Diatomite was slightly modified with a sodium hydroxide solution. The resulting material was characterized by using energy-dispersive X-ray spectroscopy (EDX), X-ray diffraction (XRD), Fourier-transform infrared spectroscopy (FT-IR), scanning electron microscopy (SEM), and nitrogen adsorption-desorption isotherms. The so-treated diatomite has a high specific surface area (77.8 m²/g) and a high concentration of isolated silanol groups on the surface, and therefore, its adsorption capacity increases drastically in both the single and binary adsorption systems for rhodamine B and methylene blue. The binary system is more effective than the single system, with methylene blue being adsorbed more than rhodamine B. The adsorption process is spontaneous and fits well with the Langmuir isothermal model, and it depends on pH significantly.

1. Introduction

Dyes are widely used in numerous applications, such as textile, paper, plastic, and dye industries [1]. The amount of dyes produced annually worldwide is estimated at over $7 \times 10^5$ tons, and more than 100,000 commercially available dyes with different physical and chemical properties are being used [2–4]. Various dyes and their decomposition products are toxic and carcinogenic, thus posing a danger to aquatic organisms [1, 5]. Therefore, dye removal from wastewater is essential.

A large number of dyes have a complex aromatic ring structure and are difficult to degrade biologically [4, 6]. Therefore, it is necessary to reduce their concentration in wastewaters prior to biological treatment. Chemical oxidation has been extensively studied for dye removal from wastewaters [1, 7–9]. However, oxidation often produces intermediate products that can cause secondary pollution. Meanwhile, the adsorption technique has proven to be a simple, efficient, and attractive way to remove nonbiodegradable pollutants (including dyes) from wastewaters [5, 10, 11]. To remove dyes from complex aqueous solutions, a variety of adsorbents have been used, such as banyan aerial roots [12], peat [2], bentonite [13], mesoporous silica nanoparticles [14], clay [15, 16], activated banana peel carbon [17], silica extracted from rice husk [18], and zeolite [19], and some of them exhibit high performance. However, the search for new, effective, cheap, and environmentally friendly adsorbents is on the way.

Diatomite is a low-density, small-particle sedimentary rock consisting mainly of amorphous silica (SiO₂·nH₂O) derived from diatoms. Diatomite encompasses a variety of structures and has high porosity (up to 80%), a large specific surface area, and multiple hydroxyl groups on the surface [3, 6, 10, 11, 20]. These properties enable diatomite to be a potential adsorbent for the pollutants present in industrial wastewaters, including dyes. Besides, diatomite is abundant in nature, cheap, and environmentally friendly [11]. Several studies have dealt with the applicability of natural diatomite in the adsorption field [6, 10, 11, 21–23]. Other studies have focused on diatomite surface modification with metals or organic functional groups to improve adsorption efficiency.
Table 1: Main characteristics of the dyes used in this study.

<table>
<thead>
<tr>
<th>Dye</th>
<th>RB</th>
<th>MB</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type</td>
<td>Basic violet 10, C.I.45170, cationic</td>
<td>Basic blue 9, C.I.52015, cationic</td>
</tr>
<tr>
<td>Phase</td>
<td>Solid</td>
<td>Solid</td>
</tr>
<tr>
<td>Molecular formula</td>
<td>C_{28}H_{31}O_{3}N_{2}Cl</td>
<td>C_{16}H_{18}N_{3}SCl</td>
</tr>
<tr>
<td>Molecular weight (g/mol)</td>
<td>479.03</td>
<td>319.85</td>
</tr>
</tbody>
</table>

