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Research Article

Causes of Early Age Cracking on Concrete Bridge Deck Expansion Joint Repair Sections

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Cracking of newly placed binary Portland cement-slag concrete adjacent to bridge deck expansion dam replacements has been observed on several newly rehabilitated sections of bridge decks. This paper investigates the causes of cracking by assessing the concrete mixtures specified for bridge deck rehabilitation projects, as well as reviewing the structural design of decks and the construction and curing methods implemented by the contractors. The work consists of (1) a comprehensive literature review of the causes of cracking on bridge decks, (2) a review of previous bridge deck rehabilitation projects that experienced early-age cracking along with construction observations of active deck rehabilitation projects, and (3) an experimental evaluation of the two most commonly used bridge deck concrete mixtures. Based on the literature review, the causes of concrete bridge deck cracking can be classified into three categories: concrete material properties, construction practices, and structural design factors. The most likely causes of the observed early-age cracking were found to be inadequate curing and failure to properly eliminate the risk of plastic shrinkage cracking. These results underscore the significance of proper moist curing methods for concrete bridge decks, including repair sections. This document also provides a blueprint for future researchers to investigate early-age cracking of concrete structures.

1. Introduction

Longitudinal early age cracking of concrete repair sections adjacent to bridge deck expansion dam replacements (Figure 1) has been observed on several newly rehabilitated bridge decks. This research was aimed at assessing the causes of cracking in these full-depth concrete repair sections and creating a methodology to quantify these causes. Transverse early age cracking of concrete bridge decks has been a common problem reported by many state DOTs [1–11]. Although many studies have been performed since the 1980s to identify the causes and effective mitigation practices for early age cracking on concrete bridge decks, very few studies

have focused on cracking in repair sections, especially next to rehabilitated deck expansion dams. The published literature addressing cracking in deck repair sections is limited [12–17] and focuses mostly on closure pour acceleration [12], complete shear failure of reinforcing steel [14], or the durability of specific repair materials such as polymer-modified cementitious concrete and epoxy-binder concretes [15–17]. This paper evaluates the causes of the observed longitudinal cracking by assessing the effect of concrete material properties, construction and curing practices, and structural design of repair sections. The authors maintain that the longitudinal early age cracking observed in repair sections near bridge deck dams is similar in nature to the transverse cracking of

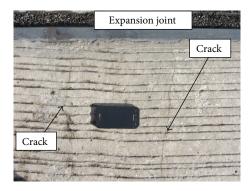


FIGURE 1: Early age longitudinal concrete cracking on concrete adjacent to bridge deck dam rehabilitations (cell phone: 4.5×2 inches for comparison).

newly constructed bridge decks. Restrained shrinkage and thermal contraction result in tensile stress development in concrete with the potential of cracking that is predominantly in the direction perpendicular to the longest dimension of the concrete member (i.e., transverse for full bridge decks and longitudinal for dam repair sections).

2. Research Objective

The main objective of this research is to identify the causes of longitudinal early age cracking in concrete deck segments placed adjacent to the newly replaced bridge deck expansion joints. This study satisfies this objective via a three-part investigation into the cracking propensity of concrete repairs on bridge decks placed in the recent decade through a case study involving bridge decks in Pennsylvania. These three parts consist of (1) a comprehensive literature review, (2) a review of past bridge deck rehabilitation projects that experienced early age cracking and construction inspection of active bridge dam rehabilitation projects, and (3) an experimental evaluation of the fresh and hardened properties of concrete in the laboratory to quantify the risk of cracking of the two most commonly used concrete mixtures for bridge deck construction and rehabilitation. This three-part investigation can then be utilized by other researchers to investigate early age cracking occurrences on bridges under their purview.

3. Literature Review

The factors that affect early age cracking on concrete bridge decks are divided into three categories: (1) concrete material properties, (2) construction practices, and (3) structural design factors. Each section that follows identifies the primary and secondary contributors to early age concrete cracking on bridge decks.

3.1. Concrete Material Properties. Concrete material properties have been the subject of the majority of past research for the mitigation of early age cracking on bridge decks. Excessive slump [2, 5–7, 18, 19], excessive cement content [2, 5–7, 18–23], and excessive compressive strength [4, 6, 22]

are commonly recognized as the primary contributors to the early age cracking of concrete. Fiber reinforcement [6, 11, 24–27] significantly reduces concrete cracking.

Previous research shows a clear correlation between slump and the tendency of concrete to crack at early ages [10, 24, 28]. Increased slump can increase the settlement of fresh concrete over reinforcing bars and result in cracking [10]. Maximum allowable slump values of 50 mm [29], 63.5 mm [30], or 89–100 mm [7] have been proposed.

