

Modeling Recruitment Maneuvers with a Variable Compliance Model for Pressure Controlled Ventilation

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A nonlinear mathematical model for pressure controlled, variable compliance ventilation is proposed, solved, and analyzed. The effect of the variable compliance on the key outcome variables, tidal volume, average lung volume, total PEEP, and mean alveolar pressure, is presented. Using human data, the variable compliance model is used to investigate effects of recruitment maneuvers on the key outcome variables.

Keywords: Pressure controlled ventilation; Variable compliance; Recruitment; Nonlinear model

NOMENCLATURE

$V_i(t)$	Inspiratory lung volume, $0 \leq t \leq t_i$	R_i	Inspiratory resistance
$V_e(t)$	Expiratory lung volume, $t_i \leq t \leq t_{\text{tot}}$	R_e	Expiratory resistance
V_T	Tidal volume	C_{ave}	Average compliance over one breath
V_{ave}	Average lung volume over one breath	$C_i(V)$	Compliance function during inspiration
P_{ex}	End-expiratory pressure	$C_e(V)$	Compliance function during expiration
V_{ex}	End-expiratory volume	a_{ij}	$j = 1, 2, 3$. Compliance parameters during inspiration
P_m	Mean alveolar pressure	b_{ij}	$j = 1, 3$. Compliance parameters during inspiration
t_i	Inspiratory time	a_{ej}	$j = 1, 2, 3$. Compliance parameters during expiration
t_e	Expiratory time	b_{ej}	$j = 1, 3$. Compliance parameters during expiration
t_{tot}	Length of one breath	V_{ij}^s	$j = 1, 2$. Volumes at which compliance function changes form during inspiration
t_{ij}	$j = 1, 2$. Times of compliance changes during inspiration	V_{ej}^s	$j = 1, 2$. Volumes at which compliance function changes form during expiration
t_{ej}	$j = 1, 2$. Times of compliance changes during expiration		
f	Number of breaths per minute		
D	Inspiratory time fraction		
P_{peep}	Applied PEEP during expiration		
P_{set}	Applied ventilator pressure		

INTRODUCTION

Numerous mathematical models for the mechanical ventilation of patients with acute respiratory failure have previously been presented in the medical and scientific

literature (Wald *et al.*, 1968; Barbini, 1982; Marini *et al.*, 1989; Burke *et al.*, 1993; Chandra *et al.*, 1993; Crooke and Marini, 1993; Marini and Crooke, 1993; Hotchkiss *et al.*, 1994; 1996; Morgenstern and Kaiser, 1995; Crooke *et al.*, 1996). The mathematical models range from

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one-, two-, or multi-compartment models, permit different resistances for inspiration and expiration, incorporate PEEP, and cover the basic clinical modes of ventilation. However, all of these models have assumed that the compartment (lung) compliance is constant during inspiration and expiration, often with the same compliance. The need of new models for volume dependent compliance as a diagnostic technique in ARDS patient has been advocated in Mols *et al.* (1999). In this paper, we propose a mathematical model for one-compartment, pressure preset ventilation that incorporates a variable compliance.

Despite its conceptual simplicity and great success in predicting *gross* behaviors of the pulmonary system in response to imposed pressures or flows, a unicompartamental, linear model of the respiratory system is clearly an oversimplification. Recent data, including that of Jonson and Svantesson (1999), has identified regions of differing compliance characteristics, with *lower* and *upper* inflection points, above and below which the compliance behavior of the lung differs. The work of Gattioni *et al.* (1995) suggests that *recruitment* of dependent and collapsed airspaces is in large part responsible for the phenomenon of the lower inflection point (LIP). Solway *et al.* (see for e.g. Yap *et al.*, 1994) have highlighted the potential role of small airway collapse in restricting gas access to particular alveoli. Airspace overdistension is felt likely the underlying cause of the upper inflection point (UIP). Recent data (see for e.g. Hickling, 1998; 2001) demonstrates that regional overdistension may occur at volumes lower than the upper inflection point that is identified from pressure–volume curves obtained at the airway opening. Laboratory studies of Mols (Mols *et al.*, 2001) have shown that the volume-dependent alterations of the lung compliance during mechanical ventilation with associated PEEP levels to maintain alveolar recruitment have a marked impact on pulmonary gas exchange. However, in some cases, a simple recruitment maneuver may not lead to better oxygenation (Fujino *et al.*, 2001). In a recent paper (Villagra *et al.*, 2002), recruitment maneuvers in 17 patients with acute respiratory distress syndrome (ARDS) were studied. These researchers concluded that recruitment maneuvers for ARDS patient have no short-term benefit on oxygenation and may even lead to regional alveolar over distension which in turn may result in the redistribution of blood flow in the lung. Hence, the evidence on the benefits of recruitment maneuvers is mixed. This raises the question: Is there a way for the clinician to know when it is suitable and when it is not? In this paper, we hope to provide a starting point for an answer to this question by providing a mathematical model that is capable of providing a mechanical description of what happens pre- and post-recruitment maneuver. This will not immediately link the oxygenation with the maneuvers, but it may serve as a mechanical proxy for this important clinical variable.

