

## Research Article

# Compressive Strength Prediction of Stabilized Dredged Sediments Using Artificial Neural Network

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Received 11 November 2020; Revised 20 February 2021; Accepted 13 March 2021; Published 22 March 2021

Academic Editor: Wei Liu

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Stabilized dredged sediments are used as a backfilling material to reduce construction costs and a solution to environmental protection. Therefore, the compressive strength is an important criterion to determine the stabilized dredged sediments application such as road construction, building construction, and highway construction. Using the traditional method such as empirical approach and experimental methods, the determination of compressive strength of stabilized dredged sediments is difficult due to the complexity of this composite material. In this investigation, the artificial neural network (ANN) model is introduced to forecast the compressive strength. To perform the simulation, 51 experimental datasets were collected from the literature. The dataset consists of 4 input variables (water content, cement content, air foam content, and waste fishing net content) and output variable (compressive strength). Evaluation of the models was made and compared on training dataset (70% data) and testing dataset (30% remaining data) by the criteria of Pearson's correlation coefficient (R), Mean Absolute Error (MAE), and Root Mean Square Error (RMSE). The results show that the ANN model can accurately predict the compressive strength of stabilized dredged sediments with low water content. The cement content is the most important input affecting the unconfined compressive strength. The important input affecting the unconfined compressive strength can be in the following order: cement content > air foam content > water content > waste fishing net.

## 1. Introduction

Vietnam has a coastline about 3260 km followed by 49 large and small harbors with a system of estuarine serving ships. Especially in the Mekong Delta, transportation on the river system plays an important role in regional economic development. The dredged sludge needs to be treated to avoid environmental pollution. Furthermore, the dredged sludge amount is a challenge posed in the exploitation of estuaries and harbors. The Mekong Delta is characterized by soft soils, so that the requirement of soft soils improvement for construction works is very large. Stabilization/solidification is widely used in the treatment of contaminated sediments by mixing binders materials into the dredged sediments. Using stabilization/solidification technology has two purposes, which are (i) treating the environment and (ii) using a backfilling material to reduce construction costs and use of recycled materials such as dredged sediments, respectively.

Stabilization/solidification is the improvement of the physical dredged sediments properties such as

compressive strength, liquid limit, plastic limit, viscosity, and permeability [1–5]. Some binders are commonly used such as Portland cement, lime, limestone, fly ash, slag, gypsum, phosphorus, and many other commercial products. Considered as a construction material, Tsuchida [6] used dredged sediments, cement, air foam, and waste fishing net to form a lightweight material (cf. Figure 1). Dredged sediment has high water content; light foam nature reduces the density of stabilized dredged sediment but increases porosity. The waste fishing net has high shear strength. Therefore, the compressive strength of stabilized dredged sediments is importantly affected by the mix design (cement, water, air foam, and waste fishing net). That implies to be difficult to determine empirically relationship between the compressive strength and the composition of mix design, so that, in order to formulate the complex relationship, a suitable prediction model is demanded.

Over the past four decades, the method of artificial intelligence (AI) based on computer science has received a

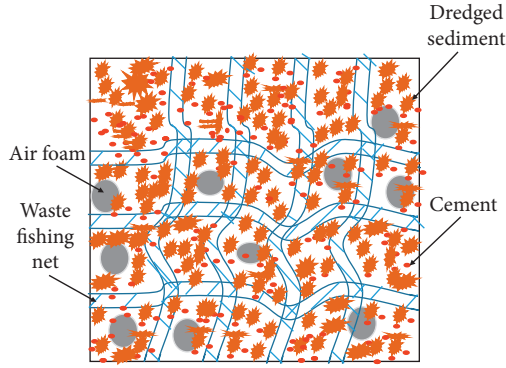


FIGURE 1: Mix design of stabilized dredged sediments using cement, air foam, and waste fishing net according to [7].

lot of attention from scientists applying on abundant sector such as earth science [8, 9] and civil engineering [10, 11]. Among AI algorithms, artificial neural networks (ANN) are often applied to solve various technical problems. Many complex issues related to structural engineering [12] and materials science [11, 13–17] have been successfully solved. Therefore, in this article, the authors propose the application of ANN model to predict compressive strength of stabilized dredged sediments using mix design, cement, air foam, and waste fishing net.

