Research Article

Fair Resource Allocation with QoS Guarantee in Secure Multiuser TDMA Networks

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We investigate a secure multiuser time division multiple access (TDMA) system with statistical delay quality of service (QoS) guarantee in terms of secure effective capacity. An optimal resource allocation policy is proposed to minimize the $\beta$-fair cost function of the average user power under the individual QoS constraint, which also balances the energy efficiency and fairness among the users. First, convex optimization problems associated with the resource allocation policy are formulated. Then, a subgradient iteration algorithm based on the Lagrangian duality theory and the dual decomposition theory is employed to approach the global optimal solutions. Furthermore, considering the practical channel conditions, we develop a stochastic subgradient iteration algorithm which is capable of dynamically learning the intended wireless channels and acquiring the global optimal solution. It is shown that the proposed optimal resource allocation policy depends on the delay QoS requirement and the channel conditions. The optimal policy can save more power and achieve the balance of the energy efficiency and the fairness compared with the other resource allocation policies.

1. Introduction

Due to the broadcast nature of wireless communications, much more attention has been paid to the issues of privacy and security in wireless communication networks. Traditionally, security is achieved by cryptographic encryption protocols of the upper layers. However, the security of encryption will be invalid if the wiretappers have huge computational power. From the information-theoretic perspective, physical-layer security can guarantee the reliable secure transmission via utilizing the physical characteristics of wireless channels. The concept of information-theoretic secrecy was originally introduced by Shannon [1]. Then, a relaxed notion of secrecy was presented by Wyner in his seminal work [2] based on the concept of a wiretap channel model. It is shown that the transmitter can securely transmit the messages to the receiver with a non-zero rate (called secrecy rate) if the receiver enjoys better channel conditions than the eavesdropper. The results were subsequently extended to the broadcast channels [3] and Gaussian channel [4], respectively. Various physical-layer techniques, such as the use of interference or artificial noise to confuse the eavesdropper, the multi-antenna, beamforming, and resource allocation techniques, were proposed in [5–8] to improve the secrecy capacity, also known as the largest secrecy rate.

In recent years, a large amount of work has been devoted to the resource allocation based on physical-layer security. In [9–12], resource allocation schemes of OFDM secrecy systems were studied in the case of single-user system, two-user system, and multiuser system, respectively. Specifically, joint power and subcarrier allocation were investigated for the network with the coexistence of secure users and normal users [11]. Furthermore, a joint subcarrier and power allocation algorithm with artificial noise was designed in [12] to improve the security of the OFDM wiretap channels. In addition, the secure resource allocation was widely investigated in relay networks. Reference [13] considered an amplify-and-forward (AF) relay-aided secure multicarrier communication system...
and solved the resource allocation problem to maximize the sum secrecy rate. On the other hand, J. Huang proposed the cooperative jamming strategies for two-hop relay networks and investigated the optimization problem of maximizing the secrecy rate with certain power constraints and minimizing the transmit power with a fixed secrecy rate [14]. Moreover, large-scale multiple-input multiple-output (MIMO) technique was exploited by the relay system in the presence of a passive eavesdropper and an energy-efficient power allocation scheme was proposed in [15]. Recently, some researchers also focused on the secure resource allocation problem of the cognitive radio networks (CRNs) [16]. In [17], instantaneous and ergodic resource allocation problems were investigated in CRNs with guaranteed secrecy rate of the primary users. Secure robust resource allocation was taken into account for the relay-assisted CRNs in [18]. Different from the above two literatures, [19] proposed the power allocation policy for the physical-layer security in cognitive relay networks from the perspective of auction theory. Device-to-Device (D2D) communications have also been proposed recently to improve the spectral efficiency. Physical-layer security in D2D communications was studied in [20–22] and the corresponding resource allocation schemes were proposed.

It is worth mentioning that the framework employed above is not suitable for the delay-sensitive multimedia applications since Shannon theory places no restriction on the delay of the transmission scheme. However, delay-tolerant guarantee as one of the essential QoS merits plays a pivotal role in the secure communications. Furthermore, deterministic delay bound QoS is commonly not available in wireless networks due to the unpredictable nature of the wireless fading channels. Based on the effective capacity theory proposed by Wu and Negi in [23, 24], our preliminary work has investigated the delay QoS guarantee for secrecy system [25], which took the secure effective capacity as the QoS metric. Reference [26] also discussed the security problem under the QoS constraints for CR system with similar method. Secure effective capacity framework based on the effective capacity theory is employed as a bridge for the cross-layer model, where the queue at the data link layer can be served by the resource allocation scheme of the physical layer. It is a convenient approach to investigate the QoS support mechanisms for wireless secure communications.

