**Research Article**

**Damage Localization and Quantification of Truss Structure Based on Electromechanical Impedance Technique and Neural Network**

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Truss structure is widely used in civil engineering. However, it is difficult to quantitatively monitor the state of truss structures because of the connection diversity and complexity of truss structures. In this paper, electromechanical impedance (EMI) technique was proposed to measure impedance spectra by using PZT elements and backpropagation (BP) neural network was used as an effective nonlinear conversion tool to quantify the health state of truss structures. Firstly, frequency band of the spectrum was experimentally determined by the trial-and-error approach. Then four connection rods of this truss structure were selected for experimental research. These connection rods were loosened gradually with a small angle increment and the impedance spectra were recorded. Then, the measured data were compressed through dividing the frequency range into multiple subbands. And RMSD values of these bands showed that data points were reduced while damage features remained. Finally, one four-layered BP neural network model was constructed based on these compressed data. The research results showed that compressed impedance data could retain their damage features. After the training, the developed neural network model could not only determine the location of loosened rod, but also quantify the loosening levels.

1. **Introduction**

As an effective structural health monitoring technique, electromechanical impedance (EMI) technique has gained widespread attention for its traits of high local sensitivity, easy installation of sensors, and nonparametric model analysis [1–3]. EMI technique has unique advantages, especially in the field of real-time health monitoring of some complex and irregular structures, such as truss structures [4] and connection bolts. The influence of the added mass and shape of PZT patches was also reported [6].

Sun et al. [4] first proposed EMI technique to monitor the health state of truss structures and validated the effectiveness and potential of this technique to characterize such complex and irregular structures. Yan et al. [7] combined EMI technique with reverberation matrix method to quantitatively evaluate structural damage in Timoshenko beams. To solve the difficulty in the evaluation of damage severity and location, Yang and Divsholi [8] and Divsholi and Yang [9] divided the whole testing frequency range into multiple subbands. Annamdas and Yang [10] adopted EMI technique to monitor the health state of excavation support structures after experimental study. The result showed that, although the variations in signatures were not exactly proportional to load magnitudes, such unexpected things could be predicted on the site in the presence of loads. These researches proved that the structure state, especially the state of complex and irregular structures, could be expressed with EMI technique. However, it is always difficult to obtain visual results through direct observations of impedance spectrum. It is required to process raw data with artificial intelligence algorithms, such as neural network technology.

Artificial neural network is a kind of intelligent damage identification system. With nonlinear mapping ability, parallel computation ability, and good robustness, the neural network can be used as the postprocessing tool of EMI
3. Experimental Study

In this paper, one three-layer truss structure was adopted as an experimental subject. For this truss structure sample, total height was 1500 mm and both length and width were 500 mm. The length of its diagonal rods was 700 mm, and all rods were connected through spherical ball joints with bolt holes. Structural health state was changed when connection rods were loose. The real part of impedance was recorded by PZT elements through a precise impedance analyzer. After compressing and normalization, these data were treated as input samples and neural network was established with these samples. Finally, damage states, that is, loosening levels of connection rods, will be quantified with the trained neural network.

As shown in Figure 2(b), experimental device consists of a precise impedance analyzer (Agilent 4294A), a personal computer (PC), and a truss structure. As experimental subjects, the rods 1, 2, 3, and 4 and joints A and B were labeled and illustrated in Figure 2(a). In this study, two identical circular PZT elements, with the 12 mm diameter and 1 mm thickness, were bonded on the surface of joints A and B, respectively. When damage states (i.e., loosening levels) of rods 1, 2, 3, and 4 were changed, impedance spectra would be correspondingly tested and recorded. As illustrated in Figure 2(b), in order to quantify the loosening levels of connection rods in experiments, the dial and the pointer were bonded on rod 3 and on the connector between the rod and joint B, respectively. The maximum deflection position of connection rods is 20 degrees from initial position by 2-degree angle increment. Measured impedance data measured with PZT elements can be imported from impedance analyzer to PC through GPIB interface.

3.1. Selection of Experimental Frequency Band. Generally, the most sensitive frequency band is always in the testing frequency range containing multiple peaks [15, 16]. However, monitoring area will greatly decrease if EMI technique is applied in the excessively high frequency range (above 500 kHz) [17]. In this paper, the frequency range from 100 kHz to 300 kHz was selected as the initial testing range. Figure 3 shows the real impedance spectra in the range of 100–300 kHz measured at joints A and B under health states. According to Figure 3, it can be found that the peaks of impedance spectra obtained at joints A and B are mainly between 160 kHz and 240 kHz.