## 2. Machine Learning Method

**2.1. Artificial Neural Network.** The artificial neural network (ANN) is a mathematical model designed to perform a specific task, based on processing information of human brain with neurons process. Until now, ANN has been successfully used in many areas of life [18]. Regarding functional approximations, ANN model solutions are often more accurate than those provided by traditional methods, such as multivariate nonlinear regressions. The ANN structure is created by three or more layers including an input layer, an output layer, and one or more hidden layers (Figure 2). The input layer takes the values of the input and sends them to the available neurons in the hidden layer. Within each neuron, a weighted input is calculated. The sum of this value and the deviation value is modified by the activation function. Finally, the output signal is sent to the neurons in the next layer.

The mathematical process can be constructed as follows:

$$y_j = f\left(\sum_{i=1}^n w_{ij}x_i + b_j\right), \quad (1)$$

where  $x_i$  is input value  $I$ ,  $y_j$  is output value  $I$ , and  $w_{ij}$  and  $b_j$  are weight and deviation value.

A tangent hyperbolic function was used in this investigation, as it could lead to more accurate results. That is confirmed by the investigation of Karlik and Olgac [19]. This function varies from  $-1$  to  $1$  and is expressed as follows:

$$y_i = f(\text{net}) = \frac{2}{1 + e^{-2 \cdot \text{net}}} - 1, \quad (2)$$

where  $f$  is the activation function according to the terms of the calculated network value.

Neural networks need training to show effective performance. Training means that the weight and deviation of network are determined such that the minimum error between the target (actual value) and the output (network value) occurs. Therefore, during the training of neural networks, back-propagation algorithms (BP) are often used to train the network. The Levenberg-Marquardt algorithm (LMA) is usually the fastest back-propagation algorithm for tool training [20, 21]. Therefore, LMA is applied in this study.

The LM algorithm provides a solution called least squares of the following form:

$$f(x) = \frac{1}{2} \sum_{j=1}^m r_j^2(x), \quad (3)$$

where  $x = (x_1, x_2, \dots, x_n)$  is vector and  $r_j$  is function of  $\mathfrak{R}^n \rightarrow \mathfrak{R}$ .  $r_j$  is  $r$  when  $m \geq n$ . For simplicity,  $f$  is represented as a residual vector  $r: \mathfrak{R}^n \rightarrow \mathfrak{R}^m$  and is shown as follows:

$$r(x) = (r_1(x), r_2(x), \dots, r_m(x)). \quad (4)$$

At this time,  $f$  can be rewritten as  $f(x) = (1/2)\|r(x)\|^2$ . The derivative of  $f$  can be written in the Jacobi matrix and is defined as follows:

$$J(x) = \frac{\partial r_j}{\partial x_i}; \quad 1 \leq j \leq m; \quad 1 \leq i \leq n. \quad (5)$$

First, consider that every function  $r_i$  is linear. Here, Jacobian is constant and therefore is given by the square root as follows:

$$f(x) = \frac{1}{2}\|Jx + r(0)\|^2. \quad (6)$$

We get

$$\begin{aligned} \nabla f(x) &= J^T (Jx + r), \\ \nabla^2 f(x) &= J^T J. \end{aligned} \quad (7)$$

Placing  $\nabla f(x) = 0$ , we get  $x_{\min} = -(J^T J)^{-1} J^T r$ . This is the result of the normal equation. Going back xxxx“the nonlinear case”

$$\nabla f(x) = \sum_{j=1}^m r_j(x) \nabla r_j(x) = J(x)^T r(x), \quad (8)$$

$$\nabla^2 f(x) = J(x)^T J(x) + \sum_{j=1}^m r_j(x) \nabla^2 r_j(x).$$

The special property of square problems is with the Jacobi matrix; it is possible to get the Hessian matrix basically ( $\nabla^2 f(x)$ ) if possible approximate  $r_{js}$  by linear functions  $\nabla^2 r_j(x)$  is small or small residual ( $r_j(x)$ ). The Hessian matrix in this case simply becomes

$$\nabla^2 f(x) = J(x)^T J(x). \quad (9)$$

The results are the same as those for linear cases.

