Research Article

Subchannel Analysis of Wire Wrapped SCWR Assembly

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Application of wire wrap spacers in SCWR can reduce pressure drop and obtain better mixing capability. As a consequence, the required coolant pumping power is decreased and the coolant temperature profile inside the fuel bundle is flattened which will obviously decrease the peak cladding temperature. The distributed resistance model for wire wrap was developed and implemented in ATHAS subchannel analysis code. The HPLWR wire wrapped assembly was analyzed. The results show that: (1) the assembly with wire wrap can obtain a more uniform coolant temperature profile than the grid spaced assembly, which will result in a lower peak cladding temperature; (2) the pressure drop in a wire wrapped assembly is less than that in a grid spaced assembly, which can reduce the operating power of pump effectively; (3) the wire wrap pitch has significant effect on the flow in the assembly. Smaller $H_{wire}/D_{rod}$ will result in stronger cross flow a more uniform coolant temperature profile, and also a higher pressure drop.

1. Introduction

The supercritical water-cooled reactor (SCWR) is essentially a water reactor operating above the thermodynamic critical point of water ($P_c = 22.064$ MPa). It is considered as one of the most promising Generation IV reactors because of its simplicity, high thermal efficiency, and nearly fifty years of industrial experience from thermal-power stations with a SCW cycle [1]. Evolving from the existing designs, there are currently two types of SCWR concepts [2]: (a) a large reactor pressure vessel containing the reactor core (fuelled) heat source, analogous to conventional PWRs and BWRs, and (b) distributed pressure tubes or channels containing fuel bundles, analogous to conventional CANDU and RBMK nuclear reactors. The arrangement of separated moderator (moderator box in pressure vessel type and heavy water moderator in calandria in pressure tube type) is applied in each design, due to the sharp change in the thermal properties of coolant near the pseudo-critical point.

To obtain a small water volume fraction in core, tight lattices are necessary. Wire wrap spacers, an alternative to grid spacers, have been used extensively in LMFBR [3] and tight-lattice high-conversion cores [4], mainly due to their advantageous pressure drop and better mixing capability. As a consequence, the required coolant pumping power is decreased and the coolant temperature profile inside the fuel bundle is flattened which will obviously decrease the peak cladding temperature. The other potential advantage of wire wrap spacer is that it can improve the heat transfer at the rod gap where heat transfer deterioration occurs in SCWR assembly. For SCWR design, wire wrapped assembly has been selected in both three-pass HPLWR [5] and US SCWR [6].

The influence of wire wrap under supercritical pressure conditions should be well studied. Himmel et al. [7] studied the mixing coefficients for a subchannel flow through a HPLWR fuel assembly with 40 wire wrapped fuel pins in a square arrangement, and their analyses were concentrated on a section of 3 subchannels between the assembly box and the inner moderator box walls. Laurien et al. [8] carried out the heat transfer experiments with a 10 mm rod inside a square vertical channel with a wire wrapped helically around it. The results showed that, based on the comparison with an identical channel without the helical wrapped wire, the wire spacer did not enhance the heat transfer significantly under normal heat transfer conditions but helped improve the heat transfer in the pseudo-critical region and shift the onset of the deterioration to downstream. Chandra et al. [9] analyzed the wire wrap effect with CFD method. The results showed that the adiabatic helical wire wrap around the inner heated cylinder of the annulus prevented the heat transfer...
deterioration from occurring in the considered test case, even at very high heat fluxes. This was related to the enhanced production of the turbulent kinetic energy by the presence of helical wire wrap, which increased the turbulent mixing effect and consequently the heat transfer and finally reduced the wall temperature.

To better understand the behavior of the coolant and cladding under the influence of wire wrap in the whole assembly, subchannel analysis is an effective and simpler method. The present paper developed a subchannel code for wire wrapped SCWR bundle based on the ATHAS code.

