Research Article
Theoretical Modelling and Effectiveness Study of Slotted Stand-Off Layer Damping Treatment for Rail Vibration and Noise Control

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A promising means of reducing railway noise is to increase the damping of the rail, which decreases the vibration of the rail to reduce noise. To achieve this goal, a slotted stand-off layer damping treatment has been developed, and a compound track model with this treatment is developed for investigating the effectiveness of this treatment in terms of the vibration reduction. Through the dynamic analysis of the track undergoing the slotted stand-off layer damping treatment, some guidelines are proposed on the selection of materials and structure parameters for this treatment. In addition, the prototype of the optimal slotted stand-off layer damping treatment has been built and tested in the laboratory. It is found that the slotted stand-off damping treatment shows significant effects in decreasing the amplitude of the acceleration of the rail and a significant reduction of sound emission reflected as the radiation sound pressure level decreases by 8.2 and 9.4 dB at vertical excitation and lateral excitation, respectively, in the frequency range of 0–4000 Hz.

1. Introduction

With the development of the high-speed railway and urban rail transit, railway noise has become a growing public concern in the world today. There are plenty of noise sources associated with the railway. However, in general, railway noise is composed mainly of three types: rolling noise, traction noise, and aerodynamic noise [1]. Figure 1 presents the predominant noise sources in the total noise level depending on train speed, of which rolling noise is the greatest contributor to the overall noise level when the train is running at a speed of less than 300 km/h [2].

Extensive work has been conducted to understand the mechanism of railway rolling noise generation [3–6]. The vibration of the wheel, rail, and sleeper caused by surface roughness of the rail and train wheel contributes to the overall spectrum of noise. Figure 2 shows, over the whole frequency range, the contribution of the three elements. It is an example of the calculations by Thompson with the TWINS software, which have been validated in extensive field measurements [7, 8]. Amongst them, the rail is a dominant source in the frequency region of 450–2000 Hz, and it generates a larger contribution to the total noise above 2000 Hz. This fact means that rail radiation is one of the significant sources of rolling noise.

Numerous measurements have been taken to mitigate the acoustic emission of rails; however, the application of dampers to the rail, in the form of dynamic absorbers or superficial damping layers, is theoretically and practically the most effective. A dynamic absorber can be designed to affect only some specific frequencies so that their damping effect is concentrated within the frequency ranges of interest. Many experts have paid much attention to the application of dynamic absorbers in rails. Maes and Sol presented a double tuned rail damper, which is used to reduce the first two vertical “pined-pined” vibrations of the rail. The damper is mounted between two sleepers on the rail. Measurements at a test track of the French railway company showed that the wave decay rate of rail vibration can be effectively increased by the rail damper [9]. Ho et al. developed a
2. Working Principle of the Slotted Stand-Off Layer Damping Treatment

Applying a surface damping treatment to a stiff beam, plate, shell, and other thin-walled structures can reduce the amplitude of a vibration [16]. When the damping treatment is applied as a single-layer coating, sometimes known as a free-layer damping, energy is dissipated as a result of the extension and compression of the damping material while the base structure bends during vibration. A significant increase in energy dissipation can be achieved by attaching a stiff layer (or constraining layer) on top of the viscoelastic layer, as shown in Figure 3. This dissipation occurs because large shear strains are generated in the damping material when the system bends during vibration. Adding a stand-off layer
to the constraining damping treatment between the base layer and the damping layer could further increase the shear angle of the damping layer. This damping treatment has been termed passive stand-off layer damping treatment. However, for the effective operation of passive stand-off layer damping treatment, the stand-off layer must have high shear stiffness and, at the same time, must not significantly affect the bending stiffness of the composite structure. Based on this principle, in one variation of passive stand-off layer damping treatment, slots are introduced into the stand-off layer. Slotted stand-off layer damping treatment, as shown in Figure 4, has been thought to have an important advantage over continuous passive stand-off layer damping treatment [17].

In general, the stand-off layer has no internal damping properties. Therefore, the damping ratio $\eta$ is used to assess the vibration reduction effect of the stand-off layer damping treatment as the traditional constraining damping treatment. The damping ratio $\eta$ can be defined, according to the “strain energy method,” as the ratio between the energy dissipated by the damping layer in each strain cycle and that stored in the system:

$$\eta = \frac{D_0}{2\pi W_0},$$

(1)

where $D_0$ is the dissipated energy in the damping layer and $W_0$ is the stored energy of the system in a strain cycle.