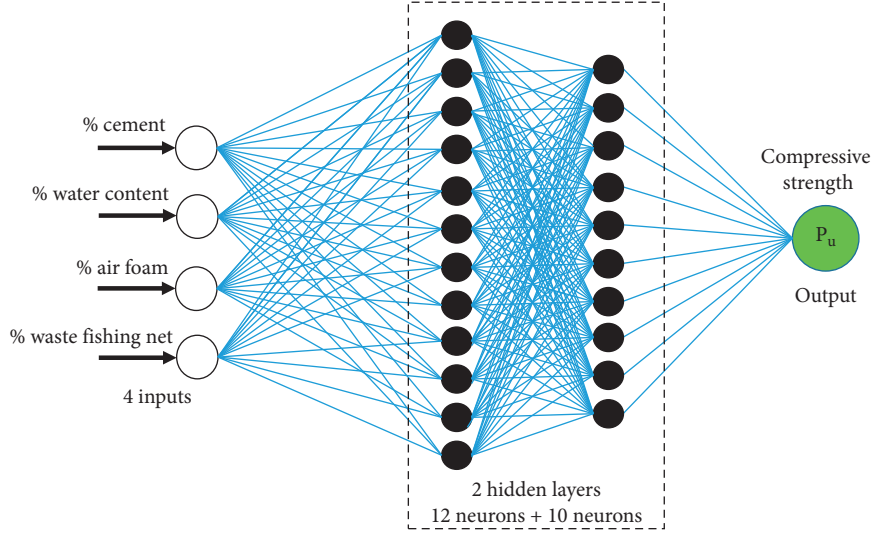


FIGURE 2: Architecture for the developed ANN: 4 inputs, 2 hidden layers, and 1 output.

**2.2. Structure of the ANN Model.** The effectiveness of the ANN model depends on the structure of the neural network (NN), that is, the number of hidden layers and the number of neurons. The ANN structure was chosen to predict the stabilized dredged sediments in this investigation, including 4 layers. The input layer consists of 4 neurons corresponding to 4 input variables (cement content, water content, air foam content, and waste fishing net content), and the output layer includes 1 neuron representing compressive strength. According to [22, 23], the accuracy of the ANN model is depends strongly on the structure of the ANN model such as number of hidden layers and number of neurons in each hidden layer. For comparison with the ANN model proposed by Park and Kim [7], number of hidden layers is assumed to be equal to 2 and number of neurons in each hidden layer is manually chosen. The number of neurons in each hidden layer is varied from 9 to 12 neurons to cover the range of neuron as suggested in previously research, such as in the works of Neville [24] and Hush [25]. Therefore, 16 ANN architectures are built. The performance of each model is evaluated to determine the best ANN architecture.

**2.3. Performance Evaluation.** In this investigation, the three criteria used are correlation coefficients (R) (Pearson's correlation coefficient), Mean Absolute Error (MAE), and Root Mean Square Error (RMSE) to evaluate the accuracy of the developed ANN model [26]:

$$\begin{aligned}
 \text{RMSE} &= \sqrt{\frac{1}{N} \sum_{j=1}^N (p_{0,j} - p_{t,j})^2}, \\
 R &= \frac{\sum_{j=1}^N (p_{0,j} - \bar{p}_0)(p_{t,j} - \bar{p}_t)}{\sqrt{\sum_{j=1}^N (p_{0,j} - \bar{p}_0)^2 \sum_{j=1}^N (p_{t,j} - \bar{p}_t)^2}} \quad (10) \\
 \text{MAE} &= \frac{1}{N} \sum_{j=1}^N (p_{0,j} - p_{t,j}),
 \end{aligned}$$

where  $N$  is the number of datasets,  $p_0$  and  $\bar{p}_0$  are the actual experiment value and the average experimental value, and  $p_t$  and  $\bar{p}_t$  are the predicted value and the average predicted value, calculated according to the ANN model.  $R$  measures the predicted and experimental value association; if  $R$  is closer to 1, the ANN model is more accurate. RMSE calculates the square root average difference between the expected values and the experimental values and the difference between the experimental and the predicted values is determined by MAE criteria.

### 3. Database Construction

In this investigation, the data was extracted from [7], in which 51 experimental pieces of data of stabilized dredged sediments are designed with cement, air foam, and waste fishing net. The ANN model uses 4 input variables: (1) cement content (% by weight), (2) water content, (3) air foam content (% by weight), and (4) waste fishing net content (% by weight). Output parameter is considered to be unconfined compressive strength  $P_u$  (kN/m<sup>2</sup>). The dataset was randomly divided into two subdatasets, and 70% of the data were used to train the ANN models corresponding to 36 samples. The remaining 30% of the data correspond to the 15 samples used in the testing model. The initial statistical analysis of the dataset is presented in Table 1.

