



Research Article

Secure and Efficient Searchable Public Key Encryption for Resource Constrained Environment Based on Pairings under Prime Order Group

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Searchable public key encryption scheme is a key technique for protecting data confidentiality in today's cloud environment. Specifically, public key encryption with conjunctive and disjunctive keyword search (PECDK) can provide flexible search options without sacrificing keywords security and thus attracts a lot of attention nowadays. However, the most effective PECDK scheme is based on the inner product encryption (IPE), which needs more time and space cost. In this paper, by utilizing the bilinear pairing with a prime order group, we propose an efficient PECDK scheme needing less time and storage consumption. The proposed scheme is proven to be secure under a rigorous security definition. The theoretical analysis and experimental results demonstrate that our proposed scheme can significantly improve the time and space efficiency over the state-of-the-art scheme.

1. Introduction

In the era of big data, more and more companies and individuals are willing to share their data over the cloud platform. If the data is stored in plaintext form, the cloud service providers can easily access and analyze the data illegally, which may lead to a big threaten to some sensitive data, e.g., electronic health and personal credit records. To protect data privacy, encrypting data before outsourcing it to the cloud server is a common approach. But, this brings a new issue of how to perform keyword search over these unreadable ciphertext. A straightforward solution is to download all the encrypted data to the client and decrypt it. After obtaining all unencrypted data, users can utilize the common information retrieval technique used on the plaintext to perform keywords query. However, this approach requires a very high communication, storage, and computing costs, which are not applicable for large scale networks. This issue put forward a new challenge: how to effectively search for encrypted data without decrypting it first.

Searchable encryption (SE) is a promising method to address this problem. SE can be classified into two categories according to its applications: searchable symmetric key encryption (SSE) and searchable public key encryption (SPE). Based on many researchers' work these years, SSE can support advanced query conditions like Boolean keywords search, multikeywords rank search, and top- k similarity keywords search. Works [1–3] dealt with multikeywords search, where the query condition contains more than one keyword. Considering the fact that it is not practical to return all the search results, more recent works like [4–6] focused on the multikeywords rank search. Sometimes, users want to search documents related to their query keywords rather than the documents that precisely match those keywords. The SSE schemes supporting similarity keywords search were created to address this issue [7, 8].

Conversely, SPE is difficult to support advanced search function without sacrificing security as anyone who has the public key (pk) can create encrypted index or ciphertext, and easily perform chosen keywords attack. In addition, the SSE scheme is generally more efficient than the SPE scheme.

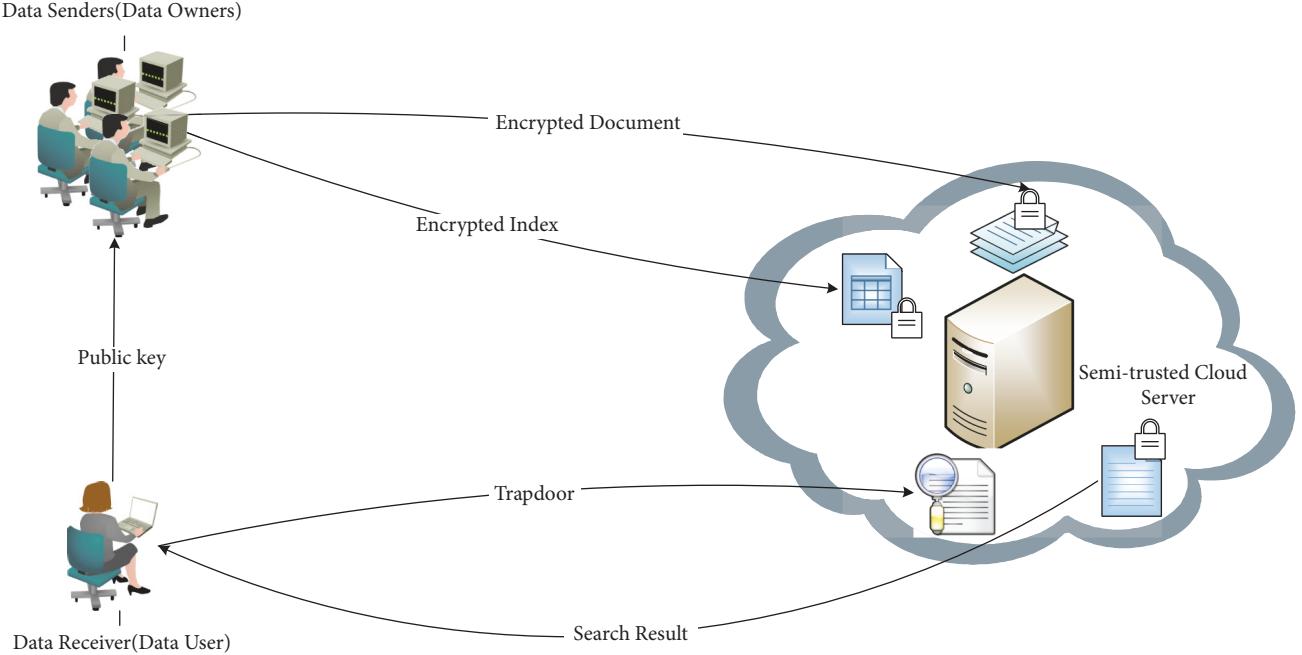


FIGURE 1: Architecture of searchable public key encryption (SPE).

Although the SPE scheme has these weaknesses, it still holds some advantages for many applications. Specifically, for the application in which there are many data senders and only one data receiver (Figure 1), SSE needs that all senders and the receiver hold the same symmetric key to generate the encrypted data. So, if one of the senders is compromised by an adversary, then the data for all senders will be leaked. Compared with SSE, in SPE, the public key can be accessed by all senders, and the private key is only given to the receiver. Thus, SPE can naturally solve the security problem of key management in this application [9] and is an irreplaceable solution.

The first SPE named as public key encryption with keyword search (PEKS) was introduced in [10], in which senders who hold pk can send their encrypted documents with encrypted indexes to a server, and the receiver holding secret key (sk) can make a keyword search over the encrypted data. However, this scheme only supports a single keyword search. How to construct a public key encryption scheme supporting a complex query conditions such as the Boolean keyword search is a significant problem. Specifically, as two typical Boolean keyword search schemes, conjunctive and disjunctive keyword search over encrypted data in the public key setting are needed to be developed.

Park et al. [11] first proposed the public key encryption with conjunctive keyword search (PECK) scheme that supports keywords search like $w_1 \wedge w_2 \wedge w_3$, where w_1, w_2 and w_3 are query words. After that, many PECK schemes [12, 13] were proposed to improve the efficiency and security. The first public key encryption with disjunctive keyword search (PEDK) scheme was proposed by Katz et al. [14]. In their work, they proposed an inner product encryption (IPE) scheme and converted this IPE scheme into a PEDK scheme,

which supports keywords search like $w_1 \vee w_2 \vee w_3$. In an IPE scheme, the secret key corresponding to a predicate vector \vec{v} can decrypt the ciphertext associated with an attribute vector \vec{x} if and only if $\vec{x} \cdot \vec{v} = 0$. According to this property, we know that, by converting index and query keyword set into an attribute and a predicate vector, respectively, an IPE scheme can be changed into a SPE scheme supporting multikeywords search.

In the practical cloud environment, the user usually perform conjunctive and disjunctive keywords search simultaneously. In [15], Zhang and Lu proposed an approach of converting an IPE scheme into a public key encryption with conjunctive and disjunctive keyword search (PECDK) scheme and gave a concrete scheme. In their scheme, the size of each document's index, the size of a trapdoor, and the time cost of pairing operations in the test process are all $O(N)$. Since N is the number of keywords in a dictionary, the previous PECDK scheme is impractical if N is a large integer. Inspired by this problem, we proposed a new approach to build an efficient PECDK scheme with less time and space overhead [16]. However, these two PECDK schemes are based on the IPE scheme [17], which is a costly cryptographic prototype. In this paper, we aim to build an efficient PECDK scheme using an alternative method.

Main Works. In the scheme introduced in [17], the user first converts an index and a query keyword set into an attribute and a predicate vector, respectively. After this, the user can construct encrypted index and trapdoor by applying the attribute and predicate vectors to the encryption and key generation algorithms of IPE. The keyword search process can be executed by adopting the decryption algorithm of IPE. However, this scheme is constructed by utilizing many group operations due to being based on the IPE scheme. The

IPE scheme adopts a technique called dual pairing vector space (DPVS), which generates n^2 group elements to create the public key and secret key. By using these keys, both the storage size of the obtained indices and the time cost of the search process are linear with $O(n^2)$. To address this issue, we aim to create an efficient PECDK scheme without using IPE as the infrastructure. We take advantage of the conversion method similar to the one introduced in [16] for creating a group of vectors. Then, by applying these vectors to the prime order pairing groups, a PECDK scheme with a better time and space complexity than the previous schemes is presented. Security of our construction is based on decision linear Diffie-Hellman (DLIN) assumption in the random oracle model. In addition, we design an experiment that verifies the efficiency of the proposed scheme and give a detailed comparison with the previous scheme. The experiment result shows that the key generation, index building, trapdoor generation, and testing algorithms in our scheme are more efficient than those in the previous one. Besides, the space cost for indices in our scheme is also less than that in the previous one. In practice, client device, e.g., a mobile device, has less storage space and limited computation capacity. Thus, compared with the previous scheme, ours is much more suitable for the resource constrained environment.

Related Work. There are two classes of searchable encryption schemes in terms of different cryptography primitives: searchable symmetric key encryption (SSE) and searchable public key encryption (SPE).