2. Model Description

2.1. Basic Conservation Equations of ATHAS. The basic equations of the mathematical model [10] are derived by applying the general equations of continuity, energy, and momentum to a subchannel $i$ control volume $j$. The equations are as follows.

Mass. Consider

$$\frac{\partial}{\partial t} \langle \rho \rangle + \frac{\partial}{\partial Z} (\langle \rho u \rangle A) + \sum_{k=1}^{n_l} \left[ (\rho V_k) S \right]_k = 0,$$  \hspace{1cm} (1)

where the density, the axial mass flux, and the lateral mass flux are defined by

$$\langle \rho \rangle = \frac{1}{V} \int_V \rho \, dV, \quad \langle \rho u \rangle = \frac{1}{A} \int_A \rho u \, dA,$$

$$\langle \rho V \rangle = \frac{1}{A} \int_A \rho V \, dA.$$  \hspace{1cm} (2)

The first term is the time rate of change of mass per unit axial length and the second is spatial variation in axial mass flux per unit length. The last term is the sum on all gap connections of the lateral mass flux per unit length which is the cross flow associated with subchannel analysis.

Energy. Consider

$$\frac{\partial}{\partial t} \langle \rho h \rangle + \frac{\partial}{\partial Z} (\rho h u A) + \sum_{k=1}^{n_l} \left[ (\rho h V_k) S \right]_k$$

$$= \sum_{r=1}^{n_r} \left[ P_r \Phi_r H_r (t_r - t_f) \right]_r + \sum_{W=1}^{n_W} \left[ L_W H_W (t_W - t_f) \right]_W$$

$$+ \frac{\partial}{\partial Z} \left[ \frac{A}{A} \langle k_f \rangle \right]_A - \sum_{k=1}^{n_k} \left[ \frac{S \cdot C_g k_f}{L_c} (t_f - t_i) \right]_k$$

$$- \sum_{k=1}^{n_k} \left[ W^{r_{kn_k} - h_k} \right]_k.$$  \hspace{1cm} (3)

The equation considers the heat transfer from the rod and wall-to-channel (if necessary) to the control volume, the axial fluid heat conduction, the lateral fluid heat conduction through the gap between two channels, and turbulent energy input.

Axial Momentum. Consider

$$\frac{\partial}{\partial t} \langle \rho V \rangle + \frac{\partial}{\partial Z} \langle \rho u^2 \rangle A + \sum_{k=1}^{n_l} \left[ (\rho V_k u_k) S \right]_k$$

$$= - \frac{A}{\partial Z} \langle \rho \rangle - \frac{1}{2} \left( \frac{f}{D_x} + \frac{C}{\Delta Z} \right) \langle \rho u^2 \rangle A$$

$$- g \frac{\Delta A}{\Delta Z} \cos \theta - C_T \sum_{k=1}^{n_k} \left[ W' (u_i' - u_f') \right]_k.$$  \hspace{1cm} (4)

The first term at the left side is the time rate of change of momentum per unit axial length and the second and third are the spatial variation in axial momentum per unit length. The four terms at right side are the total pressure force on the control volume, axial drag force, the gravity force, and the force due to turbulent mixing, respectively.

Lateral Momentum. Consider

$$C_s \left\{ \sum_{k=1}^{n_l} \left[ (\rho V_k) S \cos \beta \right]_{kj} - \sum_{k=1}^{n_l} \left[ (\rho V_k) S \cos \beta \right]_{kj} \right\}$$

$$+ \frac{\partial}{\partial t} \langle \rho V_k \rangle V, S + \frac{\partial}{\partial Z} (\rho V_k) A, S$$

$$= b \left( \langle \rho \rangle_{AJ} - \langle \rho \rangle_{AI} \right) - \frac{1}{2} l g k (\rho V_k^2)$$

$$- g \frac{\rho V_k}{\sin \theta \cos \beta}.$$  \hspace{1cm} (5)

The first term at the left side is the net lateral momentum flux and the factor $C_s$ is included to help account for the imperfect coupling between communicating gaps. The second and third terms at the left side are the time rate of change of lateral momentum per unit lateral length and spatial variation in lateral momentum per unit length. The three terms at the right side are the pressure difference between adjacent channels, the total drag force, and the gravity force, respectively.