There is a strong positive relationship between concrete cracking and increased cement content [6, 10, 20]. Cement paste is the phase in concrete that undergoes shrinkage, while aggregates do not shrink and have a lower coefficient of thermal expansion. In addition, high cement content results in higher heat of hydration and increased risk of thermal cracking [6, 18]. The maximum recommended cement content to prevent early age cracking has been reported as 362 to 430 kg/m³ of concrete. However, 297 to 320 kg/m³ is also noted to do the trick [7]. The literature also recommends a cement paste fraction not greater than 0.35, including air content [6, 10] (27% if excluding air content [7]).

An increase in the compressive strength of concrete is usually achieved by increasing the cement content and reducing the water to cementitious materials ratio (w/cm), which results in higher heat of hydration [31-33] and higher drying and autogenous shrinkage, as well as higher modulus of elasticity and lower creep [6, 23, 34]. A higher modulus and lower creep result in higher tensile stresses from shrinkage [6, 23, 34]. In addition, lower w/cm increases the need for proper moist curing due to lack of bleed water, which results in higher risk of plastic shrinkage cracking [2]. Several studies have recommended narrowing the range of allowable w/cm to reduce cracking, as mixtures with too low or too high w/cm have been shown to be more susceptible to cracking [10, 21, 30, 35]. Allowable w/cm in the range 0.40 [5] to 0.48 [29] has been suggested, with a more recent study suggesting a w/cm in the range 0.42 to 0.45 [7]. Concrete strength much higher than that specified by structural design should not be permitted, as it exacerbates cracking [4].

Other factors that affect the heat of hydration and risk of thermal cracking include cement type and fineness, batching temperature, ambient temperature and solar radiation [30], and coefficient of thermal expansion of concrete [31, 36–40]. Secondary concrete material properties that are known to modestly influence early age cracking are aggregate type [1, 6, 7, 18, 21], cement type [2, 6], air content [6, 9, 21, 22], use of mineral admixtures [6, 22, 31, 41–46], type of chemical admixtures [6, 7, 11, 22, 46–51], and concrete properties such as Poisson's ratio [6] and thermal conductivity [31, 40].

3.2. Construction Practices. Construction methods and site ambient conditions can contribute to early age cracking of concrete. Inadequate moist curing [4, 6, 7, 10, 11, 45], insufficient compaction [6, 7, 52], and ambient conditions that promote rapid evaporation of bleed water [5, 6, 41, 53–55] contribute the most to early age cracking.

Insufficient vibration of concrete together with insufficient cover thickness over top reinforcement can increase plastic and settlement cracking [52]. This is especially significant for concrete with high water content and high slump. Undervibration of concrete tends to cause an increase in cracking, while overvibration has little effect [6]. A well-graded mix may mitigate these effects.

Plastic shrinkage cracking is directly related to the evaporation rate of bleed water from the surface of fresh concrete [36, 53, 55]. Plastic cracks occur when the bleed water evaporates faster than the rate of bleeding, and as such, the surface of fresh concrete dries, resulting in capillary tensile stresses [51]. Evaporation rate is a function of the ambient relative humidity, concrete and air temperatures, and wind speed and can be estimated based on the nomograph in ACI 308R-01 [53]. Special considerations such as installing wind breaks or fog sprayers should be implemented when evaporation rates exceed 1 kg/m²/hr for normal concrete and 0.5 kg/m²/hr for concrete with low w/cm [6].

Proper moist curing reduces cracking caused by plastic shrinkage in fresh concrete. Delayed curing tends to increase the cracking risk. Also, use of chemical evaporation retarders can help to decrease the number of cracks formed before the start of moist curing. Curing should begin immediately after finishing [6, 10, 45]. When wet burlaps are used, the first layer of presoaked burlap should be applied 10 minutes after strike-off, with the application of a second layer within 5 additional minutes [7]. Moist curing should continue for a minimum of 7 days [4], but 14 days is preferred [56].

The sequence and length of concrete deck placement can have some (secondary) contribution to early age cracking [22, 35, 52]. This, however, is primarily relevant in continuous multispan bridges where flexural cracking can appear in negative moment regions caused by the dead load of concrete that is subsequently placed in the positive moment area [52]. Unless due to a mistake in structural design of the deck, tensile stresses caused by dead and live loads on the bridge are far smaller than the restrained shrinkage stresses and are unlikely to result in early age cracking [6, 10, 20]. Vibrations due to adjacent traffic lanes will only contribute to plastic cracking when concrete is undervibrated or has too high of slump [52].