As the extended application of the secure effective capacity for secure wireless networks, we propose a cross-layer model based on the power and time slot allocation policy for wiretap time division multiple access (TDMA) systems, where the delay-tolerant requirement is considered. Regarding the existence of multiple users in the system, a class of so-called $\beta$-fair cost functions was introduced to balance the energy efficiency and the fairness [27]. First, we discuss the issue of minimizing a general cost function of the average user power subjected to the delay QoS constraint of the individual user. A dual-based iterative algorithm based on the Lagrangian dual technique [28, 29] and the dual decomposition theory [30, 31] is employed to solve the optimization problem. In addition, according to the stochastic optimization theory, we develop a stochastic subgradient iterative algorithm with unknown cumulative distribution function (CDF) of the fading channel, which can dynamically learn the underlying channel distribution and approach the optimal solution. Then, we also provide the non-delayed policy without considering the delay QoS requirement for comparison.

To summarize, the main contributions of this work are as follows.

(1) The secure effective capacity based on the cross-layer framework is employed for the wiretap TDMA system.

(2) Based on the cross-layer framework, two resource allocation schemes are addressed, the optimal resource allocation policy, and the non-delayed resource allocation policy. The optimal policy adaptively allocates the power and time slot to minimize the utility functions of the average user power subjected to the delay QoS requirement. The non-delayed policy minimizes the objective function without considering the delay QoS guarantee.

(3) The optimization problem is solved and analyzed based on the Lagrangian duality theory and the stochastic optimization theory. The optimal policy can get better energy efficiency and also achieve the balance of the energy efficiency and the fairness.

The rest of the paper is organized as follows. Section 2 describes the system model and the delay QoS guarantee. The optimal resource allocation algorithm and the non-delayed resource allocation policy are proposed in Sections 3 and 4, respectively. Section 5 provides the numerical results to illustrate the performance of the proposed resource allocation schemes. Finally, conclusions and discussions are drawn in Section 6.

2. System Overview and Delay QoS Guarantee

In this section, we first present the system model of the wiretap TDMA system. Then, the issues of the statistical delay QoS guarantee are addressed based on the secure effective capacity.

2.1. System Model. In this paper, we investigate a network consisting of multiple users, one legitimate receiver, and one eavesdropper. $L$ users communicate with the legitimate receiver in the presence of an eavesdropper, which is shown in Figure 1. All the users are equipped with single antenna, and the solid and dash lines represent the main and the wiretap links, respectively. We adopt the TDMA scheme as the multiple access scheme to eliminate the multiple interference in the system and the channel is shared by multiple users at different time slots. For user $l$, let $h_l$ and $g_l$ denote the main and the wiretap channel power gains, respectively. We assume a discrete-time block-fading channel model such that $h_l$ and $g_l$ remain constant within a frame duration $T_f$ but experience a jointly stationary and ergodic fading process from one frame to another with continuously joint known probability density function (PDF). Then, at time slot $n$, the received signals at the legitimate receiver and the eavesdropper from the transmit user $l$ are given by

$$y_{l}(n) = \sqrt{h_{l}(n)}x_{l}(n) + a_{l}(n),$$
$$z_{l}(n) = \sqrt{g_{l}(n)}x_{l}(n) + b_{l}(n),$$

(1)
respectively, where $x_i(n)$ represents the transmitted signal, and $a_i(n)$ and $h_i(n)$ denote the corresponding additive white Gaussian noise (AWGN) with zero-mean and unit variance at the $i$-th legitimate receiver and the eavesdropper, respectively. Like [5, 7], we suppose that all the users have full knowledge of both the main channel state information (CSI) and the wiretap CSI which are described by the vectors $h := [h_1, \ldots, h_L]^T$ and $g := [g_1, \ldots, g_L]^T$, respectively, where $[.]^T$ denotes the transposition. Herein, we neglect the time reference for simplicity. We assume that each time slot is shared by multiple users over non-overlapping and dedicated time slots $\tau_l = 1$ and we have $\sum_{l=1}^L \tau_l \leq 1$. We further assume that the users allocated no transmission time slots will not be allocated any power. Given $\tau_l$ and the corresponding transmit power $p_l$, the instantaneous secrecy rate of the $l$-th user is given by [32, 33] as follows:

$$r_{se}(\tau_l, p_l) = \begin{cases} \tau_l \left[ \log_2 \left( 1 + \frac{h_l p_l}{\tau_l r_l} \right) - \log_2 \left( 1 + \frac{g_l p_l}{\tau_l r_l} \right) \right], & \tau_l > 0, \ h_l > g_l \quad (2) \\
0, & \text{else} \end{cases}$$

which shows that the secrecy can be achieved when the main channel is better than the eavesdropper channel; i.e., $h_l > g_l$.

2.2. Delay QoS Guarantee. In this subsection, we utilize the secure effective capacity to measure the throughput of the secrecy system under QoS constraint. The effective capacity characterizes the maximum constant arrival rate that the channel can support and guarantees a given delay QoS requirement.