SSE. Song et al. [18] introduced the definition of searching on encrypted data and gave a concrete scheme. Then, Goh [19] defined a formal security definition for SSE and presented an effective conjunctive keywords search scheme by using a technique called Bloom Filter. Soon afterward, many works [20, 21] were constructed to improve the search efficiency and security level. These schemes failed to achieve a sublinear search speed. To address this issue, by taking advantage of tree structures, such as r-tree and kd-tree, SSE schemes with sublinear search time were released in [22, 23]. The SSE scheme supporting Boolean keywords search with sublinear search time was given in [24]. In order to support queries with rich expressiveness, SSE schemes supporting media data and similarity keywords search are introduced in [25, 26]. More important, these works also support dynamic update. In practical application, the search engine should return the top- k related documents to users instead of returning all the search results. Some SSE schemes, supporting rank search, are proposed in [4–6] to obtain more accurate query results.

SPE. The first SPE scheme is called public key encryption with keyword search (PEKS), which was proposed by Boneh et al. [10]. Then, Abdalla et al. [27] defined the computational and statistical consistency in PEKS and presented a statistically consistent scheme. However, this work only supports a single keyword search. The concept of PECK was first proposed in [11]. They defined the security model of this mechanism and gave two constructions. One requires many bilinear pairing operations, while the other needs more private keys. Hwang and Lee [28] designed a more

efficient scheme in a multiple users setting. However, all these constructions use the keyword field as additional information for keyword search. The keyword field may leak more information to the public. To eliminate the keyword field, Boneh and Waters [29] presented a public key encryption scheme called hidden vector encryption (HVE), which supports a conjunctive search, comparison queries ($x \geq a$), and subset queries ($x \in S$) on encrypted data.

In order to create a SPE scheme supporting disjunctive keyword search, Katz et al. [14] proposed a public key encryption scheme called inner product encryption (IPE), which is related to the attribute-based encryption (ABE) [30, 31]. Recently, in order to better utilize the encrypted data and improve the security, some public key schemes which can support verifiable attribute-based search over outsourced encrypted data are proposed in [32–37]. For supporting advanced keywords search function, Zhang and Lu proposed the first PECDK scheme [15] by combining an efficient IPE scheme [17] and a keyword conversion method. However, their scheme is a costly solution due to using an IPE scheme. In fact, the PECDK scheme based on an IPE scheme needs more computation and storage cost than the one without utilizing an IPE scheme as a foundation. Therefore, in this paper, we will find a new method irrelevant to IPE to construct a more efficient PECDK scheme.

Organization. The remainder of the paper is organized as follows: The model and security definitions of PECDK are defined in Section 2. In Section 3, we propose our PECDK scheme and give the security proof for the scheme. The analysis of the presented PECDK scheme is described in Section 4. Section 5 presents some conclusions.

2. Preliminaries

In this section, we will give a formal definition of the PECDK model and the corresponding security model. Our scheme is based on this model and proven to be secure under this security model. Moreover, we also briefly introduce some basic ingredients used to create our scheme, including the bilinear pairing and the complexity assumption.

2.1. Model of PECDK. In PECDK, let pk, sk be the receiver's public key and secret key. When a sender wants to send a message M to a receiver with keywords w_1, w_2, \dots, w_n , she uses the standard public key encryption system to encrypt M and uses pk and keywords w_1, w_2, \dots, w_n to construct the encrypted index of M . After that, she sends the encrypted message M and the encrypted index of M to the server. When the receiver wants to retrieve messages including a specific list of keywords, he takes the sk , a symbol, and keyword set Q as input to construct a trapdoor T_Q and sends T_Q to the server. Note that the symbol is used to refer to the type of query, e.g., conjunctive form or disjunctive form. When the server receives the trapdoor, it tests each encrypted index by using the trapdoor and returns the matched messages to the receiver.

According to the description above, we give the model of PECDK based on the previous definition introduced in [16].

Definition 1. There are four probabilistic polynomial time algorithms in the PECDK scheme. There are KenGen, IndexBuild, Trapdoor, and Test:

- (1) *KeyGen*(1 γ): choosing a security parameter γ , this algorithm outputs the key pair (pk, sk) in which pk is the public key and sk is the secret key.
- (2) *IndexBuild*(pk, W): the algorithm is performed by the sender to produce an encrypted index I_W by using a keyword set $W = \{w_1, w_2, \dots, w_n\}$ and pk .
- (3) *Trapdoor*($sk, \{Q, sym\}$): the receiver runs this algorithm to produce a trapdoor. It takes $sk, sym \in \{\vee, \wedge\}$, and the keyword query $Q = \{q_1, q_2, \dots, q_m\}$ as input to generate a trapdoor T_Q , where $m \leq n$. \vee and \wedge represent disjunctive and conjunctive keywords search, respectively.
- (4) *Test*(pk, T_Q, I_W): it takes the trapdoor $T_Q = \{t_Q, sym\}$, the secure index I_W , and the public key pk as input. If sym is \wedge , it means that the trapdoor is for conjunctive keywords search. In this case, the output is 1 if $Q \subseteq W$, or 0 otherwise. If sym is \vee , disjunctive keywords search should be performed. In this case, if $Q \cap W \neq \emptyset$, it outputs 1, or 0 otherwise.

Correctness Property. Let $\{Q, sym\}$ and W be a query and a keyword set, respectively. Suppose that pk, sk, I_W , and T_Q are correctly generated by *KeyGen*(γ), *IndexBuild*(pk, W), and *Trapdoor*($sk, \{Q, sym\}$), respectively. The correctness property of PECDK involves two situations described as follows.

- (1) When there is a conjunctive keywords search (sym is \wedge), $Test(pk, T_Q, I_W) = 1$ holds if $Q \subseteq W$. Otherwise, it holds with negligible probability.
- (2) When there is a disjunctive keywords search (sym is \vee), $Test(pk, T_Q, I_W) = 1$ holds if $Q \cap W \neq \emptyset$. Otherwise, it holds with negligible probability.

In practical use, if a sender would like to send a message M with keyword set W , a ciphertext with the form of $\{Enc(pk, M), IndexBuild(pk, W)\}$ will be created, where $Enc(\cdot)$ is a frequently used public key encryption scheme, e.g., RSA. Similar with other related works [10, 11, 28], the proposal only concentrate on searchable encryption part, which is PECDK in this paper.

2.2. Security Definition of PECDK. Since previous PECDK schemes are based on the IPE scheme, the security definition also depends on the security of IPE. For the PECDK scheme without using IPE, we need to give a new security definition. Inspired by the previous security definition called indistinguishability of ciphertext from random (IND-CR-CKA) introduced in [28], we define a security game under the PECDK model.

The security game is described as follows.

- (1) **Setup:** the challenger \mathbb{C} runs the *KeyGen*(1 γ) algorithm to generate the public key pk and the secret key sk . Then, \mathbb{C} gives pk to the attacker \mathbb{A} .
- (2) **Phase 1:** the attacker \mathbb{A} can adaptively ask the challenger \mathbb{C} for the trapdoor T_Q for any query Q of his choice.
- (3) **Challenge:** \mathbb{A} selects a target keyword set W^* and sends it to \mathbb{C} . After receiving W^* , \mathbb{C} selects a random keyword set R and sets $W^0 = W^*$ and $W^1 = R$. Suppose that $\{Q_1, sym_1\}, \{Q_2, sym_2\}, \dots, \{Q_t, sym_t\}$ are queries which are asked to construct trapdoors in Phase 1, where t is the number of trapdoors queried in Phase 1. For each $i \in [1, t]$, the only restriction is that $|Q_i \cap W^0| = 0 = |Q_i \cap W^1|$, where the number of the keywords in $Q_i \cap W^0$ and $Q_i \cap W^1$ is denoted by $|Q_i \cap W^0|$ and $|Q_i \cap W^1|$, respectively. Then, \mathbb{C} picks a random bit $\beta \in \{0, 1\}$, produces $I_\beta = IndexBuild(pk, W^\beta)$, and sends $\{I_\beta, W^0, W^1\}$ to \mathbb{A} .
- (4) **Phase 2:** \mathbb{A} can continue to ask for trapdoor T_Q for any query Q of his choice, and subject to the same restriction as before.
- (5) **Response:** \mathbb{A} outputs $\beta' \in \{0, 1\}$ and wins the game if $\beta' = \beta$.

\mathbb{A} 's advantage can be expressed as a function of the security parameter (1 γ):

$$Adv_A^{Game}(1^\gamma) = \left| Pr[\beta' = \beta] - \frac{1}{2} \right| \quad (1)$$

Then, we have the following definition.

Definition 2. According to the game above, a PECDK is semantic secure if, for any probabilistic polynomial time attacker \mathbb{A} , the function $Adv_A^{Game}(1^\gamma)$ is negligible.

2.3. Bilinear Pairings. Let G_1, G_2 be two cyclic groups of prime order q . There are three properties in the bilinear pairings map $\hat{e} : G_1 \times G_1 \rightarrow G_2$.

- (1) **Bilinear:** $\hat{e}(a^u, b^v) = \hat{e}(a, b)^{uv}$, where $a, b \in G_1$ and $u, v \in \mathbb{Z}_q^*$.
- (2) **Nondegenerate:** if $g \in G_1$, then $\hat{e}(g, g) \in G_2$.
- (3) **Computable:** for any $a, b \in G_1$, $\hat{e}(a, b)$ can be efficiently computable.

An efficient bilinear map can be obtained by applying the Weil pairing or the Tate pairing [38].

2.4. Complexity Assumption. We review the complexity assumption named Decision 1 Bilinear Diffie-Hellman Inversion (Decision 1-BDHI) assumption [11], which is related to the bilinear pairing. The security of our scheme is based on this assumption.

Decision l-BDHI Assumption: Given a tuple $D = \{g, g^x, g^{x^2}, \dots, g^{x^l}\}$ with the random choice of $x \in Z_q^*$ and $g \in G_1$, it is argued that an algorithm \mathbb{C} outputting $b \in \{0, 1\}$ has advantage ε in solving the *decision l-BDHI* problem in G_1 if

$$\begin{aligned} Adv_B^{D-l-BDHI} \\ &= \left| \Pr[B(D, \hat{e}(g, g)^{1/x}) = 1] - \Pr[B(D, R) = 1] \right| \quad (2) \\ &\geq \varepsilon \end{aligned}$$

where the probability ($\Pr[\cdot]$) is over the random choice $R \in G_2$ and random bits chosen by \mathbb{C} .

