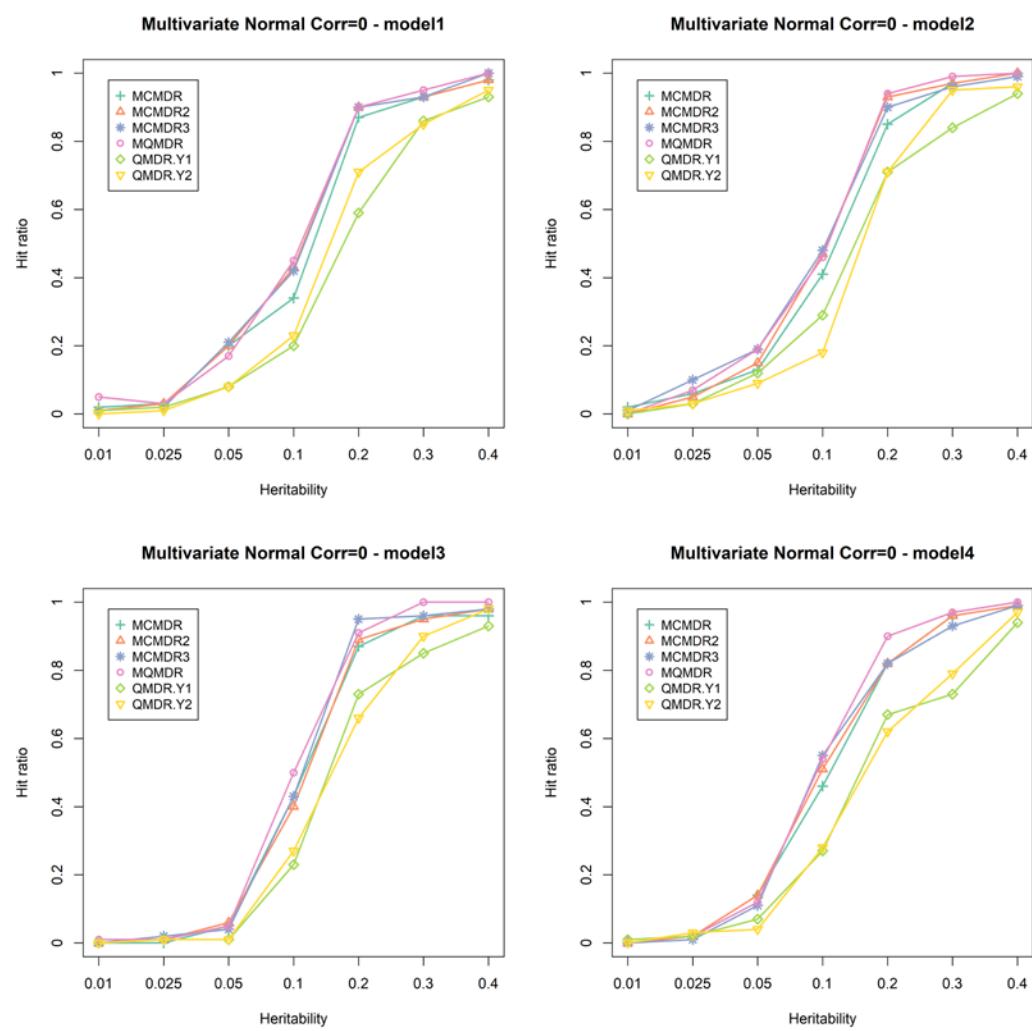
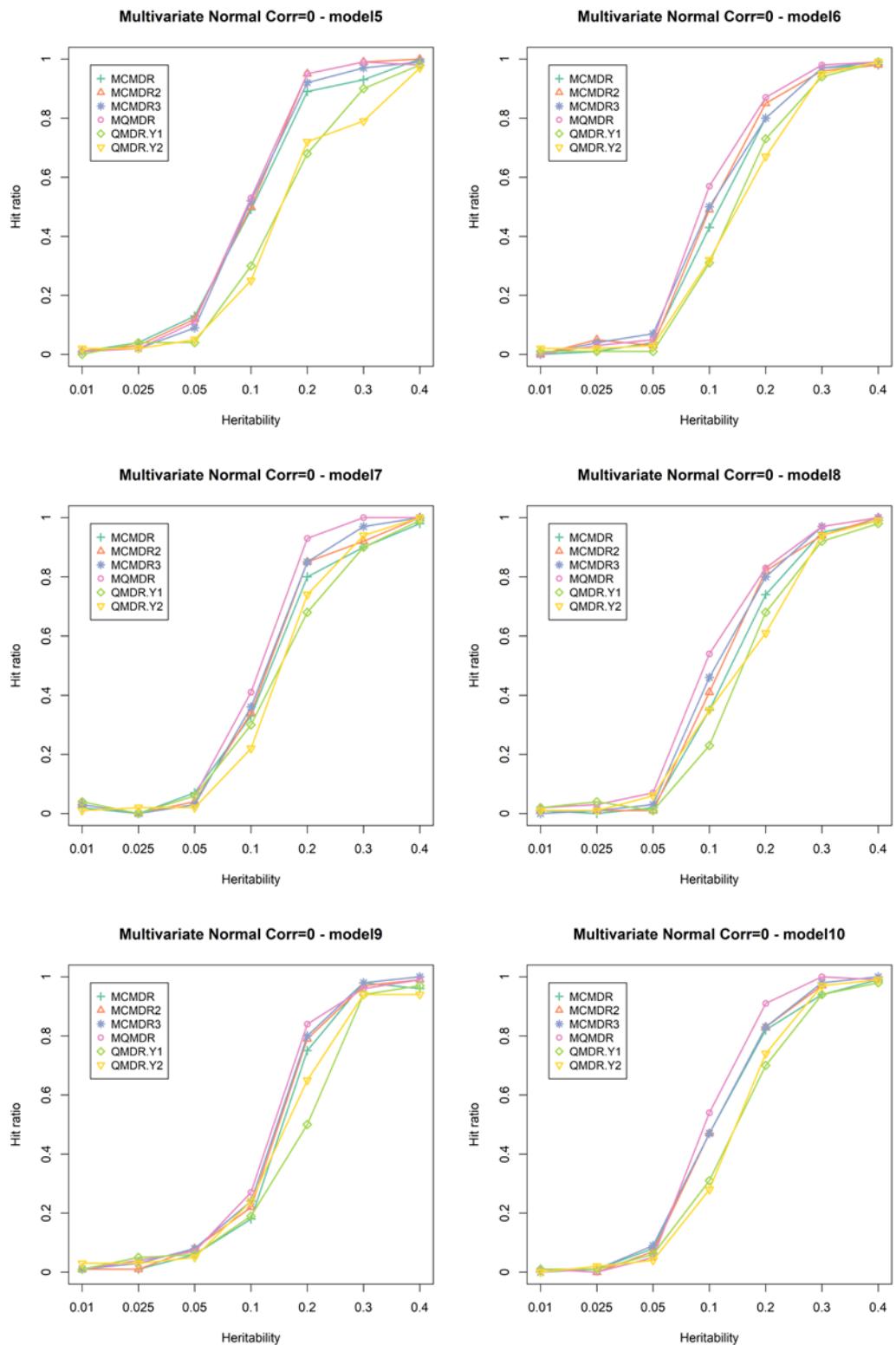