2. Principle of Structural Health Monitoring Based on EMI Technique

Theoretical basis of EMI technique was first put forward by Liang et al. [14]. He analyzed one-dimensional model of the structure with PZT element. PZT impedance values were only related to structural mechanical impedance. Figure 1 is the 1D model adopted by Liang et al. [14].

According to the coupling effect, the positive and inverse piezoelectric effects, and frequency dependent admittance of PZT, Y(ω) can be expressed as in the following equation:

\[
Y(\omega) = \frac{1}{V} = i\omega \left( e_{33}^{PZT} (1 - i\delta) - \frac{Z_s(\omega)}{Z_s(\omega) + Z_a(\omega)} d_{33}^a \right)
\]

where \(Z_a\) is mechanical impedance of PZT; \(Z_s\) is structural mechanical impedance; \(\overline{Y}^E\) is the complex Young modulus of PZT; \(d_{33}^a\) is coupling coefficient between PZT and structure; \(\varepsilon\) is the dielectric constant; \(\delta\) is the dielectric loss tangent of the PZT; \(a\) is the geometry constant of PZT. According to (1), the first part of the equation only contains parameters of PZT, which remain unchanged if PZT elements are fixed on the surface of structure. Admittance value will be decided only by \(Z_s\). Thus, structural damages, defects, connection conditions, or other physical changes can be represented by the variation of impedance spectra, which are measured by PZT element.
Since it is difficult to obtain intuitive results through direct observations of impedance variation, statistical algorithms are usually used to process impedance spectra [18–20]. One of the most common statistical algorithms is root mean square deviation (RMSD). Deviation degree among impedance spectra under different damage states can be converted into damage indices with RMSD to evaluate structural damage state according to the comparison results of damage indices.

Since sensitive frequency band could improve the sensitivity of defect detection and quantification, the first step was to determine a proper frequency band by the trial-and-error approach.

Experimental procedure of determining sensitive sub-bands was shown as follows. Firstly, the whole test frequency range was divided into 10 subbands and impedance spectra were recorded. Each subband was 20 kHz and contained 401 data points. Secondly, rod 1 was loosened to the maximum deflection position (20 degrees) and impedance spectra were recorded as step 1. Then, rod 1 was restored to its initial position. Finally, rod 2 was loosened to the maximum deflection position (20 degrees) and impedance spectra were recorded as step 1.

The whole testing frequency range was divided into 10 subbands and each subband included 401 data points. One RMSD value in each subband can be calculated. Therefore, the total number of RMSD sets was 10 in the whole frequency spectrum. Each RMSD in subband was

\[
M = \sum_{i=1}^{n} \sqrt{\frac{(Z_{i,1} - Z_{i,2})^2}{(Z_{i,1})^2}},
\]

where \(M\) represents the RMSD value of subband; \(Z_{i,1}\) is the impedance value of the \(i^{th}\) frequency point in this subband under health state or baseline state; \(Z_{i,2}\) is impedance value of the \(i^{th}\) frequency point in this subband under damage state. It can be found that damage indices will increase with the increment of impedance spectra deviation degree between damage state and health state, indicating the more severe damage state [19].

Firstly, the data obtained from step 1 were treated as baseline state and the data obtained from step 2 were treated as the damage state. Damage indices of different frequency ranges could be calculated when rod 1 was in the loose state. Then, rod 1 was restored to its initial position. The data from step 4 were treated as the damage state while spectrum data from step 1 were treated as baseline. Damage indices of different frequency range could be calculated when rod 2 was in the loose state. Then, joint B was tested according to the same method. Therefore the sensitivity of different subbands was represented by RMSD values, as shown in Figure 4. Series number of bands, such as 1 and 2, represents the subbands of 100–120 kHz and 120–140 kHz, respectively.

When the monitoring point is joint A, EMI technique shows the highest sensitivity to the loosening levels of rods in the frequency range of 160–220 kHz; when the monitoring point is joint B, EMI technique shows the highest sensitivity in the frequency ranges of 120–180 kHz, 200–220 kHz, and 260–300 kHz. Therefore, the frequency range of 160–180 kHz was selected for further study, which was very sensitive to the variation of joints A and B.

3.2. Tests in Different Loosening Levels of Rods. In order to obtain impedance spectra of the truss structure with different rods under different loosening levels, the experiments were performed according to the following procedure. Firstly, rod 1 was loosened to the maximum deflection position. Then, rod 1 was tightened to the initial position. The real part of impedance spectrum was recorded after each variation until rod 1 was tightened to its initial state. Each data set contains 401 data points. While the rod was loosened to the maximum deflection position, it was defined as state 1 and the initial position was defined as state II. Because impedance spectra corresponding to rod 1 were nearly unchanged, rod 1 was loosened to exceed the maximum deflection position. These spectra could indicate all loosening levels of rod 1 if...
Figure 3: Real impedance spectra in the range of 100–300 kHz measured from (a) joint A and (b) joint B under health states.