Definition 3. The Decision l-BDHI assumption holds in G_1 , if no probabilistic polynomial time algorithm has advantage at least ε in solving the Decision l-BDHI problem in G_1 .

3. PECDK Scheme

Based on previous definitions and notations, in this section, we give our PECDK scheme without using IPE. Our scheme mainly involves three steps. Initially, we utilize a keyword conversion method inspired by the approach introduced in [16] to convert the index and query keywords into a set of vectors. Moreover, by applying the bilinear pairing under the prime order group, we encrypt these vectors to construct encrypted index and trapdoor. Eventually, a test algorithm is built to perform secure keywords query. The method adopted in the first step is described in Section 3.1, and the algorithms used in the second and third steps are given in Section 3.2.

3.1. Keywords Conversion Method. The keywords in query and index are strings; thus we need to change all the keywords to a group of integers. Moreover, in order to verify whether the query matches the index or not, the integers between the query and index must hold some relationships. According to these concerns, we introduce a method that can convert the index and query set into a matrix and a vector.

This method is based on the relationship between the roots and coefficients in an equation of degree n with one unknown. Specifically, the roots and coefficients are used to create a matrix of index keywords and a vector of query keywords, respectively. By adopting a prime order group to encrypt the matrix and vector, an encrypted index and query can be built. The relationship between the matrix and vector can be utilized to construct the test algorithm.

Suppose that any keyword w can be expressed as $\{0, 1\}^*$; we define a function $H_1 : \{0, 1\}^* \rightarrow Z_p^*$. Since p is a large prime and is larger than the number of all words, H_1 can be collision-resistance. This means that, if $i \neq j$, then $H_1(w_i) \neq H_1(w_j)$, where w_i and w_j are two distinct keywords. Let $W = \{w_1, w_2, \dots, w_n\}$ and $Q = \{q_1, q_2, \dots, q_m\}$ be two keyword sets, where $m < n$. The method can be listed into three steps and described as follows.

(1) For the keyword set $W = \{w_1, w_2, \dots, w_n\}$, we construct a matrix for W :

$$\begin{pmatrix} H_1(w_1)^0 & H_1(w_1)^1 & \cdots & H_1(w_1)^n \\ H_1(w_2)^0 & H_1(w_2)^1 & \cdots & H_1(w_2)^n \\ \vdots & \vdots & \ddots & \vdots \\ H_1(w_n)^0 & H_1(w_n)^1 & \cdots & H_1(w_n)^n \end{pmatrix} \quad (3)$$

Note that $H_1(w_1), H_1(w_2), \dots, H_1(w_n)$ can be seen as the roots of equation:

$$f(x) = (x - H_1(w_1))(x - H_1(w_2)) \dots (x - H_1(w_n)) \quad (4)$$

(2) For the query $\{q_1, q_2, \dots, q_m\}$, we create an equation:

$$\begin{aligned} f(x) &= (x - H_1(q_1))(x - H_1(q_2)) \dots (x - H_1(q_m)) \\ &= a_m x^m + a_{m-1} x^{m-1} + \dots + a_0 x^0 \end{aligned} \quad (5)$$

According to the coefficient of the $f(x)$, a vector $\vec{a} = \{a_0, a_1, \dots, a_m\}$ can be obtained.

(3) Suppose that $\vec{w}_i = \{H_1(w_i)^0, H_1(w_i)^1, \dots, H_1(w_i)^n\}$ is from the i -th row of the matrix (3); we can infer that if there is a keyword $w_i \in W$ such that $w_i \in Q$, where $i \in [1, m]$, according to (5), it is not difficult to verify that $\vec{a} \cdot \vec{w}_i = 0$. Based on this property, we can build the test algorithm.

3.2. Construction of PECDK. By combining the keyword conversion method and the bilinear pairing under prime order group, we propose a PECDK scheme which allows the user to perform conjunctive and disjunctive keyword search over encrypted data. Our key idea is as follows. First, by adopting the keyword conversion method introduced in Section 3.1, we change the index and query keyword set into an index matrix and a query vector, respectively. Then, by using a set of elements randomly chosen from the prime order group, we encrypt the index matrix to the secure index and the query vector to the trapdoor, respectively. Specifically, in order to guarantee the scheme's security, the encryption process relies strictly on the complexity assumption given in Section 2.4. Finally, by taking advantage of the properties of the bilinear pairing, both conjunctive and disjunctive keywords search can be achieved. Specifically, for the conjunctive keywords search, the matched documents are returned if and only if all the keywords in the query are including in the index keyword set. For the disjunctive logic query, the matched documents are returned if and only if the intersection between the index and the query keyword set is not an empty set.

According to the above ideas, the concrete construction is proposed in the following paragraphs. Because of making use of the prime order group, the proposed scheme is more efficient than the previous scheme adopting the IPE cryptosystem on the time and space complexities. Experimental results showing the advantages of our scheme can be found in Section 4.

- (i) *KeyGen*(1^γ): given a security parameter γ , the algorithm generates two cyclic groups G_1, G_2 of prime order q and a bilinear pairing $\hat{e} : G_1 \times G_1 \rightarrow G_2$. It picks a random generator g of G_1 and two hash functions $H_1 : \{0, 1\}^* \rightarrow Z_q^*$ and $H_2 : G_2 \rightarrow \{0, 1\}^{\log_2 q}$. Choosing $2n + 3$ random numbers $\alpha_0, \alpha_1, \dots, \alpha_n, \beta_0, \beta_1, \dots, \beta_n, \theta \in Z_q^*$, it computes $\{X_0 = g^{\alpha_0}, X_1 = g^{\alpha_1}, \dots, X_n = g^{\alpha_n}, Y_0 = g^{\beta_0}, Y_1 = g^{\beta_1}, \dots, Y_n = g^{\beta_n}, Z = g^\theta, \mu = \hat{e}(g, g)\}$. After this, it outputs the public key $pk = \{X_0, X_1, \dots, X_n, Y_0, Y_1, \dots, Y_n, Z, \mu, g, H_1, H_2, \hat{e}\}$ and the secret key $sk = \{\alpha_0, \alpha_1, \dots, \alpha_n, \beta_0, \beta_1, \dots, \beta_n, \theta\}$, where pk is also open to the public.
- (ii) *IndexBuild*(pk, W): the algorithm generates $n^2 + 2n$ random numbers r_1, r_2, \dots, r_n and $u_{ij} \in Z_q^*$, where $i \in [1, n], j \in [0, n]$. Given a keyword set $W = \{w_1, w_2, \dots, w_n\}$ and the public key pk , for each word $w_i \in W$, it computes $A_{ij} = X_j^{r_i} \times g^{r_i H_1(w_i)^j + u_{ij}}, B_{ij} = Y_j^{u_{ij}}, C_i = Z^{r_i} = g^{\theta r_i}$ and $D_i = H_2(\mu^{r_i})$, where $i \in [1, n]$ and $j \in [0, n]$. The index of the keyword set W is

$$I_W = \begin{pmatrix} A_{10} & A_{11} & \dots & A_{1n} & B_{10} & B_{11} & \dots & B_{1n} & C_1 & D_1 \\ A_{20} & A_{21} & \dots & A_{2n} & B_{20} & B_{21} & \dots & B_{2n} & C_2 & D_2 \\ \vdots & \vdots \\ A_{n0} & A_{n1} & \dots & A_{nn} & B_{n0} & B_{n1} & \dots & B_{nn} & C_n & D_n \end{pmatrix} \quad (6)$$

Note that the secure index can be seen as an encrypted version of matrix (3).

- (iii) *Trapdoor*($sk, \{Q, sym\}$): when the algorithm receives a keyword query $Q = \{q_1, q_2, \dots, q_m\}$, where $m \leq n$, it will construct a vector $\vec{a} = \{a_m, a_{m-1}, \dots, a_0\}$ by utilizing (5). Given a vector \vec{a} and sk , $t_{1j} = g^{a_j / (\sum_{j=0}^m \alpha_j a_j + \sum_{j=0}^m a_j u \theta)}$ and $t_{2j} = t_{1j}^{1/\beta_j}$ can be computed, where u is a random number in Z_q^* and $j \in [0, m]$. Let $t_3 = u$ and $sym \in \{\vee, \wedge\}$; the trapdoor for the keyword query Q is $T_Q = (t_{10}, t_{11}, \dots, t_{1m}, t_{20}, t_{21}, \dots, t_{2m}, t_3, sym)$.
- (iv) *Test*(pk, T_Q, I_W): when the algorithm receives a trapdoor T_Q and a secure index I_W , it works as follows:

- (1) If the symbol in T_Q is \vee ,
- The algorithm chooses a counter i and sets $i = 1$.
 - If $i > n$, then it goes to step (c); otherwise it checks whether $H_2(test_{i1}/test_{i2}) = D_i$, where $test_{i1} = \prod_{j=0}^m \hat{e}(t_{1j}, A_{ij} C_i^{t_3}), test_{i2} = \prod_{j=0}^m \hat{e}(t_{2j}, B_{ij})$. If so, the algorithm outputs 1 and ends. Otherwise, it sets $i = i + 1$ and goes to step (b).
 - The algorithm outputs 0 and ends.

- (2) If the symbol in T_Q is \wedge ,
- The algorithm chooses two counters i and j and sets $i = 1$ and $j = 1$.
 - If $i > n$, then it goes to step (c); otherwise it tests whether $H_2(test_{i1}/test_{i2}) = D_i$, where $test_{i1} = \prod_{j=0}^m \hat{e}(t_{1j}, A_{ij} C_i^{t_3}), test_{i2} = \prod_{j=0}^m \hat{e}(t_{2j}, B_{ij})$. If so, then the algorithm sets $j = j + 1$. Otherwise, it does nothing. After that, it sets $i = i + 1$ and goes to step (b).
 - If $j = m$, the algorithm outputs 1 and ends. Otherwise, it outputs 0 and ends.