## Supplemental materials

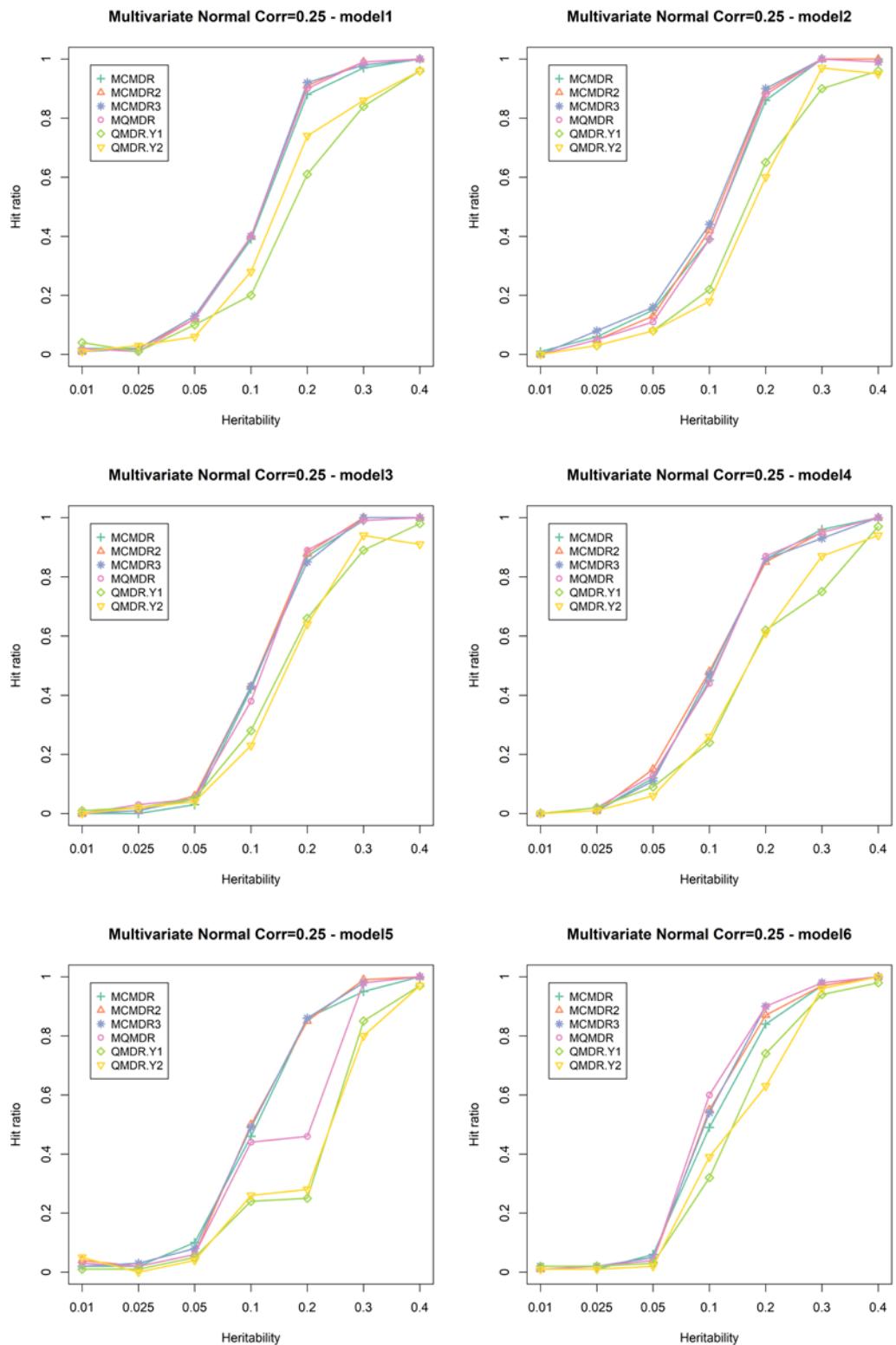
There were 10 combinations of minor allele frequencies (MAFs), and 5 models for each simulation setup. The MAF was 0.2, up to model 5. From models 6 to 10, the MAF was 0.4. We also considered correlation values of 0, 0.25, and 0.5. CMDR (multi-CMDR), MCMDR2 (multi-CMDR without trimming), MCMDR3 (multi-CMDR without membership score), MQMDR (multi-QMDR), QMDR.Y1 (QMDR with  $Y_1$ ), and QMDR.Y2 (QMDR with  $Y_2$ )