The used cement content ranges from 8% to 20% by weight of untreated sediment (mean value of 12.5% and standard deviation of 2.5%). The water content ranges from 125% to 250% by weight of untreated sediment (mean value of 168.2% and standard deviation of 32.5%). The used air foam ranges from 1% to 5% by weight of untreated sediment (mean value of 2.4% and standard deviation of 1%). The used waste fishing net ranges from 0% to 0.2% by weight of untreated sediment (mean value of 0.1% and standard deviation of 0.1%).

TABLE 1: Initial statistical analysis of the dataset.

Variable	Cement	Water content	Air foam	Waste fishing net	$P_u$
Unit	% by weight	% by weight	% by weight	% by weight	$\text{kN/m}^2$
Role	Input	Input	Input	Input	Output
Count	51.0	51.0	51.0	51.0	51.0
Mean	12.5	168.2	2.4	0.1	38.0
Std <sup>a</sup>	2.5	32.5	1.0	0.1	26.5
Min	8.0	125.0	1.0	0.0	7.9
$Q_{25}$	12.0	156.0	2.0	0.0	15.7
$Q_{50}$	12.0	156.0	2.0	0.1	27.2
$Q_{75}$	12.0	171.5	2.0	0.1	60.4
Max	20.0	250.0	5.0	0.2	100.7

<sup>a</sup>Standard deviation.

## 4. Results and Discussion

During back-propagation network training, the cycle of sending all training samples across the network is called an epoch. The training process will be repeated until the error at the network output reaches an acceptable value (less than the initial specified error threshold). The objective of this process is to minimize the error between actual data and simulation data. Training and testing processes are also used to determine the optimal number of epochs for the model. Figure 3 shows the best performance of the ANN models for training and test processes with 500 epochs. This number of epochs has been chosen to prevent the proposed ANN model from overfitting.

With ANN architecture containing 2 hidden layers, 16 structures are investigated, as shown in Figure 4 for the training datasets. Figures 4(a)–4(c) show the values of  $R$ , RMSE, and MAE, respectively. It is worth nothing that 10 neurons in the second hidden layer produce higher prediction accuracy. The best architecture containing, respectively, 12 neurons and 10 neurons for first and second hidden layers is observed to achieve the best accuracy of training part with highest value of  $R$  and lowest values of RMSE and MAE. That is a good example to show that a suitable ANN architecture should be determined before performing any further simulations. The best ANN architecture is used for predicting the compressive strength of stabilized dredged sediments.

Using the ANN model [4–12], the prediction of stabilized dredged sediments compressive strength for training and testing part is shown in Figures 5(a) and 5(b), respectively. Figure 5 shows that the ANN model's results and experimental results are almost identical for each sample in the training phase. It shows that the prediction capacity of the ANN model is excellent. Therefore, the ANN model can predict relatively accurately for the testing phase.

The regression model for the training and testing parts is shown in Figures 6(a) and 6(b), respectively. From the figure above, we can see that the prediction ability of the ANN model is quite close to the experimental compressive strength, but there are still high errors for testing part, high water content such as 218% (see Table 2).

The correlation value obtained for training is  $R=0.95$  and the control is  $R=0.94$ . This shows that applying the

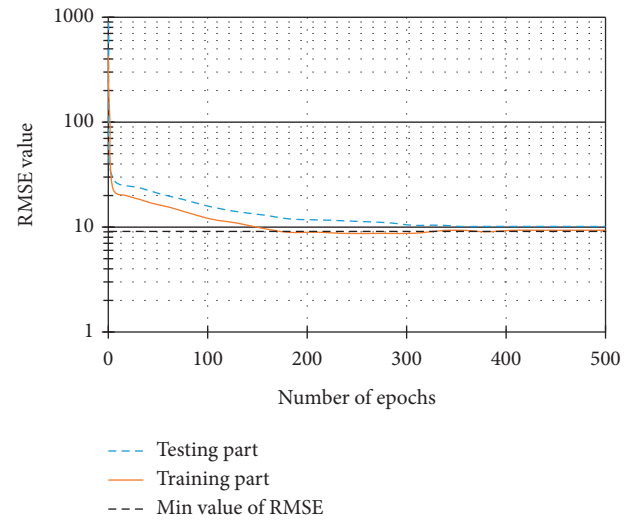


FIGURE 3: RMSE value of training part and testing part in function of number of epochs.

