Optimized control for dynamical performance of the polishing robot in unstructured environment

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Abstract. In this paper, the dynamical performance of polishing robot working in unstructured environment is investigated. Structure mechanism and operating principle of a polishing robot are introduced firstly, and its dynamical model is established. Then, a S-shaped acceleration-deceleration path planning method and a human-simulated intelligent control (HSIC) strategy are proposed. The S-shaped acceleration-deceleration path planning method is to switch the magnitude and direction of the abrupt velocities between motion sections in order to improve the work efficiency, the smoothness of movement and the processing accuracy. The HSIC control strategy is built based on the unstructured environment information measured by ultrasonic sensors, in which the appropriate programs prepared in advance are determined according to the size and sign of both the control error and its change rate. Simulation results show that the intelligent control strategy combining with optimum path planning method are effective to reduce the structure vibration, to improve the stability and the control accuracy of the polishing robot system.

Keywords: Polishing robot, unstructured environment, path planning, human-simulated intelligent control (HSIC)

1. Introduction

A polishing robot is an important automatic machine for the purpose of finishing process to obtain required metal surface quality and shape accuracy of a workpiece, and it is widely used in space, aviation, manufacturing industry and so on [1–3]. The working environment of the polishing robot is a typical unstructured environment, such as the workpiece surface is unknown in advance and can not be described in mathematical expression. For the reason of the unstructured environment, it is often difficult to ensure the finishing accuracy in work, and spends much time and needs well-experienced operators mostly. So it is meaningful to develop novel kinds of polishing robotic equipment [4–6]. For the existing machines for surface finishing process, many of them are the conventional machine tools [7,8], the classical robots [9–11] and the parallel robots [12,13], and so on. The industrial robot based polishing system has many advantages such as big workspace and good flexibility, but its finishing plan and track of free-form surface are difficult. The CNC machine tool has good trajectory error but not acceptable error when polishing irregular surfaces. The parallel polishing machine is usually faster and more rigid than a traditional polishing robot but its workspace is usually more limited [14].

At present, much works about the polishing process research used for polishing with bound abrasives has been done, such as the polishing expert system integrated with sensor information [6,15], an intelligent polishing system using an acoustic emission-based intelligent monitoring scheme, and the optimization of process parameters based
Table 1

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Range of shell’s internal diameter (mm)</td>
<td>300~600</td>
</tr>
<tr>
<td>Range of shell’s length (mm)</td>
<td>600~3000</td>
</tr>
<tr>
<td>Speed of big arm’s movement (mm/s)</td>
<td>3</td>
</tr>
<tr>
<td>Speed of polishing head (r/s)</td>
<td>50</td>
</tr>
<tr>
<td>Linear speed of rotating bracket (mm/s)</td>
<td>30~32</td>
</tr>
<tr>
<td>Polishing accuracy (mm)</td>
<td>&lt; 0.04</td>
</tr>
<tr>
<td>Temperature (°C)</td>
<td>−20~70</td>
</tr>
</tbody>
</table>

Fig. 1. Structure diagram of polishing robot system.

In this paper, the artificial intelligent based optimal control a polishing robot in unstructured environment is studied with especially considering the goal of the structure vibration and machining accuracy. Firstly, the main structure mechanism of the polishing robot is presented, and the dynamical model of it is established. The designing of the controller with practical components is presented. Then, a S-shaped acceleration-deceleration path planning method is proposed. A HSIC strategy is built based on the unstructured environment information measured by ultrasonic sensors, which is to summarize human control experience, imitate human control behavior, and describe the control strategies by the mathematical rules. Finally, the conclusions are made.

2. Practical setup and kinetic equations of the polishing robot

As shown in Fig. 1, a polishing robot is divided into two parts: the main body and the deputy body. The deputy body is a rotating bracket that drives the workpiece of a thin shell structure to rotate around the x-axis. The position of the end-effector in the plane of xoy is determined by the big arm (in translating motion) and the forearm (in rotating motion). The wrist (in rotating motion) ensures the end-effector contract with work surface in tangent direction.

The working principle of the robot is depicted in Fig. 2. The practical setup is shown in Fig. 3. Main technical parameters of the system are listed in Table 1.