Figure 4: RMSD values calculated from different subbands when (a) rod 1 and rod 2 and (b) rod 3 and rod 4 of the truss structure were loosened to determine sensitive frequency band.

other rods remained unchanged. The same procedures were performed to determine other damage states. Similarly, after rod 1 returned to its initial position, the spectra of rod 2, rod 3, and rod 4 were tested according to the same experimental procedure for rod 1. The total number of data sets was 44. Figure 5 shows the impedance spectra measured by PZT elements. For the purpose of observation, only the spectra corresponding to the states 1, 3, 5, 7, and 9 were given, and some parts of these figures were zoomed so that variances of spectra could be found.

From these zoomed parts shown in Figure 5, it is obvious that impedance peaks start to move horizontally and vertically when these rods are tightened gradually. Comparing Figures 5(a) and 5(b) with Figures 5(c) and 5(d), the most obvious phenomenon is that the spectra measured at joint A contain more impedance peaks.

In this study, impedance spectra remained nearly unchanged when the looseness of rods was more serious than that of state 1. Therefore, the spectra corresponding to state 1 of each rod were selected as baseline and RMSD values were calculated with (2). The results were shown in Figure 6. It is compatible with the previous arguments that RMSD values corresponding to joint A are generally larger than those corresponding to joint B, since there are more impedance peaks in spectra measured from joint A. It can be also found that RMSD values corresponding
to rod 2 are generally larger than those corresponding to rod 1 and that RMSD values corresponding to rod 3 are larger than those corresponding to rod 4, indicating that the variations of impedance spectra are different, even at the same joint. However, for one certain rod, RMSD values increase monotonously. Therefore, damage location can be determined by the differences among RMSD values corresponding to different rods and the severity of loosened rod can be evaluated based on the characteristics of monotonic increment of RMSD values.

3.3. Loosening Identification and Quantification Based on BP Neural Network. In this study, one BP neural network was adopted to process measured data so that loosening levels could be expressed quantitatively and more clearly. Figure 7 provides a simplified model of this kind of network. Training samples and testing samples are imported from input layer. The calculated results were exported from output layer.

Theoretically, neural network with one hidden layer is enough to simulate any nonlinear relationship between inputs and outputs. But this network could not meet the requirements of too high precision. Therefore, in this study, neural network included one input layer, two hidden layers, and one output layer. Sigmoid nonlinear function was selected as transfer function. Connective weights and bias values were assigned randomly and network was partly initialized.

Each impedance spectrum measured by the impedance analyzer contains 401 data points. If these data points are all treated as input vectors, network training speed will become...
As shown in Figure 6, RMSD values calculated from the whole frequency band increased as the rods were restored to their initial positions. However, as shown in Figures 5(a) and 5(b), impedance spectra also show monotonous variation in some local frequency bands. Even if the total frequency range is divided into several subbands and RMSD values are calculated, damage features can be distinguished from each other. RMSD values calculated from different subbands are shown in Figure 8. The total frequency range was divided into 10 subbands. For the rods 1 to 4, state 1 was treated as their respective baselines and (2) was applied to calculate RMSD values. In order to ensure that all subfrequencies contained the same number of data points, the first frequency band of 160–162 kHz included points 1 to 41 and the second frequency band of 162–164 kHz included points 41 to 81. A series of numbers were assigned to represent different frequency bands. For example, the numbers 1 and 2 represent 160–162 kHz and 162–164 kHz, respectively.

As illustrated in Figure 8(a), RMSD values increase monotonically in 160–162 kHz and 170–180 kHz. Furthermore, the same phenomenon appears in the following frequency bands: 166–172 kHz and 174–178 kHz (Figure 8(b)); 162–166 kHz, 170–174 kHz, and 178–180 kHz (Figure 8(c)); 168–178 kHz in Figure 8(d). And it can be found that, in other frequency bands, these RMSD values do not increase monotonically. But experimental results by Min proved that neural network could adjust the weights as required during the training process [21, 22]. If the variation trend of RMSD values of one band is similar to that of target results, RMSD values measured in this band have the most significant influence on output results after the training, such as band 1, band 6, and band 8 in Figure 8(a). But the influences on other bands are small. Therefore the compressed impedance data could be all treated as input vectors and the effect of irregular changes will decrease as training error converges to target value.

As shown in Figure 6, RMSD values corresponding to the rods connected to the same joints under different states: (a) rod 1 and rod 2; (b) rod 3 and rod 4.