ANN model for predicting the compressive strength of stabilized dredged sediments is very feasible due to high accuracy and low error. For training dataset, the function " $y = x - 0.15$ " is set to show the correlation between experimental data and the ANN model's data. Similarly, the function " $y = 1.1x + 0.17$ " is set for correlation in the control dataset. For RMSE indicators, the biggest errors are 9.1948 and 10.3390 with training and testing, respectively. For MAE indicators, the biggest errors are 3.9001 and 8.6535, respectively, for training and testing (Table 3). Therefore, the ability to predict is relatively high.

To prove the accuracy of the ANN model, Table 2 shows the 51 experimental pieces of data of [7] and compares them with the ANN model's results. It can be seen that the ANN simulation's results give very low errors in most cases, except for the high water content. The biggest error of the ANN model compared to the experiment is 382.2% and the lowest is 0.0% for 156% of water content. The ANN model predicts relatively correctly with lower water content, which importantly affects the accuracy of the ANN model.

In fact, the investigation of Park and Kim [7] has developed an ANN model for predicting the unconfined compressive strength of reinforced lightweight soil. The

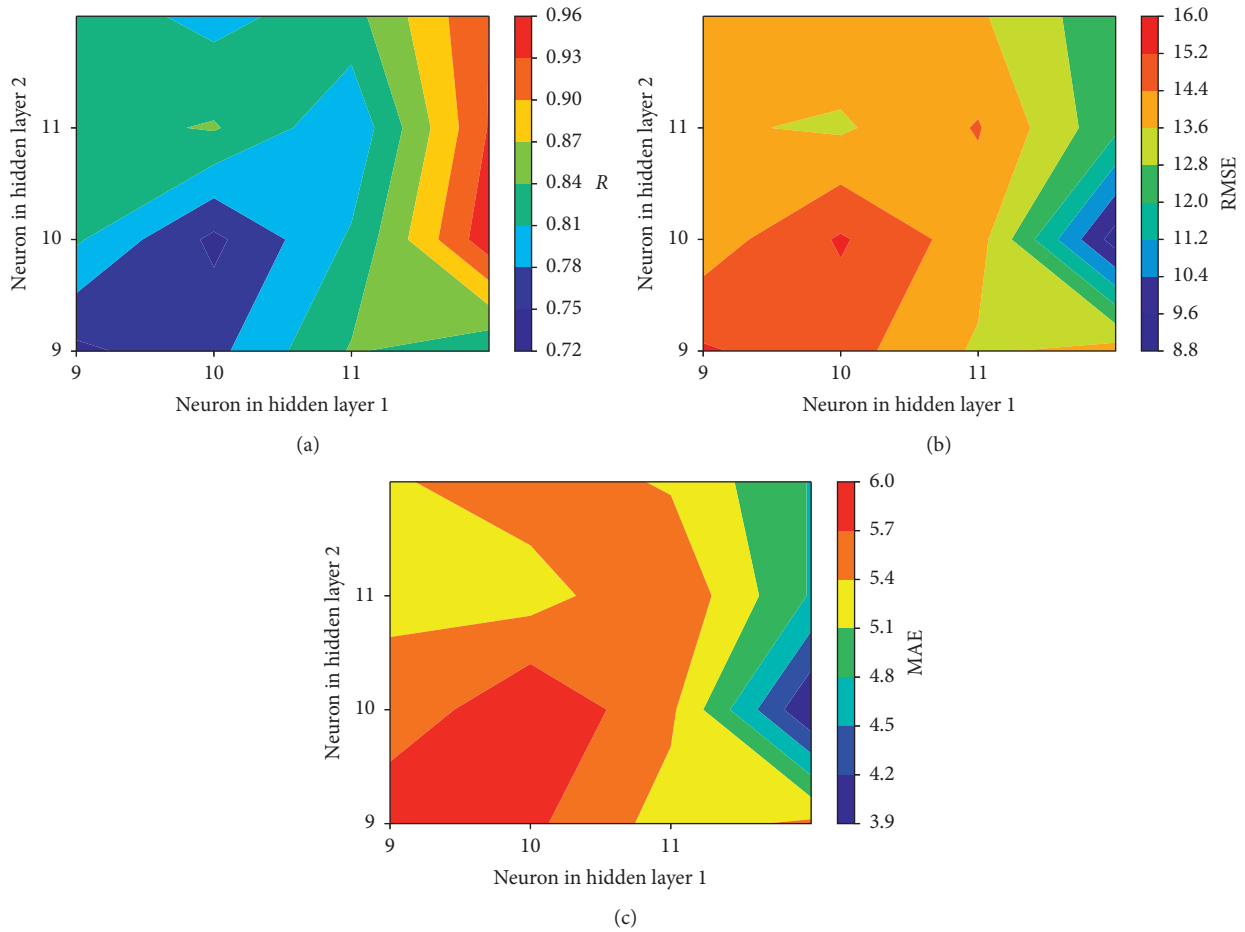


FIGURE 4: Color map of ANN with 2 hidden layers in function of the neuron in the hidden layer for the training part with respect to (a) values of  $R$ , (b) value of RMSE, and (c) value of MAE.