Nonlinear elastic pressure versus volume curves have been studied extensively in recent years (Silva *et al.*, 1992; Servillo *et al.*, 1997; Nikischin *et al.*, 1998; Svantesson *et al.*, 1998; Venegas *et al.*, 1998; Jonson and Svantesson, 1999; Jonson *et al.*, 1999). If one assumes that the elastic pressure of the lungs, P_{elastic} , is proportional to the lung volume, V , then $P_{\text{elastic}} = kV$. If we take k to be a constant, then $1/k$ is called the lung compliance, C . A plot of the elastic pressure versus the volume produces a straight line in the $P_{\text{elastic}}-V$ plane and hence, it yields a *linear* relationship between these two quantities. However, if we assume that k and hence C , depends on V , then a plot of elastic pressure versus volume produces a *nonlinear* relationship. The $P_{\text{elastic}}-V$ curves produced by the nonlinear models are sigmoidal in shape. Often the case, the nonlinear relationship between elastic pressure and volume differs between inspiration and expiration (see for e.g. Suki *et al.*, 1998; Jonson and Svantesson, 1999). The explanation for the sigmoidal shape is that during low lung volumes, the compliance is low, but increasing, due to opening of collapsed lung units. At a particular volume (which in this paper is denoted by V_{i1}^s or in the medical literature by V_{LIP}), a transition region is entered where the compliance is constant. A third stage is entered at a higher volume (V_{i2}^s or V_{UIP}) where the compliance is actually decreasing. The sequence of events is reversed during expiration. The shape of the $P_{\text{elastic}}-V$ curves is affected by disease (see e.g. Jonson and Svantesson, 1999) and can be shifted by recruitment maneuvers (Hickling, 1998; Svantesson *et al.*, 1998). To reduce ventilator-induced lung damage, it is often recommended that the ventilation be within the second segment (flat section) of the compliance function. As we will see in the human data presented, recruitment maneuvers can result in a shift in the compliance function (V_{i1}^s and V_{i2}^s becomes smaller) and can produce lower tidal volumes, lower average lung volumes, higher end-expiratory pressures, and lower mean alveolar pressures for a given setting of airway pressures (P_{set} and P_{peep}) that are applied by the ventilator during inspiration and expiration.

THE BASIC ONE-SEGMENT MODEL

The mathematical model for pressure controlled ventilation (PCV) incorporates a pressure that is applied to a single compartment (lung) with a compliance function C , inspiratory resistance R_i , and expiratory resistance R_e . The ventilator cycle is split into two parts: inspiration of duration t_i and expiration of duration t_e . The total length of each cycle is $t_{\text{tot}} = t_i + t_e$. During inspiration, a preset pressure, denoted by P_{set} , is applied to the airway and during expiration, the ventilator applies a constant pressure, denoted by P_{peep} , which may be zero. We assume that each new breath is identical to the previous breath. For the flow into and out of the lung we assume that it is equal to the instantaneous rate of change of the volume of the lung.

In this model, the symbol, $V(t)$, represents the volume above the volume of the lung at the end of the previous breath. Hence, $V(t)$ is referenced to a constant volume V_{ex} which is explained below. Assuming breaths of uniform length (t_{tot}), this means that V is zero at the beginning and ending of each breath. We consider the pressure balances in the system:

$$P_{resistive} + P_{elastic} + P_{ex} = P_{vent}. \quad (2.1)$$

The term P_{ex} is called the end-expiratory pressure and represents the pressure that remains in the lung after the completion of each breath. The volume of the lung above its rest volume at the end of each breath is denoted by V_{ex} and is related to P_{ex} through the equation $P_{ex} = V_{ex}/C(V_{ex})$. During inspiration, $P_{vent} = P_{set}$ and during expiration $P_{vent} = P_{peep}$. For the elastic pressures, we assume that $P_{elastic} = V(t)/C(V + V_{ex})$. Lastly, it is assumed that the resistive pressure is proportional to the flows in and out of the lung: $P_{resistive} = RV$. The volume in the lung (above V_{ex}) is then given by the ordinary differential equations:

Inspiration

$$R_i \left(\frac{dV_i}{dt} \right) + \frac{V_i}{C_i(V_i + V_{ex})} + P_{ex} = P_{set}, \quad (2.2)$$

$$0 \leq t \leq t_i$$

Expiration

$$R_e \left(\frac{dV_e}{dt} \right) + \frac{V_e}{C_e(V_e + V_{ex})} + P_{ex} = P_{peep}, \quad (2.3)$$

$$t_i \leq t \leq t_{tot}.$$

It is assumed that the $V_i(0) = 0$ and $V_e(t_i) = V_i(t_i) = V_T$ (the *tidal volume*) and serve as initial conditions for Eqs. (2.2) and (2.3), respectively. The unknown end-expiratory pressure P_{ex} and end-expiratory volume V_{ex} are determined by the equation $V_e(t_{tot}) = 0$. The initial-value problems for inspiratory and expiratory phases can be solved exactly. For example, one finds for the inspiratory volume:

$$V_i(t) = \frac{a_i + b_i V_{ex}}{b_i(1 + b_i(P_{set} - P_{ex}))} \left[b_i(P_{set} - P_{ex}) - \Phi \left(-b_i(P_{set} - P_{ex}) e^{-b_i(P_{set} - P_{ex}) - \frac{(b_i(P_{set} - P_{ex}) - 1)^2 t}{(a_i + b_i V_{ex}) R_i}} \right) \right]$$

where the parameters a_i and b_i define the compliance functions: $C_i(V_i + V_{ex}) = a_i + b_i(V_i + V_{ex})$. Here Φ is the *productlog* function i.e. $\Phi(z)$ is a branch of the solutions of $z = ue^u$. A similar expression can be computed for $V_e(t)$ which depends on the compliance function $C_e(V_e + V_{ex}) = a_e + b_e(V_e + V_{ex})$. The end-expiratory pressure is determined by solving the equation $V_e(t_{tot}) = 0$ for P_{ex} and V_{ex} , using the fact that

$P_{ex} = V_{ex}/C_e(V_{ex})$. Due to the transcendental nature of this equation, this equation must be solved numerically. Having the solution for the one-segment model, we extend it to a model where the inspiratory and expiratory parts of the breathing cycle are broken down into three segments upon which the compliance functions are of the above form.