Chemical structure

Figure 1: UV-Vis absorption spectra for aqueous solutions of (a) RB, (b) MB, and (c) both of the dyes along with alkali-activated diatomite at various adsorption times.
or expand its applications [1, 7–9, 24–32]. In some studies, natural diatomite is treated thermally [3, 10, 20, 33, 34], with acids [3, 20, 35–37], or with alkalines [4, 37, 38] to enhance its application performance. Other studies use diatomite as a raw material to manufacture other products [14, 35, 39–42]. The diatomite purified by calcining is also investigated by Yuan et al. [43]. They discovered that when the temperature increases, the condensation of surface silanol groups occurs. Hydrogen-linked hydroxyl groups condense more easily than isolated hydroxyl groups. Bronsted acid centers also condense at high temperatures. This condensation reduces the adsorption capacity of the diatomite treated by calcining toward base dyes. When treated with acids (normally at high concentration: 5 M H2SO4 [3], 5 M HCl [35], 1–5 M HCl [36], 10% HCl [20], and 1 M H2SO4 [37]), it is difficult to perform the modification and is easily contaminated by secondary pollution. Therefore, numerous studies have focused only on diatomite purification because it is cheap, easy to operate, and environmentally friendly [4]. When purified with alkali, diatomite retains its hydroxyl groups on the surface, and they are excellent adsorption centers for many metals as well as dyes.

Since most industrial wastewaters contain different pollutants, it is important to investigate the effect of multicomponent systems on the adsorption capacity. Various studies have studied the simultaneous removal of different pollutants from aqueous solutions [2, 5, 44] to assess the competitiveness of adsorbates. In this study, natural diatomite is activated by treating with low-concentrated sodium hydroxide (NaOH), hydrochloric acid (HCl), and methylene blue (MB) in single and binary systems. The equilibrium isotherms and thermodynamic parameters of the adsorption processes are studied. In addition, the effect of the solution pH on the adsorption efficiency of MB in the single system is also investigated.

## 2. Materials and Methods

### 2.1. Materials

Natural diatomite was obtained from Phu Yen province, Vietnam. Natural diatomite was washed several times with water, dried at 100°C, sieved, and stored in closed containers for further tests. The product is called purified diatomite.

Sodium hydroxide (NaOH), hydrochloric acid (HCl), and potassium chloride (KCl) were purchased from Guangdong (China). Methylene blue (Guangdong, China) and rhodamine B (HiMedia, India) dyes were used as adsorbates. A summary of the main characteristics of these dyes is given in Table 1 [3, 5, 22, 27, 37].

### 2.2. Activation of Diatomite

Purified diatomite was activated with NaOH to enhance the adsorption capacity. The purified diatomite sample was immersed in a 3% NaOH solution at a ratio of 1:10 (w/w) and stirred at 100°C for 2 h to remove impurities and organics. Then, the solid was filtered, washed several times with distilled water, dried at 100°C, and sieved. The obtained alkali-activated diatomite was stored in closed containers for further tests.

### 2.3. Characterization

The chemical analysis of diatomite was performed by using energy-dispersive X-ray spectroscopy (EDX, JEOL JED-2300, Japan) at different sites of the material. The powder X-ray diffraction (XRD) patterns were recorded by VNU-D8 Advance, Bruker, Germany, with Cu Kα radiation (λ = 1.5406 Å). Fourier-transform infrared spectra (FT-IR) were measured on a Jasco FT/IR-4600 spectrometer (Japan) with a range of 4000–400 cm⁻¹. The morphology of diatomite was observed with scanning electron microscopy (SEM) using SEM JMS-5300LV (Japan). Nitrogen adsorption/desorption isotherm measurements were conducted using a TriStar 3000 analyzer. Samples were pretreated by heating at 250°C for 5 h with N2 before the measurements.

### 2.4. Point of Zero Charge

The point of zero charge (pH_PZC) of the adsorbent was determined to follow the methods of Mahmood et al. [45], Jing et al. [46], and Du and Hoai [47]. To a series of 100 mL Erlenmeyer flasks, 50 mL of a 0.01 M KCl solution was added. The initial pH (pH_I) of the solutions was adjusted, ranging from 2 to 12, by adding a 0.1 M HCl or 0.1 M NaOH solution. Then, 0.1 g of the adsorbent was added to each flask and mixtures were shaken for 48 h. The final pH (pH_F) of the solutions was measured. The difference between the final and initial pHs (ΔpH = pH_F − pH_I) was plotted against the pH_I. The point of intersection of the curve with the abscissa, at which ΔpH = 0, provides pH_PZC.