Correctness. The key idea of disjunctive keywords search is to determine whether there exists an $i \in [1, n]$ such that $w_i \in Q$. For the conjunctive keywords search, we need to check whether there are m keywords $w_{\phi(1)}, w_{\phi(2)}, \dots, w_{\phi(m)}$ such that $w_{\phi(j)} \in Q$, where $\phi(j) \in [1, n]$ and $j \in [1, m]$. According to these ideas, we know that the essence of test algorithm is to verify whether $w_i \in Q$. In the proposed scheme, it is can be verified that $test_{i1}/test_{i2} = \hat{e}(g, g)^{r_i + r_i \sum_{j=0}^m a_j H_1(w_i)^j / (\sum_{j=0}^m \alpha_j a_j + \sum_{j=0}^m a_j u \theta)}$. If $w_i \in Q$, there is $\sum_{j=0}^m a_j H_1(w_i)^j = 0$. Thus, it must be $test_{i1}/test_{i2} = \hat{e}(g, g)^{r_i}$ and $H_2(test_{i1}/test_{i2}) = D_i$. Based on this, we argue that our scheme is correct.

3.3. Security Analysis

Theorem 4. *The proposed PECDK scheme is secure according to security definition in the random model if Decision ($q_T + 1$)-BDHI is hard.*

Proof. Suppose that an algorithm \mathbb{A} has advantage ε in breaking the PECDK under the security definition. Suppose \mathbb{A} makes at most q_T trapdoor queries, we can build an algorithm \mathbb{C} which solves the decision $(q_T + 1)$ -BDHI assumption with a probability at least $\varepsilon' = \varepsilon/e(nq_T + 1)$, where e is the base of the natural logarithm, and n is the number of keywords in an index. Let g be a generator of G_1 . Given $g, g^x, g^{x^2}, \dots, g^{x^{q_T+1}}, R$, if $R = \hat{e}(g, g)^{1/x}$, the algorithm \mathbb{C} outputs 1, 0 otherwise. The interaction between the algorithm \mathbb{C} and the algorithm \mathbb{A} is as follows:

- (i) *Setup*: the algorithm \mathbb{C} works as follows:

- The algorithm \mathbb{C} randomly chooses q_T numbers $\rho_1, \rho_2, \dots, \rho_{q_T} \in Z_q^*$ and returns $f(z) = \prod_{i=1}^{q_T} (z + \rho_i) = \sum_{i=0}^{q_T} c_i z^i$.
- \mathbb{C} computes $U = g^{f(x)} = g^{\sum_{i=0}^{q_T} c_i x^i}, V = g^{x f(x)} = g^{\sum_{i=0}^{q_T} c_i x^{i+1}}$, and $f_i(z) = (1/(z + \rho_i))f(z) = \sum_{i=0}^{q_T-1} d_i z^i$, where $i \in [1, q_T]$. Then, \mathbb{C} gets $U^{1/(x+\rho_i)} = g^{f_i(x)} = g^{\sum_{i=0}^{q_T-1} d_i x^i}$ and stores the pairs $\{\rho_i, g^{f_i(x)}\}$ in a list named *S-list*, where $i \in [1, q_T]$.

- (3) \mathbb{C} computes $(f(z) - c_0)/z = \sum_{i=1}^{q_T} c_i z^{i-1}$ and sets $R_U = \widehat{e}(g^{\sum_{i=1}^{q_T} c_i x^{i-1}}, g^{\sum_{i=0}^{q_T} c_i x^i + c_0}) \times R^{c_0^2}$. If $R = \widehat{e}(g, g)^{1/x}$, $R_U = \widehat{e}(g^{\sum_{i=1}^{q_T} c_i x^{i-1}}, g^{\sum_{i=0}^{q_T} c_i x^i + c_0}) \times R^{c_0^2} = \widehat{e}(g^{(f(x)-c_0)/x}, g^{f(x)+c_0}) \times R^{c_0^2} = \widehat{e}(g, g)^{(f^2(x)-c_0^2)/x} \times \widehat{e}(g, g)^{c_0^2/x} = \widehat{e}(g, g)^{f^2(x)/x} = \widehat{e}(U, U)^{1/x}$.
- (4) \mathbb{C} randomly chooses $2n + 4$ numbers $s_0, s_1, \dots, s_n, t_0, t_1, \dots, t_n, \eta, \lambda \in Z_q^*$ and constructs $X_i = V^{s_i} \times U^{-\eta^i}, Y_i = U^{t_i}$ for each $i \in [0, n]$. Let $Z = V^\lambda$, \mathbb{C} gives \mathbb{A} the public key $pk = \{U, X_0, X_1, \dots, X_n, Y_0, Y_1, \dots, Y_n, Z, \mu = \widehat{e}(U, U), g, H_1, H_2, \widehat{e}\}$. The corresponding sk is $\{s_0 x - \eta^0, s_1 x - \eta^1, \dots, s_n x - \eta^n, t_0, t_1, \dots, t_n, \lambda x\}$, where the values $\{s_0 x - \eta^0, s_1 x - \eta^1, \dots, s_n x - \eta^n, \lambda x\}$ are unknown to \mathbb{C} .
- (ii) H_1, H_2 -queries: the random oracles H_1 or H_2 can be queried by \mathbb{A} at any time. To answer H_1 -queries, \mathbb{C} keeps a list of tuples (w_j, h_j, σ_j) called H_1 -list which is empty initially. When \mathbb{A} queries the random oracle H_1 at a point $w_i \in \{0, 1\}^*$, algorithm \mathbb{C} answers as follows:

H_1 -queries:

- (1) If the query w_i is already in a tuple (w_i, h_i, σ_i) on H_1 -list, then \mathbb{C} responds with $H_1(w_i) = h_i$, where $h_i \in Z_q^*$.
- (2) Otherwise, \mathbb{C} generates a random coin $\sigma_i \in [0, nq_T]$ so that $Pr[\sigma_i = 0] = 1/(nq_T + 1)$.
- (3) If $\sigma_i = 0$, \mathbb{C} sets $h_i = \eta$. Otherwise, \mathbb{C} picks a random $a_i \in Z_q^*$ and sets $h_i = a_i$.
- (4) \mathbb{C} adds the tuple (w_i, h_i, σ_i) to H_1 -list and answers \mathbb{A} with $H_1(w_i) = h_i$.

H_2 -queries are similar to H_1 -queries. To answer H_2 queries from \mathbb{A} , \mathbb{C} holds a list of tuples (φ_j, ψ_j) called H_2 -list which is initially empty. When \mathbb{A} queries the random oracle H_2 at a point $\varphi_i \in G_2$, algorithm \mathbb{C} responds as follows:

H_2 -queries:

- (1) If the query φ_i already appears on H_2 -list in a tuple (φ_i, ψ_i) , then \mathbb{C} responds with $H_2(\varphi_i) = \psi_i$, where $\psi_i \in \{0, 1\}^{\log_2 q}$.
 - (2) Otherwise, \mathbb{C} picks a random $b_i \in \{0, 1\}^{\log_2 q}$ and sets $\psi_i = b_i$.
 - (3) \mathbb{C} adds the tuple (φ_i, ψ_i) to H_2 -list and responds \mathbb{A} with $H_2(\varphi_i) = \psi_i$.
- (iii) Trapdoor queries: when \mathbb{A} queries a trapdoor of the keyword set $Q_i = \{q_{i1}, q_{i2}, \dots, q_{im}\}$ and sym , the algorithm \mathbb{C} answers as follows:

- (1) \mathbb{C} runs H_1 -queries algorithm to obtain h_{ij} , where $h_{ij} = H_1(q_{ij})$ for each $j \in [1, m]$. Let

$(w_{ij}, h_{ij}, \sigma_{ij})$ be the corresponding tuples on H_1 -list, for each $j \in [1, m]$; if $\sigma_{ij} = 0$, then \mathbb{C} reports failure and terminates.