THE THREE-SEGMENT MODEL

Svantesson *et al.* (1998) calculated the elastic pressure–volume ($P_{elastic} - V$) curves of 15 healthy anesthetized adults in a study of lung recruitment as a means of improving ventilator management. Using specific and averaged values for the 15 subjects, they constructed the $P_{elastic} - V$ curves and found that the compliance of the lungs during inflation transverses three zones: increasing compliance, constant compliance, and decreasing compliance. During inflation from low lung volumes, the compliance increases linearly with volume up to a particular lung volume, which we denote by $V_{i_1}^s$, at which point the compliance remains constant up to a second particular volume, $V_{i_2}^s > V_{i_1}^s$, at which point the compliance decreases linearly. Depending on the applied pressures, P_{set} and P_{peep} , the inflation cycle may encompass one, two, or all three of these segments. This type of compliance function is pictured in Fig. 1. This piecewise linear compliance function for inspiration can be represented mathematically as

$$C_i(V_i) = \begin{cases} a_{i_1} + b_{i_1} V_i & \text{if } 0 \leq V_i \leq V_{i_1}^s \\ a_{i_2} & \text{if } V_{i_1}^s \leq V_i \leq V_{i_2}^s \\ a_{i_3} + b_{i_3} V_i & \text{if } V_{i_2}^s \leq V_i \leq V_T. \end{cases} \quad (3.1)$$

The $P_{elastic} - V$ curve for this type of compliance function is pictured in Fig. 2. Similar types of figures can be drawn for the expiratory compliance function $C_e(V)$:

$$C_e(V_e) = \begin{cases} a_{e_3} + b_{e_3} V_e & \text{if } 0 \leq V_e \leq V_{e_2}^s \\ a_{e_2} & \text{if } V_{e_2}^s \leq V_e \leq V_{e_1}^s \\ a_{e_1} + b_{e_1} V_e & \text{if } V_{e_1}^s \leq V_e \leq V_T. \end{cases} \quad (3.2)$$

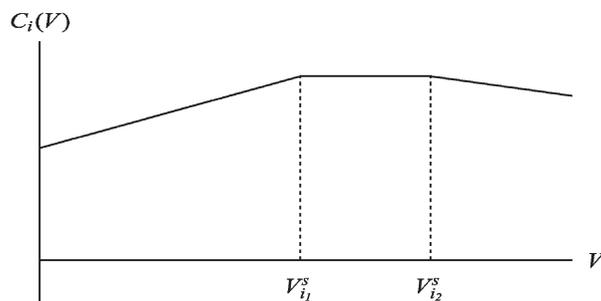


FIGURE 1 Three-segment compliance model: lung inspiratory compliance versus lung volume.

The basic one-segment model (Eqs. (2.2) and (2.3)) can now be generalized to the three-segment model by assuming that during inspiration and expiration, the compliance functions, $C_i(V)$ and $C_e(V)$ are changing according to Eqs. (3.1) and (3.2). In particular, we assume that the lung volumes satisfy the following system of differential equations:

Inspiration

$$R_i \left(\frac{dV_{i_1}}{dt} \right) + \frac{V_{i_1}}{a_{i_1} + b_{i_1}(V_{i_1} + V_{\text{ex}})} + P_{\text{ex}} = P_{\text{set}}, \quad (3.3)$$

$$0 \leq t \leq t_{i_1}$$

$$R_i \left(\frac{dV_{i_2}}{dt} \right) + \frac{V_{i_2}}{a_{i_2}} + P_{\text{ex}} = P_{\text{set}}, \quad t_{i_1} \leq t \leq t_{i_2} \quad (3.4)$$

$$R_i \left(\frac{dV_{i_3}}{dt} \right) + \frac{V_{i_3}}{a_{i_3} + b_{i_3}(V_{i_3} + V_{\text{ex}})} + P_{\text{ex}} = P_{\text{set}}, \quad (3.5)$$

$$t_{i_2} \leq t \leq t_i$$

Expiration

$$R_e \left(\frac{dV_{e_1}}{dt} \right) + \frac{V_{e_1}}{a_{e_1} + b_{e_1}(V_{e_1} + V_{\text{ex}})} + P_{\text{ex}} = P_{\text{peep}}, \quad (3.6)$$

$$t_i \leq t \leq t_{e_1}$$

$$R_e \left(\frac{dV_{e_2}}{dt} \right) + \frac{V_{e_2}}{a_{e_2}} + P_{\text{ex}} = P_{\text{peep}}, \quad t_{e_1} \leq t \leq t_{e_2} \quad (3.7)$$

$$R_e \left(\frac{dV_{e_3}}{dt} \right) + \frac{V_{e_3}}{a_{e_3} + b_{e_3}(V_{e_3} + V_{\text{ex}})} + P_{\text{ex}} = P_{\text{peep}}, \quad (3.8)$$

$$t_{e_2} \leq t \leq t_{\text{tot}}.$$

In Eqs. (3.5)–(3.8), we require that the solutions satisfy the continuity conditions: $V_{i_1}(t_{i_1}) = V_{i_2}(t_{i_1})$, $V_{i_2}(t_{i_2}) = V_{i_3}(t_{i_2})$, $V_{i_3}(t_i) = V_{e_1}(t_i)$, $V_{e_1}(t_{e_1}) = V_{e_2}(t_{e_1})$, and $V_{e_2}(t_{e_2}) = V_{e_3}(t_{e_2})$. We also have the initial and boundary conditions: $V_{i_1}(0) = 0$, $V_{i_3}(t_i) = V_T$, and $V_{e_3}(t_{\text{tot}}) = 0$. These continuity conditions require the following restrictions be placed on the parameters of the compliance functions:

$$a_{i_2} = a_{i_1} + b_{i_1} V_{i_1}^s \quad (3.9)$$

$$a_{i_3} = a_{i_2} - b_{i_3} V_{i_2}^s \quad (3.10)$$

$$a_{e_2} = a_{e_1} + b_{e_1} V_{e_1}^s \quad (3.11)$$

$$a_{e_3} = a_{e_2} - b_{e_3} V_{e_2}^s. \quad (3.12)$$

As in the case of the basic one-segment model, the end-expiratory pressure is determined by numerically solving for P_{ex} the equation: $V_{e_3}(t_{\text{tot}}) = 0$.