As for $D_0$,

$$D_0 = \pi \cdot G''(\omega) \cdot V \cdot \gamma^2,$$

(2)

where $\gamma$ is the shear strains of the damping layer, $G''(\omega)$ is the loss modulus of the damping material, and $V$ is the volume of the damping layer. The addition of a slotted stand-off layer only increases shear strains, thereby reducing the vibration of the base layer more effectively.

### 3. Optimisation Analysis of Slotted Stand-Off Layer Damping Treatment

Some studies have been conducted in the past to investigate the application of stand-off layer damping treatment in industrial fields and the corresponding calculation of their damping ratios. Generally, the theoretical solution for the loss factor calculation is unfortunately available only for simple geometry structures. More recently, an alternative approach, based on numerical finite element calculations, allowed the consideration of a different component shape, as in the case of a rail. Furthermore, in the slotted stand-off layer damping treatment system, the bonding layers used to connect these layers are found to have a measurable and significant effect on the response of the structure. Therefore, the finite element model presented here includes an epoxy layer between the base layer and the slotted stand-off layer and a contact cement layer between the slotted stand-off layer and the damping layer. The six-layered model incorporating a primer layer and an epoxy layer, as shown in Figure 5, proposed by Yellin et al. [18], is adopted in this study to model slotted stand-off layer damping treatment.

#### 3.1. Numerical Procedure for the Damping Ratio Calculation

In the present work, an approach based on a steady-state harmonic analysis in the frequency range of interest has been adopted. This approach directly integrates the equations of motion of the system. Thus, all of the vibration modes involved at any excitation frequency will be taken into consideration. This approach, therefore, simulates the actual behaviour of the component. To this end, a postprocessing
procedure for the ANSYS commercial code has been developed and can be generally applied to any component shape and material. In particular, the dependence of the elastic and viscous properties of the damping layer material on frequency and temperature will be taken into account to define these properties directly as supplied by the producer. The results calculated in this way are very flexible.

The specific procedure calculates the damping ratio \( \eta \) in the discretized form.

(a) The dissipated energy \( D_0 \) mainly derives from the shear deformations of the damping layer:

\[
D_0 = \sum_i (D_0)_i = \sum_{j=1}^{2\pi} W''_{\text{shear},i},
\]

whereby

\[
W''_{\text{shear},i} = \iiint G''(\omega) \sum_{j=1}^{2\pi} \gamma_{ij}^2 \, dx \, dy \, dz,
\]

so,

\[
D_0 = \pi \cdot G''(\omega) \sum_i \left[ V_i \sum_{j=1}^{2\pi} \gamma_{ij}^2 \right].
\]

(b) The stored energy \( W_0 \) mainly derives from two parts, namely, the stored energy from the damping layer generated by shear deformations and the stored energy from the other five layers generated by elastic deformations:

\[
W_0 = \sum_i (W_0)_i = \sum_i \left( W_s + W_v + W'_{\text{shear}} \right),
\]

where \( W_s \), \( W_v \), and \( W'_{\text{shear}} \) denote the elastic deformation energy.

For the \( i \)th element \((i = 1 \ldots n)\),

\[
W_i = \frac{1}{2} \left( \sigma_1^2 + \sigma_2^2 + \sigma_3^2 \right)
\]

\[
= \frac{1}{2E} \left[ \sigma_1^2 + \sigma_2^2 + \sigma_3^2 - 2\nu (\sigma_1 \epsilon_1 + \sigma_2 \epsilon_2 + \sigma_3 \epsilon_3) \right],
\]

\[
W_v = \frac{1}{2E} \left( \sigma_1 + \sigma_2 + \sigma_3 \right) (\epsilon_1 + \epsilon_2 + \epsilon_3)
\]

\[
= \frac{1 - 2\nu}{6E} (\sigma_1 + \sigma_2 + \sigma_3)^2
\]

\[
= \frac{3(1 - 2\nu)}{2E} \sigma_{\text{oct}}^2,
\]

\[
W_{Si} = W_{ij} - W_v
\]

\[
= \frac{1}{2E} \left[ \sigma_1^2 + \sigma_2^2 + \sigma_3^2 - 2\nu (\sigma_1 \epsilon_1 + \sigma_2 \epsilon_2 + \sigma_3 \epsilon_3) \right]
\]

\[
- \frac{1 - 2\nu}{3} (\sigma_1 + \sigma_2 + \sigma_3)^2
\]

\[
= \frac{1}{12G} \left[ (\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2 \right]
\]

\[
= \frac{1}{6G} \sigma_{\text{Mises}}^2
\]

\[
= \frac{1 + \nu}{3E} \sigma_{\text{Mises}}^2
\]

\[
W_{\text{shear},i} = \frac{G'(\omega)}{2} \sum_{j=1}^{2\pi} \gamma_{ij}^2.
\]