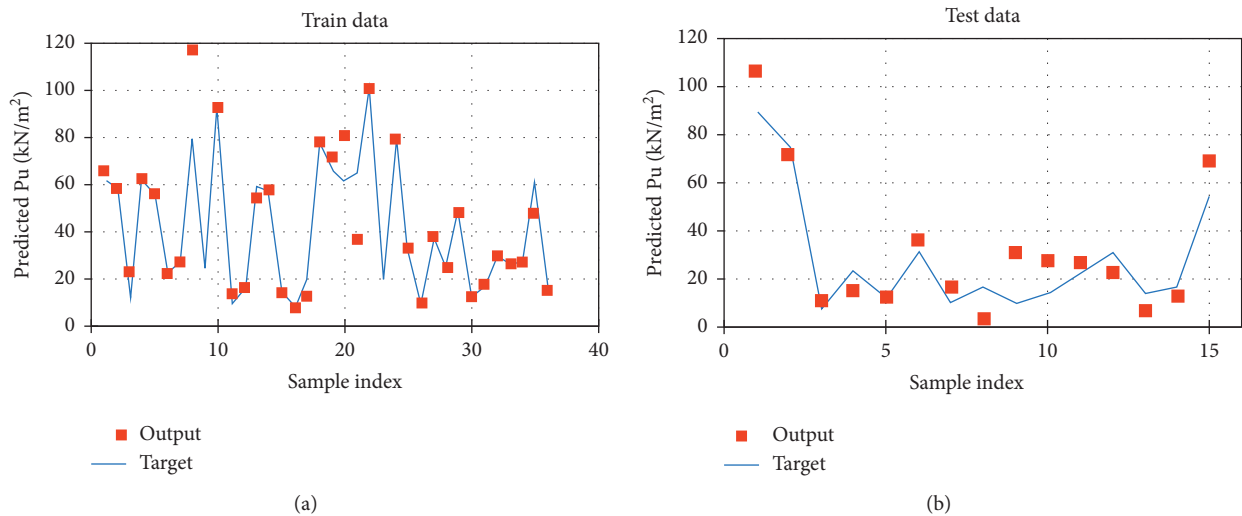


FIGURE 5: Predicted compressive strength of stabilized dredged sediments by the ANN model. (a) Training. (b) Testing.

ANN structure in this investigation is a single hidden layer containing 4 neurons. The performance of this ANN model was only evaluated through Pearson's correlation coefficient  $R$ , which was equal to 0.97 and 0.96 for training and testing

parts, respectively. The number of hidden layers such as single layer or multiple hidden layers is always a big challenge of the ANN structure [22, 23]. In our investigation, a new ANN structure is developed consisting of two hidden