### 2.5. Adsorption

#### 2.5.1. Adsorption Experiments

Adsorption experiments were carried out with a typical batch approach in a 250 mL round flask with a reflux condenser. In each experiment, 0.02 g of the adsorbent was stirred with 100 mL of a solution containing RB (or MB or a mixture of RB and MB) at a specific concentration, and the temperature of the reactor was fixed at 30 or 45°C. After a certain interval, 5 mL of the solution was withdrawn and centrifuged to remove the adsorbent, and the concentration of the remaining solution was determined. The concentration of dyes was determined with the UV-Vis

<table>
<thead>
<tr>
<th>Element</th>
<th>Purified diatomite</th>
<th>Alkali-activated diatomite</th>
</tr>
</thead>
<tbody>
<tr>
<td>O</td>
<td>52.72 ± 1.48</td>
<td>49.06 ± 1.27</td>
</tr>
<tr>
<td>Mg</td>
<td>0.53 ± 0.06</td>
<td>0.53 ± 0.04</td>
</tr>
<tr>
<td>Al</td>
<td>10.36 ± 0.87</td>
<td>11.59 ± 0.03</td>
</tr>
<tr>
<td>Si</td>
<td>30.56 ± 0.59</td>
<td>27.50 ± 1.42</td>
</tr>
<tr>
<td>K</td>
<td>0.20 ± 0.09</td>
<td>1.09 ± 0.83</td>
</tr>
<tr>
<td>Ca</td>
<td>0.21 ± 0.05</td>
<td>0.17 ± 0.03</td>
</tr>
<tr>
<td>Ti</td>
<td>0.91 ± 0.17</td>
<td>1.23 ± 0.10</td>
</tr>
<tr>
<td>Fe</td>
<td>4.50 ± 0.10</td>
<td>6.02 ± 0.27</td>
</tr>
<tr>
<td>Na</td>
<td>—</td>
<td>1.77 ± 0.24</td>
</tr>
<tr>
<td>Cl</td>
<td>—</td>
<td>1.03 ± 0.19</td>
</tr>
<tr>
<td>Total</td>
<td>100</td>
<td>100</td>
</tr>
</tbody>
</table>
method on UVD-3000 (Labomed, USA) at $\lambda_{\text{max}} = 554 \text{ nm}$ for RB and $\lambda_{\text{max}} = 664 \text{ nm}$ for MB (Figure 1). The adsorbed capacity ($q_t$ or $q_e$) and removal efficiency ($R$) of the dye adsorbed onto the adsorbent were calculated according to the following equations:

$$q_t = \frac{(C_0 - C_t) \times V}{m} \text{ (mol} \cdot \text{g}^{-1}),$$  \hspace{1cm} (1)

$$q_e = \frac{(C_0 - C_e) \times V}{m} \text{ (mol} \cdot \text{g}^{-1}),$$  \hspace{1cm} (2)

$$R = \frac{(C_0 - C_e)}{C_0} \times 100 \%,$$  \hspace{1cm} (3)

where $C_0$ and $C_t$ are the concentrations of the dyes in the solution (mol·L$^{-1}$) at time $t = 0$ and $t = t$, respectively; $C_e$ is the concentration of the dyes in the solution (mol·L$^{-1}$) at

**Figure 2:** XRD pattern (a) and FT-IR spectra (b) of the diatomite samples.

**Figure 3:** SEM images. (a, b) Purified diatomite. (c, d) Alkali-activated diatomite.
equilibrium; \( V \) is the volume of the solution (L); and \( m \) is the weight of the dry adsorbent (g).