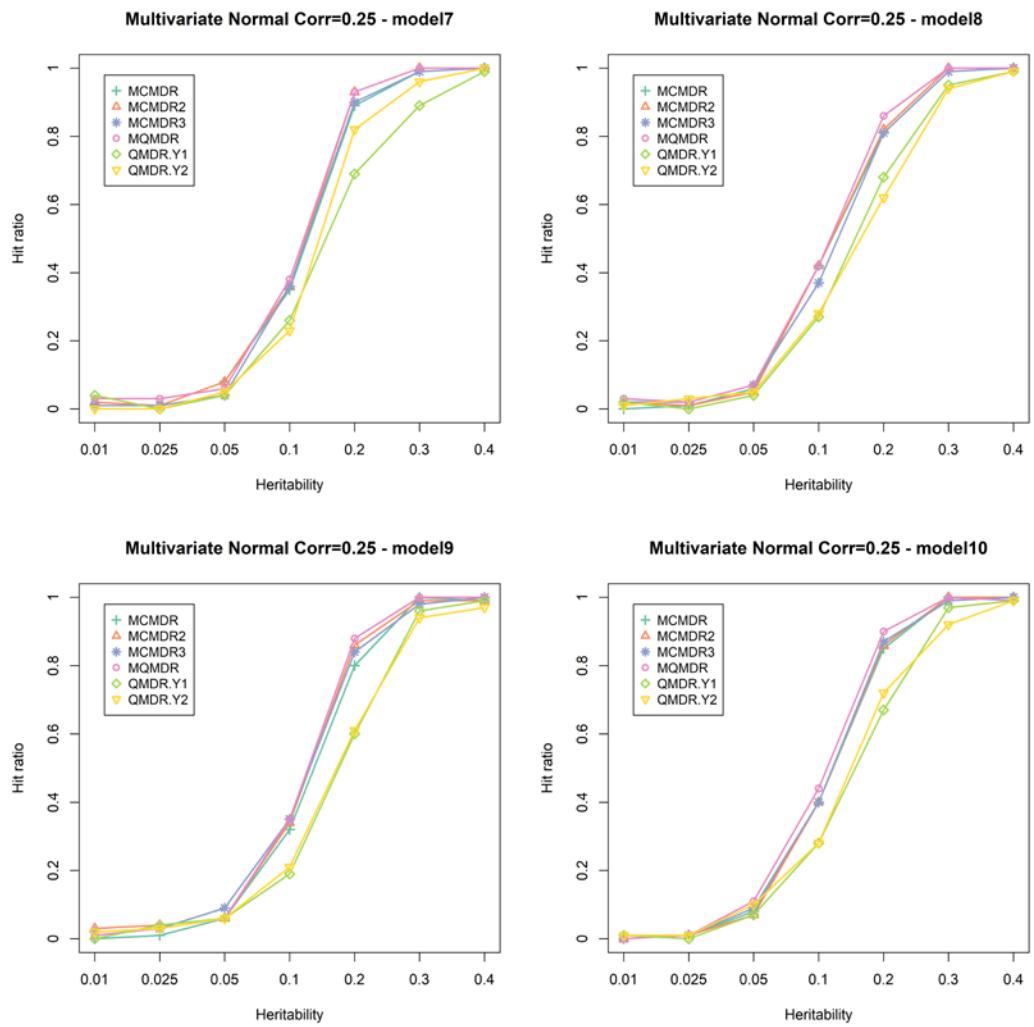
### Multivariate Normal Distributions



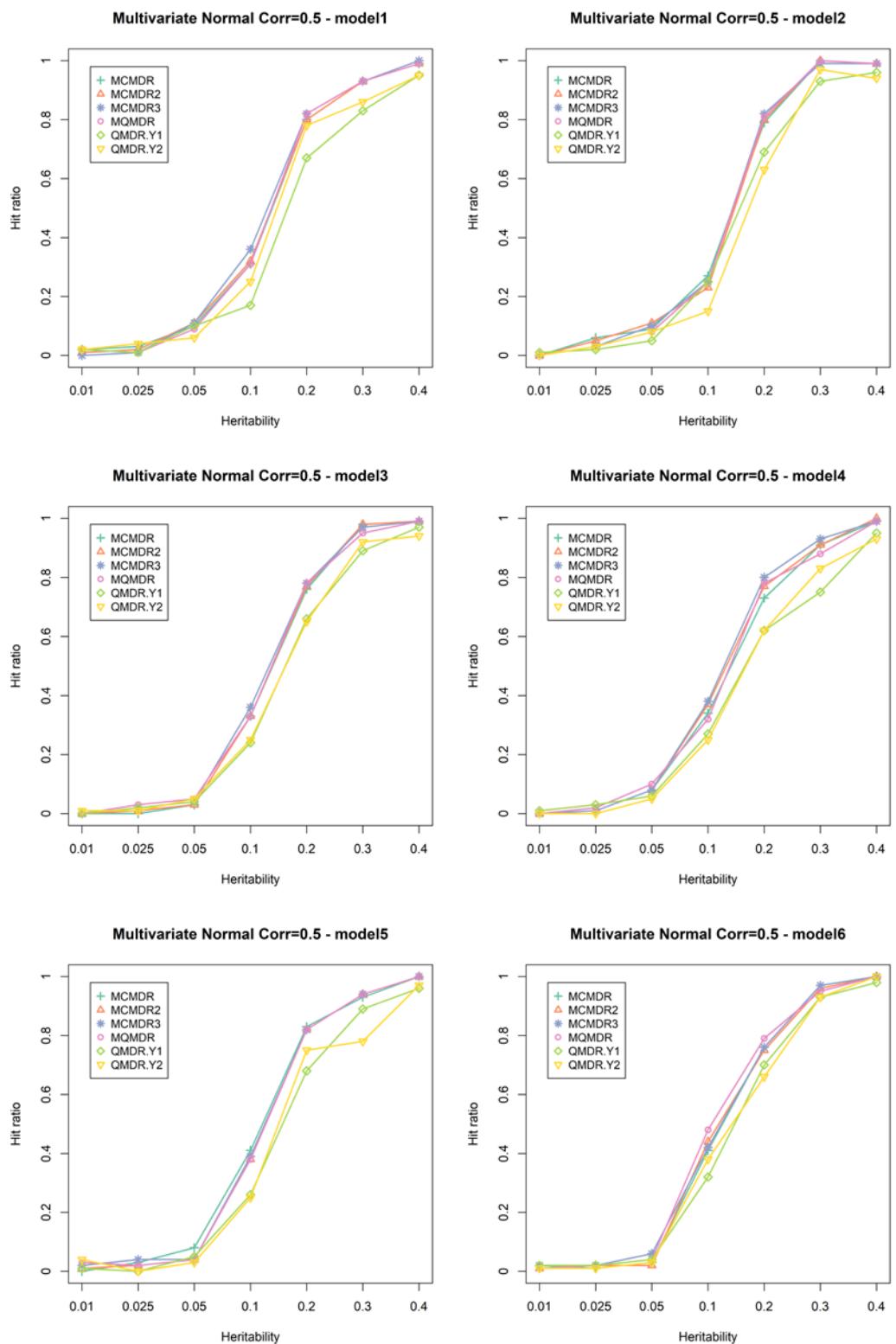


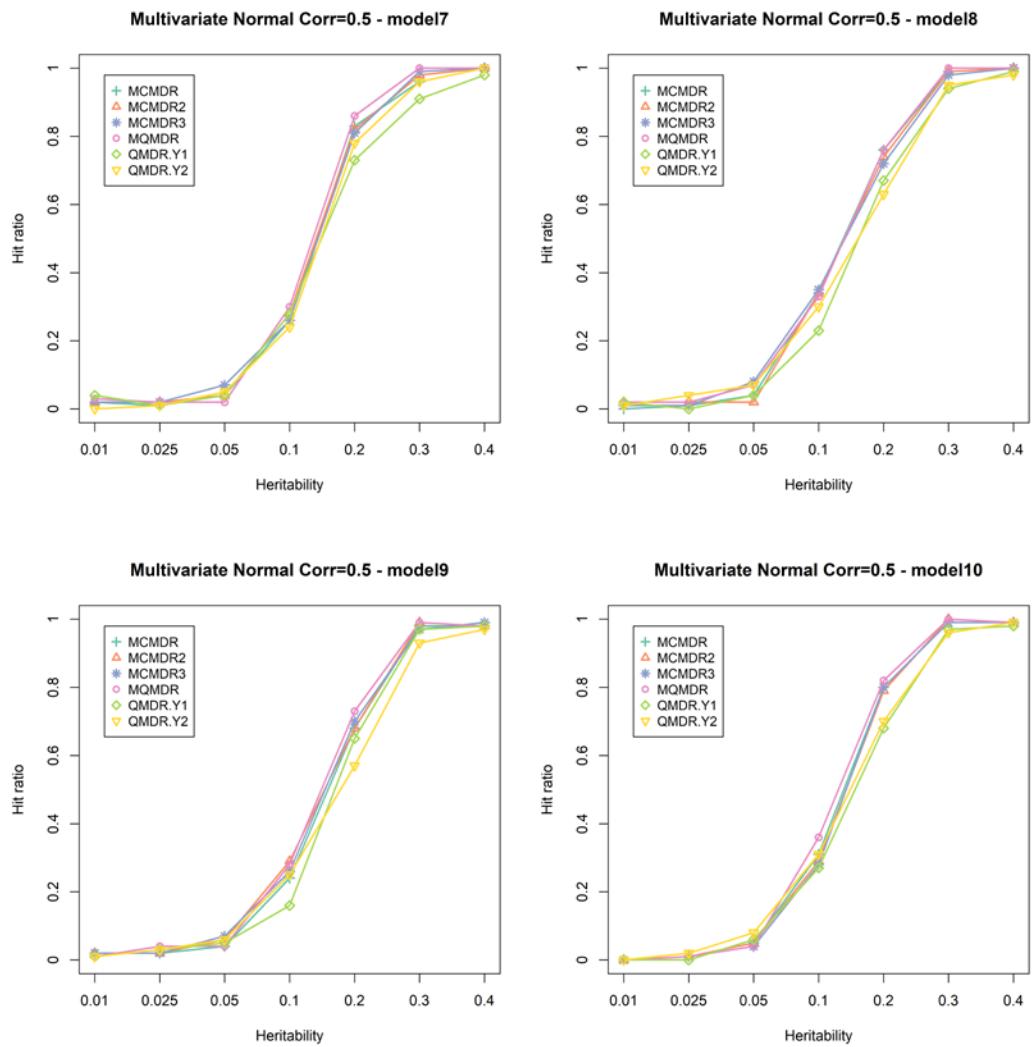
**Supplemental Figure 1.