Substituting (7) into (6) gives

\[
W_0 = \sum_i V_i \left[ \frac{1 + \nu}{3E} \sigma_{\text{Mises}}^2 + \frac{3(1 - 2\nu)}{2E} \sigma_{\text{oct}}^2 + \frac{G'(\omega)}{2} \sum_{j=1}^{2\pi} \gamma_{ij}^2 \right],
\]

where \( V_i \) is the volume of the \( i \)th element, \( \gamma_{ij} \) is the \( j \)th shear deformation of the \( i \)th element, \( \sigma_{\text{Mises}} \) is the von Mises stress of the \( i \)th element, \( \sigma_{\text{oct}} \) is the octahedral stress of the \( i \)th element, \( G' \) is the storage shear modulus, \( G'' \) is the loss shear modulus, \( E \) is Young’s modulus of elasticity, and \( \nu \) is the Poisson ratio.

The damping ratio \( \eta \) can be obtained by substituting (5) and (8) into (1).

3.2. Choice of the Material and Configuration of the Slotted Stand-Off Layer Damping Treatment. Several commercial damping materials were examined in this project. One of these, VER-IPN, was chosen because of its high loss-factor values in the temperature and frequency ranges of interest, as depicted in Figure 6. The slotted stand-off layer was made from Dyad606 with high shear strength. Its density and Young’s modulus of elasticity were 1200 kg/m² and 500 MPa, respectively, as tested. Although the epoxy layer and primer layer were relatively thin, they should be as stiff as possible; therefore, a strong adhesive that has good synthetic properties was developed. The adhesive had a tensile modulus of approximately 1.65 GPa. The material used for the constraining layer can be either Al-2A14, with an elastic modulus of \( E = 73.1 \) GPa, or steel-3Cr13Mo, with an elastic modulus of \( E = 206 \) GPa.

However, it is not easy to choose the best arrangement for slotted stand-off damping treatment. The rail waist and the rail foot are the weakest zones of the rail; therefore, such parts appear to be the most feasible in terms of application...
and the most promising in terms of effectiveness. However, this solution shows difficulties in shaping the damping layer to match the rail profile. A 60 kg/m rail, which is the most widely used in China, is studied in this paper. The basic idea is to apply a slotted stand-off damping treatment to specified zones of a widely used rail, without additional machining operations on the rail itself. Several solutions were initially proposed and examined, taking the following design requirements into consideration: damping efficiency, safety, and reliability under working conditions (in particular, mechanical resistance, weathering resistance, moisture and solvent resistance, and thermal and fire resistance), ease of manufacturing and application, weight, and cost. Finally, the slotted stand-off layer damping treatment is arranged according to the special structure of the rail, as depicted in Figure 7, consisting of four major parts: an inverted T-shaped constraining layer of uniform thickness (3), connected to the rail with a slotted stand-off layer with uniform thickness (1) and sandwiched between the slotted stand-off layer and the constraining layer with a slot with a thickness-variable damping layer (2); the rail (4) is surrounded by stand-off layer. The strong adhesive is applied to each layer.

The numerical procedure described above was used to examine the effectiveness of different configurations. The modifiable structural size of the slotted stand-off layer damping treatment was defined, as shown in Figure 8. In particular, the calculations were carried out for the following seven cases (also shown in Table 1), where \( h_1 \) is the zone thickness of the slotted stand-off layer without slots, \( h_2 \) is the slot thickness of the slotted stand-off layer, \( t_1 \) is the slot width, \( t_2 \) is the zone width of the slotted stand-off layer without slots, \( h_3 \) is the thickness of the constraining layer, \( t_3 \) are the three important structural sizes of the constraining layer, and \( \alpha \) is the slope of the constraining layer.