The parameters, $V_{i_1}^s$ and $V_{i_2}^s$ for inspiration and $V_{e_1}^s$ and $V_{e_2}^s$ for expiration, are inputs for the model. The times, t_{i_1} , t_{i_2} , t_{e_1} , t_{e_2} , that appear in Eqs. (3.5)–(3.8) are determined by the equations, $V_{i_1}(t_{i_1}) = V_{i_1}^s$, $V_{i_2}(t_{i_2}) = V_{i_2}^s$, $V_{e_1}(t_{e_1}) = V_{e_1}^s$, and $V_{e_2}(t_{e_2}) = V_{e_2}^s$, respectively.

These equations can be solved analytically for the transition times:

$$t_{i_1} = - \frac{R_i}{(1 - b_{i_1}(P_{\text{set}} - P_{\text{ex}}))^2} \times \left[b_{i_1}(1 - b_{i_1}(P_{\text{set}} - P_{\text{ex}}))V_{i_1}^s + (a_{i_1} + b_{i_1}V_{\text{ex}})\log \Psi \right] \quad (3.13)$$

$$t_{i_2} = t_{i_1} - (a_{i_1} + b_{i_1}V_{\text{ex}} + b_{i_1}V_{i_1}^s)R_i \times \log \left(\frac{(a_{i_1} + b_{i_1}V_{\text{ex}} + b_{i_1}V_{i_1}^s)(P_{\text{set}} - P_{\text{ex}}) - V_{i_2}^s}{(a_{i_1} + b_{i_1}V_{\text{ex}} + b_{i_1}V_{i_1}^s)(P_{\text{set}} - P_{\text{ex}}) - V_{i_1}^s} \right) \quad (3.14)$$

where

$$\Psi = \frac{(a_{i_1} + b_{i_1}V_{\text{ex}} + b_{i_1}V_{i_1}^s)(P_{\text{set}} - P_{\text{ex}}) - V_{i_1}^s}{(a_{i_1} + b_{i_1}V_{\text{ex}})(P_{\text{set}} - P_{\text{ex}})}$$

and

$$t_{e_1} = - \frac{R_e}{(1 + b_{e_1}P_{\text{ex}})^2} \left[b_{e_1}(1 + b_{e_1}P_{\text{ex}}(V_{i_1}^s - V_T)) + (a_{e_1} + b_{e_1}V_{\text{ex}})\log \Phi \right] \quad (3.15)$$

$$t_{e_2} = t_{e_1} - R_e(a_{e_1} + b_{e_1}V_{\text{ex}} + b_{e_1}V_{e_1}^s) \times \log \left(\frac{V_{e_2}^s + a_{e_1} + b_{e_1}(V_{e_1}^s + V_{\text{ex}})}{V_{e_1}^s + a_{e_1} + b_{e_1}(V_{e_1}^s + V_{\text{ex}})} \right) \quad (3.16)$$

where

$$\Phi = \frac{a_{e_1} + b_{e_1}(V_{e_1}^s + V_{\text{ex}})P_{\text{ex}} + V_{e_1}^s}{a_{e_1} + b_{e_1}(V_T + V_{\text{ex}})P_{\text{ex}} + V_T}.$$

In Fig. 3, the three-segment, variable compliance model is used to calculate the lung volume over one cycle for parameter settings that are given in the caption of the figure. The $P_{\text{elastic}}-V$ curve for this simulation is shown in Fig. 4 and graphs of the compliance functions are shown in Fig. 5. The vertical lines in this figure indicate the

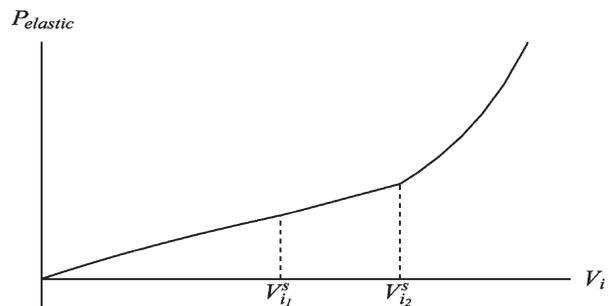


FIGURE 2 $P_{\text{elastic}}-V$ curve inspiration for the three-segment model.