** Hit-ratios for multivariate normal distributions with zero correlation, for 10 models.





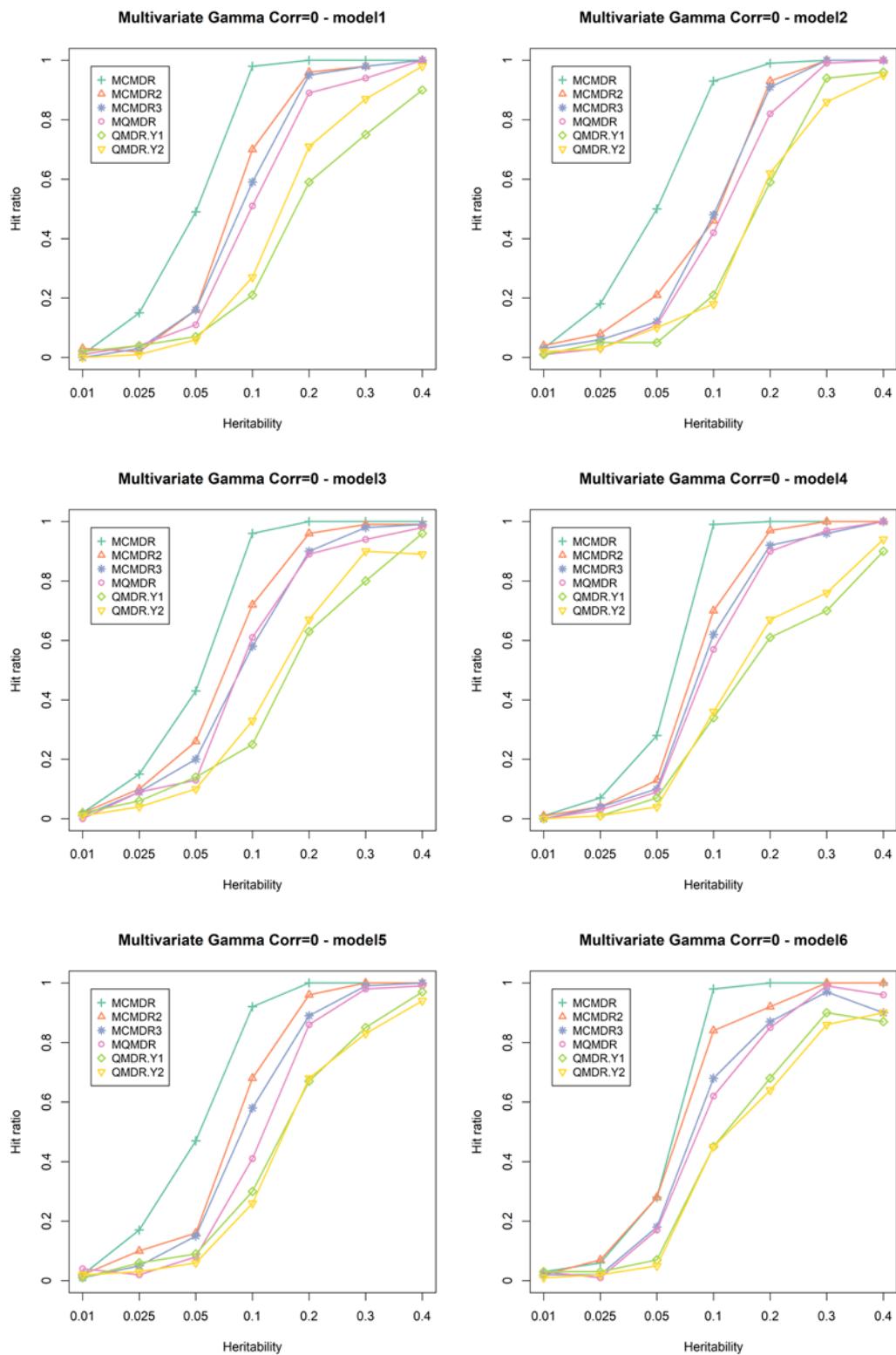
**Supplemental Figure 2.** Hit-ratios for multivariate normal distributions with correlation 0.25, for 10 models.