Previous research has shown that the length of a rail mode with twelve spans can yield the whole resonance and antiresonance characteristics of a rail in the frequency range of 0–5000 Hz [19]. Thus, the length of the rail mode with twelve spans (with a total length of 7.2 m) is applied in the present work. The rails are fastened by the WJ-7 flexible fastening systems every 0.6 m, and the fastening systems are fixed on the prestressed reinforced concrete sleepers III. Moreover, the operating temperature of the damping material is assumed to be 30°C. To represent realistic working conditions, two forcing actions, one twice as much as the other, are applied simultaneously on the railhead surface in the vertical and lateral directions, as shown in Figure 9; these actions simulate the typical main loads transmitted from the wheel to the rail (11).

The force \( F \) is calculated as follows:

\[
F = (1 + \alpha_1) \cdot (1 + \alpha_2) \cdot P,
\]

where \( \alpha_1 = 0.6 \frac{\nu}{100} \), \( \alpha_2 = 0 \), when \( \nu \) is less than 120 km/h,

\[
\alpha_1 = 0.72, \quad \alpha_2 = 0.3 \frac{\Delta \nu}{100}, \quad \Delta \nu = \nu - 120,
\]

when \( \nu \) is larger than 120 km/h,

\[
\text{where } \nu \text{ is the vehicle speed and } P \text{ is the axle load of the vehicle.}
\]

The axle load \( P \) of 15T (CRH3 high-speed train) is studied in this paper, and the speed of the train is 300 km/h. Therefore, the force \( F \) is 397,270 N.

4. Results

Thirteen representative frequencies were chosen from the modal analysis of the track model described above. The damping ratios calculated from the seven different cases are shown in Table 2. The following can be deduced from Table 2.

(a) The damping ratio \( \eta \) of the rail with the slotted stand-off layer damping treatment is mostly greater than 0.017. However, the \( \eta \) of the standard rail is only 0.0001–0.0006. This result means that the damping ratio \( \eta \) of the rail with the slotted stand-off layer damping treatment far outweighs the \( \eta \) of the standard rail.

(b) The zone thickness of the slotted stand-off layer without slots imposes different influences on specific eigenmodes, as noted by comparing the results of Cases 1 and 2. The thickness of Case 1 is more effective for the first, third, fifth, sixth, eighth, and thirteenth eigenmodes, whereas that of Case 2 is more effective for the other eigenmodes. Furthermore, in view of the great rigidity of the material of the slotted stand-off layer, as mentioned, it is more reasonable to apply the thickness from Case 2.

(c) The structural dimensions of the slot exert a strong influence on the damping ratios, as highlighted by comparing the results of Cases 2 and 3 and Cases 4 and 5: the thicker and wider the slot, the greater the damping ratios in the frequency range of greatest interest. The influence of the zone width of the slotted stand-off layer without the slot is contrary to the structural dimensions of the slot: the wider the zone of the slotted stand-off layer without slots, the smaller the total width of the slot.
Figure 7: Cross section of the rail with the slotted stand-off layer damping treatment.

(a) Cross section of the rail with damping treatment
(b) Detailed characteristic of slotted stand-off layer

Figure 8: Parameter definitions of the slotted stand-off layer damping treatment.

Table 1: Tests of the material and configuration.