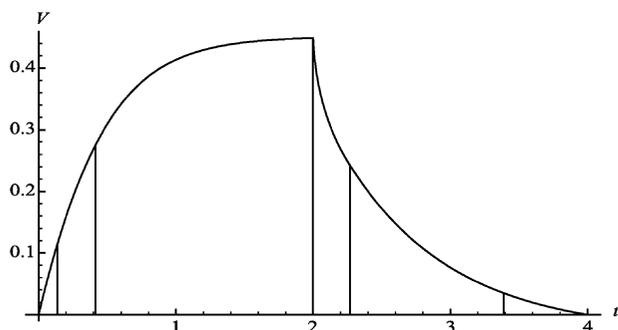


FIGURE 3 Lung volume curve over one breath for three-segment model $V_{i_1}^s = 0.32$ L, $V_{i_2}^s = 0.48$ L, $V_{e_1}^s = 0.44$ L, $V_{e_2}^s = 0.24$, $a_{i_1} = 0.016$ L/cm H₂O, $a_{i_2} = 0.026$ L/cm H₂O, $a_{i_3} = 0.0034$ L/cm H₂O, $b_{i_1} = 0.0321$ /cm H₂O, $b_{i_3} = -0.0161$ /cm H₂, $a_{e_1} = 0.113$ L/cm H₂O, $a_{e_2} = 0.039$ L/cm H₂O, $a_{e_3} = 0.019$ L/cm H₂O, $b_{e_1} = -0.1661$ /cm H₂, $b_{e_3} = 0.0821$ /cm H₂, $R_i = R_e = 20$ cm H₂O/L/s, $P_{\text{set}} = 25$ cm H₂O, $P_{\text{peep}} = 5$ cm H₂O, $t_i = 2$ s, and $t_{\text{tot}} = 4$ s. The vertical lines denote the times at which the form of the compliance function is changing.

times over the breathing cycle at which there is a change in the compliance function, i.e. t_{i_1} , t_{i_2} , t_i , $t_i + t_{e_1}$ and $t_i + t_{e_2}$. In Fig. 3, $P_{\text{ex}} = 5.7391$ cm H₂O, $V_{\text{ex}} = 0.205$ L, $t_{i_1} = 0.136$ s, $t_{i_2} = 0.413$ s, $t_i + t_{e_1} = 2.268$ s and $t_i + t_{e_2} = 3.390$ s. The model does exhibit hysteresis in the $P_{\text{elastic}}-V$ curve and for this example the compliance functions for inspiration and expiration are different. In Fig. 4, the arrows pointing upward are during inspiration and downward during expiration. The choices for parameters (V_{i_k} , V_{e_k} , a_{i_m} , b_{i_n} , a_{e_m} , b_{e_n}) for this simulation were taken to illustrate the generality of the model. Values for these parameters that come from human data will be used in the next section of the paper.

It is worthwhile to see the effect of the variable compliance on the lung volume. In Fig. 6, the lung volumes are graphed for the variable compliance model (solid curve) and the constant compliance model (dashed curve). For C in the constant compliance model, we have used the average compliance for the three-segment model during inspiration and expiration (C_{ave}). The average

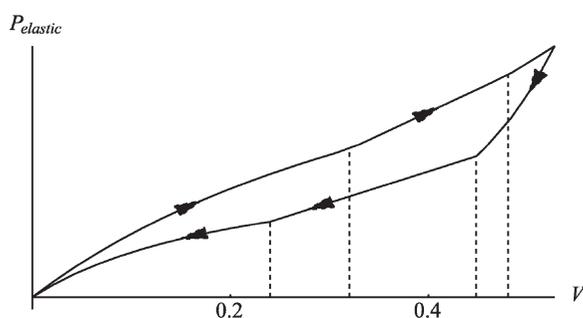


FIGURE 4 $P_{\text{elastic}}-V$ curve used in simulation for Fig. 3. The vertical dashed lines denote the volumes at which the form of the compliance function is changing form. The arrowheads indicate inspiration or expiration.

compliance was calculated using the formula:

$$C_{\text{ave}} = \left(\frac{D}{V_T}\right) \sum_{j=1}^3 \left(\int_{V_{i_{j-1}}+V_{\text{ex}}}^{V_{i_j}+V_{\text{ex}}} C_i(V) dV \right) + \left(\frac{1-D}{V_T}\right) \sum_{j=1}^3 \left(\int_{V_{e_{j-1}}+V_{\text{ex}}}^{V_{e_j}+V_{\text{ex}}} C_e(V) dV \right)$$

where $V_{i_0} = V_{e_3} = 0$ and $V_{i_3} = V_{e_0} = V_T$. We note the differences in the two models, in particular, the higher lung volume for the constant compliance model. However, this is not the general rule and by changing the compliance function parameters it is possible to have the tidal volume for the variable compliance model larger than the constant compliance model.

Important linkages exist between clinician set parameters: applied airway pressure (P_{set} and P_{peep}), frequency of breathing (f), inspiratory time fraction ($D = t_i/t_{\text{tot}}$) and clinically important outcomes: end-expiratory pressure (P_{ex}), tidal volume (V_T), mean alveolar pressure (P_m), and average lung volume (V_{ave}). The mean alveolar pressure is defined as the average elastic pressure over one breath plus the end-expiratory pressure P_{ex} . In particular, it is defined mathematically as

$$P_m = \left(\frac{D}{t_i}\right) \sum_{j=1}^3 \int_{t_{i_{j-1}}}^{t_{i_j}} \frac{V_{i_j}(t)}{C_{i_j}(V_{i_j}(t) + V_{\text{ex}})} dt + \left(\frac{1-D}{t_{\text{tot}} - t_i}\right) \sum_{j=1}^3 \int_{t_{e_{j-1}}}^{t_{e_j}} \frac{V_{e_j}(t)}{C_{e_j}(V_{e_j}(t) + V_{\text{ex}})} dt + P_{\text{ex}}$$

The intervals, $[t_{i_{j-1}}, t_{i_j}]$ and $[t_{e_{j-1}}, t_{e_j}]$, are the subintervals of $[0, t_i]$ and $[t_i, t_{\text{tot}}]$, respectively, for the different segments in the variable compliance model. The average lung volume is defined in an analogous way. The linkage between the key outcome variables and the frequency has been studied in the constant compliance case by Marini *et al.* (Marini *et al.*, 1989; Marini and Crooke, 1993). It was shown in these papers that in different types of lung diseases (e.g. obstructive and restrictive), the mathematical model gave robust predictions for the key outcome variables and theoretically provided the clinician with a means of choosing the input parameters of mechanical ventilation that optimize the desired results. In keeping with this spirit, we offer predictions of the three-segment model for the key outcome variables as functions of f , using clinically observable values for the applied pressures and inspiratory time fraction. In particular, we compare these with the predictions of the constant compliance model (using the average compliance of the three-segment model) and probe for meaningful differences. In the simulations for Fig. 7, the following values for the physiologic and ventilator parameters have been chosen: $R_i = R_e = 20$ cm H₂O/l/s, $P_{\text{set}} = 25$ cm H₂O, $P_{\text{peep}} = 5$ cm H₂O, and $D = 0.5$. The values of the parameters in the compliance functions are in Fig. 3.