- (2) Otherwise, \mathbb{C} constructs a trapdoor for query $\{Q_i, sym\}$. \mathbb{C} first computes $f'(x') = \prod_{i=1}^m (x' + h_{ij}) = a'_m x'^m + a'_{m-1} x'^{m-1} + \dots + a'_1 x' + a'_0$. Then, for each $j \in [0, m]$, \mathbb{C} can compute $l_{ij} = -(\sum_{j=0}^m a'_j \eta^j)/a'_j \rho_i$ and $v_i = -(\sum_{j=0}^m a'_j \eta^j + \rho_i \sum_{j=0}^m a'_j s_j)/\rho_i \lambda \sum_{j=0}^m a'_j$ through an equality of $1/(x' + \rho_i) = a'_j l_{ij}/(\sum_{j=0}^m a'_j (s_j x' - \eta^j) + v_i \lambda \sum_{j=0}^m a'_j x')$. Obviously, $(U^{1/(x'+\rho_i)l_{i0}}, U^{1/(x'+\rho_i)l_{i1}}, \dots, U^{1/(x'+\rho_i)l_{im}}, U^{1/(x'+\rho_i)l_{i0}t_0}, U^{1/(x'+\rho_i)l_{i1}t_1}, \dots, U^{1/(x'+\rho_i)l_{im}t_m}, v_i, sym)$ is the trapdoor for the keyword query Q_i .
- (3) \mathbb{C} searches S-list to obtain the tuple $\{\rho_i, g^{f_i(x')}\}$. Then \mathbb{C} sends $(g^{f_i(x')/l_{i0}}, g^{f_i(x')/l_{i1}}, \dots, g^{f_i(x')/l_{im}}, g^{f_i(x')/l_{i0}t_0}, g^{f_i(x')/l_{i1}t_1}, \dots, g^{f_i(x')/l_{im}t_m}, v_i, sym)$ to the algorithm \mathbb{A} as the correct trapdoor for the query Q_i
- (iv) Challenge: algorithm \mathbb{A} produces a keyword set $W^* = \{w_{01}, w_{02}, \dots, w_{0n}\}$, which is what \mathbb{A} wants to challenge. Then, \mathbb{A} sends the target keyword set W^* to \mathbb{C} . \mathbb{C} chooses a random keyword set $R' = \{w_{11}, w_{12}, \dots, w_{1n}\}$ and sets $W^0 = W^*$ and $W^1 = R'$. The only restriction is that the previous trapdoor queries cannot distinguish W^0 and W^1 . If there is any previous trapdoor that can break the restriction, \mathbb{C} regenerates the keyword set W^1 . Then \mathbb{C} selects a random bit $\beta \in \{0, 1\}$ and runs the above algorithm for responding to H_1 -queries to obtain the values $h_{\beta 1}, h_{\beta 2}, \dots, h_{\beta n}$, where $H_1(w_{\beta i}) = h_{\beta i}, w_{\beta i} \in W^\beta, i \in [1, n]$. Let $(w_{\beta i}, h_{\beta i}, \sigma_{\beta i})$ be the corresponding tuples on H_1 -list, if there is no $\sigma_{\beta i} = 0$ for all $i \in [1, n]$, then \mathbb{C} terminates. Otherwise, \mathbb{C} generates the challenge PECDK index I_β of W^β as follows:
 - (1) If $\sigma_{\beta i} = 0$, \mathbb{C} computes $A_{\beta ij} = U^{r_{\beta i}s_j + y_{\beta ij}}$, $B_{\beta ij} = U^{t_j y_{\beta ij}}$, $C_{\beta i} = U^{r_{\beta i}\lambda}$, and $D_{\beta i} = H_2(R_U^{r_{\beta i}})$, where $j \in [0, n]$. Observe that if $R = \widehat{e}(g, g)^{1/x}$, then $R_U = \widehat{e}(U, U)^{1/x}$. So, the above values are equivalent to $A_{\beta ij} = X_j^{r_{\beta i}/x} \times U^{r_{\beta i}\eta^j/x + y_{\beta ij}}$, $B_{\beta ij} = Y_j^{y_{\beta ij}}$, $C_{\beta i} = Z^{r_{\beta i}/x}$, and $D_{\beta i} = H_2(\widehat{e}(U, U)^{r_{\beta i}/x})$, where $j \in [0, n]$. It means that this is a valid PECDK encryption of keyword $w_{\beta i}$ when $R = \widehat{e}(g, g)^{1/x}$.
 - (2) Otherwise, \mathbb{C} computes $A_{\beta ij} = V^{r_{\beta i}s_j} \times U^{r_{\beta i}h_{\beta i}^j + y_{\beta ij} - r_{\beta i}\eta^j}$, $B_{\beta ij} = U^{t_j y_{\beta ij}}$, $C_{\beta i} = V^{r_{\beta i}\lambda}$, $D_{\beta i} = H_2(\widehat{e}(U, U)^{r_{\beta i}})$, where $j \in [0, n]$.

(3) \mathbb{C} sends

$$I_\beta = \begin{pmatrix} A_{\beta 10} & A_{\beta 11} & \dots & A_{\beta 1n} & B_{\beta 10} & B_{\beta 11} & \dots & B_{\beta 1n} & C_{\beta 1} & D_{\beta 1} \\ A_{\beta 20} & A_{\beta 21} & \dots & A_{\beta 2n} & B_{\beta 20} & B_{\beta 21} & \dots & B_{\beta 2n} & C_{\beta 2} & D_{\beta 2} \\ \vdots & \vdots \\ A_{\beta n0} & A_{\beta n1} & \dots & A_{\beta nn} & B_{\beta n0} & B_{\beta n1} & \dots & B_{\beta nn} & C_{\beta n} & D_{\beta n} \end{pmatrix} \quad (7)$$

and two keyword sets W^0 and W^1 to \mathbb{A} .

- (v) *More queries:* \mathbb{A} continues to inquire trapdoor queries. The restriction is similar to the *challenge* phase.
- (vi) *Response:* \mathbb{A} outputs a guess $\beta' \in \{0, 1\}$. \mathbb{C} will output 1 if $\beta' = \beta$. Otherwise, \mathbb{C} will output 0.

Now, we show that the algorithm \mathbb{C} can solve the decision $(q_T + 1)$ -BDHI assumption with probability at least $\epsilon' = \epsilon/e(nq_T + 1)$. First of all, we should analyze the probability that \mathbb{C} does not abort in *trapdoor queries* phase and *challenge* phase. We define two events:

- ω_1 : \mathbb{C} does not abort due to any of \mathbb{A} 's trapdoor queries.
- ω_2 : \mathbb{C} does not abort in *challenge* phase for generating I_β .

Suppose that q_T is large enough. Therefore, the probability of the event ω_1 is at least $(1 - 1/(nq_T + 1))^{nq_T} \geq 1/e$. The probability of the event ω_2 is $1/(nq_T + 1)$.

If $R = \hat{e}(g, g)^{1/x}$, \mathbb{A} 's view is identical to its view in a real attack game. Since we assume that \mathbb{A} can break the PECDK scheme with an advantage ϵ , it must satisfy $|Pr[\beta' = \beta] - 1/2| \geq \epsilon$. If R is a random number, where $R \in G_2$, then $|Pr[\beta' = \beta]| = 1/2$ since \mathbb{A} made a random guess.

Therefore, let $D = \{g, g^x, g^{x^2}, \dots, g^{x^{q_T+1}}\}$; we have that

$$\begin{aligned} & \left| Pr[B(D, \hat{e}(g, g)^{1/x}) = 1] - Pr[B(D, R) = 1] \right| \\ & \geq \frac{\epsilon}{e(nq_T + 1)} \end{aligned} \quad (8)$$

Then we conclude the theorem. \square

4. Performance Analysis

In this section, we first give a detailed theoretical analysis for the previous scheme and then compare it with the proposed one. After that, we set up an experiment to show that our scheme has better performance than the previous one. For simplicity, we denote the proposed scheme and the previous one by PECDK-1 and PECDK-2, respectively.

4.1. Theoretical Analysis. In an IPE scheme, each ciphertext associated with an attribute vector \vec{x} can be decrypted by the secret keys corresponding to the predicate vector \vec{v} if and only if $\vec{v} \cdot \vec{x} = 0$. The PECDK-2 is based on the approach of converting an IPE scheme into a PECDK scheme. In order to analyze the efficiency of the previous one, we will introduce the conversion method, which is described as follows.

Suppose that $Q = \{q_1, q_2, \dots, q_m\}$ and $W = \{w_1, w_2, \dots, w_n\}$ are two keyword sets. By utilizing an IPE scheme, (c_1, c_2, \dots, c_n) is the index of W , where c_i is a ciphertext of the vector $\{w_i^m, w_i^{m-1}, \dots, w_i^0\}$ and $i \in [1, n]$. Suppose that $f(x) = a_m x^m + a_{m-1} x^{m-1} + \dots + a_1 x + a_0 = (x - H_1(q_1))(x - H_1(q_2)) \dots (x - H_1(q_m))$; the trapdoor of Q is $\{k_a, sym\}$, where k_a is a secret key of the vector $\{a_m, a_{m-1}, \dots, a_0\}$. Let the decryption algorithm be $DEC(pk, CT, KEY)$, where pk is the public key, CT is the ciphertext, and KEY is the secret key. For each $i \in [1, n]$, the test algorithm can be performed by implementing $DEC(pk, c_i, k_a)$. According to different search function, there are two situations:

- (1) For sym is \vee , if there is at least one $i \in [1, n]$ such that the decryption algorithm $DEC(pk, c_i, k_a)$ outputs 1, the test algorithm outputs 1, otherwise, 0.
- (2) For sym is \wedge , the test algorithm will verify whether there are m c_i that can be decrypted by the decryption algorithm $DEC(pk, c_i, k_a)$. If so, the test algorithm outputs 1, otherwise, 0.

PECDK-2 is based on the IPE presented in [17]. For this IPE scheme, the time cost of setup, encryption, key generation, and decryption are all linear with $O(N^2)$, $O(N^2)$, $O(N^2)$, and $O(N)$, respectively, where N is the length of the predicate or attribute vector. Moreover, the space overhead of public key, master secret key (msk), ciphertext, and secret key is linear with $O(N^2)$, $O(N^2)$, $O(N)$, and $O(N)$, respectively. According to the conversion method mentioned above, we have the following results.

- (1) The pk and sk in the previous scheme are the same as the pk and msk in the IPE scheme. Thus, the time and space cost of pk and sk are both linear with $O(n^2)$.
- (2) Since the index of the previous scheme contains n ciphertexts of IPE, the time and space cost of index are linear with $O(n^3)$ and $O(n^2)$, respectively. Because the algorithm of trapdoor generating is similar with that of the index building, the time and space cost of trapdoor is also linear with $O(n^3)$ and $O(n^2)$, respectively.
- (3) The test algorithm needs to perform n times decryption algorithm. Thus, the time cost of test is proportional to the square of n .

For our scheme, pk contains $2n + 3$ elements in group G_1 and one element in G_2 , and sk involves $2n + 3$ elements in Z_p^* . Thus, we know that the time and space cost of KeyGen algorithm in our scheme are both linear with $O(n)$. Because the IndexBuild algorithm generates $2n^2 + 3n$ elements in group G_1 and n elements in G_2 , the time and space cost of IndexBuild algorithm are both linear with $O(n^2)$. The time cost and space cost of Trapdoor algorithm are both $O(m)$ since this algorithm creates $2m + 2$ elements in group G_1 . Whether $sym = \wedge$ or $sym = \vee$, the test algorithm executes at most $O(mn)$ pairing operations. Therefore, we can reckon that the time cost of test algorithm is less than $O(mn)$.