3.3. Structural Design Factors. Structural design factors that are recognized as primary contributors to early age concrete deck cracking include inadequate cover thickness [6, 10] and improper reinforcing bar sizes and spacing [4–6, 10, 20, 21, 28, 37, 57]. A top cover depth of 50–75 mm on monolithic bridge decks has exhibited the least amount of cracking [10]. At least a 50 mm concrete cover is necessary to avoid settlement cracking [6]. Increasing the reinforcement bar size and spacing increases the cracking risk of bridge decks [5, 10, 25, 58]. The use of a maximum bar size of # 5 and maximum bar spacing of 150 mm has been recommended [4, 5, 35].

Secondary structural design factors that influence early age deck cracking include bridge structure type [10], bridge deck type [4, 6, 10, 59], deck thickness [5, 6, 9, 20, 21, 29, 35], deck end conditions [4, 10, 20], girder type [6, 10, 20, 45], and

mechanical loading [4, 6, 10, 20]. Review of the joint detail will assist in this part of the investigation.

4. Review of Past and Active Deck Rehabilitation Projects

This section provides the information obtained from site visits to 11 past bridge deck expansion dam rehabilitation projects and 2 active deck dam rehabilitation projects in Pennsylvania. The variables considered by the research team during these site visits include the following:

- concrete mixture proportions and material properties: w/cm, cementitious materials content, cement type, aggregate type and content, mineral and chemical admixtures, plastic air content, slump (design and measured at site), and 28-day compressive strength (structural design, minimum required by job specifications, and laboratory test results);
- (2) construction and curing practices: removal of old dam and adjacent concrete, cleaning and preparing the repair area, cleaning and epoxy coating of existing rebar within the repair area, installing new dam and additional rebar, placement, compacting and finishing concrete, ambient air temperature, relative humidity and wind speed, concrete temperature at placement, curing methods, and duration;
- (3) structural design factors: reinforcing bar size and spacing and cover thickness.

The most important findings are provided below.

- 4.1. Concrete Material Properties. Records showed that the past projects' concrete mixtures yielded laboratory tested 28day compressive strength results of up to 39.4 MPa, which is 43% higher than the strength required by the structural design (27.6 MPa) and 27% higher than the strength required by the job specifications (31.0 MPa). A similar observation was made during the review of active projects. The excessive strength of concrete makes it more prone to early age cracking due to a higher shrinkage, higher stiffness, and lower capacity for creep and stress relaxation. The slumps measured were in excess of 200 mm, which is in contrast with the literature recommendations of 50–100 mm [7, 10, 29, 52, 57]. This excessive slump can contribute to settlement cracking. To prevent such occurrences in the future, the authors recommend enforcing a maximum allowable slump and a maximum allowable 28day compressive strength, which should not be considerably higher than the minimum slump and strength required in the project specifications.
- 4.2. Construction Practices. During observation of construction practices in active projects, it was observed that the finished concrete surfaces remained exposed to evaporation for 30 to 40 minutes past final finish without application of an evaporation retarder. Also, ambient condition monitoring and evaporation remediation equipment (i.e., fog sprayer, etc.) were not present at the site. Such practices can significantly increase the risk of plastic shrinkage cracking. Average

summer temperature highs in northern Pennsylvania are 29°C and the average summer lows are 17°C. Average afternoon relative humidity readings are 53%. The average winter high temperatures are 1°C and the average winter low temperatures are -7°C with average afternoon relative humidity readings of 60%. Without proper monitoring oversight of concrete placed in the afternoon during the summer, plastic shrinkage can be expected. The literature recommendation of application of the first layer of presoaked burlap 10 minutes after the strike-off and a second layer within 5 minutes [7] was not followed. The QA team mentioned that it has not mandated the contractor to adhere to strict moist curing practices on the dam rehabilitation projects. It could be reasoned that similar curing practices were followed by the same contractor on the past projects that experienced early age cracking.

4.3. Structural Design Factors. Upon review of the joint detail, the required longitudinal and transverse reinforcing steel in the bridge deck dam area was calculated based on both ACI 318-11 [56] and AASHTO LRFD, 2012 [60] requirements for temperature and shrinkage steel (Table 1). The calculations indicated that the actual bar area per foot of deck, based on the as-built drawings of past projects, was adequate. Also, diaphragm beams were consistently located below the concrete deck dam repair sections, providing substantial support to withstand the load at that location. The majority of reinforcing bar sizes were number 5 and number 6, with a bar spacing of 6 inches. The deck cover thickness was between 50 and 75 mm. These conditions match the literature recommendations [5, 6, 10, 35]. Early age concrete cracking, therefore, is unlikely caused by structural design of the deck and reinforcing bars.