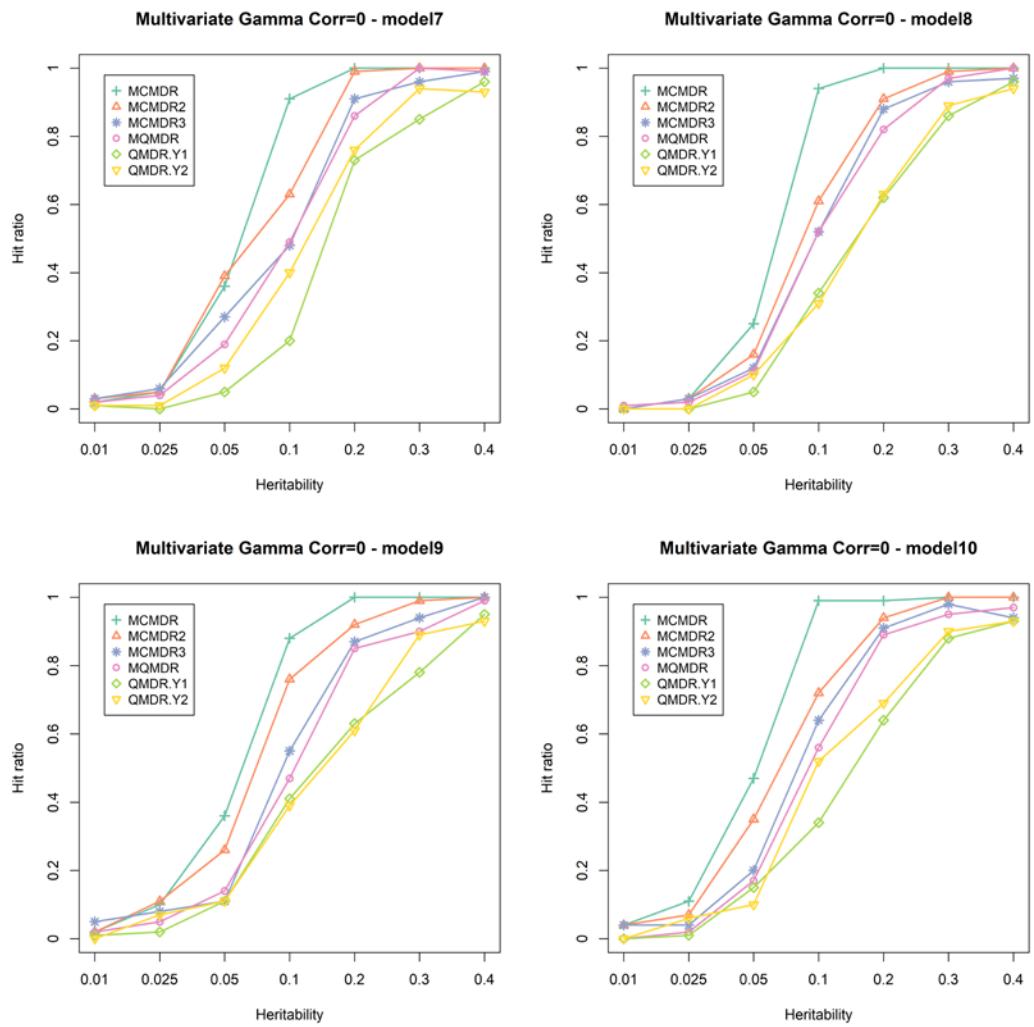




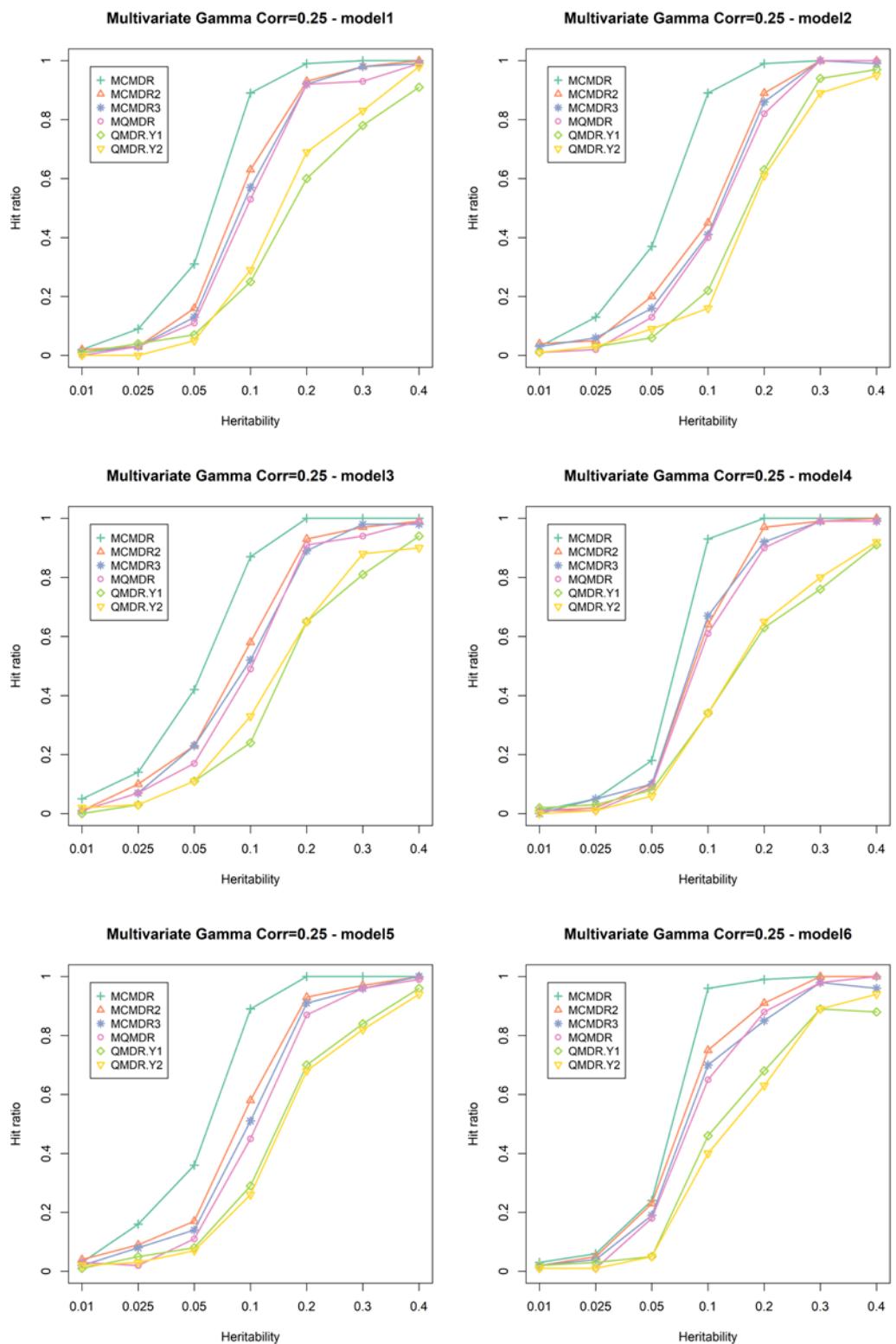
**Supplemental Figure 3.** Hit-ratios for multivariate normal distribution with correlation 0.5 for 10 models