There are three ultrasonic rangefinders on the big arm, numbered as 1, 2 and 3, and their length is b. The sensor 1 is fixed on the big arm in the direction y. The sensors 2 and 3 are for exploring the inclined planes. The last two sensors can swing driven by a servo motor, where o’ and ψ denote the swing centre and the angle between the axes of the two sensors respectively.
The three degrees of freedom of the robot are: the displacement of the big arm $d_1$, and the rotational joints of $\theta_2$ and $\theta_3$. Besides, $\beta$ represents the angle between the axis of the end-effector and the tangent of the environmental surface, and $\gamma$ denotes the angle between the tangent of the environmental surface and the $x$-axis, and $\alpha$ represents the distance between the point $o'$ and the big arm, and $l_0$ denotes the distance between the point $o'$ and the joint of the big arm and the forearm. The lengths of the big arm, forearm and the wrist are $l_1$, $l_2$ and $l_3$, respectively.

The equations of each joint variable of the robot by kinematics inverse transformation are as follows

\[
\begin{align*}
\dot{d}_1(t) &= x(t) - l_2(1 - \cos \theta_2(t)) - l_3(1 - \cos \psi(t)) + r \sin \psi(t) \\
\dot{\theta}_2(t) &= \arcsin \left( \frac{1}{l_2} (y(t) - l_3 \sin \psi(t) - r \cos \psi(t)) \right) \\
\dot{\theta}_3(t) &= \theta_2(t) - \psi(t)
\end{align*}
\]

where $\psi(t) = \gamma(t) + \pi/2 - \beta(t)$.

The structure diagram of the robot is shown in Fig. 4. The Masses of the big arm, forearm and wrist are respectively $m_1$, $m_2$ and $m_3$, and their corresponding position vectors are respectively $\mathbf{r}_1$, $\mathbf{r}_2$ and $\mathbf{r}_3$.

The position vectors are

\[
\mathbf{r}_1 = (d_1 + l_1) \mathbf{i}
\]
Fig. 4. The structure diagram of main body.

\[ r_2 = r_1 + (l_2 \cos \theta_2) \mathbf{i} + (l_2 \sin \theta_2) \mathbf{j} \]
\[ = (l_1 + d_1 + l_2 \cos \theta_2) \mathbf{i} + (l_2 \sin \theta_2) \mathbf{j} \]  
\[ \text{(3)} \]

\[ r_3 = r_2 + (l_3 \cos \theta_3) \mathbf{i} + (l_3 \sin \theta_3) \mathbf{j} \]
\[ = (l_1 + d_1 + l_2 \cos \theta_2 + l_3 \cos \theta_3) \mathbf{i} + (l_2 \sin \theta_2 + l_3 \sin \theta_3) \mathbf{j} \]  
\[ \text{(4)} \]

Then, the velocity vectors \( \mathbf{v}_1, \mathbf{v}_2 \) and \( \mathbf{v}_3 \) are as follows

\[ \mathbf{v}_1 = \frac{dr_1}{dt} = (\dot{x}_1) \mathbf{i} \]
\[ \mathbf{v}_2 = \left( \dot{d}_1 - l_2 \dot{\theta}_2 \sin \theta_2 \right) \mathbf{i} + \left( l_2 \dot{\theta}_2 \cos \theta_2 \right) \mathbf{j} \]
\[ \mathbf{v}_3 = \left( \dot{d}_1 - l_2 \dot{\theta}_2 \sin \theta_2 - l_3 \dot{\theta}_3 \sin \theta_3 \right) \mathbf{i} + \left( l_2 \dot{\theta}_2 \cos \theta_2 + l_3 \dot{\theta}_3 \cos \theta_3 \right) \mathbf{j} \]
\[ \text{(5)} \]

The kinetic energy equation of system is

\[ K = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 + \frac{1}{2} m_3 v_3^2 \]
\[ = \frac{1}{2} (m_1 + m_2 + m_3) d_1^2 + \frac{1}{2} (m_2 + m_3) l_2^2 \dot{\theta}_2^2 + \frac{1}{2} m_3 l_3^2 \dot{\theta}_3^2 \]
\[ - (m_2 + m_3) l_3 d_1 \dot{\theta}_2 \dot{\theta}_3 \sin \theta_3 + m_3 l_2 \dot{\theta}_2 \dot{\theta}_3 \cos (\theta_3 - \theta_2) \]  
\[ \text{(8)} \]

The potential energy referencing to the coordinate origin is

\[ P = m_1 g r_1 + m_2 g r_2 + m_3 g r_3 = m_2 g l_2 \sin \theta_2 + m_3 g (l_2 \sin \theta_2 + l_3 \sin \theta_3) \]
\[ = (m_2 + m_3) g l_2 \sin \theta_2 + m_3 g l_3 \sin \theta_3 \]  
\[ \text{(9)} \]