5. Experimental Evaluation of Bridge Deck Concrete Mixtures

The objectives of this task were to experimentally evaluate the cracking risk of concrete mixtures commonly used for bridge deck rehabilitation. These mixtures are denoted here as Mixture number 1 and Mixture number 2. Mixture number 1 was used on all the bridge decks that experienced early age concrete cracking. Mixture number 2 was subsequently developed and implemented by the state for use on bridge decks. With a reduction in the paste content and slight increase in the w/cm, it is demonstrated that Mixture number 2 provides a significant improvement in both field applications (no cracking) and laboratory experiments (demonstrated below), which is expected from the literature recommendations [6, 10, 20]. The experimental method provided herein can be used by future researchers to investigate the cracking propensity of their concrete mixtures.

5.1. Materials. Table 2 provides the concrete mixture proportions for Mixture number 1 and Mixture number 2. Mixture number 1 used a w/cm of 0.43 while Mixture number 2 used a w/cm of 0.44. The coarse aggregate was an ASTM C33 number 57 crushed limestone with an oven dry (OD) specific

gravity of 2.70 and absorption capacity of 0.23%. The fine aggregate met ASTM C33 with an OD specific gravity of 2.52, absorption capacity of 2.02%, and fineness modulus of 2.60. Quarries were the same as outlined by previous bridge deck dam rehabilitation projects.

An ASTM C150 type I cement with an ASTM C989 grade 100 ground granulated blast furnace slag (GGBFS) as a 35% cement replacement by weight was used in both mixtures. The hydration of binary OPC-GGBFS binders, when compared to conventional 100% OPC binders, tend to have a reduced early age strength while the pozzolanic reaction allows the system to attain a similar or greater later age (28 and 90 days) strength. An air-entraining admixture, midrange water reducer, and set retarding admixture were used to achieve a target plastic air content of 6.0% and slump of 100 mm.

5.2. Experimental Methodology and Results. The tests performed on the concrete mixtures were separated into three categories: (1) fresh properties (slump test: ASTM C143-05a and plastic air content: ASTM C231-10), (2) mechanical properties (indirect tensile strength: ASTM C 496-11, uniaxial compressive strength: ASTM C 39-05, and elastic modulus: ASTM C469-10), and (3) shrinkage and temperature properties (drying shrinkage: ASTM C157-08, restrained ring shrinkage: ASTM C1581-09, heat of hydration: ASTM C1064-08, and coefficient of thermal expansion: ASTM C531-00). Since the w/cm was greater than 0.42, autogenous shrinkage was deemed negligible (60). A description of the experiments along with the results and discussion is provided below.

5.2.1. Fresh Properties. Slumps measured were between 89 and 115 mm and within the acceptable range of 100 ± 38 mm. The air content range was between 5.4% and 6.4%. These values are adequate when compared to literature [7, 10, 29, 52, 57] and within the acceptable range of $6.0 \pm 1.5\%$.

5.2.2. Mechanical Properties. Mechanical property testing was performed using a standard load frame. All specimens were moist cured for their duration until moments before testing. Uniaxial compressive strength (f_c) of concrete was measured at 1, 3, 7, 28, and 90 days. With the aid of a compressometer, the 1-, 7-, and 28-day elastic moduli (MOE) were obtained within the elastic region of the concrete stress-strain curve, from the $50 \,\mu\varepsilon$ point to 40% of the ultimate (failure) stress for each age (i.e., known as the chord modulus). The f_c and MOE measurements were obtained using 101 × 203 mm concrete cylinders. Three duplicate specimens were cast for $f_c{'}$ testing and two duplicate specimens were cast for MOE testing. The indirect tensile strength testing was performed on 150×300 mm cylinders allowed to moist cure for 28 days before testing. The indirect tensile strength value recorded is the average of two duplicate specimens.