According to the above analysis, we will give two tables to demonstrate the comparison. Let $|T_e|$ be the time cost for

TABLE 1: Comparison with the previous PECDK scheme in time complexity.

	PECDK-1	PECDK-2
Key Generation	$O(n^2) T_{G_1} + T_e $	$(2n+3) T_{G_1} + T_e $
Index Building	$(4n^2 + 2n) T_{G_1} + n T_{G_2} $	$(3n^2 + 4n) T_{G_1} + n T_{G_2} $
Trapdoor Generation	$(4m+2) T_{G_1} $	$(2m+2) T_{G_1} $
Testing	$2n(2m+1) T_e $	$2n(m+1) T_e $

TABLE 2: Comparison with the previous PECDK scheme in space complexity.

	PECDK-1	PECDK-2
PK size	$O(n^2) G_1 + G_2 $	$(2n+3) G_1 + G_2 $
SK size	$O(n^2) G_1 $	$(2n+3) Z_p $
Trapdoor size	$(4m+2) G_1 $	$(2m+2) G_1 + Z_p $
Index size	$(4n^2 + 2n) G_1 + G_2 $	$(2n^2 + 4n) G_1 + G_2 $

a pairing operation [15] on G_1 , and $|T_{G_1}|$ and $|T_{G_2}|$ be the time cost for the exponential operation on G_1 and G_2 , where G_1 and G_2 are two groups of a prime order. For evaluating the time complexity, we only take these two operations into account since the time cost of these two operations is much more than the time cost of other operations like group add operation. The theoretical analysis of time complexity is shown in Table 1.

We denote the size of an element of Z_p , G_1 , and G_2 by $|Z_p|$, $|G_1|$, and $|G_2|$, respectively. The comparison result of space complexity is shown in Table 2.

4.2. Experimental Results. We implement our construction in JAVA with Java Pairing Based Cryptography (JPBC) library [39]. In our implementation, the bilinear map is instantiated as Type A pairing (base field size is 128 bits), which offers a level of security equivalent to 1024-bit DLOG [16]. Our experiment was run on Intel(R) Core(TM) i7-4570 CPU at 3.60GHz processor with 8GB memory size. Such an experiment is based on a group of artificial keyword sets with different number of keywords in each set (i.e., $n = 5; 10; 15; 20; 25$), where each keyword set can be seen as an index of a document. In each keyword set, we denote each keyword as an unique integer in the range of $[0, 1000]$, where 1000 can be regarded as the number of different words in the artificial keyword sets. We encrypt each keyword set with PECDK-1 and PECDK-2 schemes, and the encrypted indices were stored on our machine and then execute random queries over these encrypted indices (the number of documents and queries is denoted by D and Q_t , respectively). In addition, for simplicity, we denote the conjunctive and disjunctive keyword search by CKS (conjunctive keywords search) and DKS (disjunctive keywords search), respectively.

4.2.1. Time Overhead. Figure 2 shows that the impact of n on the time consumption. The statements of Figure 2 are described as follows.

- (1) Figure 2(a) shows that the execution time of key generation in PECDK-2 is linear with $O(n^2)$, while

that in PECDK-1 is linear with n . The time cost of the key generation algorithm in PECDK-2 is nearly 100 times than that in PECDK-1 since PECDK-2 needs to generate a pair of orthogonal matrices and more exponential operations on G_1 .

- (2) In Figure 2(b), we can find that the time cost of creating index in PECDK-2 is much more than that in PECDK-1, though the time complexities of index building in PECDK-1 and PECDK-2 are both linear with $O(n^2)$. The reason for this situation is that the DPVS structure used in PECDK-2 is based on a pair of orthogonal matrices, which will bring more exponential operations on G_1 and some additional matrix operations.
- (3) The time consumption of testing in PECDK-1 and PECDK-2 is illustrated in Figure 2(c). In Figure 2(c), we can find that time cost of CKS and DKS in PECDK-1 is much less than that in PECDK-2. In addition, whether PECDK-1 or PECDK-2, the time cost in DKS is slightly less than that in CKS since DKS may test fewer keywords than CKS.
- (4) The time complexity of trapdoor generation in PECDK-1 is independent with n , while that in PECDK-2 is linear with $O(n)$. The trapdoor generation algorithm in PECDK-1 still needs much less time cost than that in PECDK-2 with the same reason described in (2).

Figure 3 shows the impact of m on the time consumption. Because the key generation and index algorithms are not related to the parameter m , we only focus on the trapdoor generation and test algorithms. The comparison is stated as follows.

- (1) The time costs of trapdoor generation in PECDK-1 and PECDK-2 are both linear with $O(m)$, which is shown in Figure 3(a). However, the time cost of creating trapdoor in PECDK-2 is nearly 10 times than that in PECDK-1. The reason for this is that PECDK-2 needs more exponential operations on G_1 .

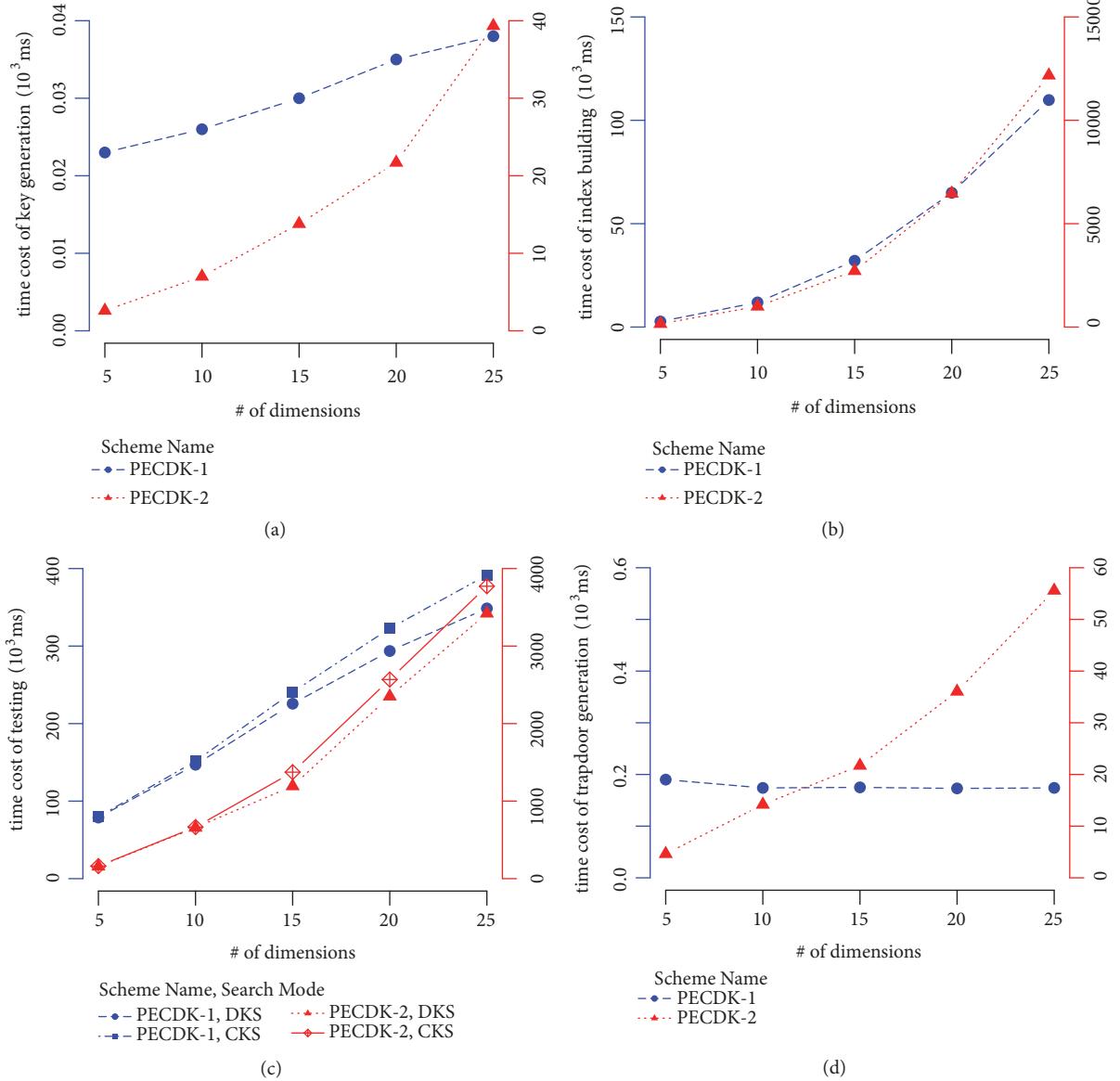


FIGURE 2: Impact of n on the time cost of key generation (a), index building (b), testing (c), and trapdoor generation (d) (blue and red scale are for PECDK-1 and PECDK-2, respectively, and $D = 100$, $m = 5$, $Q_t = 10$, $n = \{5; 10; 15; 20; 25\}$).

(2) Figure 3(b) shows that the time cost of testing in PECDK-1 is linear with $O(m)$, while that in PECDK-2 is not related with m . The reason is that the predicate vector and attribute vector must have the same dimension in an IPE scheme. So, we must convert the query keyword set into a predicate vector having the same length as the attribute vector generated from the index keyword set. According to this, the time cost of testing in PECDK-2 is independent to m actually. In addition, the time cost in DKS is also slightly less than that in CKS since DKS needs less test operations.

4.2.2. Storage Overhead. The storage cost of pk and sk , indices, and trapdoors are illustrated in Figure 4. The comparison results are listed as follows.