The dissipative energy of the system is

\[ D = \frac{1}{2} c_1 d_1^2 + \frac{1}{2} c_2 \dot{\theta}_2^2 + \frac{1}{2} c_3 \left( \dot{\theta}_3 - \dot{\theta}_2 \right)^2 \]
\[ \text{(10)} \]

The total work done by the external force is

\[ W = F_1 d_1 + \tau_2 \dot{\theta}_2 + \tau_3 \dot{\theta}_3 \]  
\[ \text{(11)} \]

With the Lagrange principle of the following
∂W/∂q_i = d/dt ∂K/∂q_i + ∂D/∂q_i + ∂P/∂q_i, i = 1, 2, · · · , n (12)

We can obtain the system’s kinetic equation as follows

\[ F_1 = (m_1 + m_2 + m_3)\ddot{d}_1 - (m_2 + m_3)l_2(\dot{\theta}_2 \sin \theta_2 + \dot{\theta}_2^2 \cos \theta_2) - m_3l_3(\ddot{\theta}_3 \sin \theta_3 + \dot{\theta}_3^2 \cos \theta_3) + c_1\dot{d}_1 \]

\[ \tau_2 = (m_2 + m_3)(l_2 \dot{\theta}_2 - \ddot{d}_1 \sin \theta_2)l_2 + m_3l_2l_3 \theta_3 \cos(\theta_3 - \theta_2) - m_3l_2l_3(\ddot{\theta}_3 - 2\dot{\theta}_2) \sin(\theta_3 - \theta_2) \]

\[ \tau_3 = -m_3l_3 [\ddot{d}_1 \sin \theta_3 - l_2 \dot{\theta}_2 - l_2 \dot{\theta}_2^2 \sin (\theta_3 - \theta_2)] m_3l_3^2 \ddot{\theta}_3 + c_3 (\theta_3 - \theta_2) + m_3gl_3 \cos \theta_3 \] (13)

3. Planning method for S-shaped acceleration-deceleration path

The planning for the acceleration-deceleration path of the polishing robot carried out in Cartesian coordinate space to ensure the motion trajectory of the end-effector keeping in strict accordance with the required goal. Shown in Fig. 5, a\(_{max}\), -a\(_{max}\), v, v\(_0\), v\(_f\) and l\(_0\) are the maximum acceleration, maximum deceleration, average feed velocity, initial velocity, end velocity and initial displacement.

In the S-shaped acceleration-deceleration planning, one of the motion segments is divided into seven time intervals of (T\(_1\) ~ T\(_7\)). The corresponding both feed velocity and acceleration are planned as continuous functions with time variable. With this planning method, the vibration and shock of the robot can be suppressed effectively [3].

Considering the motion trajectory of the end-effector AB + BC + CD shown in Fig. 1, there are two ellipsoid ends tangent to the junctions on cylinder and with the same direction of velocity. The switching modes of velocity are all straight line segments, where the direction in arc segments is invariant as shown in Fig. 6. The end-effector doesn’t
Table 2

<table>
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<th>The third section</th>
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Fig. 7. Step response curve of typical dyadic system.

4. Human-simulated intelligent control strategy

The control strategy of the polishing robot hopes that the end-effectors’ motion trajectory and working profiles are completely consistent and the contact force keeps constant. But the tracking error exists certainly, especially in the unstructured enviroment. The method of human-simulated intelligent control (HSIC) is presented in this paper. In HSIC, the control variables are adjusted in real-time according to the position error and its change rate between the desired control force and the contact force of the end-effector referring to the workpiece.

If the robot system of trajectory tracking and position control can be simplified as a linear system, the HSIC can be described by using a step response function shown in Fig. 7.

The characteristic variables of HSIC are important for the dynamic process of the robot, and their signs (negative or positive) are listed in Table 3.

In order to describe the dynamic characteristics of HSIC, two errors are defined as follows.