Table 3 provides the results of the mechanical properties testing. Mixture number 1 had a greater 7-, 28-, and 90-day f_c due to a lower w/cm. Mixture number 1 had a lower 1-day MOE. The two mixtures had comparable 7- and 28-day MOE. The 28-day f_c of Mixture number 1 and Mixture number 2 was 42.1 MPa and 38.3 MPa, which are

 ${\it Table 1: Temperature and shrinkage steel calculations for bridge decks.}$

| Job | Bridge | D. . | Bar area/foot of deck | ACI tempera- | LRFD |
|--------|--------|---------------------------|-----------------------|-----------------------------|-----------------------------------|
| number | number | Direction | (in ² /ft) | ture/shrinkage (in^2/ft) | temperature/shrinkage (in^2/ft) |
| 1 | 1 | Westbound Pier 1 | 1.448 | 0.027 | 0.072 |
| 1 | 1 | Westbound Pier 2 | 1.448 | 0.027 | 0.072 |
| 1 | 1 | Westbound Pier 3 | 1.448 | 0.027 | 0.072 |
| 1 | 1 | Eastbound Pier 1 | 1.448 | 0.029 | 0.076 |
| 1 | 1 | Eastbound Pier 2 | 1.448 | 0.029 | 0.076 |
| 1 | 1 | Eastbound Pier 3 | 1.448 | 0.029 | 0.076 |
| 1 | 2 | Westbound Pier 1 (span 1) | 1.448 | 0.031 | 0.072 |
| 1 | 2 | Westbound Pier 1 (span 2) | 1.448 | 0.029 | 0.068 |
| 1 | 2 | Westbound Pier 2 (span 3) | 1.448 | 0.031 | 0.072 |
| 1 | 2 | Westbound Pier 2 (Span 2) | 1.448 | 0.029 | 0.068 |
| 1 | 2 | Eastbound Pier 1 (span 1) | 1.448 | 0.029 | 0.068 |
| 1 | 2 | Eastbound Pier 1 (span 2) | 1.448 | 0.027 | 0.065 |
| 1 | 2 | Eastbound Pier 2 (span 3) | 1.448 | 0.029 | 0.068 |
| 1 | 2 | Eastbound Pier 2 (Span 2) | 1.448 | 0.027 | 0.065 |
| 2 | 1 | Westbound Pier 1 | 1.37 | 0.031 | 0.085 |
| 2 | 1 | Westbound Pier 2 | 1.37 | 0.031 | 0.085 |
| 2 | 1 | Eastbound Pier 1 | 1.37 | 0.031 | 0.085 |
| 2 | 1 | Eastbound Pier 2 | 1.37 | 0.031 | 0.085 |
| 2 | 2 | Westbound Pier 1 | 1.448 | 0.029 | 0.076 |
| 2 | 2 | Westbound Pier 2 | 1.448 | 0.029 | 0.076 |
| 2 | 2 | Eastbound Pier 1 | 1.448 | 0.027 | 0.072 |
| 2 | 2 | Eastbound Pier 2 | 1.448 | 0.027 | 0.072 |
| 2 | 3 | Westbound Pier 1 (Span 1) | 1.696 | 0.029 | 0.068 |
| 2 | 3 | Westbound Pier 1 (Span 2) | 1.696 | 0.027 | 0.065 |
| 2 | 3 | Westbound Pier 2 (Span 2) | 1.448 | 0.027 | 0.065 |
| 2 | 3 | Westbound Pier 2 (Span 3) | 1.448 | 0.029 | 0.068 |
| 2 | 3 | Eastbound Pier 1 (Span 1) | 1.696 | 0.031 | 0.072 |
| 2 | 3 | Eastbound Pier 1 (Span 2) | 1.696 | 0.027 | 0.065 |
| 2 | 3 | Eastbound Pier 2 (Span 2) | 1.696 | 0.027 | 0.065 |
| 2 | 3 | Eastbound Pier 2 (Span 3) | 1.696 | 0.029 | 0.068 |
| 3 | 1 | Eastbound Pier 1 (Span 1) | 1.333 | 0.031 | 0.07 |
| 3 | 1 | Eastbound Pier 2 (Span 1) | 1.333 | 0.031 | 0.07 |
| 3 | 2 | Pier 1 (Span 1) | 1.565 | 0.033 | 0.072 |
| 3 | 2 | Pier 1 (Span 2) | 1.565 | 0.032 | 0.069 |
| 3 | 2 | Pier 2 (Span 2) | 1.565 | 0.032 | 0.069 |
| 3 | 2 | Pier 2 (Span 3) | 1.565 | 0.033 | 0.072 |
| 3 | 3 | Pier 1 (Span 1) | 1.565 | 0.033 | 0.072 |
| 3 | 3 | Pier 1 (Span 2) | 1.565 | 0.032 | 0.069 |
| 3 | 3 | Pier 2 (Span 2) | 1.565 | 0.032 | 0.069 |
| 3 | 3 | Pier 2 (Span 3) | 1.565 | 0.033 | 0.072 |
| 3 | 4 | Pier 1 (Span 1) | 1.565 | 0.035 | 0.075 |
| 3 | 4 | Pier 1 (Span 2) | 1.565 | 0.033 | 0.072 |
| 3 | 4 | Pier 2 (Span 2) | 1.565 | 0.033 | 0.072 |
| 3 | 4 | Pier 2 (Span 3) | 1.565 | 0.035 | 0.072 |