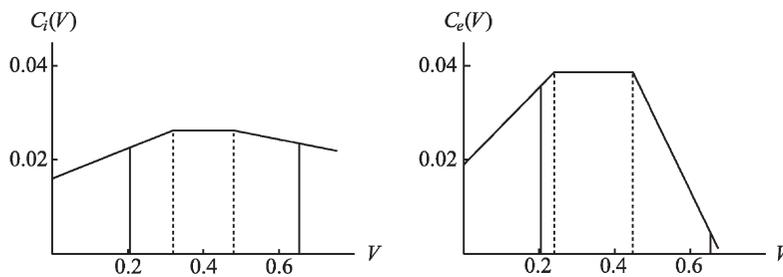


FIGURE 5 Compliance functions used in simulation for Fig. 3. The dashed lines are the volumes at which the compliance functions are changing form and the solid lines are V_{ex} and $V_T + V_{ex}$.

In these simulations, there is hysteresis in the $P_{elastic}-V$ curves. The compliances in the constant compliance model simulations are the average compliance of the three-segment models and range from $C_{ave} = 0.02671$ to $0.02841/\text{cm H}_2\text{O}$. For $f = 5-18$, all three segments of the inspiratory and expiratory compliance functions are traversed. For $f = 19-35$, three segments are used during inspiration and two segments during expiration. For $f = 36-40$, two segments of the inspiratory and expiratory compliance functions are traversed. In this last set of simulations, $V_{ex} > V_{i1}^s, V_{e2}^s$. We note some differences between the constant compliance and three-segment models for clinically relevant values of the physiologic and ventilator parameters. In particular, there are differences in the tidal volume and average volumes at the lower frequencies and the mean alveolar pressures at the high frequencies. The differences in the end-expiratory pressures are insignificant. The greatest percentage difference in tidal volumes was 16.5% at $f = 8$. The greatest difference in average volumes was 13.5% and 13.6% in mean alveolar pressures. A similar comparison can be done for the key outcome variables versus the inspiratory time fraction D .

RECRUITMENT AND THE THREE-SEGMENT MODEL

The value of any mathematical model for a physiologic process lies in its utility to predict the outcome of

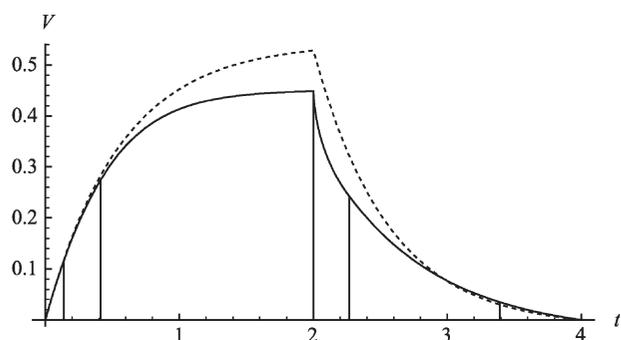


FIGURE 6 Constant compliance and three-segment models: The solid curve is the lung volume of the three-segment model in Fig. 3 and the dashed curve is the volume curve for the constant compliance model with $C = C_{ave} = 0.107$.

the process in a realistic setting. In this spirit we use the variable compliance model to predict key clinical outcomes (tidal volume, average volume, mean alveolar pressure) using ranges of the input variables (frequency, applied airway pressure, duty cycle) that are found in the ICU and patient parameters (compliance and resistance) that characteristic of healthy or sick individuals. Experimental studies indicate that mechanical ventilation may lead to up-regulation of inflammatory mediators and exacerbate pulmonary injury. Two important factors in ventilator-associated lung injury (VALI) are alveolar

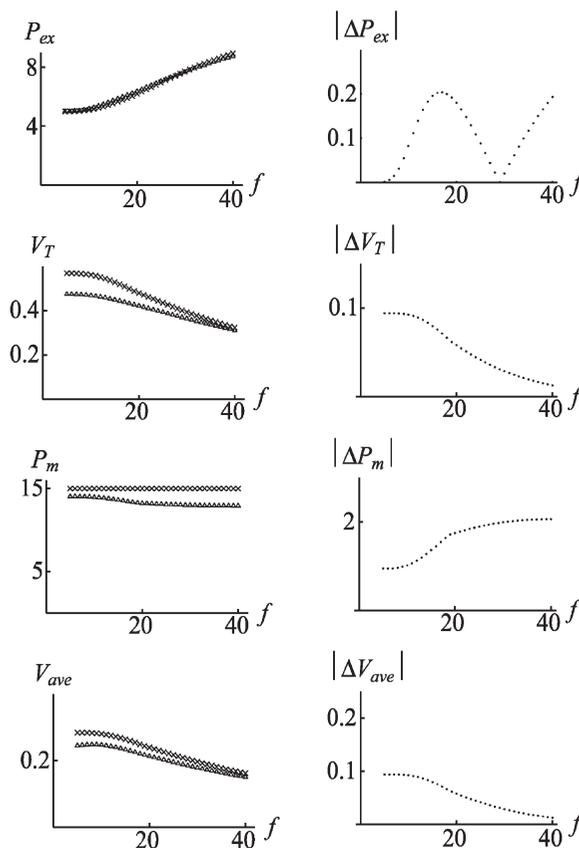


FIGURE 7 End-expiratory pressures, tidal volumes, mean alveolar pressures, and average volumes for constant and three-segment models as function of frequency (left panel) and their absolute differences (right panel). In the left panel graph, the triangles are quantities for the three-segment model and the crosses are for the constant compliance model.