The error between the desired position and the actual position is
Table 3
Symbol change of characteristic variables

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<tr>
<th></th>
<th>OA</th>
<th>AB</th>
<th>BC</th>
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<th>DE</th>
<th>EF</th>
<th>FG</th>
<th>GH</th>
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<td>&lt;0</td>
<td>&lt;0</td>
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<td>&lt;0</td>
<td>&lt;0</td>
<td>&lt;0</td>
<td>&gt;0</td>
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<tr>
<td>$\Delta e_n$</td>
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<td>&lt;0</td>
<td>&gt;0</td>
<td>&gt;0</td>
<td>&lt;0</td>
<td>&lt;0</td>
<td>&gt;0</td>
<td>&gt;0</td>
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<tr>
<td>$e_n \cdot \Delta e_n$</td>
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<td>&lt;0</td>
<td>&lt;0</td>
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<td>&lt;0</td>
<td>&lt;0</td>
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</table>

Fig. 8. Ideal trajectory of force error of HSIC.

$$e = S_d - S_c$$  \hspace{1cm} (14)

where $S_d$ is the desired position of robot system and $S_c$ is the actual position.

The change rate of the position error is

$$\Delta e_n = e_n - e_{n-1}, \Delta e_{n-1} = e_{n-1} - e_{n-2}$$  \hspace{1cm} (15)

where $e_n$ is the position error at the $n$th sampling period; $e_{n-1}$ is the position error at the $(n-1)$th sampling period; and $e_{n-2}$ is the position error at the $(n-2)$th sampling period.

The position changing trend is described and forecasted based on the negative or positive signs of the above characteristic variables. If $e_n \cdot \Delta e_n < 0$, systematic development changes towards trend of error diminution, such as OA, BC, DE and FG in Fig. 7, which indicates there are the extreme values. Contrarily, if $e_n \cdot \Delta e_n > 0$, the process changes towards trend of error aggrandizement, such as AB, CD, EF and GH, which indicates there is no extreme value. The characteristic variable $\Delta (\Delta e_n)$ represents the change rate of the position error. As is shown in Fig. 7, it is an overshoot part for ABC part because of $\Delta (\Delta e_n) > 0$, and an undershoot part for CDE part because of $\Delta (\Delta e_n) < 0$. In the process of establishing trajectory tracking model, the signs of $e_n, e_n \cdot \Delta e_{n-1}$ and $\Delta e_n$ are identified and used to recognize the dynamic behaviors of the trajectory in real time.

In order to improve the effectiveness of the trajectory tracking with a HSIC algorithm, the ideal trajectory of the position error is given and shown in Fig. 8.

The dotted lines in Fig. 8 indicate the desired target trajectory $f(e, \dot{e})$. The thresholds’ values of position error are $e_1, e_2, e_3$ and $e_4$, and their change rates are $\dot{e}_1, \dot{e}_2, \dot{e}_3$ and $\dot{e}_4$, correspondingly. The above eight parameters are determined according to the actual requirements of the robot. Different control development processes in the five regions in Fig. 8 are as follows:

1) While the position error is bigger, the corresponding region 1 adopts as far as possible big control action.
2) While the position error increases, the corresponding region 2 uses PID (Proportion – Integral – Differential) control.

3) While the position error decreases and tends to target slowly, the corresponding region 3 applies proportional control.

4) While the position error decreases and tends to target rapidly, the corresponding region 4 adopts PD (proportion – differential) control.

5) When the position error and the change rate of the error all satisfy the request, the corresponding region 5 keeps the current control model.

According to above regulation, the characteristic elements of trajectory tracking of the HSIC control can be expressed as

\[ Q = [q_1 \ q_2 \ q_3 \ q_4 \ q_5 \ q_6 \ q_7 \ q_8 \ q_9] \]  \hspace{1cm} (16)

where, \( q_1: e_n \cdot \Delta e_n \leq 0; q_2: |e_n| \geq e_1; q_3: |e_n| \geq e_2; q_4: |e_n| \geq e_3; q_5: |e_n| \geq e_4; q_6: |\dot{e}_n| \geq \dot{e}_1; q_7: |\ddot{e}_n| \geq \ddot{e}_2; q_8: |\dddot{e}_n| \geq \dddot{e}_3; q_9: |\dddot{e}_n| \geq \dddot{e}_4. \]

The characteristic model is expressed as

\[ \Phi = [\phi_1 \ \phi_2 \ \phi_3 \ \phi_4 \ \phi_5] \]  \hspace{1cm} (17)

where, \( \phi_1 \Rightarrow [q_2]; \ \phi_2 \Rightarrow [q_1 \cap \bar{q}_2]; \)

\[ \phi_3 \Rightarrow [(q_1 \cap \bar{q}_2 \cap \bar{q}_3 \cap q_8) \cup (q_1 \cap \bar{q}_2 \cap q_4 \cap \bar{q}_7 \cap q_8) \cup (q_1 \cap q_2 \cap q_3 \cap \bar{q}_6 \cap q_7)]; \]

\[ \phi_4 \Rightarrow [(q_1 \cap \bar{q}_2 \cap q_3 \cap q_6) \cup (q_1 \cap \bar{q}_3 \cap q_7) \cup (q_1 \cap q_4 \cap \bar{q}_7 \cap q_8) \cup (q_1 \cap q_5 \cap \bar{q}_8 \cap q_9)]; \]

\[ \phi_5 \Rightarrow [q_1 \cap q_5 \cap q_9]. \]