The influence of initial pH (3, 5, 7, 9, and 11) was also studied in a single system with a similar procedure.

2.5.2. Isothermal Models. In this work, the Langmuir and Freundlich two-parameter models were used to analyze the adsorption equilibrium data.

The Langmuir model is based on the assumption that the adsorption is a monolayer; that is, the adsorbates form a monolayer and all the sorption sites on the adsorbent surface have the same affinity for the adsorbates. The Langmuir isotherm equation [48] is as follows:

\[
q_e = q_m \times \frac{K_L \times C_e}{1 + K_L \times C_e},
\]

where \( q_m \) is the maximum monolayer adsorption capacity of the adsorbent (mol·g\(^{-1}\)) and \( K_L \) is the Langmuir constant (L·mol\(^{-1}\)). The other parameters are described above. The Langmuir constant is a measure of the affinity between the adsorbate and the adsorbent and relates to the free energy of adsorption [5]. The most commonly used linear form of the Langmuir equation [2-5, 13, 18, 20, 32, 42, 49-51] is

\[
\frac{C_e}{q_e} = \frac{1}{q_m} \times C_e + \frac{1}{K_L \times q_m}.
\]

The plot of \( C_e/q_e \) versus \( C_e \) is a straight line with the slope \( 1/q_m \) and intercept \( 1/(q_m \cdot K_L) \).

The Freundlich expression is an exponential equation and therefore assumes that as the adsorbate concentration increases, the concentration of the adsorbate on the adsorbent surface also increases. The Freundlich isotherm is expressed by the following empirical equation [48]:

\[
q_e = K_F \times C_e^{1/n},
\]

where \( n \) is the heterogeneity factor, and \( K_F \) is the Freundlich constant (mol\(^{(1-1/n)}\)·L\(^{1/n}\)·g\(^{-1}\)). \( n \) and \( K_F \) are dependent on temperature; \( n \) indicates the extent of the adsorption, and \( K_F \) expresses the degree of nonlinearity between the solution concentration and the adsorption.

Table 3: Textural properties of the diatomite samples.

<table>
<thead>
<tr>
<th>Sample</th>
<th>( S_{\text{BET}} ) (m(^2)·g(^{-1}))</th>
<th>( S_{\text{mic}} ) (m(^2)·g(^{-1}))</th>
<th>( S_{\text{ext}} ) (m(^2)·g(^{-1}))</th>
<th>( V_{\text{mic}} ) (cm(^3)·g(^{-1}))</th>
<th>( V_{\text{tot}} ) (cm(^3)·g(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Purified diatomite</td>
<td>55.4</td>
<td>19.2</td>
<td>36.2</td>
<td>0.0088</td>
<td>0.0623</td>
</tr>
<tr>
<td>Alkali-activated diatomite</td>
<td>77.8</td>
<td>19.7</td>
<td>59.1</td>
<td>0.0089</td>
<td>0.0924</td>
</tr>
</tbody>
</table>

Figure 4: Nitrogen adsorption-desorption isotherms (a) and pore size distributions (b) of the diatomite samples.

Figure 5: Determination of the point of zero charge of the diatomite samples.
The linear form of the Freundlich equation is
\[ \log(q_e) = \log(K_F) + \frac{1}{n} \times \log(C_e). \] (7)

The plot of \( \log(q_e) \) versus \( \log(C_e) \) is a straight line with the slope \( 1/n \) and intercept \( \log(K_F) \).

2.5.3. Thermodynamic Parameters. To determine whether the adsorption process occurs spontaneously or not, we have to study the thermodynamic parameters. At equilibrium, the Gibbs free energy of adsorption (\( \Delta G^\circ \)) is an important quantity for determining the spontaneity of the process itself and is calculated according to the following equation:
\[ \Delta G^\circ = -RT \times \ln K_e, \] (8)
where $K_e$ is the thermodynamic equilibrium constant; $R$ is the universal gas constant (8.314 J·mol$^{-1}$·K$^{-1}$); and $T$ is the absolute temperature in Kelvin.