<table>
<thead>
<tr>
<th>Case</th>
<th>$h_{1i}/\text{mm}$</th>
<th>$t_{c1}/\text{mm}$</th>
<th>$\alpha$</th>
<th>$t_{c2}/\text{mm}$</th>
<th>$t_{c3}/\text{mm}$</th>
<th>$h_{c}/\text{mm}$</th>
<th>$h_{c2}/\text{mm}$</th>
<th>$t_{s2}/\text{mm}$</th>
<th>$t_{s1}/\text{mm}$</th>
<th>Damping layer material</th>
<th>Constraining layer material</th>
</tr>
</thead>
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<tr>
<td>1</td>
<td>8</td>
<td>100</td>
<td>4%</td>
<td>55</td>
<td>45</td>
<td>3</td>
<td>2</td>
<td>30</td>
<td>20</td>
<td>VER-IPN</td>
<td>Al-2A14</td>
</tr>
<tr>
<td>2</td>
<td>6</td>
<td>100</td>
<td>4%</td>
<td>55</td>
<td>45</td>
<td>3</td>
<td>2</td>
<td>30</td>
<td>20</td>
<td>VER-IPN</td>
<td>Al-2A14</td>
</tr>
<tr>
<td>3</td>
<td>6</td>
<td>100</td>
<td>4%</td>
<td>55</td>
<td>45</td>
<td>3</td>
<td>3</td>
<td>30</td>
<td>20</td>
<td>VER-IPN</td>
<td>Al-2A14</td>
</tr>
<tr>
<td>4</td>
<td>6</td>
<td>100</td>
<td>4%</td>
<td>55</td>
<td>45</td>
<td>3</td>
<td>3</td>
<td>20</td>
<td>20</td>
<td>VER-IPN</td>
<td>Al-2A14</td>
</tr>
<tr>
<td>5</td>
<td>6</td>
<td>100</td>
<td>4%</td>
<td>55</td>
<td>45</td>
<td>3</td>
<td>3</td>
<td>20</td>
<td>30</td>
<td>VER-IPN</td>
<td>Al-2A14</td>
</tr>
<tr>
<td>6</td>
<td>6</td>
<td>100</td>
<td>4%</td>
<td>55</td>
<td>45</td>
<td>2</td>
<td>3</td>
<td>20</td>
<td>30</td>
<td>VER-IPN</td>
<td>Steel-3Cr13Mo</td>
</tr>
<tr>
<td>7</td>
<td>6</td>
<td>100</td>
<td>4%</td>
<td>55</td>
<td>45</td>
<td>2</td>
<td>3</td>
<td>20</td>
<td>30</td>
<td>VER-IPN</td>
<td>Steel-3Cr13Mo</td>
</tr>
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Table 2: Damping ratio $\eta$ of the seven cases.

<table>
<thead>
<tr>
<th>Frequency</th>
<th>Case 1</th>
<th>Case 2</th>
<th>Case 3</th>
<th>Case 4</th>
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<th>Case 7</th>
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<td>0.017</td>
<td>0.019</td>
<td>0.021</td>
<td>0.025</td>
<td>0.024</td>
<td>0.028</td>
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<td>200</td>
<td>0.022</td>
<td>0.023</td>
<td>0.024</td>
<td>0.026</td>
<td>0.031</td>
<td>0.031</td>
<td>0.035</td>
</tr>
<tr>
<td>600</td>
<td>0.033</td>
<td>0.031</td>
<td>0.034</td>
<td>0.035</td>
<td>0.044</td>
<td>0.042</td>
<td>0.044</td>
</tr>
<tr>
<td>1000</td>
<td>0.041</td>
<td>0.042</td>
<td>0.044</td>
<td>0.048</td>
<td>0.059</td>
<td>0.061</td>
<td>0.065</td>
</tr>
<tr>
<td>1300</td>
<td>0.132</td>
<td>0.128</td>
<td>0.119</td>
<td>0.129</td>
<td>0.163</td>
<td>0.156</td>
<td>0.187</td>
</tr>
<tr>
<td>1500</td>
<td>0.209</td>
<td>0.231</td>
<td>0.214</td>
<td>0.248</td>
<td>0.287</td>
<td>0.293</td>
<td>0.358</td>
</tr>
<tr>
<td>2100</td>
<td>0.164</td>
<td>0.163</td>
<td>0.171</td>
<td>0.187</td>
<td>0.212</td>
<td>0.218</td>
<td>0.269</td>
</tr>
<tr>
<td>2500</td>
<td>0.132</td>
<td>0.128</td>
<td>0.162</td>
<td>0.158</td>
<td>0.176</td>
<td>0.175</td>
<td>0.218</td>
</tr>
<tr>
<td>2700</td>
<td>0.121</td>
<td>0.130</td>
<td>0.152</td>
<td>0.175</td>
<td>0.185</td>
<td>0.194</td>
<td>0.191</td>
</tr>
<tr>
<td>3000</td>
<td>0.108</td>
<td>0.121</td>
<td>0.132</td>
<td>0.154</td>
<td>0.146</td>
<td>0.144</td>
<td>0.132</td>
</tr>
<tr>
<td>3400</td>
<td>0.290</td>
<td>0.321</td>
<td>0.414</td>
<td>0.374</td>
<td>0.392</td>
<td>0.389</td>
<td>0.432</td>
</tr>
<tr>
<td>3700</td>
<td>0.415</td>
<td>0.436</td>
<td>0.356</td>
<td>0.498</td>
<td>0.564</td>
<td>0.544</td>
<td>0.614</td>
</tr>
<tr>
<td>4000</td>
<td>0.479</td>
<td>0.387</td>
<td>0.412</td>
<td>0.453</td>
<td>0.534</td>
<td>0.512</td>
<td>0.587</td>
</tr>
</tbody>
</table>

Figure 9: Schematic plot of the forcing actions.