The information source stream from the upper layers and the service process driven by the resource control scheme at the physical layer are matched via the queue at the data link layer. It is assumed that the source message stream has a specified delay bound $D_{\max}$ [23, 24] and the violation probability of the delay bound should not be larger than a certain nonnegative value $\varepsilon$ as

$$\Pr \{ D(\infty) > D_{\max} \} \leq \varepsilon, \quad (3)$$

where $D(\infty)$ is the delay experienced by a source message stream in a steady state. Then, we mark the QoS requirement of the source message stream as $\{D_{\max}, \varepsilon\}$. As shown in [24], the effective capacity is related to the theory of large deviations. The probability of $D(\infty)$ exceeding the delay bound $D_{\max}$ can be expressed as follows:

$$\Pr \{ D > D_{\max} \} \approx e^{-\theta D_{\max}}, \quad (4)$$

where $E_B$ is defined as the effective bandwidth of the source message stream, $\theta^*$ is a value obtained by solving the function $E_C(\theta) = E_B$, and $E_C(\theta)$ represents the effective capacity denoted as

$$E_C(\theta) = \lim_{M \to \infty} \frac{1}{M} \log \left( \mathbb{E} \left[ \exp \left( -\theta \sum_{n=0}^M R[n] \right) \right] \right), \quad (5)$$

where $\theta$ is a positive constant termed as QoS exponent and $\{R[n], n = 0, 1, 2, \ldots\}$ is a discrete-time, stationary, and ergodic stochastic service process. $\mathbb{E}[\cdot]$ is the expectation operator. When the service processes are uncorrelated, the effective capacity can be expressed as

$$E_C(\theta) = -\frac{1}{\theta} \log \left( \mathbb{E} \left[ \exp \{-\theta R[n]\} \right] \right). \quad (6)$$

Note that, for the secrecy system mentioned in this paper, if the channel gains during one frame satisfy $h_l > g_l$, the transmit data can be securely transferred at the non-zero secrecy rate. Thus, the secure effective capacity can be mathematically calculated as

$$E_{se}(\theta) = -\frac{1}{\theta} \log \left( \mathbb{E} \left[ e^{-\theta R_{se}} \right] \right). \quad (7)$$

Obviously, the secure effective capacity bounded by the minimal service rate is a monotonically decreasing function of $\theta$. Given the delay bound $D_{\max}$, the delay violation probability can be characterized by the QoS exponent $\theta$. A small $\theta$ corresponds to a loose violation probability requirement, while a large $\theta$ matches a strict QoS requirement. For multimedia applications, the secure effective capacity can be calculated with given $\theta$. Only if $E_{se}(\theta) \geq E_B$ holds, the delay QoS guarantee can be satisfied.

3. Resource Allocation Policy with Delay QoS Guarantee

In this section, we investigate the joint power and time slot allocation policy to minimize the total cost of average power subjected to the given delay QoS constraint specified by the
secure effective capacity of each user. The cost function is a $\beta$-
fair cost function with a nonnegative parameter $\beta$ which can be
employed to formulate the fair energy-efficient resource allocation
and it is shown as

$$V_\beta (\cdot) = \frac{(\cdot)^{1+\beta}}{1 + \beta}.$$ (8)

It is a convex and monotonically increasing function. The
$\beta$-fairness is achieved by distributing the power to the user
link that has consumed the smallest amount of power. The
function achieves power minimization which seeks the most
energy-efficient resource allocation with $\beta = 0$ and min-max
fairness with $\beta \rightarrow \infty$ as two special cases.

To guarantee the QoS requirement of the secrecy system,
the secure effective capacity with the corresponding delay
QoS exponent should be no less than the effective bandwidth
denoted as $E := [E_1, \ldots, E_L]^T$. Let $\bar{p} := [\bar{p}_1, \ldots, \bar{p}_L]^T$, $r(h, g) := [r_1(h, g), \ldots, r_L(h, g)]^T$, and $p(h, g) := [p_1(h, g), \ldots, p_L(h, g)]^T$ represent the average user power vector, the
time fraction vector, and the power vector adapted to the CSI
$h$ and $g$, respectively. Thus, we can formulate the optimization
problem as

$$\min_{p, \tau, h, g} \sum_{l=1}^{L} V_\beta (\bar{p}_l)$$

s.t. $\bar{p}_l \geq E_{h, g} [p_l(h, g)],$

$$-\frac{1}{\theta_l} \log \left[ E_{h, g} \left[ e^{\theta r_{sec}(\tau_l(h, g), p(h, g))} \right] \right] \geq E_l,$$ (9)

$$\sum_{l=1}^{L} \tau_l(h, g) \leq 1,$$

$$\tau_l(h, g) \geq 0, \quad p_l(h, g) \geq 0,$$

where $\theta_l$ represents the QoS exponent of the $l$-th user and $l = 1, \ldots, L$. We find that the objective function in (9) is convex
with respect to $\bar{p}_l$ and the second constraint can be converted into

$$E_{h, g} \left[ e^{\theta r_{sec}(\tau_l(h, g), p(h, g))} \right] \leq e^{-\delta E_l}.$$ (10)