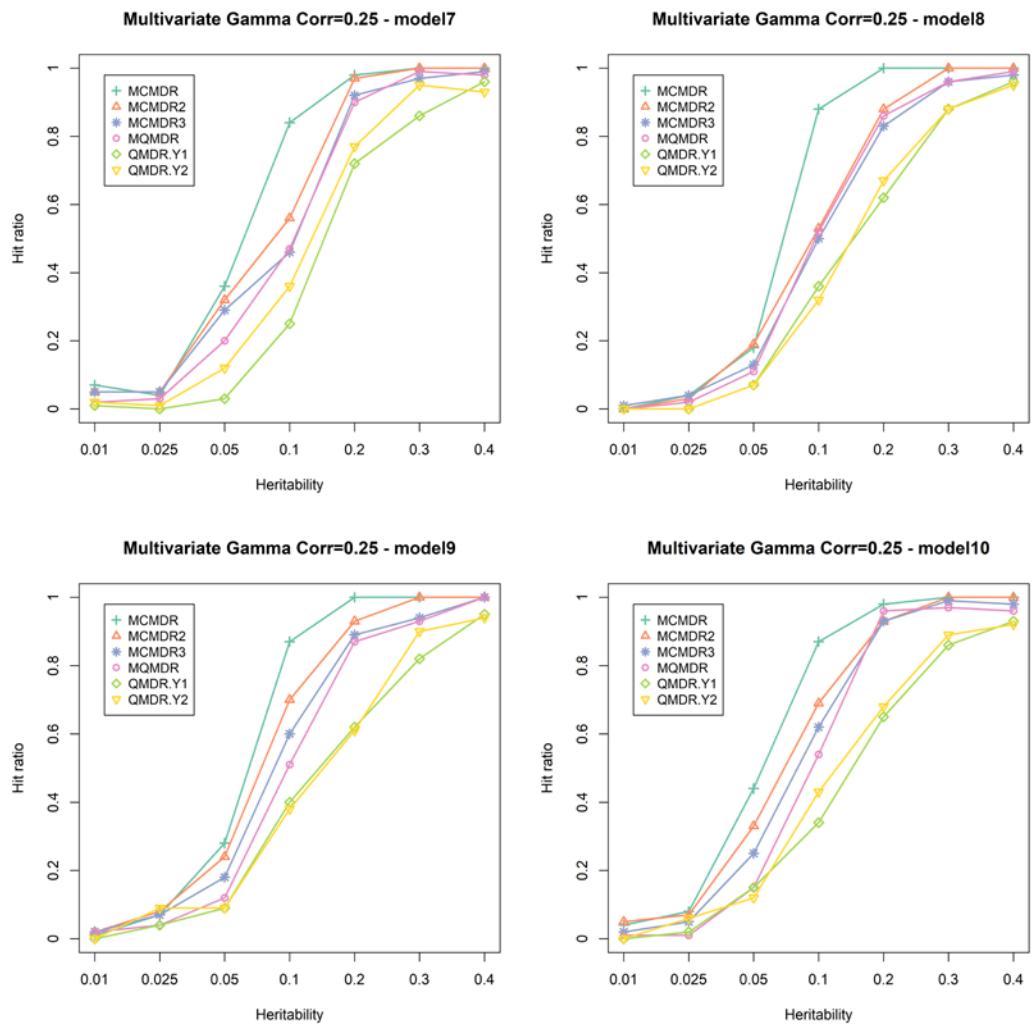
# Multivariate Gamma Distribution



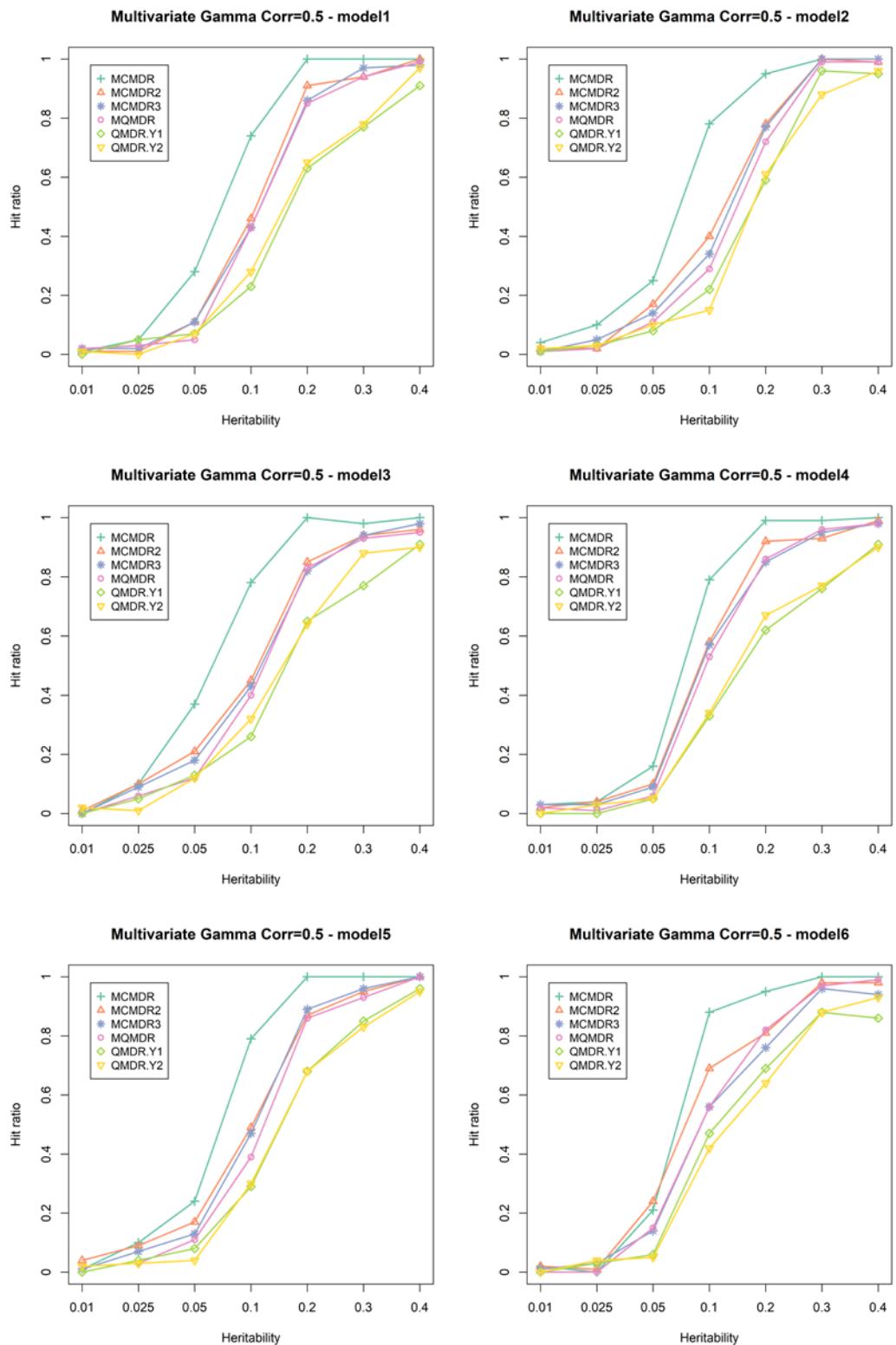


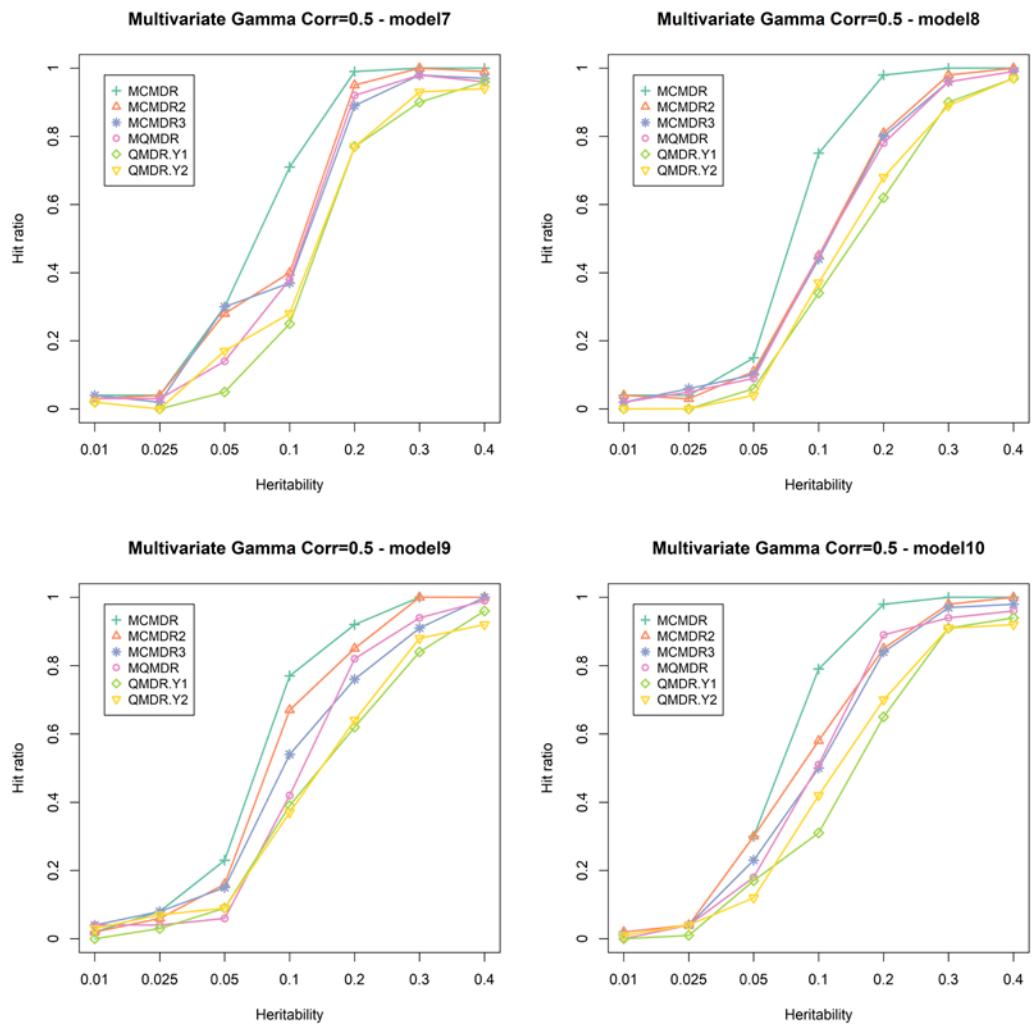
**Supplemental Figure 4.** Hit-ratios for multivariate gamma distributions, with zero correlation, for 10 models.





**Supplemental Figure 5.** Hit-ratios for multivariate gamma distributions, with correlation 0.25, for 10 models.





**Supplemental Figure 6.** Hit-ratios for multivariate gamma distributions, with correlation 0.5, for 10 models.

## Multivariate normal distribution

|                  | <b>MCMDR1</b> | <b>MCMDR2</b> | <b>MCMDR3</b> | <b>MQMDR</b> | <b>QMDR.Y1</b> | <b>QMDR.Y2</b> |
|------------------|---------------|---------------|---------------|--------------|----------------|----------------|
| <b>HET:0.01</b>  | 0.005         | 0.003         | 0.007         | 0.004        | 0.005          | 0.005          |
| <b>HET:0.025</b> | 0.005         | 0.007         | 0.006         | 0.005        | 0.007          | 0.004          |
| <b>HET:0.05</b>  | 0.005         | 0.007         | 0.006         | 0.008        | 0.01           | 0.012          |
| <b>HET:0.1</b>   | 0.004         | 0.002         | 0.002         | 0.004        | 0.005          | 0.005          |
| <b>HET:0.2</b>   | 0.005         | 0.004         | 0.005         | 0.006        | 0.004          | 0.011          |
| <b>HET:0.3</b>   | 0.009         | 0.005         | 0.005         | 0.007        | 0.003          | 0.007          |
| <b>HET:0.4</b>   | 0.005         | 0.008         | 0.003         | 0.005        | 0.008          | 0.006          |