The constitutive correlations selected in the analysis are shown as follows based on Shan et al.’s work [10].


$$f = 0.3164 \text{Re}^{-0.25}.$$  \hspace{1cm} (6)

Heat transfer coefficient: Bishop correlation (1964) [12] for supercritical water:

$$N_u_x = 0.0069 \text{Re}_x^{0.9} \text{Pr}_x^{0.66} \left( \frac{P_r}{P_b} \right)^{0.43} \left( 1 + 2.4 \frac{D}{x} \right).$$  \hspace{1cm} (7)

Turbulent mixing factor: Rowe and Angle correlation [13] in the bundle condition:

$$\beta = 0.021 \cdot \text{Re}^{-0.1}.$$  \hspace{1cm} (8)
The selection of Blasius correlation, Bishop correlation (1964), and Rowe and Angle correlation in this paper can obtain relatively high maximum cladding surface temperature and present more conservative estimate.

The code has been validated under supercritical pressure condition [14] and successfully applied in the analysis of pressure vessel and pressure tube type SCWR bundle [10, 15, 16].

2.2. Wire Wrap Model. Hydraulic resistance model which was initially proposed by Ninokata et al. [17] is developed to account for the existence of the wire wrap spacer in rod bundle. These models are of "distributed resistance" type and add flow resistance term into the axial and transverse momentum equations as a function of subchannel geometry and flow velocity. The models are general enough to cover a wide range of geometrical parameters, wire position, and flow regime.

In the subchannel formulation, it is a common practice to assume three types of control volume for (1) mass and energy balance, (2) lateral momentum balance, and (3) axial momentum balance. Figure 1 illustrates the typical mass and energy balance control volume (ABCDEF-LMNJPQ) and lateral momentum control volume (SPTUKV-GYZWOX). Note that the control volume for the axial momentum balance is staggered in the axial direction with respect to the energy and mass balance control volume.

In this study, focus is mainly placed on the momentum balance conservation equation, that is, (4) and (5). The second terms at the right side of (4) and (5) represent the momentum exchange between the solid surface and the fluid. These terms, which are the forces exerted on the fluid by the wall, are replaced with the distributed resistance terms. These terms for the rod bundles with wire wraps can be divided into four components, as shown in Figure 2. These forces of $F^L_R$ and $F^K_N$ are estimated by correlations depending on the direction of the dominant flow. Each force can be written as

\[ F^L_R = R(c) \left( \frac{A_R}{A^W} \right) \cos \alpha, \]
\[ F^K_N = R(c) \left( 1 - \frac{A_R}{A^W} \right) \cos (\varphi - \alpha), \]

where

\[ R(c) = \frac{A^W f_{M}(c)}{8} \rho c |c| c^2 = u^2 + v^2. \]

For the predominantly axial flow,

\[ F^L_R = \frac{A^W f_{M}(c)}{8} |v| v \left( \frac{D^R}{S_T} \right)^{0.4} \left( \frac{S_L}{S_T} \right)^{0.6}, \]
\[ F^K_N = \frac{A_{WP} f_{M}}{2} |v_k| v_k, \]

where $f_c$ is a friction factor based on the cross flow Reynolds number, $S_T$ is the rod pitch, and $S_L$ is the distance between two rods in a transverse row (Figure 3).