By evaluating the Hessian matrix $r_{sec}(\tau_l(h, g), p_l(h, g))$ at
$\tau_l(h, g)$ and $p_l(h, g)$, we can prove that $r_{sec}(\tau_l(h, g), p_l(h, g))$ is a jointly concave function of $\tau_l(h, g)$ and $p_l(h, g)$. Since
the expectation and exponent operations preserve the concavity,
the constraint in (10) is also convex. In addition, the remaining
constraints are all convex. Hence, (9) is a convex
optimization problem with unique optimal solution.

3.1. Optimal Resource Allocation Algorithm. In this subsection,
an optimal time slot and power allocation algorithm
for the optimization problem (9) is proposed based on the
Lagrangian dual technique in [28]. Let $\lambda := [\lambda_1, \ldots, \lambda_L]^T$ and $\xi := [\xi_1, \ldots, \xi_L]^T$ be the Lagrange multipliers associated with
the average power constraint and the delay QoS constraint,
respectively. For convenience, we set $X := \{\bar{p}, \tau(\cdot), \bar{\tau}(\cdot)\}$, $Y := \{h, g\}$. Then, the average power constraint
and delay QoS constraint are relaxed to form the Lagrangian function as

$$L(X, Y) = \sum_{l=1}^{L} V_\beta (\bar{p}_l) + \sum_{l=1}^{L} \lambda_l \left( \mathbb{E}_{Y} [p_l(Y)] - \bar{p}_l \right) + \sum_{l=1}^{L} \xi_l \cdot \left( \mathbb{E}_{Y} \left[ e^{\delta r_{sec}(\tau_l(Y), p(Y))} \right] - e^{-\delta E_l} \right)$$

$$= \sum_{l=1}^{L} \left( V_\beta (\bar{p}_l) - \lambda_l \bar{p}_l \right)$$

$$+ \sum_{l=1}^{L} \mathbb{E}_{Y} \left[ \lambda_l p_l(Y) + \xi_l \cdot e^{\delta r_{sec}(\tau_l(Y), p(Y))} \right]$$

$$- \sum_{l=1}^{L} \xi_l e^{-\delta E_l}.$$ (11)

The master dual function is further expressed as

$$D(Y) = \min_{X} \left\{ L(X, Y) \right\}$$

s.t. $\sum_{l=1}^{L} \tau_l(h, g) \leq 1,$

and the dual problem of (9) can be expressed as $\max_{Y \in D(Y)} D(Y)$. To find the optimal joint power and time slot allocation
$(\bar{p}^*, \tau^*, p^*)$ by solving the master dual function (12), we need to solve the decoupled subfunctions below:

$$\min_{\bar{p}_l} \sum_{l=1}^{L} \left( V_\beta (\bar{p}_l) - \lambda_l \bar{p}_l \right),$$ (13)

and

$$\min_{\bar{p}_l} \sum_{l=1}^{L} \mathbb{E}_{Y} \left[ \lambda_l p_l(Y) + \xi_l \cdot e^{\delta r_{sec}(\tau_l(Y), p(Y))} \right]$$

$$- \sum_{l=1}^{L} \xi_l e^{-\delta E_l}.$$ (14)

s.t. $\sum_{l=1}^{L} \tau_l(Y) \leq 1.$

For each user $l$, (13) can be decoupled as

$$\min_{\bar{p}_l} V_\beta (\bar{p}_l) - \lambda_l \bar{p}_l.$$ (15)

It is clear that solving (15) is equivalent to solve (13). For
given $\lambda_l$, (15) is a deterministic convex optimization problem.
Hence, we can readily solve it and get the optimal solution as

$$\bar{p}_l(Y) = \lambda_l^{1/\beta}.$$ (16)

For the subfunction (14) associated with $(\tau^*, p^*)$, it can be decoupled as subfunctions under each channel realization
like $h$ and $g$. Hence, the solution of (14) can be reduced to solve the following function:

$$\min_{p,\tau} \sum_{l=1}^{L} \left[ \lambda_l p_l \left( Y \right) + \xi_l \cdot e^{-\theta r_m \left( \tau_l \left( Y \right) \right) p_l \left( Y \right) \right]$$

(17)

s.t. \[ \sum_{l=1}^{L} \tau_l \left( Y \right) \leq 1. \]