(d) The thickness of the constraining layer has some effect on the damping ratio $\eta$ of the rail with slotted stand-off layer damping treatment, as shown by comparing the results of Cases 5 and 6. Case 5 has damping ratios slightly larger than that of Case 6 in addition to the fourth, sixth, seventh, and ninth eigenmodes. However, a 3 mm thick aluminium plate or steel plate is more difficult to be machined and shaped than 2 mm plates. Therefore, it is better to adopt the 2 mm thick constraining layer. The difference between steel and aluminium constraining layers (Cases 6 and 7) is significant, and the damping ratio of the former is obviously greater than that of the latter.

(e) In sum, to obtain as great of a noise reduction as possible in the frequency range of interest and to manufacture the system as easily as possible, Case 7 is the best choice.

5. Laboratory Measurements of Vibration and Noise

Laboratory measurements of accelerance and noise were carried out on the Chinese 60 kg/m standard rail with the slotted stand-off layer damping treatment according to Case 7 to test its actual effectiveness compared with that of the standard rail. For the sake of economy and convenience, the length of the standard rail with the slotted stand-off layer damping treatment was 0.6 m, as shown in Figure 10.

The characteristics of this slotted stand-off layer damping treatment are as follows.

(a) It has a total mass of 12 kg. Because the sleeper spacing is assumed to be 0.6 m, the mass per meter of rail length is 20 kg.

(b) It is designed to be fitted on the rail without any modifications made to the rail, to the sleepers, or to the supporting ballast layer.

(c) The adhesive strength of the efficient noise-reduction glue is proven to be effective after 2 million cycles of fatigue testing.

(d) The electrical isolation is maintained.

(e) The radiation of sound by the slotted stand-off layer damping treatment itself is negligible.

5.1. Laboratory Measurements and Analysis of Accelerance

The model used for laboratory measurements and analyses of acceleration of the rail with the slotted stand-off layer damping treatment and standard rail is presented below. The rail grid model was constructed with prestressed reinforced concrete sleepers III, on which there were fastened rails with the slotted stand-off layer damping treatment, or 60 kg/m standard rails using WJ-7 flexible fastenings. For the testing of the acceleration admittance of the samples, the method of measuring the response to mechanical shock was used in accordance with ISO 7626-5 [20]. Mechanical shock was stimulated using an impulse hammer in the vertical and lateral direction on the railhead. A part of this hammer is a force...
detector. The response was measured using accelerometers at different points of the rail structure, on the rail head, rail waist, and rail foot of the midpoint of the rail-specimen, as shown in Figure 11.

The measuring system consisted of a DHDAS-5920 PULSE modulator analyser for recording the vibration parameters together with three LC0102 acceleration detectors and a LC1303 shock stimulation hammer. The accelerometers were fastened to the measured construction by means of epoxy resin adhesives.

A comparison of the vertical and lateral accelerance of the rail head between the standard rail and the rail with the slotted stand-off damping treatment is depicted in Figures 12(a) and 12(b), respectively. In Figure 12(a), it is possible to observe a general decrease in the vertical accelerance amplitude of the rail head of the rail with the slotted stand-off damping treatment in the frequency range of 0–4000 Hz, relative to the case without the slotted stand-off damping treatment, as the maximum acceleration reading decreased from 0.29 m s\(^{-2}\)/N to 0.078 m s\(^{-2}\)/N. From Figure 12(b), the lateral acceleration amplitude of the rail with the slotted stand-off damping treatment is approximately 0.0015 m s\(^{-2}\)/N in the low frequency range of 0–200 Hz and the middle frequency range of 200–1000 Hz. This result means that the lateral vibration of the rail head in a frequency range of 0–2000 Hz is almost completely damped out by the slotted stand-off damping treatment. Additionally, it can be observed from the figure that compared to the standard rail, the lateral acceleration amplitude of the rail with the slotted stand-off damping treatment decreased from 0.05 m s\(^{-2}\)/N to 0.019 m s\(^{-2}\)/N in the high frequency range of 1000–4000 Hz. Thus, it was possible to obtain significant reductions in the vertical and lateral vibration levels of rail head by taking the slotted stand-off damping treatment approach in the frequency range of 0–4000 Hz.