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It is obvious that RMSD values of different subfrequency ranges corresponding to the variations of joints A and B are different. And those values corresponding to the variations of rods connected to the same joint are not the same as well. RMSD values calculated from the variations of rods connected to joint A are always larger than the RMSD values.
Figure 8: RMSD values of different subfrequency ranges for the structure under different health states and the color of histograms: (a) the variation of rod 1; (b) the variation of rod 2; (c) the variation of rod 3; (d) the variation of rod 4.

In this study, RMSD values are normalized through (3) and treated as input vectors. Within these vectors, 12 data sets were selected as testing samples, while others were treated as training samples:

$$R = \frac{r - r_{\min}}{r_{\max} - r_{\min}}$$

(3)

In this equation, $r$ and $R$ represent RMSD values before and after normalization, respectively. $r_{\min}$ and $r_{\max}$ represent the minimum and maximum RMSD values in all input data, respectively. From the previous discussion, it can be concluded that the larger the number of the divided frequency subbands is, the more the comprehensive information compressed data will be contained and the easier it is to improve the ability of damage identification. Since more input data would decrease training rate and lead to the difficulty of network convergence, more tests were performed to select the properly divided frequency subbands. Finally, the number of divided frequency subbands was confirmed to be 25. The first hidden layer contained 100 neurons. The second hidden layer contained 50 neurons and output layer contained 3 neurons. The first and the second neurons of output layer were defined as damage location and the third neurons were defined as damage information. The three neurons were, respectively, joint number, rod number, and severity. Joint number 0 represents joint A while joint number 1 represents joint B. Rod number 0 represents rod 1 or rod 3 while rod number 1 represents rod 2 or rod 4. Severity outputs were 0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, and 1, which were multiplied by 10 to obtain intuitive results. For example, 012 indicated that...
Table 1: Expected outputs and actual outputs of testing samples.

<table>
<thead>
<tr>
<th>Rod 1</th>
<th>Damage states</th>
<th>2</th>
<th>4</th>
<th>8</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output</td>
<td>Expected</td>
<td>0</td>
<td>0</td>
<td>1–3</td>
</tr>
<tr>
<td></td>
<td>Actual</td>
<td>0.0004</td>
<td>0.0001</td>
<td>1.6398</td>
</tr>
<tr>
<td>Rod 2</td>
<td>Damage states</td>
<td>1</td>
<td>3</td>
<td>7</td>
</tr>
<tr>
<td>Output</td>
<td>Expected</td>
<td>0</td>
<td>1</td>
<td>0–2</td>
</tr>
<tr>
<td></td>
<td>Actual</td>
<td>0.0062</td>
<td>0.9990</td>
<td>1.0841</td>
</tr>
<tr>
<td>Rod 3</td>
<td>Damage states</td>
<td>2</td>
<td>7</td>
<td>9</td>
</tr>
<tr>
<td>Output</td>
<td>Expected</td>
<td>1</td>
<td>0</td>
<td>1–3</td>
</tr>
<tr>
<td></td>
<td>Actual</td>
<td>0.9977</td>
<td>0.0002</td>
<td>1.9314</td>
</tr>
<tr>
<td>Rod 4</td>
<td>Damage states</td>
<td>1</td>
<td>5</td>
<td>8</td>
</tr>
<tr>
<td>Output</td>
<td>Expected</td>
<td>1</td>
<td>1</td>
<td>0–2</td>
</tr>
<tr>
<td></td>
<td>Actual</td>
<td>0.9946</td>
<td>0.9975</td>
<td>1.6656</td>
</tr>
</tbody>
</table>

rod 2 connected to joint A was under damage state 2; 113 indicated that rod 4 connected to joint B was under damage state 3.

For rod 1, damage states 2, 4, and 8 were selected as testing samples, as shown in Table 1. For other rods, testing samples were also shown in Table 1. Then other data sets were treated as training samples. The target error was 0.0005 and neural network was built and trained. After training for 4634 times, target error reached the allowed limits. Testing samples were imported into the trained neural network and testing results were shown in Table 1. However, if one sample was not involved in training process, the network could only evaluate its damage state through the information contained in the training sample. For test samples, only the upper and lower limits of damage severity were given. Since the increment of adjacent RMSD values is irregular, the trained network can determine the range of damage severity and cannot yield an exact value. For one sample corresponding to damage state $n$, if its damage severity is classified into the level between $n-1$ and $n+1$, this result can be treated as correct result. According to this criterion, damage location can be identified solely by the trained network and almost all damage states can be evaluated correctly. Only the output result corresponding to rod 3 under state 7 has an error rate which is 1.1% above the upper limit. This means that the trained network cannot only recognize the location of loose rods but also quantitatively evaluate its loosening levels. Therefore, the combination of EMI technique and artificial neural network will have a broad application prospect in intelligent health monitoring of complex structures including truss structures.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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