It is easily proved that (17) is a convex optimization problem and its optimal solutions $p_l^* \left( Y, \Psi \right)$ and $\tau_l^* \left( Y, \Psi \right)$ can be obtained via the algorithms given in the following subsection. For $\forall l = 1, \ldots, L$, the dual problem of max$_{\Psi \in D} J \left( \Psi \right)$ can be solved by the subgradient iterative algorithm as

$$\lambda_l \left[ n + 1 \right] = \lambda_l \left[ n \right] + \alpha \left[ n \right]$$

$$\cdot \left( E_Y \left[ p_l^* \left( Y, \Psi \left[ n \right] \right) \right] \right) - \bar{p}_l \left( \Psi \left[ n \right] \right)$$

(18)

$$\xi_l \left[ n + 1 \right] = \xi_l \left[ n \right] + \alpha \left[ n \right]$$

$$\cdot \left( E_Y \left[ e^{-\theta r_m \left( \tau_l \left( Y \right), \Psi \left[ n \right] \right) p_l \left( Y, \Psi \left[ n \right] \right) \right] \right) - \theta E_l \right),$$

where $n$ represents the time index and $\alpha \left[ n \right]$ is the step size.

### 3.2 Joint Power and Time Slot Allocation Policy for Each Channel Realization

In this subsection, we aim to investigate the convex optimization function (17) and propose an optimal joint power and time slot allocation policy for each channel realization with given $\lambda$ and $\xi$. By relaxing the time slot constraint, the Lagrangian function becomes

$$J \left( \tau_l \left( Y \right), p_l \left( Y \right) \right)$$

$$= \sum_{l=1}^{L} \left[ \lambda_l p_l \left( Y \right) + \xi_l \cdot e^{-\theta r_m \left( \tau_l \left( Y \right) \right) p_l \left( Y \right) \right] + \eta$$

(19)

$$\cdot \left( \sum_{l=1}^{L} \tau_l \left( Y \right) - 1 \right),$$

where $\eta$ denotes the Lagrangian multiplier associated with the time slot constraint. Then, we propose the optimal time slot and power assignment policy.

Define $p_l^* \left( Y, \Psi \right)$ and $\tau_l^* \left( Y, \Psi \right)$ as the desired optimal solutions. Applying the Karush-Kuhn-Tucker (KKT) conditions, for $\forall l = 1, \ldots, L$, we can derive the necessary and sufficient conditions on $p_l^* \left( Y, \Psi \right)$ and $\tau_l^* \left( Y, \Psi \right)$ as

$$\frac{\partial J \left( \tau_l \left( Y \right), p_l \left( Y \right) \right)}{\partial p_l \left( Y, \Psi \right)} = \begin{cases} 0, & p_l^* \left( Y, \Psi \right) > 0 \\ < 0, & p_l^* \left( Y, \Psi \right) = 0, \end{cases}$$

(20)

$$\frac{\partial J \left( \tau_l \left( Y \right), p_l \left( Y \right) \right)}{\partial \tau_l \left( Y \right)} = \begin{cases} > 0, & \tau_l^* \left( Y, \Psi \right) = 0 \\ = 0, & 0 < \tau_l^* \left( Y, \Psi \right) < 1 \\ < 0, & \tau_l^* \left( Y, \Psi \right) = 1. \end{cases}$$

(21)

Equation (21) means that the derivative at the minimum point is zero if the minimum lies within the constraint region $(0, 1)$. If the minimum is located on the boundary of the constraint region, the derivative is either positive or negative pointing towards the interior of the constraint region along all directions. With the above two optimality conditions, we can calculate the optimal power and time slot allocation arithmetically. From (20), we can obtain

$$\lambda_l = \frac{\xi_l \beta_l}{\log 2} \cdot e^{-\theta p_l \left( Y, \Psi \right)/g \left( Y, \tau_l \left( Y \right) \right)}$$

(22)

$$= \frac{h_l - g_l}{(1 + h_l p_l \left( Y, \Psi \right)/\tau_l \left( Y \right)) (1 + g_l p_l \left( Y, \Psi \right)/\tau_l \left( Y \right))} = 0.$$

Let $\{\tau_l^* \left( Y, \Psi \right), \forall l \}$ be the optimal time slot assignment; then the corresponding power allocation $p_l^* \left( Y, \Psi \right)$ satisfies the following formula:

$$\frac{(1 + g_l p_l^* \left( Y, \Psi \right)/\tau_l^* \left( Y, \Psi \right))^{B-1}}{(1 + h_l p_l^* \left( Y, \Psi \right)/\tau_l^* \left( Y, \Psi \right))^{B-1}} = \frac{\gamma_0}{h_l - g_l},$$

(23)

$$\gamma_0 < h_l - g_l, \quad \tau_l^* \left( Y, \Psi \right) > 0,$$

$$\gamma_0 \geq h_l - g_l, \quad \tau_l^* \left( Y, \Psi \right) = 0,$$

with $B \triangleq \theta \tau_l^* \left( Y, \Psi \right)/\log 2$ and $\gamma_0 \triangleq (\lambda_l \cdot \log 2)/\xi_l \beta_l$. It is observed that the power allocation of the active user has the same form as that for the single-user QoS-driven secrecy system [25, eq.(15)] with different cutoff thresholds at each channel realization. Furthermore, we analyze the time slot allocation policy which follows Lemma 1.