overdistension due to high transpulmonary pressures and repeated alveolar collapse and reopening due to ventilation at low lung volumes (Mancini *et al.*, 2001). To keep alveolar extension within safe limits, it is suggested that tidal volumes be limited to 6–7 ml/kg, applied inspiratory pressures less than 35 cm H₂O, and applied PEEPs between 8–11 cm H₂O. A dynamic model that predicts volumes and pressure during ventilation may aid in the implementation of such lung protective strategies.

The elastic pressure–volume relationship of the respiratory system during inspiration or expiration can be modeled using the three-segment model described in the previous section. During inspiration, the lower inflection point ($V_{i_1}^s$) of the elastic pressure–volume curve can be used to establish a theoretical optimal value for PEEP in patients with acute lung injury (ALI) and/or acute respiratory distress syndrome (ARDS) (Maggiore *et al.*, 2001). It has been demonstrated (Amato *et al.*, 1998; Papadakos and Lachmann, 2002) that a substantial reduction of mortality in ARDS patients was achieved by using tidal volumes and applied PEEPs that result in inflation volumes that are between the two inflection points of the static elastic pressure–volume curve.

Svantesson *et al.* (1998) studied 15 healthy adults (9 females and 6 males) to determine the effect of recruitment maneuvers on their $P_{\text{elastic}}-V$ curves. The recruitment maneuver involved inflating the lungs to a pressure of 40 cm H₂O for a period of 15 s. They measured variables that can be used to calculate the parameters in the three-segment model (assuming no hysteresis in the $P_{\text{elastic}}-V$ curves) before and after the recruitment maneuver. Their data has been used to calculate $V_{i_1}^s$, $V_{i_2}^s$, a_{i_1} , b_{i_1} , a_{i_3} , and b_{i_3} for each patient. A summary of the calculations is presented in Tables I and II. We note that data from patient 9 is not listed because of missing data in the original work (Svantesson *et al.*, 1998). Although averages might be deemed of little value on a small data set, it is worth noting that the upper and lower inflection

points, on average, are lowered by the recruitment maneuvers on these healthy individuals.

Using the values of the parameters in Tables I and II, simulations were performed to compute lung volume profiles and key outcome variables, before and after recruitment, using pressure controlled ventilation. For these simulations, the following ventilation parameters were chosen: $P_{\text{set}} = 30$ cm H₂O, $P_{\text{peep}} = 5$ cm H₂O, $t_{\text{tot}} = 3$ s, $D = 0.5$, $R_i = 3$ cm H₂O/l/s, and $R_e = 5$ cm H₂O/l/s. Simulations for patient 1 are shown in Fig. 8. The values for the key outcome variables are: (before) $V_T = 1.730$, $V_{\text{ave}} = 0.953$, $V_{\text{ex}} = 0.313$, $P_{\text{ex}} = 5.292$, $P_m = 18.155$, and $C_{\text{ave}} = 0.072$; (after) $V_T = 1.508$, $V_{\text{ave}} = 0.877$, $V_{\text{ex}} = 0.494$, $P_{\text{ex}} = 5.644$, $P_m = 15.235$, and $C_{\text{ave}} = 0.088$. In this case, the tidal volume, average volume, and mean alveolar pressure decrease after recruitment. One should notice that the flat part of the compliance function has been extended considerably and the inflection points, $V_{i_1}^s$ and $V_{i_2}^s$, have been lowered.

In Fig. 9, the lung volumes and compliance functions for patient 2 are shown before and after the recruitment maneuver. The values for the key outcome variables are: (before) $V_T = 2.534$, $V_{\text{ave}} = 1.393$, $V_{\text{ex}} = 0.298$, $P_{\text{ex}} = 5.7085$, $P_m = 19.141$, and $C_{\text{ave}} = 0.095$; (after) $V_T = 1.925$, $V_{\text{ave}} = 1.095$, $V_{\text{ex}} = 0.556$, $P_{\text{ex}} = 5.900$, $P_m = 16.991$, and $C_{\text{ave}} = 0.093$. In this individual, we observe a similar change in the key outcome variables as was seen in patient 1. However, there is one important difference for patient 2 after the recruitment maneuver: the ventilation starts above the lower inflection point. Looking at the compliance functions (before and after), we see that the plateau region of the compliance function (the region that is often targeted by clinicians) is increased.