TABLE 2: Mixture proportions and experimental results for Mixture number 1 and Mixture number 2.

| | Mixture number 1 Proportions by weight kg/m ³ | Mixture number 2 Proportions by weight kg/m ³ |
|--|--|--|
| Cementitious material | 390 | 362 |
| Cement | 254 | 236 |
| GGBFS | 136 | 127 |
| Water* | 168 | 160 |
| Coarse aggregate | 1103 | 1103 |
| Fine aggregate | 603 | 645 |
| w/cm | 0.43 | 0.44 |
| Cementitious paste Content (%) | 35.6 | 33.8 |
| Peak heat of hydration (°C) | 36 | 36 |
| Concrete COTE (strain/°C) | 8.69E - 06 | 8.44E - 06 |
| Thermal strain ($\mu \varepsilon$) | 116 | 113 |
| Unrestrained drying Shrinkage ($\mu \varepsilon$) | 418 | 378 |
| 28-day indirect tensile strength | 2.59 | 2.82 |
| Age of cracking during restrained ring test (day) | >28, 11, 15 | >40, >40, >40 |
| Average stress rate for restrained ring test (MPa/day) | 0.19 | 0.08 |

^{*}Including the water mass necessary to saturate aggregates.

considerably larger than the structural design requirements of 27.6 MPa and the literature recommendations of 20.7 to 31.0 MPa for bridge deck applications [6]. The reduced early age stiffness of Mixture number 2 assists in preventing early age cracking. The reduced paste content and pozzolanic reaction of the binary OPC-GGBFS system facilitate reduced early age stiffness while still obtaining later age stiffness and strength values that allow the carrying of loads necessary for vehicular traffic. Also, these binary systems create a complex microstructure that makes the system more resistant to moisture and chloride ingress [31]. As mentioned before, high compressive strengths are generally attributed to low w/cm and higher cement contents. These conditions favor higher stress development and higher cracking risk of concrete due to a higher heat of hydration, higher drying shrinkage, higher modulus of elasticity, and lower creep. Overall, the use of excessively strong concretes should be avoided and may contribute to the cracking noticed in this study. Table 2 shows Mixture number 2 was developed for better performance by reducing the paste content. Also, Table 3 shows Mixture number 2 has a greater tensile strength than Mixture number 1 (2.59 MPa and 2.82 MPa, resp.). This greater tensile strength may also assist in the reduced cracking propensity of Mixture number 2.

5.2.3. Shrinkage and Temperature Properties. The heat of hydration of fresh concrete was measured according to ASTM C1064-08, using type T thermocouples placed mid-height of well-insulated $152 \times 152 \, \mathrm{mm}$ concrete cylinders. Before the test, all type T thermocouples were calibrated in the temperature range $0-60\,^{\circ}\mathrm{C}$. The thermocouple output was recorded automatically by a data acquisition unit once every 30 minutes after casting concrete. Two specimens were tested for each mixture.

The coefficient of thermal expansion (COTE) was measured using equivalent mortar specimens in a saturated condition according to ASTM C531-00. Mortar bars ((25 \times 25 × 280 mm) according to ASTM C490-11) were prepared by excluding the coarse aggregates from the previously developed concrete mixtures. This is specified by ASTM C531 to limit the temperature gradients that could develop in larger concrete prisms (75×75 mm cross section). Mortars were mixed according to ASTM C305-06 and cast in prism molds using a vibrating table. Gage studs were placed at the opposite 25×25 mm ends to facilitate length measurements. Testing began after the specimens were moist cured for 14 days. The results from four duplicate prisms were used and averaged to determine the COTE of each mixture in the saturated condition. The saturated specimens were heated to a temperature of 80°C while being fully submerged in saturated lime-water bath. After at least 16 hours at 80°C, the specimens' length was recorded to the nearest 0.0025 mm. The specimens were then submerged back into the limewater bath and cooled to a temperature of 60°C. After at least 16 hours at 60°C, the specimens' lengths were recorded. This temperature cycle (80°C to 60°C and reverse) was continued until the specimens reached a constant length upon cooling to 60°C. This took approximately 1–3 weeks. Once a constant length was achieved at 60°C, prism shrinkage ceased and the true COTE was obtained.