**Lemma 1.** Assume that, for each channel realization, i.e., $h$ and $g$; in the context of secure transmission, there exists at most one user allocated with a strictly positive power and we assert it the "winner-takes-all" policy.

The users in the system whose channel gains may not satisfy the secrecy communication condition $h_l > g_l$ will not participate in the time slot allocation; i.e., $\tau_l^* \left( Y, \Psi \right) = 0$ for $h_l < g_l$. The following derivations are all satisfied with $h_l > g_l$. Taking the partial derivative of (19) with respect to $\tau_l \left( Y \right)$, we have

$$\frac{\partial J \left( \tau_l \left( Y \right), p_l \left( Y \right) \right)}{\partial \tau_l \left( Y \right)} = \eta - \xi_l \beta_l$$

(24)

$$\cdot e^{-\theta p_l \left( Y, \Psi \right)/g \left( Y, \tau_l \left( Y \right) + h_l p_l \left( Y \right)/g \left( Y, \tau_l \left( Y \right) + g_l p_l \left( Y \right) \right) \right)}$$

$$\cdot \left[ \log_2 \left( 1 + h_l p_l \left( Y, \Psi \right)/\tau_l \left( Y \right) \right) + \frac{1}{\log 2} \right.$$
Here, we substitute $p_i^*(Y, \Psi)$ obtained by (23) into (24) and simplify it with (22). According to the KKT condition (21), for all $l = 1, \ldots, L$, we can get
\[
\tau_l^*(Y, \Psi) = \begin{cases} 
1, & \eta < Q_l(Y, \Psi) \\
0, & \eta > Q_l(Y, \Psi),
\end{cases}
\]
(25)

where $Q_l(Y, \Psi)$ is termed as the quality function and written as
\[
Q_l(Y, \Psi) = \lambda_l \cdot \log_2 \left( \frac{1 + h_l p_i^*(Y, \Psi) \left(1 + g_l p_i^*(Y, \Psi) \right)}{1 + g_l p_i^*(Y, \Psi)} - \lambda_l p_i^*(Y, \Psi) \right).
\]
(26)

Since the constraint must be satisfied, only the user whose $Q_l(Y, \Psi)$ is the smallest can occupy the whole time slot. In detail, we write
\[
\tau_l^*(Y, \Psi) = 1, \\
\tau_l^*(Y, \Psi) = 0,
\]
(27)

where $l^* = \arg \max_l Q_l(Y, \Psi)$.
(28)

Given a time slot, there will be a set $\{Q_1(Y, \Psi), Q_2(Y, \Psi), \ldots, Q_L(Y, \Psi)\}$ with $L$ elements related to different corresponding users. The user $l$ whose $Q_l(Y, \Psi)$ is the minimum in the set will occupy the whole time slot. That is to say, we can easily derive the time slot allocation scheme with the obtained set $\{Q_1(Y, \Psi), Q_2(Y, \Psi), \ldots, Q_L(Y, \Psi)\}$.

3.3. Stochastic Joint Time Slot and Power Allocation Algorithm.

According to Lagrangian duality theory [30], the strong duality of the primary problem (9) should hold, which guarantees the solution of the primary problem through the dual problem $\max_{\Psi \in \mathcal{D}} D(\Psi)$. To solve this dual problem, we need the explicit knowledge of the CDF of the fading channel in order to evaluate the expected values $E_{f}[\cdot]$, whereas for some practical wireless communication environments, it is impractical or impossible to obtain the CDF of the fading channels. Thus, the joint power and time slot allocation algorithm which can operate without the knowledge of the channel CDF and approach the optimal strategy by learning the channel statistics should be achieved urgently. The above issue can be solved via the utilization of the stochastic optimization theory in [34]. Note that $D(\Psi)$ is a convex function of $\Psi$, thus $\max_{\Psi \in \mathcal{D}} D(\Psi)$ is a stochastic convex optimization problem. Hence, employing the stochastic subgradient iterative method [35] with unknown channel CDF, we can get a stochastic subgradient iteration algorithm based on the channel realizations ($h[n]$ and $g[n]$) at time slot $n$ for all $l = 1, \ldots, L$ as
\[
\tilde{\lambda}_l [n + 1] = \tilde{\lambda}_l [n] + \alpha [n] \left( p_i^* \left( Y [n], \tilde{\Psi} [n] \right) - \bar{p}_l^* \left( \tilde{\Psi} [n] \right) \right),
\]
(29)

where $\bar{\cdot}$ denotes the stochastic estimation, compared with (18). Equations (29) and (18) correspond to the primary and averaged systems, respectively. We can prove the convergence of the stochastic subgradient iteration by employing the stochastic locking theorem in [36]. The stochastic locking theorem holds only if certain regularity conditions are satisfied, such as the stochastic Lipschitz conditions for system perturbations. According to [37], we have the following Lemma 2 which confirms that these regularity conditions are satisfied for the primary and average systems with TDMA scheme, provided that the continuous channel CDF can be obtained.