Similar conclusions are observed in Figures 13 and 14, which present the analysis of the comparison of the accelerance of the rail waist and the rail foot between the standard rail and the rail with the slotted stand-off damping treatment. It can be observed from these figures that the performance of the slotted stand-off damping treatment placed at the surface of the rail for attenuating the vibrations of the rail waist and rail foot is quite effective in the frequency range of 0–4000 Hz.

Based on Figures 12, 13, and 14, it is possible to conclude that the slotted stand-off damping treatment decreases the amplitude of the accelerance of the rail in the frequency range of 0–4000 Hz, especially in the middle frequency range of 200–1000 Hz and the high frequency range of 1000–4000 Hz.

5.2. Laboratory Measurements and Analysis of Noise. The measurement procedure was conducted according to ISO 3744 for the source sound power emission calculation in free-field conditions by sound pressure measurements [21]. In this case, the sound power, which depends on the exciting force, was normalised by this force. The acoustic measurements were carried out in a semianechoic room according to the engineering method of ISO 3744 in the frequency range of 0–4000 Hz.

The model and its installation are the same as those applied in Section 5.1. The exciting force is an impulse caused by the falling weight (250 g). The vertical falling location is fixed over the midpoint of the rail-specimen along its length, 40 cm away from the rail head in the vertical direction and 3.5 cm away from the rail centreline in the lateral direction. Meanwhile, the lateral falling location is fixed over the midpoint of the rail-specimen along its length, 22 cm away from the rail head in the vertical direction and 45 cm away from the rail centreline in the lateral direction, as shown in Figure 15. The measurement was made using a microphone mounted on the midpoint of the rail-specimen along its
length and 50 cm away from the rail centreline in the lateral direction, as shown in Figures 16 and 17.

The laboratory results for the rail with the slotted stand-off damping treatment showed a significant reduction in sound emission compared to the standard rail under the vertical falling weight excitation, as shown in Figure 18; the radiation sound pressure level decreases by 8.2 dB. It can also be observed from Figure 19 that the rail with the slotted stand-off damping treatment produced less noise compared to the standard rail under the lateral falling weight excitation, with differences of up to 9.4 dB. Furthermore, within the frequency range of 200–4000 Hz, the noise level reduction is greater than that within the frequency range of 0–200 Hz under both vertical and lateral falling weight excitation.

6. Conclusions

The aim of this work was to design an innovative low-noise rail for high-speed trains. A slotted stand-off damping treatment was adopted for its effectiveness at reducing noise emission over a wide frequency range of 0–4000 Hz and for the possibility of applying it to existing rails. The choice of materials and treatment was the topic of the study. Several limitations had to be considered: ease of construction,
shaping and assembly, safety, commercial availability, weight, and costs. To better understand the influence of the design parameters and to aid in the selection of those parameters, a numerical finite element calculation method for the loss factor was developed, and extensive studies on an actual rail model were conducted. The results of these analyses led to the construction of a prototype with a 2 mm thick steel constraining layer, 6 mm thick Dyad606 stand-off layer with twelve slots that were 3 mm deep and 20 mm wide and were equally spaced at intervals of 30 mm, and a viscoelastic layer of varying thickness according to the thickness of the rail.
Laboratory measurements of the accelerance of the samples confirmed that the slotted stand-off damping treatment shows significant effects on decreasing the amplitude of the accelerance of the rail in the frequency range of 0–4000 Hz, especially in the middle frequency range of 200–1000 Hz and the high frequency range of 1000–4000 Hz. Noise emission measurements in the major acoustic interest range of 0–4000 Hz were also carried out in the laboratory. Compared to the standard rail emission, good noise reductions of approximately 8.2 dB under vertical excitation and 9.4 dB under lateral excitation were achieved in this test. In particular, the noise level reduction in the frequency range of 200–4000 Hz was greater than that within the frequency range of 0–200 Hz under both vertical and lateral falling weight excitation. Following these encouraging results, low-noise wheels proceeded to the production stage.

**Conflict of Interests**

The authors declare that there is no conflict of interests regarding the publication of this paper.

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