For the adsorption process, $K_e$ can be determined in a number of ways, depending on the experimental conditions, such as the equilibrium constant $K_C = (C_0 - C_e)/C_e$ [3, 16, 18, 20, 38], the distribution coefficient $K_d = q_e/C_e$ [12–14, 34, 37, 42, 50–52], and the Langmuir constant $K_L$ [4–6, 53, 54].

In this study, the adsorption constant in the Langmuir isotherm ($K_L$) was used to determine thermodynamic parameters ($\Delta G^o$, $\Delta H^o$, and $\Delta S^o$) for the adsorption by using the following equations [5]:

\[
\Delta G^o = -R \times T \times \ln K_L, \tag{9}
\]

\[
\Delta H^o = -R \times \frac{T_2 \times T_1}{T_2 - T_1} \times \ln \frac{K_{L1}}{K_{L2}}, \tag{10}
\]
where 1641 cm$^{-1}$ correspond to the adsorbed H$_2$O, including interlayer water and hydrogen-bonded water with surface hydroxyl groups. A broad band centered at 1101-1031 cm$^{-1}$ and two bands at 789 cm$^{-1}$ and 465 cm$^{-1}$ correspond to the asymmetric stretching vibration, symmetric stretching, and bending vibration of Si-O-Si bonds, respectively [1, 20]. The peaks observed at 20-25$^\circ$C are typical for amorphous SiO$_2$ [1, 32, 37, 39, 51]. The absence of the peak around 27$^\circ$C indicates that the diatomite in our study does not contain quartz crystals like other Phu Yen’s diatomite [1, 26, 30, 32, 35, 37, 39, 40].

The FT-IR spectra of the diatomite samples are similar (Figure 2(b)). The broad absorption bands at 3450 cm$^{-1}$ and 1641 cm$^{-1}$ correspond to the adsorbed H$_2$O, including interlayer water and hydrogen-bonded water with surface hydroxyl groups. A broad band centered at 1101-1031 cm$^{-1}$ and two bands at 789 cm$^{-1}$ and 465 cm$^{-1}$ correspond to the asymmetric stretching vibration, symmetric stretching, and bending vibration of Si-O-Si bonds, respectively [1, 20]. The peaks observed at 3699 cm$^{-1}$ and 3623 cm$^{-1}$ are assigned to surface hydroxyl groups in diatomite. The peak at 3699 cm$^{-1}$ is attributed to the isolated hydroxyl (Si-OH) on the surface of diatomite [1, 43, 55], while the peak at 3623 cm$^{-1}$ belongs to O-H stretching vibration of the aluminol groups (≡Al(OH)) [55]. Alkali-activated diatomite has high-intensity peaks for O-H stretching, indicating that more isolated hydroxyl groups are present on the surface. The peak at 536 cm$^{-1}$ corresponds to the stretching vibration of Fe-O [1]. The peak at 1380 cm$^{-1}$ is attributed to some organic substances [20]. The intensity of this peak is lower in alkali-activated diatomite than in purified diatomite samples, indicating the removal of organic substances from purified diatomite during NaOH treatment.

The SEM images show that purified diatomite consists of circular cylinders of a diameter of about 5-7 $\mu$m, with small pores on the surface (Figures 3(a) and 3(b)). However, these cylinders are partly shattered, causing the pores to become smaller and even blocked. The alkali-activated diatomite retains its multipore structure, and the pores on the surface become larger after treatment (Figures 3(c) and 3(d)). This change may be the result of the formation of soluble silicates SiO$_2^{2-}$ from SiO$_2$ [4]. Another reason for this change is probably the removal of organic constituents, leading to the increase in the pore size and hence the increase of the surface area of alkali-activated diatomite.