- Figures 4(a) and 4(b) show that the storage cost of pk and sk in PECDK-2 increases with $O(n^2)$, while that in PECDK-1 is linear with $O(n)$. Moreover, the storage cost in PECDK-2 is more than 100 times than that in PECDK-1. The reason is that the PECDK-2 needs to store two matrices.
- In Figure 4(c), we know that the storage costs of indices in PECDK-1 and PECDK-2 are both linear with $O(n^2)$. However, the storage cost in PECDK-2 is also nearly two times than that in PECDK-1 since PECDK-2 needs to store more G_1 elements than PECDK-1.
- In Figure 4(d), the storage cost of trapdoors in PECDK-1 is independent to n , while that in PECDK-2

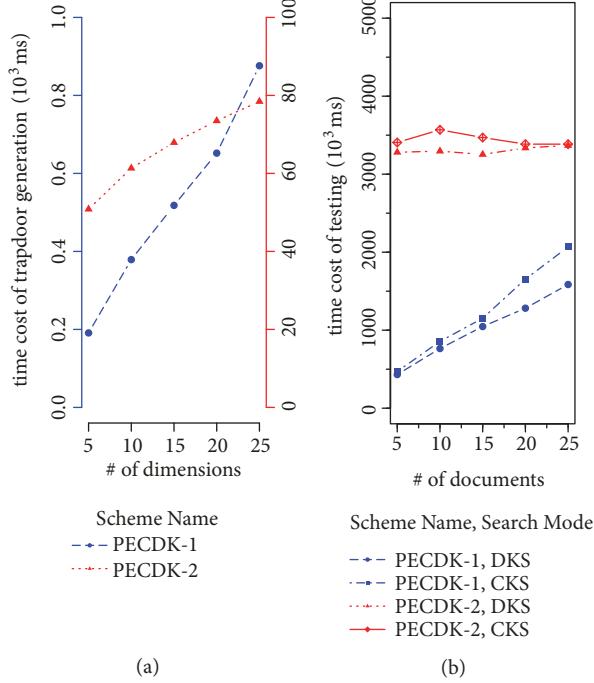


FIGURE 3: Impact of m on the time cost of trapdoor generation (a) and testing (b) (blue and red scale are for PECDK-1 and PECDK-2, respectively, and $D = 100$, $n = 25$, $Q_t = 10$, $m = \{5; 10; 15; 20; 25\}$).

TABLE 3: Impact of m on storage consumption of trapdoor generation ($n=25$, $D=100$, $Q_t = 10$).

Size of m	5	10	15	20	25
PECDK-1(kb)	6	10	14	19	23
PECDK-2(kb)	46	46	46	46	46

is linear with $O(n)$. The storage cost in PECDK-2 is still more than that in PECDK-1.

Because the size of pk , sk , and indices are not related to the parameter m , we only analyze the impact of parameter m on the storage cost of trapdoor. According to Table 3, we find that the size of trapdoor in PECDK-2 is independent with m since the query keywords must be converted into a predicate vector owing the same length to the attribute vector generated from the index keywords. The trapdoor size in PECDK-1 is linear with m and less than that in PECDK-2.

According to the experimental results described above, we can find that these results are consistent with our theoretical analysis.

4.2.3. More Comments. Generally speaking, the number of keywords in a document (n) is usually only $3 \sim 5$ (e.g., the research paper), and the number of keywords in a query (m) is often less than 10 [40]. According to above results, we can reckon that both n and m are less than 10 in the actual process of retrieval. According to the experiment result with $n = 10$ and $m = 5$, for the PECDK-1, the generation time of a single index and a single trapdoor is nearly 100 ms and 20 ms, respectively, and the test time of a single document is 15 ms.

Compared with the PECDK-2, it is more practical. Moreover, the time and storage cost of trapdoor in PECDK-1 scheme is very low, which means that the proposed scheme is fit for the mobile setting where the client has limited computation and storage resources.

Many applications require that the client cannot only add a group of documents to the server but also remove a set of documents from the server. Considering this situation, we need that the proposed scheme supports dynamic update. It means that users can update the encrypted indices and files securely. Many previous works can achieve this goal [24, 25]. In our scheme, we adopt the forward index structure in which each file has its index. Thus, it can support dynamic update naturally. For example, when a client wants to add a document, he/she will generate an encrypted document and its corresponding secure index and send them to the server. If a client wants to delete a document, he/she will send a request to the server. The server will remove the related document and the associated index according to the request.

In addition, because each document has its own encrypted index, we can easily accelerate the search process by utilizing the technique of parallel computation [6]. Thus, we argue that our scheme is more practical in the cloud platform, which has strong computing power.

5. Conclusion

In this paper, we propose an efficient PECDK scheme based on a prime order group, which has better performance than the previous PECDK scheme. Our scheme is proven to be secure under the security definition.

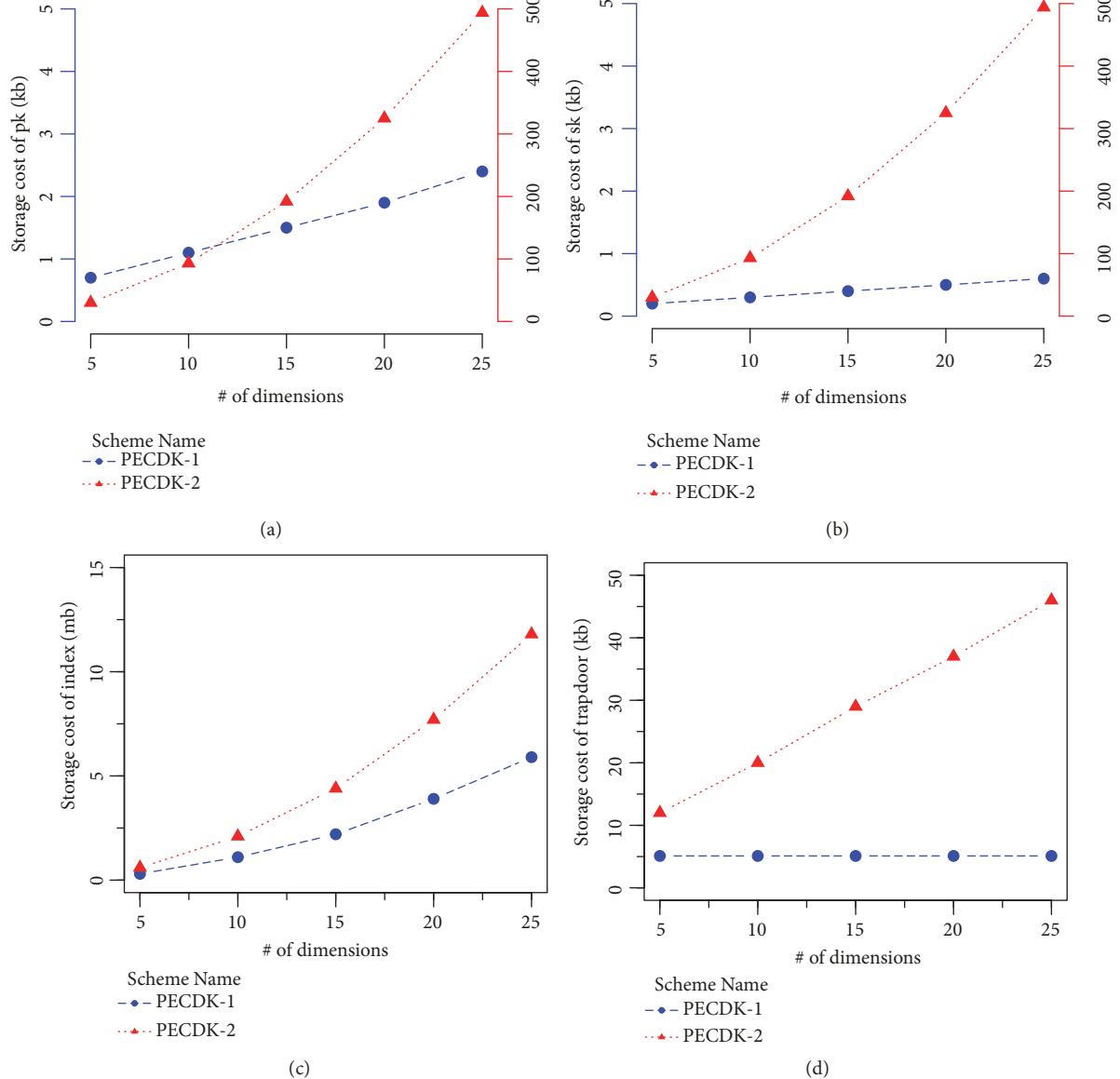


FIGURE 4: Impact of n on the storage cost of pk (a), sk (b), index (c), and trapdoor (d) (blue and red scale are for PECDK-1 and PECDK-2, respectively, and $D = 100$, $m = 5$, $Q_t = 10$, $n = \{5; 10; 15; 20; 25\}$).

To justify the efficiency of the proposed scheme, we present detailed theoretical analysis and experimental results. These results show that the proposed scheme is more practical than the most efficient PECDK scheme based on the IPE scheme. In the future, we will focus on building a SPE scheme supporting more advanced search function.

Data Availability

The artificial data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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References

- [1] Y. Zhu, D. Ma, and S. Wang, "Secure data retrieval of outsourced data with complex query support," in *Proceedings of the 2012 32nd International Conference on Distributed Computing Systems Workshops (ICDCS Workshops)*, pp. 481–490, IEEE Computer Society, Macau, China, June 2012.