The control model is expressed as

\[ \Psi = [\psi_1 \ \psi_2 \ \psi_3 \ \psi_4 \ \psi_5] \]  \hspace{1cm} (18)

where, \( \psi_1 \Rightarrow u_n = K_p \cdot e_n + K_d \cdot \dot{e}_n + K_i \int e_n \cdot dt; \psi_2 \Rightarrow u_n = \text{sgn}(e_n) \cdot U_{\text{max}}; \)

\[ \psi_3 \Rightarrow u_n = K_p \cdot e_n + K_d \cdot \dot{e}_n; \quad \psi_4 \Rightarrow u_n = K_p \cdot e_n; \quad \psi_5 \Rightarrow u_n = u_n - 1. \]

where, \( u_n \) is the controller output at the \( n \) th sampling period; \( u_{n-1} \) is the controller output at the \( (n-1) \) th sampling period; \( K_p \) is the proportion coefficient; \( K_d \) is the differential coefficient; \( K_i \) is the integral coefficient; \( U_{\text{max}} \) is the maximum controller output value.

The inference rule is expressed as

\[ \Omega = [\omega_1 \ \omega_2 \ \omega_3 \ \omega_4 \ \omega_5] \]  \hspace{1cm} (19)

where, \( \omega_1: \phi_1 \Rightarrow \psi_2; \omega_2: \phi_2 \Rightarrow \psi_1; \omega_3: \phi_3 \Rightarrow \psi_4; \omega_4: \phi_4 \Rightarrow \psi_3; \omega_5: \phi_5 \Rightarrow \psi_5. \)

5. Example

Take a third-order system as an example to study the HSIC control strategy presented in this paper, where the system is the same as that in [22]. Its transfer function is

\[ G(s) = \frac{523500}{s^3 + 87.355s^2 + 10470s} \]  \hspace{1cm} (20)

Supposing the sampling time is 1 ms and using Z-transform, Eq. (20) can be re-written as

\[ \text{yout}(k) = - \text{den}(2) \text{yout}(k-1) - \text{den}(3) \text{yout}(k-2) - \text{den}(4) \text{yout}(k-3) \]

\[ + \text{num}(2) u(k-1) + \text{num}(3) u(k-2) + \text{num}(4) u(k-3) \]  \hspace{1cm} (21)
If with PID control, the simulation results are shown in Fig. 9, where the parameters are $K_p = 0.5$, $K_i = 0.001$, $K_d = 0.001$. The average track error between the desired track and the actual track is $\Delta y_{ave} = 3.26$ mm.

If with the HSIC control, where the PID parameters are used the same, the maximum controller output is $U_{max} = 10$ mm, and the thresholds of force error and their change rate are assumed as:

- $e_1 = 15$ mm, $e_2 = 10$ mm, $e_3 = 5$ mm, $e_4 = 1$ mm;
- $\dot{e}_1 = 10$ mm, $\dot{e}_2 = 5$ mm, $\dot{e}_3 = 1$ mm, $\dot{e}_4 = 0.5$ mm.

The simulated result is shown in Fig. 10, where the average track error is $\Delta y_{ave} = 1.51$ mm.

Comparing Fig. 10 with Fig. 9, it is apparent that the effect of HSIC tracking method is better than PID control method in the same settings of control parameters. Therefore, the HSIC strategy is adopted in the polishing robot under unknown environment, as long as the parameters of HSIC are determined based on the actual requirements. In our practice, HSIC method is effective in working efficiency and accuracy of the contact force, and restrains the error enhancing ultimately.

6. Conclusions

The S-shaped acceleration-deceleration path planning method and human-simulated intelligent control (HSIC) strategy are investigated in the paper to improve the dynamic performance of the polishing robot. The S-shaped acceleration-deceleration path planning method is to switch magnitude and direction of the connection velocity among motion sections. The HSIC control strategy is well defined and the numerical simulations indicate that it is effective for a given example where the average tracking error is much smaller than that of PID control.

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References