Figure 4 shows the nitrogen adsorption-desorption isotherms and pore size distribution of the diatomite samples. The diatomite exhibits a type II isotherm and an H3-type hysteresis loop, indicating the presence of macroporous structures with nonuniform size and/or shape [56]. Thus, the morphology of the diatomite consists of a variety of shapes (Figure 3). However, the pore size distribution curves of the diatomite samples demonstrate a uniform pore size with an average diameter of 4.3 nm. The textural properties of the samples are presented in Table 3. According to the Brunauer-Emmett-Teller analysis, the purified diatomite exhibits a large specific surface area of 55.4 m$^2$/g. This value is consistent with that reported by Son et al. [6] (51 m$^2$/g) for Phu Yen’s diatomite and is much higher than that published in previous works [4, 8, 11, 20, 24, 26, 32, 38, 55] (1.0-27 m$^2$/g). It can be seen from Table 3 that the specific surface area of alkali-activated diatomite (77.8 m$^2$/g) is significantly larger than that of purified diatomite. This increase in the surface area results from the removal of organic impurities during the alkali treatment.

The zero charge point of purified diatomite is 5.7 (Figure 5). This pH$_{ZPC}$ is similar to that published in the
literature [6, 11, 21, 22]. However, the pH PZC of alkali-activated diatomite (8.9) is much greater than that of purified diatomite. This increase is probably due to the formation of isolated hydroxyl groups on the surface of the material during alkali treatment.

3.2. Isothermal Studies

3.2.1. Adsorption in Single Systems

(1) Adsorption of RB onto Purified and Alkali-Activated Diatomite Samples. Figures 6 and 7 present the Freundlich and Langmuir isothermal models for the adsorption of RB dye onto the diatomite samples at 30 and 45°C. The isothermal parameters obtained from the experimental data and the respective correlation coefficients are listed in Table 4. It can be seen that the experimental points fit the models well with high correlation coefficients (0.9104-0.9955). Table 4 also shows that the maximal RB adsorption capacity of the alkali-activated diatomite sample is greater than that of the purified diatomite sample. Thus, the activation of diatomite with sodium hydroxide enhances the adsorption of the RB basic dye on diatomite. This enhancement can be attributed to a larger number of the silanol groups formed on the surface, as well as the larger specific surface area of the material.

The results presented above show that alkali-activated diatomite is superior to purified diatomite in terms of chemical and physical properties and adsorption capacity. Therefore, in the following sections, only an alkali-activated diatomite sample is used for the adsorption of dyes from aqueous solutions.

(2) Adsorption of MB onto Alkali-Activated Diatomite. The MB adsorption isotherms onto alkali-activated diatomite are presented in Figure 8 and 9, and the corresponding isothermal parameters are listed in Table 5. It can be seen that the Langmuir isotherm model fits the experimental data better than the Freundlich model with high correlation coefficients (0.9949-0.9950). Table 5 also shows that the maximal MB adsorption capacity of the alkali-activated diatomite sample is higher than that of the purified diatomite sample. Thus, the activation of diatomite with sodium hydroxide enhances the adsorption of the MB basic dye on diatomite.