For drying shrinkage, concrete specimens were cast in $75 \times 75 \times 280$ mm rectangular molds with embedded studs. Three duplicate specimens were tested for each mixture. The initial length measurements were upon demolding at 24 hours with a comparator. After initial measurements, the specimens were submerged in a limewater bath for 27 days. After the curing period was complete, the specimens' length was measured and drying commenced. The specimens were allowed to dry in an ambient condition of $22.8 \pm 1^{\circ}$ C and $50 \pm 5\%$ RH. Comparator length measurements were performed periodically, with the final measurements occurring 157 days after casting (i.e., total drying time was 129 days).

The restrained shrinkage of the two mixtures was measured using a restrained ring test per ASTM C1581-09. The test setup includes a concrete annulus that is cast around a steel ring. After 24 hours of curing under wet burlap, the specimens were demolded by removing the exterior cardboard mold. The concrete top surface was then sealed with aluminum tape, which allowed the concrete to dry from its outside circumference inside an environmental chamber that controlled the ambient conditions at $22.8 \pm 0.5^{\circ}$ C and $50 \pm 2\%$ RH. The resulting shrinkage deformations were measured by four symmetrically placed strain gages, mounted on the inner surface of the steel ring (at mid-height). These data allow

| AGE | Mixture number 1 | (w/cm = 0.43) | Mixture number 2 (w/cm = 0.44) | | |
|-----|---------------------------|----------------------|--------------------------------|----------------------|--|
| | Compressive strength: MPa | Elastic modulus: MPa | Compressive strength: MPa | Elastic modulus: MPa | |
| 1 | 10.9 | 2.01E04 | 11.0 | 1.75 <i>E</i> 04 | |
| 3 | 21.2 | _ | 21.3 | _ | |
| 7 | 28.7 | 3.18E04 | 26.1 | 3.22E04 | |
| 28 | 42.1 | 3.69E04 | 38.3 | 3.69E04 | |
| 90 | 43.1 | _ | 40.9 | _ | |

TABLE 3: Compressive strength and elastic modulus of Mixture number 1 and Mixture number 2.

calculation of the tensile stresses that develop inside concrete as a result of restrained shrinkage. As the stresses inside the concrete grow with time, the stresses may eventually reach the tensile strength of the material, leading to concrete cracking. The age at which cracking occurs and the stress magnitude at the time of cracking provide a good indication of the susceptibility of the concrete mixture to early age cracking. Three duplicate ring specimens were cast for each mixture.

Table 2 provides the results for the temperature and shrinkage property experiments. The peak heat of hydration was approximately 36.1°C for both mixtures. This temperature is reasonable for type I cement with 35% GGBFS replacement by weight [31]. The COTE provided in Table 2 is the estimated concrete COTE that is calculated using the law of mixtures (31) based on the measured mortar COTE, the volume fraction of coarse aggregates, and the COTE of limestone coarse aggregates ($6E - 06/^{\circ}$ C). The measured mortar COTE values for Mixtures number 1 and number 2 were $10.51E - 06/^{\circ}$ C and $10.12E - 06/^{\circ}$ C, respectively. Therefore, the concrete COTE for Mixtures number 1 and number 2 can be calculated as $8.69E - 06/^{\circ}$ C and $8.44E - 06/^{\circ}$ C, respectively. It should be noted that Mixture number 1 was anticipated to show a greater COTE based on its greater paste content.

Thermal strains were estimated based on the COTE and the peak temperature resulting from the heat of hydration (36.1°C), assuming that the concrete eventually cools down to the ambient temperature of 22.8°C. For Mixtures number 1 and number 2, the resultant thermal contraction strains were approximately 116 $\mu\epsilon$ and 113 $\mu\epsilon$, respectively, as noted in Table 2. The table also provides the results of unrestrained drying shrinkage measurements. The ultimate drying shrinkage (at 129 days of drying) was recorded for Mixture number 1 as 418 $\mu\epsilon$ and for Mixture number 2 as 378 $\mu\epsilon$. The drying shrinkage evolution for these mixtures is presented in Figure 2. These values are in agreement with typical literature results for concrete containing moderate levels of GGBFS [46, 61].

Table 2 also presents the results for the restrained ring shrinkage test. For Mixture number 1, cracking occurred at 11 days (at a maximum steel strain level of $-35~\mu\epsilon$) for ring 2 and at 15 days (at a maximum steel strain level of $-34~\mu\epsilon$) for ring 3, while no cracking occurred up to 28 days for ring 1, although the steel strain climbed to $-42~\mu\epsilon$ at this age for ring 1. The strain development between all three rings was consistent. The phenomenon of only one ring not exhibiting cracking has been observed before and does not indicate inaccuracy of the test method [62] but corresponds to inherent material

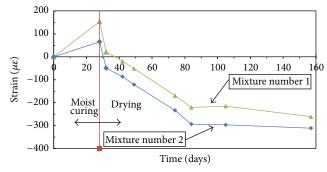


FIGURE 2: Drying shrinkage strain development over time for Mixture number 1 and Mixture number 2.

variability of concrete. For Mixture number 2, the strain development between the rings was consistent. At 28 days, ring 1 and ring 2 had a maximum steel strain level of $-56~\mu \varepsilon$, while ring 3 had a maximum steel strain level of $-53~\mu \varepsilon$. At the termination of the test at 40 days, no cracking was observed in the rings for Mixture number 2.

