-B_5	č		$\nu_4 \nu_5$	

$ \begin{array}{c} F_{\rm t} \\ R_{\rm f} \\ F_{\rm L} \\ O_{\rm m} \end{array} $	Р	[B ₁ , B ₂ , B ₃ , B ₄ , B ₅]	Each <i>P</i> result	Final result
LG(a)	a	[0.762, -0.981, -0.980, -0.976, -0.973]	B ₁ - B ₂	
0.3Ω	b	[-0.988, -0.987, -0.987, -0.981, -0.973]	healthy	B B
B ₁ -B ₂ islanded	с	[-0.987, -0.987, -0.987, -0.981, -0.971]	healthy	$D_1 - D_2$
LLG(ab)	а	[1.087, 1.006, -0.973, -0.990, -0.988]	B ₂ - B ₃	
0.3Ω	b	[0.310, 0.689, -0.969, -0.950, -0.944]	$B_2 - B_3$	B - B
B ₂ -B ₃ islanded	с	[-0.984, -0.984, -0.983, -0.976, -0.974]	healthy	$D_2^- D_3$
LLL	а	[-0.978, -0.977, -0.977, 0.427, -0.965]	B ₄ - B ₅	
/	b	[-0.973, -0.972, -0.971, 0.291, -0.956]	$B_4 - B_5$	ВВ
B ₄ -B ₅ islanded	с	[-0.971, -0.970, -0.970, 0.420, -0.956]	B ₄ - B ₅	$D_4 - D_5$
LG(b)	а	[-0.990, -0.990, -0.989, -0.981, -0.978]	healthy	
3Ω	b	[0.071, -1.027, -1.027, -1.152, -1.159]	B ₁ - B ₂	B B
B ₁ -B ₂ Grid	с	[-0.989, -0.989, -0.989, -0.981, -0.978]	healthy	$D_1 - D_2$
LLG(ac)	а	[0.435, 0.966, -0.979, -0.949, -0.946]	B ₂ - B ₃	
3Ω	b	[-0.976, -0.976, -0.976, -0.965, -0.961]	healthy	ВВ
Grid			Р. Р.	\mathbf{D}_2 - \mathbf{D}_3
B ₂ -B ₃	C	[0.303, 0.967, -0.979, -0.952, -0.945]	D ₂ -D ₃	
LLLG	а	[-0.977, -0.976, -0.976, 0.283, -0.965]	B ₄ - B ₅	
3Ω	b	[-0.965, -0.964, -0.963, 0.246, -0.956]	B ₄ - B ₅	B - B
Grid B ₄ -B ₅	с	[-0.962, -0.962, -0.961, 0.447, -0.956]	B ₄ - B ₅	D ₄ - D ₅

TABLE 10: The feature cosine of each bus and judgment results for the sample microgrid.



FIGURE 11: Sample microgrid whose nodes are with only loads.



FIGURE 12: Fault current peak value of B_1 in different R_f . (a) 0.01 Ω ; (b) 1 Ω ; (c) 10 Ω .

and current to calculate the differential direction; this method is found to work effectively under various case studies as discussed in this paper including different grounding resistances and faulty types. The advantage of the proposed method is that it is not needed to change the threshold to detect the faulty section location when the microgrid operation mode is changed and has unbalanced loads.

Data Availability

The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this article.

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