<table>
<thead>
<tr>
<th>Adsorbent</th>
<th>Adsorption capacity (mg·g⁻¹)</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alkali-activated diatomite</td>
<td>143.9-142.1*</td>
<td>The present work</td>
</tr>
<tr>
<td>Purified diatomite</td>
<td>67.0-86.1**</td>
<td>The present work</td>
</tr>
<tr>
<td>Diatomite was treated with H₂SO₄ (1 molar)</td>
<td>105.1-92.2*</td>
<td>—</td>
</tr>
<tr>
<td>Diatomite was treated with sulfuric acid</td>
<td>127</td>
<td>[37]</td>
</tr>
<tr>
<td>Diatomite was treated with sodium hydroxide</td>
<td>72</td>
<td>[37]</td>
</tr>
<tr>
<td>Sodium alginate/silicone dioxide</td>
<td>126.6 (30°C)</td>
<td>[3]</td>
</tr>
<tr>
<td>Tagaran natural clay</td>
<td>27.86 (25°C)</td>
<td>[4]</td>
</tr>
<tr>
<td>Zeolite 4A</td>
<td>148.23</td>
<td>[49]</td>
</tr>
<tr>
<td>AlMCM-41</td>
<td>131.8 (20°C)</td>
<td>[16]</td>
</tr>
<tr>
<td>α-Ag₂WO₄/SBA-15</td>
<td>44.35</td>
<td>[19]</td>
</tr>
<tr>
<td>Co and N comodified mesoporous carbon composites</td>
<td>41.9 (25°C)*</td>
<td>[5]</td>
</tr>
<tr>
<td>Modified banyan aerial roots</td>
<td>66.5 (25°C)*</td>
<td>[5]</td>
</tr>
<tr>
<td>Biosorbent prepared from inactivated Aspergillus oryzae cells</td>
<td>150</td>
<td>[50]</td>
</tr>
<tr>
<td>L-Asp capped Fe₃O₄ NPs</td>
<td>141 (25°C)</td>
<td>—</td>
</tr>
<tr>
<td>Silica extracted from rice husk</td>
<td>115.23</td>
<td>—</td>
</tr>
<tr>
<td>L-Asp capped Fe₃O₄ NPs</td>
<td>49.59 (293 K)</td>
<td>—</td>
</tr>
<tr>
<td>Biosorbent prepared from inactivated Aspergillus oryzae cells</td>
<td>6.0-6.87</td>
<td>—</td>
</tr>
</tbody>
</table>

Table 8: Thermodynamic parameters for adsorption of RB onto purified diatomite in single systems.

<table>
<thead>
<tr>
<th>Temperature (°C)</th>
<th>ΔG° (kJ·mol⁻¹)</th>
<th>ΔH° (kJ·mol⁻¹)</th>
<th>ΔS° (J·mol⁻¹·K⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
<td>-31.26</td>
<td>18.90</td>
<td>165.53</td>
</tr>
<tr>
<td>45</td>
<td>-33.74</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
were also investigated and analyzed according to the linear Freundlich and Langmuir equations. Analysis results are shown in Figure 8 and Table 5. In this case, the Langmuir model is significantly more suitable to describe the adsorption data than the Freundlich model ($R^2 = 0.9874$-0.9915 as opposed to $R^2 = 0.7353$-0.8676). That is, the adsorption mainly occurs in a monolayer. The maximum adsorption capacity of MB on alkali-activated diatomite is 7.14 × 10^{-4} and 6.90 × 10^{-4} (mol·g^{-1}) at 30 and 45 °C, respectively.

### 3.2.2. Adsorption onto Alkali-Activated Diatomite in Binary Systems

Like in the single system, in the binary system, the adsorption of the dyes at 30 or 45 °C also follows the Langmuir isothermal model with the $R^2$ values approaching 1 (Figures 9 and 10). The isothermal data in Table 6 also show that the maximum adsorption capacity of alkali-activated diatomite for MB is higher than that for RB, which is similar to the single systems (Tables 4 and 5). Specifically, the ratio of the maximum adsorption capacity of the dyes in the binary system (MB/RB = 4.55 × 10^{-4}/1.40 × 10^{-4} ≈ 3.3 times at 30 °C, and MB/RB = 4.55 × 10^{-4}/1.40 × 10^{-4} ≈ 3.1 times at 45 °C) is higher than that in the single system (MB/RB = 7.14 × 10^{-4}/3.00 × 10^{-4} ≈ 2.4 times at 30 °C, and MB/RB = 6.90 × 10^{-4}/2.97 × 10^{-4} ≈ 2.3 times at 45 °C). This proves that there is competitive adsorption in the binary system, where MB molecules preferentially adsorb onto alkali-activated diatomite compared with RB molecules. This enhanced adsorption might result from the smaller size of the MB molecule. MB molecules more easily diffuse into the pores of diatomite than RB molecules, thus occupying the adsorption sites on the adsorbent surface before the RB molecules do. Similar results are also reported by Eftekhar et al. [5].