**Lemma 2.** For ergodic fading channel with continuous CDF, if the primary system (18) and its averaged system (29) are both initialized with $\tilde{\Psi}[0] = \Psi[0]$, then, for any time interval $T$, it holds that
\[
\max_{1 \leq n \leq T/c} \| \tilde{\Psi}[n] - \Psi[n] \| \leq c_T(c),
\]
(30)

with possibility 1,

\[
\text{with } c_T(c) \rightarrow 0 \text{ as } c \rightarrow 0.
\]

Trajectory locking is the key of the asymptotic optimality of the stochastic iterations. **Lemma 2** rigorously establishes that the trajectories of the primary and average systems, corresponding to (29) and (18), respectively, remain close to each other over any time interval $T$ for small enough step size $c$. That is to say, the distance of the two trajectories is bounded in probability by a constant $c_T(c)$ which will vanish as $c \rightarrow 0$. Hence, the stochastic power and time slot allocation scheme will approach the global optimal solution of (11). The detailed theoretical analysis of the stochastic optimization algorithm is a complex and tedious work and it is not the main purpose of our paper. In addition, for any stochastic approximation scheme, the Lagrange multipliers in (19) converge to the optimal values or hover within a small neighborhood around the optimal values with the size proportional to the step size $c$.

4. Non-Delayed Resource Allocation Policy

The optimal resource allocation which satisfies the delay QoS constraint has been investigated above. In this section, we also present a non-delayed resource allocation scheme without considering the delay QoS requirement for comparison. When the delay QoS constraint of the optimization problem
(9) becomes the secrecy rate constraint, the jointly power and time slot allocation \( (p_l^*, r_l^*) \) will obey the following equations:

\[
\begin{align*}
p_l^* &= \begin{cases} 
\frac{1}{2} \left( \sqrt{\left(\frac{1}{h_l} - \frac{1}{g_l}\right)^2 + \frac{4}{\eta_l} \left(\frac{1}{g_l} - \frac{1}{h_l}\right) - \left(\frac{1}{h_l} + \frac{1}{g_l}\right)} \right), & \eta_l < h_l - g_l, \quad r_l^* > 0 \\
0, & \text{else}
\end{cases} 
\end{align*}
\]

\[
(31)
\]

\[
\tau_l^* = 1,
\]

\[
(32)
\]

\[
\tau_l^* = 0,
\]

where \( \zeta_l \) and \( \epsilon_l \) are the Lagrangian multipliers associated with the average power constraint and the secrecy rate constraint for the \( l \)-th user, respectively, and \( \eta_l \equiv \zeta_l r_l^* \log 2/\epsilon_l \).

In fact, for a given time slot, the power allocation algorithm (31) is the same as the scheme [33, eq.(7)] of the single-user secrecy system. Besides, considering the power allocation scheme (23) which supports the QoS requirement with \( \theta \rightarrow 0 \), the optimal power allocation factor \( p_l^* \) converges to (31). This phenomenon illustrates that the optimal QoS-driven resource allocation policy merges with the non-delayed policy when we relax the QoS requirement.

5. Numerical Results and Analysis

In this section, the numerical results of the proposed optimal resource allocation policy and non-delayed policy are provided to verify the foregoing theoretical analysis. We assume that the TDMA secrecy networks include three transmit users, one legitimate receiver, and one eavesdropper. The fading channels of different users are independent to each other. Besides, the channel power gains of the main user channels \( h_l \) and the wiretap channels \( g_l \) obey Rayleigh fading distributions with variance \( \bar{h}_l \) and \( \bar{g}_l \), respectively, and \( h_l > g_l \) \((l = 1, 2, 3)\). For simplicity, we assume that all the links suffer from the same delay impact. Specific system parameters are given in the corresponding figures.

The convergence performance of the Lagrange multipliers of the proposed optimal resource allocation policy is shown in Figure 2. In the simulation, six Lagrange multipliers, \((\lambda_1, \lambda_2, \lambda_3)\) and \((\xi_1, \xi_2, \xi_3)\), which are associated, respectively, with the average power constraint and the delay QoS constraint, are chosen arbitrarily to make the example. It can be observed from Figure 2 that all the six multipliers become stable after 12 iterations. Thus, we can get the same conclusion as what we have discussed in the end of Section 3 that the convergence of the proposed optimal policy can be guaranteed.