- [2] M. Raykova, A. Cui, B. Vo et al., "Usable, secure, private search," *IEEE Security & Privacy*, vol. 10, no. 5, pp. 53–60, 2012.
- [3] Z. Fu, K. Ren, J. Shu, X. Sun, and F. Huang, "Enabling personalized search over encrypted outsourced data with efficiency improvement," *IEEE Transactions on Parallel and Distributed Systems*, vol. 27, no. 9, pp. 2546–2559, 2016.
- [4] C. Wang, N. Cao, K. Ren, and W. Lou, "Enabling secure and efficient ranked keyword search over outsourced cloud data," *IEEE Transactions on Parallel and Distributed Systems*, vol. 23, no. 8, pp. 1467–1479, 2012.
- [5] Z. Fu, X. Sun, Q. Liu, L. Zhou, and J. Shu, "Achieving efficient cloud search services: multi-keyword ranked search over encrypted cloud data supporting parallel computing," *IEICE Transactions on Communications*, vol. E98B, no. 1, pp. 190–200, 2015.
- [6] Z. Xia, X. Wang, X. Sun, Q. Liu, and Q. Wang, "A secure and dynamic multi-keyword ranked search scheme over encrypted cloud data," *IEEE Transactions on Parallel and Distributed Systems*, vol. 27, no. 2, pp. 340–352, 2016.
- [7] M. Kuzu, M. S. Islam, and M. Kantarciooglu, "Efficient similarity search over encrypted data," in *Proceedings of the IEEE 28th International Conference on Data Engineering (ICDE '12)*, pp. 1156–1167, IEEE, Washington, DC, USA, April 2012.
- [8] Z. Fu, X. Wu, C. Guan, X. Sun, and K. Ren, "Toward efficient multi-keyword fuzzy search over encrypted outsourced data with accuracy improvement," *IEEE Transactions on Information Forensics and Security*, vol. 11, no. 12, pp. 2706–2716, 2016.
- [9] P. Xu, S. He, W. Wang, W. Susilo, and H. Jin, "Lightweight searchable public-key encryption for cloud-assisted wireless sensor networks," *IEEE Transactions on Industrial Informatics*, vol. 14, no. 8, pp. 3712–3723, 2018.
- [10] D. Boneh, G. Di Crescenzo, R. Ostrovsky, and G. Persiano, "Public key encryption with keyword search," in *Proceedings of the International Conference on the Theory and Applications of Cryptographic Techniques EUROCRYPT 2004*, vol. 3027 of *Lecture Notes in Computer Science*, pp. 506–522, Springer, Interlaken, Switzerland, May 2004.
- [11] D. Park, K. Kim, and P. Lee, "Public key encryption with conjunctive field keyword search," in *Proceedings of the International Workshop on Information Security Applications WISA 2004*, vol. 3325 of *Lecture Notes in Computer Science*, pp. 73–86, Springer, Jeju Island, Korea, August 2004.
- [12] B. Zhang and F. Zhang, "An efficient public key encryption with conjunctive-subset keywords search," *Journal of Network and Computer Applications*, vol. 34, no. 1, pp. 262–267, 2011.
- [13] C. Song, X. Liu, and Y. Yan, "Efficient public key encryption with field-free conjunctive keywords search," in *Proceedings of the 6th International Conference on Trusted Systems (INTRUST '14)*, vol. 9473 of *Lecture Notes in Computer Science*, pp. 394–406, Springer International Publishing, Beijing, China, December 2014.
- [14] J. Katz, A. Sahai, and B. Waters, "Predicate encryption supporting disjunctions, polynomial equations, and inner products," in *Proceedings of the 27th Annual International Conference on the Theory and Applications of Cryptographic Techniques*, vol. 4965 of *Lecture Notes in Computer Science*, pp. 146–162, Springer, Istanbul, Turkey, April 2008.
- [15] Y. Zhang and S. Lu, "POSTER: efficient method for disjunctive and conjunctive keyword search over encrypted data," in *Proceedings of the ACM SIGSAC Conference on Computer and Communications Security*, pp. 1535–1537, Hong Kong, China, December 2014.
- [16] Y. Zhang, Y. Li, and Y. Wang, "Conjunctive and disjunctive keyword search over encrypted mobile cloud data in public key system," *Mobile Information Systems*, vol. 2018, Article ID 3839254, 11 pages, 2018.
- [17] T. Okamoto and K. Takashima, "Achieving short ciphertexts or short secret-keys for adaptively secure general inner-product encryption," in *Designs, Codes and Cryptography*, vol. 77, pp. 725–771, 2015.
- [18] D. X. Song, D. Wagner, and A. Perrig, "Practical techniques for searches on encrypted data," in *Proceedings of the IEEE Symposium on Security and Privacy (S&P '00)*, pp. 44–55, IEEE, Berkeley, Calif, USA, May 2000.
- [19] E. J. Goh, "IACR cryptology eprint archive, secure indexes," Tech. Rep. 2003/216, 2003.
- [20] P. Golle, J. Staddon, and B. Waters, "Secure conjunctive keyword search over encrypted data," in *Proceedings of the 2nd International Conference (ACNS '04)*, M. Jakobsson, M. Yung, and J. Zhou, Eds., vol. 3089 of *Lecture Notes in Computer Science*, pp. 31–45, Springer, Yellow Mountain, China, June 2004.
- [21] L. Ballard, S. Kamara, and F. Monrose, "Achieving efficient conjunctive keyword searches over encrypted data," in *Proceedings of the 7th International Conference (ICICS '05)*, S. Qing, W. Mao, J. Lopez, and G. Wang, Eds., vol. 3783 of *Lecture Notes in Computer Science*, pp. 414–426, Springer, Beijing, China, December 2005.
- [22] B. Wang, M. Li, and H. Wang, "Geometric range search on encrypted spatial data," *IEEE Transactions on Information Forensics and Security*, vol. 11, no. 4, pp. 704–719, 2016.
- [23] H. Ren, H. Li, H. Chen, M. Kpibiaareh, and L. Zhao, "Efficient privacy-preserving circular range search on outsourced spatial data," in *Proceedings of the IEEE International Conference on Communications (ICC '16)*, pp. 1–7, IEEE, Malaysia, May 2016.
- [24] Q. Wang, M. He, M. Du, S. S. M. Chow, R. W. F. Lai, and Q. Zou, "Searchable encryption over feature-rich data," *IEEE Transactions on Dependable and Secure Computing*, vol. 15, no. 3, pp. 496–510, 2018.
- [25] M. Du, Q. Wang, M. He, and J. Weng, "Privacy-preserving indexing and query processing for secure dynamic cloud storage," *IEEE Transactions on Information Forensics and Security*, vol. 13, no. 9, pp. 2320–2332, 2018.
- [26] S. Kamara and T. Moataz, "Boolean searchable symmetric encryption with worst-case sub-linear complexity," in *Proceedings of the 36th Annual International Conference on the Theory and Applications of Cryptographic Techniques*, vol. 10212 of *Lecture Notes in Computer Science*, pp. 94–124, Springer International Publishing, Paris, France, April 2017.
- [27] M. Abdalla, M. Bellare, D. Catalano et al., "Searchable encryption revisited: consistency properties, relation to anonymous IBE, and extensions," in *Proceedings of the Annual International Cryptology Conference CRYPTO 2005*, vol. 3621 of *Lecture Notes in Computer Science*, pp. 205–222, Springer, Santa Barbara, Calif, USA, August 2005.
- [28] Y. H. Hwang and P. J. Lee, "Public key encryption with conjunctive keyword search and its extension to a multi-user system," in *Proceedings of the 1st International Conference on Pairing-Based Cryptography*, vol. 4575 of *Lecture Notes in Computer Science*, pp. 2–22, Springer, Tokyo, Japan, July 2007.
- [29] D. Boneh and B. Waters, "Conjunctive, subset, and range queries on encrypted data," in *Proceedings of the 4th Theory of Cryptography Conference (TCC '07)*, vol. 4392 of *Lecture Notes in Computer Science*, pp. 535–554, Springer, Amsterdam, The Netherlands, February 2007.

- [30] J. Li, Y. Wang, Y. Zhang, and J. Han, "Full verifiability for outsourced decryption in attribute based encryption," *IEEE Transactions on Services Computing*, p. 1, 2017.
- [31] J. Li, W. Yao, J. Han, Y. Zhang, and J. Shen, "User collusion avoidance CP-ABE with efficient attribute revocation for cloud storage," *IEEE Systems Journal*, vol. 12, no. 2, pp. 1767–1777, 2018.
- [32] J. Li, Q. Yu, Y. Zhang, and J. Shen, "Key-policy attribute-based encryption against continual auxiliary input leakage," *Information Sciences*, vol. 470, pp. 175–188, 2019.
- [33] J. G. Li, W. Yao, Y. C. Zhang, H. L. Qian, and J. G. Han, "Flexible and fine-grained attribute-based data storage in cloud computing," *IEEE Transactions on Services Computing*, vol. 10, no. 5, pp. 785–796, 2017.
- [34] J. Li, H. Yan, and Y. Zhang, "Certificateless public integrity checking of group shared data on cloud storage," *IEEE Transactions on Services Computing*, p. 1, 2017.
- [35] H. L. Qian, J. G. Li, Y. C. Zhang, and J. G. Han, "Privacy-preserving personal health record using multi-authority attribute-based encryption with revocation," *International Journal of Information Security*, vol. 14, no. 6, pp. 487–497, 2015.
- [36] J. G. Li, X. N. Lin, Y. C. Zhang, and J. G. Han, "KSF-OABE: outsourced attribute-based encryption with keyword search function for cloud storage," *IEEE Transactions on Services Computing*, vol. 10, no. 5, pp. 715–725, 2017.
- [37] J. G. Li, Y. R. Shi, and Y. C. Zhang, "Searchable ciphertext-policy attribute-based encryption with revocation in cloud storage," *International Journal of Communication Systems*, vol. 30, no. 1, Article ID e2942, 2017.
- [38] A. Joux, "The Weil and Tate pairings as building blocks for public key cryptosystems," in *Proceedings of the Algorithmic Number Theory, Lecture Notes in Computer Science*, C. Fieker and D. R. Kohel, Eds., vol. 2369 of *Lecture Notes in Computer Science*, pp. 20–32, Springer, Sydney, Australia, July 2002.
- [39] A. D. Caro, "The java pairing based cryptography library (jpbc)," 2013, <http://gas.dia.unisa.it/projects/jpbc/>.
- [40] H. Cui, Z. Wan, R. H. Deng et al., "Efficient and expressive keyword search over encrypted data in the cloud," *IEEE Transactions on Dependable and Secure Computing*, vol. PP, no. 99, p. 1, 2016.