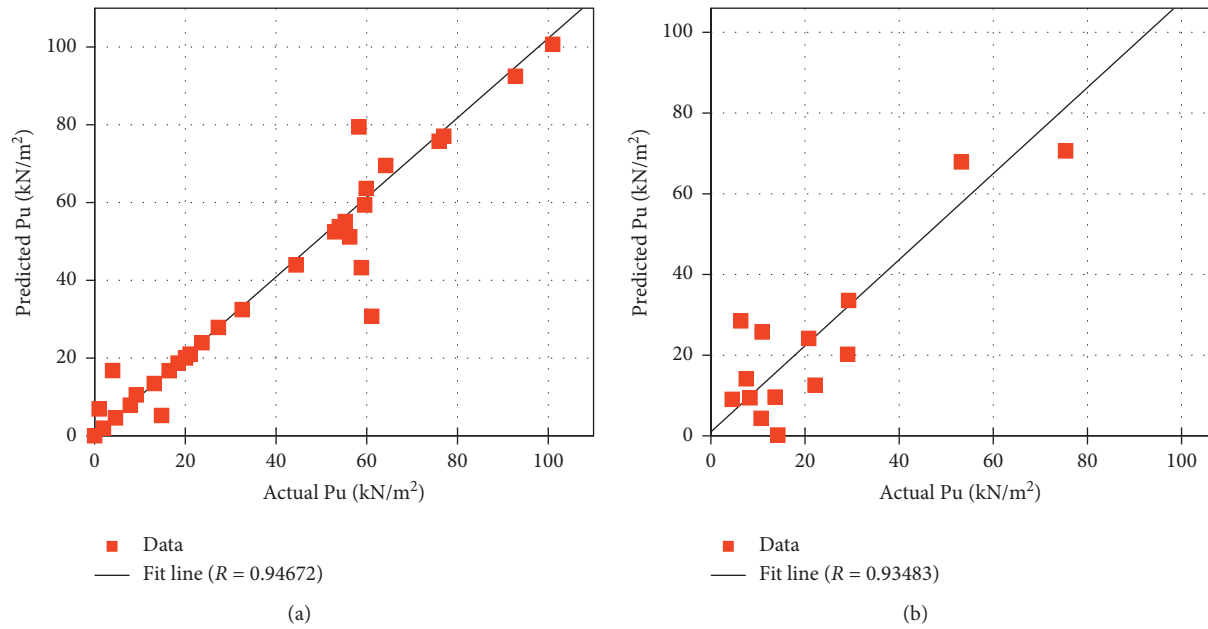


FIGURE 6: ANN regression results for (a) training and (b) testing.

TABLE 2: Comparison of experimental results and ANN model results with error (ANN-EXP)/EXP.

Sample	Dataset	% cement	% water	% air foam	% waste	Experimental	ANN	Error (%)
01	Training	12	156	1	0.143	62.81	66.49	5.54
02	Training	12	156	1	0.179	58.9	58.90	0.00
03	Training	12	156	5	0	11.56	23.63	51.08
04	Training	12	125	2	0.036	63.02	63.02	0.00
05	Training	12	156	2	0.143	56.22	56.22	0.00
06	Training	12	156	4	0.036	23.09	23.09	0.00
07	Training	12	156	2	0.179	27.23	27.23	0.00
08	Training	20	156	2	0	80.16	116.96	31.46
09	Training	12	156	3	0.179	25.2	25.20	0.00
10	Training	16	156	2	0.036	93.14	93.14	0.00
11	Training	12	250	2	0.036	8.7	14.50	40.00
12	Training	12	218	2	0	16.24	16.24	0.00
13	Training	12	156	2	0.107	59.49	55.21	-7.75
14	Training	12	156	1	0	57.56	57.56	0.00
15	Training	12	218	2	0.179	14.94	14.94	0.00
16	Training	12	250	2	0.107	7.93	7.93	0.00
17	Training	12	218	2	0.036	21.44	12.97	-65.27
18	Training	16	156	2	0.107	78.19	78.19	0.00
19	Training	12	156	1	0.107	66.79	72.41	7.76
20	Training	12	125	2	0.107	61.28	81.51	24.82
21	Training	16	156	2	0.179	64.37	36.55	-76.10
22	Training	20	156	2	0.143	100.7	100.70	0.00
23	Training	8	156	2	0.143	20.1	20.10	0.00
24	Training	12	125	2	0.143	79	79.00	0.00
25	Training	12	156	2	0	33.15	33.15	0.00
26	Training	8	156	2	0.179	9.76	9.76	0.00
27	Training	12	125	2	0	37.95	37.95	0.00
28	Training	12	156	3	0	25.06	25.06	0.00
29	Training	12	125	2	0.179	48.69	48.69	0.00
30	Training	12	250	2	0	12.2	12.20	0.00
31	Training	8	156	2	0.036	16.21	18.13	10.58
32	Training	12	187	2	0.036	29.76	29.76	0.00
33	Training	12	187	2	0.107	26.35	26.35	0.00
34	Training	12	156	3	0.107	27.4	27.40	0.00

TABLE 2: Continued.