Table 7 compares the adsorption capacity of the diatomite samples for RB and MB in this study and that of other adsorbents published in the literature. It can be seen that alkali-activated diatomite has a much higher adsorption capacity than other adsorbents. Therefore, alkali-activated diatomite might serve as a promising adsorbent for the removal of dyes from aqueous solutions.

### 3.3. Thermodynamic Studies

The spontaneity of the adsorption process and the interactions on the liquid/solid interface can be explained by using thermodynamic parameters ($\Delta G^\circ$, $\Delta H^\circ$, and $\Delta S^\circ$). If $\Delta G^\circ < 0$, the adsorption process is spontaneous; otherwise, adsorption does not occur on its own. If $\Delta H^\circ < 0$, the adsorption process is exothermic and vice versa. If $\Delta S^\circ > 0$, it is possible to infer that the adsorbent affinity for the dye increases, leading to the increase in randomness of the adsorbates at the liquid/solid interface [4, 42]; in contrast, if $\Delta S^\circ < 0$, more adsorbate molecules adhere to the adsorbent surface [13, 16, 37].

The thermodynamic parameters of RB and MB adsorption onto the diatomite samples are calculated from Equations (9)–(11). The $\Delta G^\circ$ of adsorption is negative for both the single and binary systems (Tables 8 and 9), indicating...
the spontaneity of adsorption processes. The values of $\Delta H^\circ$ and $\Delta S^\circ$ differ between the adsorption processes, indicating that the adsorption process is complex. Both the physical and chemical adsorption mechanisms are possible.

3.4. Effect of Solution pH. Figure 11 shows the effect of solution pH on the adsorption of RB and MB onto alkali-activated diatomite in the single system. The pH of the solution was adjusted between 3 and 11 with a 0.1 M HCl or 0.1 M NaOH solution.

As can be seen from Figure 11(a), the adsorption efficiency of RB reaches 94% after 240 min of contact at pH 3. At higher pH, this efficiency decreases drastically, reaching 37% up to pH 5–9 and even lower (30%) at pH 11. We know that RB has a carboxylic group in its molecule, and this group renders the molecule negative, resulting in the electric repulsion between RB and the negative surface of the adsorbent at high pH. This result is consistent with that of Eftekhari et al.[5].

For MB (Figure 11(b)), the adsorption efficiency reaches 100% after a short time (60 min) of contact at pH 3–9. The efficiency only decreases to around 60% at pH 11.

The zero charge point of alkali-activated diatomite is 8.9 (Figure 5). Theoretically, the surface of the material is positively charged when pH < 8.9 and negatively charged when pH > 8.9. This means that when the pH of the dye solution increases, the adsorption efficiency should increase because the negatively charged diatomite surface attracts the dye cations. However, in both of our cases, the adsorption efficiency decreases with pH, especially at pH 11. This demonstrates that the adsorption process is complex, and the electrostatic interaction mechanism is not suitable to describe the adsorption of RB and MB onto alkali-activated diatomite.

4. Conclusions

Alkali-activated diatomite is applied to adsorb RB and MB in the single and binary systems. The treatment with sodium hydroxide increases the surface area of the diatomite from 55.4 m$^2$/g to 77.8 m$^2$/g and creates a large number of free silanol groups on the surface of the material. This increases the material’s ability to adsorb RB and MB. The adsorption equilibrium data of RB and MB onto alkali-activated diatomite fit the Langmuir model in both the single and binary systems. MB has a higher affinity to the adsorbent than RB, and the binary system is more effective than the single system. The adsorption process is spontaneous, and the removal efficiency of both MB and RB depends on pH significantly.

Data Availability

The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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