**Supplemental Table 1.** Empirical false positive rate for multivariate normal distributions with zero correlation

|                  | <b>MCMDR1</b> | <b>MCMDR2</b> | <b>MCMDR3</b> | <b>MQMDR</b> | <b>QMDR.Y1</b> | <b>QMDR.Y2</b> |
|------------------|---------------|---------------|---------------|--------------|----------------|----------------|
| <b>HET:0.01</b>  | 0.006         | 0.001         | 0.004         | 0.006        | 0.003          | 0.006          |
| <b>HET:0.025</b> | 0.003         | 0.002         | 0.008         | 0.004        | 0.007          | 0.006          |
| <b>HET:0.05</b>  | 0.008         | 0.011         | 0.012         | 0.006        | 0.008          | 0.009          |
| <b>HET:0.1</b>   | 0.005         | 0.007         | 0.007         | 0.003        | 0.003          | 0.008          |
| <b>HET:0.2</b>   | 0.005         | 0.004         | 0.004         | 0.008        | 0.005          | 0.005          |
| <b>HET:0.3</b>   | 0.006         | 0.008         | 0.006         | 0.006        | 0.003          | 0.005          |
| <b>HET:0.4</b>   | 0.004         | 0.005         | 0.01          | 0.006        | 0.005          | 0.005          |

**Supplemental Table 2.** Empirical false positive rate for multivariate normal distributions with correlation 0.25

|                  | <b>MCMDR1</b> | <b>MCMDR2</b> | <b>MCMDR3</b> | <b>MQMDR</b> | <b>QMDR.Y1</b> | <b>QMDR.Y2</b> |
|------------------|---------------|---------------|---------------|--------------|----------------|----------------|
| <b>HET:0.01</b>  | 0.006         | 0.003         | 0.003         | 0.002        | 0.003          | 0.003          |
| <b>HET:0.025</b> | 0.003         | 0.001         | 0.006         | 0.003        | 0.007          | 0.004          |
| <b>HET:0.05</b>  | 0.01          | 0.01          | 0.012         | 0.009        | 0.006          | 0.005          |
| <b>HET:0.1</b>   | 0.003         | 0.004         | 0.003         | 0.003        | 0.004          | 0.005          |
| <b>HET:0.2</b>   | 0.006         | 0.003         | 0.006         | 0.008        | 0.006          | 0.006          |
| <b>HET:0.3</b>   | 0.007         | 0.008         | 0.006         | 0.007        | 0.006          | 0.005          |
| <b>HET:0.4</b>   | 0.005         | 0.004         | 0.005         | 0.006        | 0.004          | 0.002          |

**Supplemental Table 3.** Empirical false positive rate for multivariate normal distributions with correlation 0.5

## Multivariate gamma distribution

|                  | <b>MCMDR1</b> | <b>MCMDR2</b> | <b>MCMDR3</b> | <b>MQMDR</b> | <b>QMDR.Y1</b> | <b>QMDR.Y2</b> |
|------------------|---------------|---------------|---------------|--------------|----------------|----------------|
| <b>HET:0.01</b>  | 0.007         | 0.003         | 0.008         | 0.003        | 0.005          | 0.001          |
| <b>HET:0.025</b> | 0.004         | 0.005         | 0.003         | 0.005        | 0.008          | 0.003          |
| <b>HET:0.05</b>  | 0.008         | 0.007         | 0.005         | 0.008        | 0.006          | 0.008          |
| <b>HET:0.1</b>   | 0.004         | 0.005         | 0.003         | 0.007        | 0.009          | 0.002          |
| <b>HET:0.2</b>   | 0.006         | 0.006         | 0.003         | 0.004        | 0.008          | 0.003          |
| <b>HET:0.3</b>   | 0.002         | 0.001         | 0.001         | 0.002        | 0.001          | 0.001          |
| <b>HET:0.4</b>   | 0.002         | 0.003         | 0.003         | 0.004        | 0.005          | 0.009          |

**Supplemental Table 4.** Empirical false positive rate for multivariate gamma distributions with zero correlation

|                  | <b>MCMDR1</b> | <b>MCMDR2</b> | <b>MCMDR3</b> | <b>MQMDR</b> | <b>QMDR.Y1</b> | <b>QMDR.Y2</b> |
|------------------|---------------|---------------|---------------|--------------|----------------|----------------|
| <b>HET:0.01</b>  | 0.005         | 0.004         | 0.003         | 0.006        | 0.005          | 0.002          |
| <b>HET:0.025</b> | 0.002         | 0.005         | 0.002         | 0.003        | 0.009          | 0.002          |
| <b>HET:0.05</b>  | 0.004         | 0.007         | 0.008         | 0.007        | 0.007          | 0.004          |
| <b>HET:0.1</b>   | 0.006         | 0.002         | 0.002         | 0.008        | 0.007          | 0.006          |
| <b>HET:0.2</b>   | 0.004         | 0.006         | 0.003         | 0.003        | 0.01           | 0.002          |
| <b>HET:0.3</b>   | 0.001         | 0.001         | 0.005         | 0.002        | 0.002          | 0              |
| <b>HET:0.4</b>   | 0.002         | 0.003         | 0.008         | 0.004        | 0.006          | 0.006          |

**Supplemental Table 5.** Empirical false positive rate for multivariate gamma distributions with correlation 0.25

|                  | <b>MCMDR1</b> | <b>MCMDR2</b> | <b>MCMDR3</b> | <b>MQMDR</b> | <b>QMDR.Y1</b> | <b>QMDR.Y2</b> |
|------------------|---------------|---------------|---------------|--------------|----------------|----------------|
| <b>HET:0.01</b>  | 0.004         | 0.003         | 0.003         | 0.005        | 0.001          | 0.007          |
| <b>HET:0.025</b> | 0.005         | 0.008         | 0.009         | 0.01         | 0.006          | 0.005          |
| <b>HET:0.05</b>  | 0.004         | 0.004         | 0.007         | 0.004        | 0.007          | 0.004          |
| <b>HET:0.1</b>   | 0.009         | 0.006         | 0.004         | 0.006        | 0.006          | 0.005          |
| <b>HET:0.2</b>   | 0.005         | 0.005         | 0.003         | 0.004        | 0.01           | 0.004          |
| <b>HET:0.3</b>   | 0.001         | 0.002         | 0.005         | 0.001        | 0.005          | 0.002          |
| <b>HET:0.4</b>   | 0.001         | 0.004         | 0.003         | 0.004        | 0.005          | 0.002          |

**Supplemental Table 6.** Empirical false positive rate for multivariate gamma distributions with correlation 0.5