Sample	Dataset	% cement	% water	% air foam	% waste	Experimental	ANN	Error (%)
35	Training	12	156	2	0.036	61.86	48.14	-28.51
36	Training	12	156	5	0.143	15.2	15.20	0.00
37	Testing	20	156	2	0.107	89.82	106.17	15.40
38	Testing	16	156	2	0.143	76.01	71.65	-6.08
39	Testing	12	250	2	0.143	8.17	11.94	31.57
40	Testing	12	156	4	0.107	25.06	15.35	-63.29
41	Testing	12	156	5	0.179	11.71	12.52	6.46
42	Testing	12	187	2	0.143	32.06	36.16	11.34
43	Testing	8	156	2	0	10.86	17.17	36.76
44	Testing	12	218	2	0.143	17.50	3.63	-382.2
45	Testing	12	187	2	0	10.15	30.94	67.20
46	Testing	12	156	4	0.179	14.42	28.16	48.79
47	Testing	12	156	3	0.036	23.85	26.76	10.87
48	Testing	12	156	3	0.143	31.70	23.20	-36.66
49	Testing	12	187	2	0.179	13.95	7.33	-90.24
50	Testing	12	156	5	0.036	16.81	12.93	-30.03
51	Testing	12	156	1	0.036	54.87	68.95	20.43

TABLE 3: Pearson's correlation coefficient (R), Mean Absolute Error (MAE), and Root Mean Square Error (RMSE).

	Training	Testing
RMSE	9.1948	10.3390
MAE	3.9001	8.6535
R	0.95	0.94

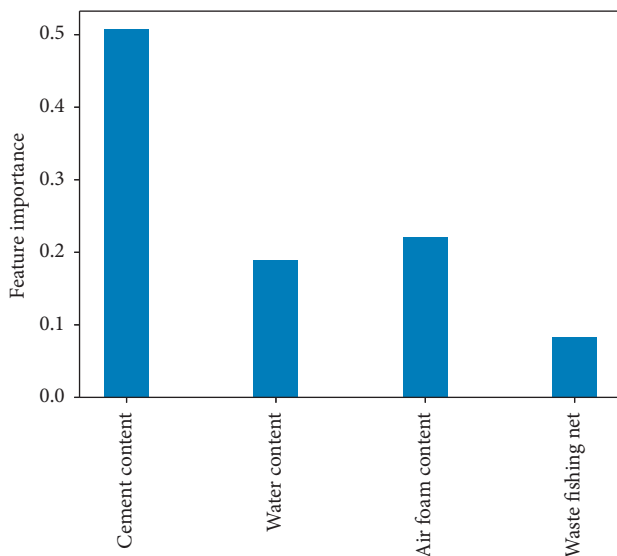


FIGURE 7: Importance of each input effect on unconfined compressive strength.

layers that contain 12 and 10 neurons, respectively. The performance of the new ANN model is considered to be Pearson's correlation coefficient  $R$ , Mean Absolute Error (MAE), and Root Mean Square Error (RMSE). Pearson's correlation coefficient  $R$  of the model is equal to 0.95 and 0.94 for training and testing parts, respectively. Comparing the performance of the ANN model, Pearson's correlation coefficient  $R$  of this paper is slightly lower than that proposed by Park and Kim [7]. However, the prediction of model is

successful with lower water content and the large error focus on the high water content of dredged sediment. Overall, it is shown that the performance of the ANN model using two hidden layers seems obviously no greater than that using a single hidden layer.

Figure 7 shows the dependence of unconfined compressive strength  $P_u$  for each input. The most important input is the cement content used for stabilizing sediments. The least important input is the waste fishing net content. The influence of air foam content on unconfined compressive strength is more important than that of water content.

## 5. Conclusion

In this paper, the ability of artificial intelligence (AI) techniques to predict the compressive strength of stabilized dredged sediments was tested. The dataset used for simulation is collected from experimental results that have been published in literature. To save time and money for conducting experiments, an ANN model was developed. In addition, to confirm and verify the performance of the ANN model, an artificial neural network (ANN) was created and adjusted by back-propagation algorithm (BP) with Levenberg-Marquardt (LMA) algorithm. The compressive strength of stabilized dredged sediments has been predicted by ANN models with network structure [4–12]. The results show that the ANN model can accurately predict the compressive strength of stabilized dredged sediments with low water content. Therefore, this algorithm is a good approach that can be applied for mix design for stabilization/solidification of dredged sediments. The important input affecting the unconfined compressive strength can be in the following order: cement content > air foam content > water content > waste fishing net. It seems to be very interesting to perform a comparison of performance between the actual model and the new model including normalized inputs, other activation functions, and other learning algorithms in future research.

## Data Availability

The data supporting this manuscript are from previously reported studies and datasets, which have been cited. The processed data are available from the corresponding author upon request.

## Conflicts of Interest

The author declares that there are no conflicts of interest.

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