The hydraulic resistance per unit volume for the solution of the axial and lateral momentum equations, respectively, can be represented as follows:

\[ \frac{1}{2} \left( \frac{f}{D^R} + \frac{C}{\Delta Z} \right) \langle \rho v^2 \rangle_A = F^L_R + F^K_N \cos \varphi + F^K_N \sin \varphi, \]
\[ \frac{1}{2} S \frac{L}{k} \langle \rho V^2 \rangle_S = F^L_R + F^K_N \sin \varphi - F^K_N \cos \varphi. \]
and 2 conducting walls are defined here. The heat transfer
between the subchannels and moderator box/assembly gap
is also considered with conducting wall model in the ATHAS
code.

Table 1 lists the geometry of the assembly and Table 2
gives the operating parameters. Figure 5 shows the rel-
ative axial power distribution, which is the result of
neutronic/thermal-hydraulics coupling analysis [19]. The
radial power distribution is assumed as uniform.

3.2. Subchannel Analysis Results with Wire Wrapped and
Grid Spaced Assemblies. To compare with the behavior of
wire wrap in the SCWR assembly, a subchannel analysis of
assembly with grid space is also taken. The parameters of grid
Figure 6: Axial cladding temperature profile in the hot channel.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fuel rod outer diameter</td>
<td>8.00 mm</td>
</tr>
<tr>
<td>Fuel rod pitch</td>
<td>9.44 mm</td>
</tr>
<tr>
<td>Pitch/diameter ratio (P/D)</td>
<td>1.18</td>
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<tr>
<td>Active height</td>
<td>4200 cm</td>
</tr>
<tr>
<td>Total height</td>
<td>4710 cm</td>
</tr>
<tr>
<td>Wire diameter</td>
<td>1.34 mm</td>
</tr>
<tr>
<td>Wire pitch</td>
<td>200 mm</td>
</tr>
<tr>
<td>Moderator box length</td>
<td>26.9 mm</td>
</tr>
<tr>
<td>Moderator box wall thickness</td>
<td>0.8 mm</td>
</tr>
<tr>
<td>Outside box length</td>
<td>72.5 mm</td>
</tr>
<tr>
<td>Outside box wall thickness</td>
<td>2.5 mm</td>
</tr>
<tr>
<td>Gap between fuel rod and box wall</td>
<td>1.43 mm</td>
</tr>
<tr>
<td>0.5 gap around one fuel assembly</td>
<td>5.0 mm</td>
</tr>
</tbody>
</table>

Table 1: Fuel assembly geometry parameters.

The comparison of axial cladding temperature profiles in the hot channel between wire wrapped and grid spaced assemblies is shown in Figure 6. The peak cladding temperature is 587.6 °C for wire wrapped assembly and 603.5 °C for grid spaced assembly, respectively. The location of peak cladding temperature is at subchannel 43, rod 25, and 3.96 m at axial position. The reason for the temperature difference is that more forced cross flow between subchannels, result in a more uniform coolant temperature profile. Figure 7 shows the coolant temperature profile at axial position where the peak cladding temperature occurs.

3.3. Sensitivity Analysis of Wire Wrap Pitch. Sensitivity analysis of wire wrap pitch was also studied. The pitch is selected according to the criteria determined by Diller [21], $H_{wire}/D_{rod} < 50$. So four $H_{wire}/D_{rod}$ values have been selected for analysis, which are $H_{wire}/D_{rod} = 20, 30, 40, \text{and} 50$, respectively.

Figure 9 shows the comparison of exit cooling temperature profiles with different $H_{wire}/D_{rod}$ values. It is found that lower $H_{wire}/D_{rod}$ will result in a more uniform profile, since the temperature difference between the hottest and coldest channels is 60.9°C for $H_{wire}/D_{rod} = 50$ and 21.9°C for $H_{wire}/D_{rod} = 20$. This is understandable because lower $H_{wire}/D_{rod}$ causes more cross flow. However, lower $H_{wire}/D_{rod}$ also leads to a higher pressure drop, as shown in Figure 10. The pressure drop is increased from 51.8 kPa for $H_{wire}/D_{rod} = 50$ to 56.1 kPa for $H_{wire}/D_{rod} = 20$.