Figure 3 shows the power consumption of the user links \( 1 - 3 \) which adopt the optimal policy under different \( \beta \)-fairness \((\beta = 0.01, 3, 6)\). In addition, two comparative schemes, non-delayed scheme and fixed-access scheme, are also included for \( \beta = 0.01 \). Here, the average normalized channel power gains for different user links are set to be \( \bar{h}_1 = 3, \bar{h}_2 = 0, \bar{h}_3 = -3, \bar{g}_1 = \bar{g}_2 = \bar{g}_3 = -3 \) dBW, and the QoS exponents for the user links \( 1 - 3 \) are \( \theta_1 = \theta_2 = \theta_3 = 1 \). From the individual average power in Figure 3, we observe that, for smaller \( \beta \) such as \( \beta = 0.01 \), the power gaps between different users are apparent and the resource allocation scheme assigns more power to the worst channel (link 3), which illustrates that we can increase the transmit power to maintain the system throughput if the channel becomes worse. It is also seen that the power consumed by different user links gets close to each other when \( \beta \) becomes larger. Meanwhile, the total average power increases if \( \beta \) increases. Hence, we can draw the conclusion that the fairness can be improved by consuming much more total power.

For comparison, Figure 3 also presents the total average power consumption of the fixed-access scheme and the non-delayed scheme. The fixed-access scheme assigns equal time fractions \((r_1 = r_2 = r_3 = 1/3)\) to the three links and each link still adopts the optimal power allocation strategy. We notice that much more total power is required for the fixed-access scheme than that of the optimal policy due to the neglect of the users diversity and fairness. Since the non-delayed policy does not consider the delay QoS requirement during the joint power and time slot allocation, more total power is also needed to achieve the delay QoS guarantee. In a word, the proposed optimal policy can save much more power and the \( \beta \)-fair cost function can balance the energy efficiency and the fairness well.

In Figures 4 and 5, we plot the total average transmit power as a function of the delay QoS exponent under different resource allocation policies. We consider two cases with different eavesdropper conditions. The total average transmit power with better eavesdropper channel condition is shown in Figure 4. Figure 5 shows the total average transmit power with worse eavesdropper channel condition. The average main user channel gains are assumed to be \( \bar{h}_1 = 3, \bar{h}_2 = 0, \) and \( \bar{h}_3 = -3 \) for the two conditions. We can observe from Figures 4 and 5 that the total average transmit power increases if the delay QoS exponent increases. As
expected, the proposed optimal resource allocation policy commonly consumes the minimal total average transmit power compared with the non-delayed policy and the fixed-access policy. In addition, the optimal resource allocation policy converges to the non-delayed policy under a relatively small QoS exponent, which is coherent with the theoretical analysis above. Furthermore, by comparing the two figures, we find that the gap between the optimal policy and the non-delayed policy becomes significant when the eavesdropper channel becomes worse, which shows the advantages of the proposed optimal allocation policy under the worse eavesdropper channel condition.

We provide the performance of the total average power versus the violation probability with delay bound \( D_{\text{max}} \) in Figure 6. In the simulation, we set the delay boundary as \( D_{\text{max}} = 20\text{ms} \). Given the delay boundary \( D_{\text{max}} \), the violation probability will arise if the delay requirement \( \theta \) decreases according to (4). Under a certain violation probability, the proposed optimal resource allocation policy can achieve the minimum total average power among the three policies. Furthermore, it can be observed from Figure 6 that the total average transmit power will decrease when the violation probability increases. That is to say, a smaller delay requirement will lead to a lower total average power, which
is in agreement with our theoretical analysis above and also matches the results in Figure 5.

6. Conclusions

In this paper, we propose a fair energy-efficient resource allocation policy for the multiuser TDMA secrecy system. The system model is established for the secure transmission in the presence of an eavesdropper. By employing the secure effective capacity and \( \beta \)-fair cost function, we analytically study the joint power and time slot allocation policy which minimizes the \( \beta \)-fair cost function of the average transmit power while fulfilling the individual delay QoS requirement. A subgradient iterative algorithm is employed to solve the optimal resource allocation problem based on the convex optimization theory. In addition, the stochastic optimization is utilized to solve the problem. The limits of the total average power with the delay QoS constraint are derived based on the analytical results. The proposed optimal resource allocation scheme exhibits excellent energy efficiency compared with the suboptimal non-delayed scheme and the fixed-access scheme, especially in the case of stringent delay QoS requirement and worse eavesdropper channel condition. It also illustrates that the proposed stochastic iterative algorithm can approach the optimal strategy.

Data Availability

The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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