According to ASTM C1581-09, an average stress rate at cracking can be determined based on the elapsed time at cracking, or, if no cracks are visible, the last day of testing. The average magnitude of the restrained shrinkage stress rate for the two mixtures was calculated accordingly and is provided in Table 2. The strain development over time is presented in Figure 3 for Mixture number 1 and Figure 4 for Mixture number 2. Please note the strain value jumps in Figure 4 at 14 days and 28 days are artifacts of the DAQ and not cracking of the concrete. The average calculated stress rate for Mixture number 1 is 0.19 MPa/day, which indicates a moderate to high potential for cracking, according to ASTM C1581, where cracking is expected for specimens between the ages of 7 and 14 days. The average calculated stress rate for Mixture number 2 is 0.08 MPa/day, indicating a low potential for cracking, where cracking is not expected within the first 28 days. The reduced paste content and slightly higher w/cm of Mixture number 2 resulted in lower shrinkage and lower risk of cracking. Considering that Mixture number 1 was implemented on all bridge decks that exhibited early age cracking, the results obtained here indicate that a transition to Mixture number 2, along with its decreased paste content and higher w/cm, improves the durability against early deck cracking in field applications.

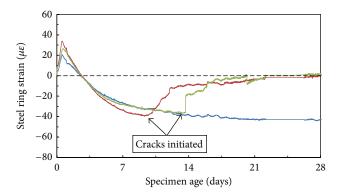


FIGURE 3: Restrained ring strain development over time for Mixture number 1. Each line denotes the average of four (4) strain readings for one ring. Three (3) rings were tested.

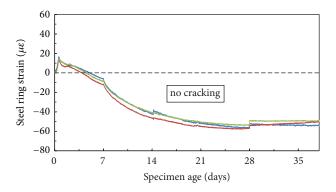


FIGURE 4: Restrained ring strain development over time for Mixture number 2. Each line denotes the average of four (4) strain readings for one ring. Three (3) rings were tested.

6. Conclusions

The main objective of this research was to identify the causes of longitudinal early age cracking in concrete deck segments placed adjacent to the newly replaced bridge deck expansion joints and to provide a blueprint of steps necessary to perform this type of investigation. The steps consisted of (1) a literature review of the causes of early age cracking on bridge decks, (2) a review of past and active bridge deck rehabilitation projects, and (3) an experimental evaluation of the two most commonly used bridge deck concrete mixtures.

The following conclusions can be stated.

- (i) The most likely causes of the observed early age cracking are inadequate moist curing practices and failure to properly eliminate the risk of plastic shrinkage cracking during construction. Moist curing must start as soon as possible and proper remediation techniques must be readily available at the construction site to limit the rate of water evaporation from the surface of fresh concrete.
- (ii) The 28-day f_c of the placed concrete exceeded the required structural design strength of 27.6 MPa by up to 43%. Also, the measured slumps were in excess of 200 mm. These excessive strength and slump values

- further exacerbate the risk of early age cracking. Construction specifications should include language to limit the maximum allowable compressive strength and slump of concrete and to evaluate the concrete for early age shrinkage cracking.
- (iii) A comprehensive experimental evaluation of bridge deck concrete mixtures showed that Mixture number 2 performs better against early age cracking. A lower cement paste content, lower COTE, lower drying shrinkage, and lower compressive strength are factors that have improved the performance of Mixture number 2.
- (iv) A review of the structural design of the deck and reinforcing bars suggested that the observed early age cracking was not likely caused by the structural design factors.

Overall, an integrated approach, to ensure proper selection and design of concrete materials, proper structural design of the deck (including the repair section), and proper construction and curing methods, is needed to minimize early age cracking of concrete deck and repair sections. Construction specifications and quality assurance practices must be updated as needed to benefit from the available knowledge in the literature to prevent early age cracking. Further research is needed to quantify the effect of cracks on the durability and service-life expectancy of bridge decks and to identify the best remediation techniques and the optimum time to repair the existing cracked bridge decks.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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