Figure 11 shows the peak cladding temperature comparison with different $H_{wire}/D_{rod}$ values. As we have discussed before, the peak cladding temperature mainly depends on whether the coolant temperature profile in subchannels is uniform or not. Higher $H_{wire}/D_{rod}$ will result in a higher cladding temperature. As for $H_{wire}/D_{rod} = 50$, the calculated peak cladding temperature is 603.3°C, nearly the same as grid spaced assembly.
4. Conclusion and Discussion

The subchannel code ATHAS is modified with distributed resistance model to meet the demand of wire wrapped SCWR assembly. Conclusions can be concluded as follows.

1. The assembly with wire wrap can obtain a more uniform coolant temperature profile than the grid spaced assembly, which will result in a lower peak cladding temperature.

2. The pressure drop in a wire wrapped assembly is less than that in a grid spaced assembly, which can reduce the operating power of pump effectively.

3. The wire wrap pitch has significant effect on the flow in the assembly. Smaller $H_{\text{wire}}/D_{\text{rod}}$ will result in stronger cross flow, a more uniform coolant temperature profile, and also a higher pressure drop.

Although the feasibility of wire wrapped assembly from the thermal-hydraulic point of view is approved in this work, the flow-induced vibration induced by wire wrap still needs further study.

Nomenclature

- $A$: Area ($m^2$)
- $C_g, C_p, C_T$: Empirical correction factor
- $D_e$: Hydraulic diameter (m)
- $f$: Frictional coefficient
- $g$: Gravity acceleration ($m/s^2$)
- $h$: Enthalpy ($J/kg$)
- $h'$: Turbulent transport enthalpy ($J/kg$)
- $H$: Heat transfer coefficient ($W/(m^2 \cdot K)$)
- $l$: Lateral pseudo length (m)
- $L$: Channel centroid distance (m)
- $K$: Frictional coefficient of spacer grid
- $p$: Pressure (Pa)
- $P$: Perimeter (m)
- $Pr$: Prandtl number
Re: Reynolds number
S: Gap width between rods (m)
t: Temperature (°C)
u: Velocity (m/s)
u′: Turbulent velocity (m/s)
V: Lateral velocity (m/s)
W: Lateral flow rate (kg/s)
W′: Turbulent mixing rate (kg/s)
Δz: Axial length (m)
c: Mixture velocity (m/s)
u: Mixture axial velocity (m/s)
v: Mixture lateral velocity (m/s)
A_R: Rod surface area (m²)
A_W: Wire surface area within a control volume (m²)
A_W': Total wetted surface area including wire spacer (m²)
D_eq: Equivalent hydraulic diameter (m)
F_R^A: Axial component of the force exerted by the rod surface (N)
F_R^L: Lateral component of the force exerted by the rod surface (N)
F_R^T: Tangential component of the force exerted by the rod surface (N)
F_W^N: Normal component of the force exerted by the wire wrap surface (N)
S_r: The rod pitch (m)
S_L: The distance between two rods in a transverse row (m)
H_wrap: Wire wrap length (m)
D_rod: Fuel rod diameter (m).

Greek Symbols
β: Direction angle, turbulent mixing coefficient
φ: Fraction of perimeter
θ: Angle between the channel axis and vertical
ρ: Density (kg/m³)
α: The velocity makes an angle from the vertical
φ: Wire wrap angle.

Subscripts
b: Bulk fluid
c: Channel
i, j: Subchannel number
f: Fluid
k: Gap number
r: Rod
w: Conduction wall.

Acronyms
ATHAS: Advanced thermal-hydraulics analysis subchannel
SCWR: Super critical water-cooled reactor
CANDU: Canada deuterium uranium
RBMK: Reactor of large capacity channel type (in Russian abbreviations)
HPLWR: High performance light water reactor.

Conflict of Interests
The authors declare that there is no conflict of interests regarding the publication of this paper.

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References


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