One might ask the question: What is the effect of the recruitment maneuvers on the parameters in the compliance functions for the 14 patients? One approach is to analyze changes in the parameters that make up the compliance functions for inspiration or expiration. On average, during inspiration, recruitment maneuvers

TABLE I Compliance function parameters for patients before recruitment maneuver

Patient	$V_{i_1}^s$	$V_{i_2}^s$	a_{i_1}	b_{i_1}	a_{i_3}	b_{i_3}
1	1.069	1.66	0.0521	0.0223	0.102	-0.0156
2	1.927	2.44	0.0405	0.0392	0.188	-0.0295
3	0.800	2.37	0.0364	0.0632	0.129	-0.0179
4	1.230	2.06	0.0504	0.0510	0.146	-0.0156
5	2.217	2.77	0.0685	0.0377	0.248	-0.0348
6	1.016	2.75	0.0353	0.0677	0.159	-0.0201
7	3.074	3.48	0.0500	0.0421	0.274	-0.0271
8	2.542	3.61	0.0624	0.0356	0.313	-0.0444
10	3.176	3.57	0.0513	0.0594	0.370	-0.0378
11	2.124	3.89	0.0457	0.0783	0.352	-0.0359
12	1.343	3.26	0.0419	0.0671	0.257	-0.0382
13	1.814	3.07	0.0518	0.0448	0.267	-0.0437
14	1.760	4.07	0.0604	0.0498	0.246	-0.0240
15	1.866	2.28	0.0272	0.0765	0.248	-0.0344
Average	1.854	2.949	0.0527	0.0492	0.228	-0.0286

Calculations based upon data taken from Svantesson *et al.* (1998).

TABLE II Compliance function parameters for patients after recruitment maneuver

Patient	$V_{i_1}^s$	$V_{i_2}^s$	a_{i_1}	b_{i_1}	a_{i_3}	b_{i_3}
1	0.575	1.38	0.0415	0.0930	0.169	-0.0536
2	0.421	1.97	0.0413	0.1300	0.157	-0.0308
3	0.990	1.53	0.0432	0.0573	0.160	-0.0394
4	1.308	1.93	0.0587	0.0545	0.172	-0.0220
5	0.801	2.22	0.0872	0.0784	0.218	-0.0305
6	1.167	1.68	0.0489	0.0627	0.155	-0.0195
7	1.148	3.03	0.0833	0.0903	0.361	-0.0574
8	1.984	2.16	0.0896	0.0345	0.253	-0.0440
10	1.805	2.79	0.1020	0.0504	0.320	-0.0453
11	2.531	2.54	0.1240	0.0339	0.283	-0.0289
12	1.392	2.00	0.0750	0.0618	0.252	-0.0453
13	0.661	1.79	0.0714	0.0871	0.233	-0.0581
14	1.513	2.88	0.0935	0.0419	0.309	-0.0526
15	0.514	1.19	0.0576	0.1190	0.148	-0.0248
Average	1.200	2.078	0.0750	0.0528	0.217	-0.0355

Calculations based upon data taken from Svantesson *et al.* (1998).

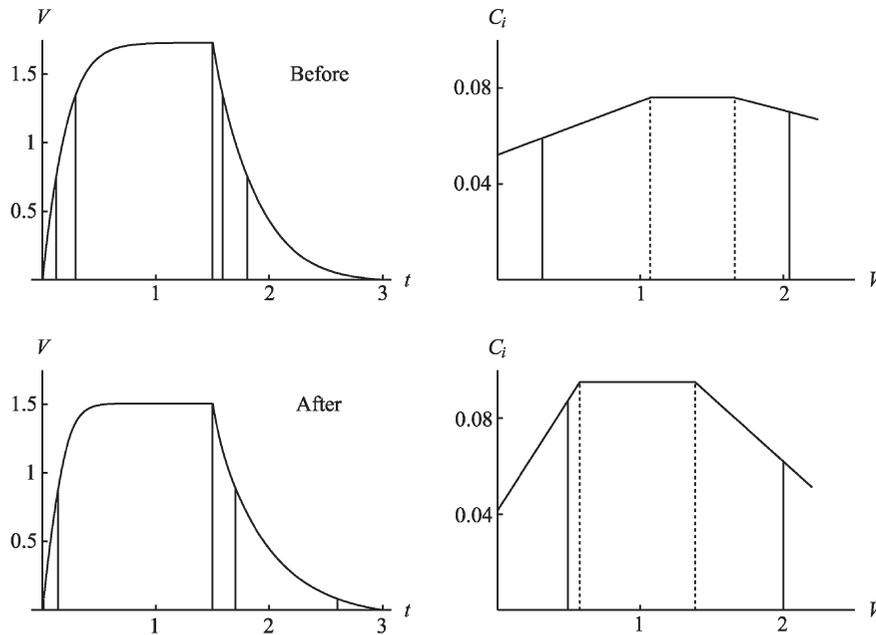


FIGURE 8 Volume and compliance functions before and after recruitment maneuver for patient 1. In the graphs of the compliance functions, the dashed lines are volumes $V_{i_1}^s$ and $V_{i_2}^s$ and the solid vertical lines are V_{ex} and $V_T + V_{ex}$.

decrease the lower inflection point volume, V_{i_2} , and increases the starting value of the compliance, a_{i_1} . The slopes of the initial segment, b_{i_1} increase and on average, the slopes of the third segment, b_{i_3} , become less negative. However, there is variation in the other parameters from patient to patient. This may be indicative of the variability that exists among individuals with and without lung disease. A second measure of change is the effect of the recruitment maneuvers on the key outcome variables: P_{ex} , V_T , P_m and V_{ave} . In Table III, the tidal volumes, end-expiratory pressures, mean alveolar pressures, and average lung volume are computed for the 14 patients. From this table, we see that the tidal volume, average

volumes, and mean alveolar pressures are lower by recruitment and there is little change in the end-expiratory pressure.

Variation in the applied PEEP for a fixed P_{set} has some effect on the key outcome variables, V_T , V_{ave} , P_{ex} , and P_m , before and after recruitment. In Table IV, the tidal volumes, end-expiratory pressures, mean alveolar pressures, and average lung volumes, before and after recruitment, are shown for different levels of applied PEEP and $P_{set} = 30$, using the compliance parameters for patient 1. For this particular situation, we see that tidal and average volumes decrease with increasing P_{peep} while end-expiratory pressure and mean alveolar pressure

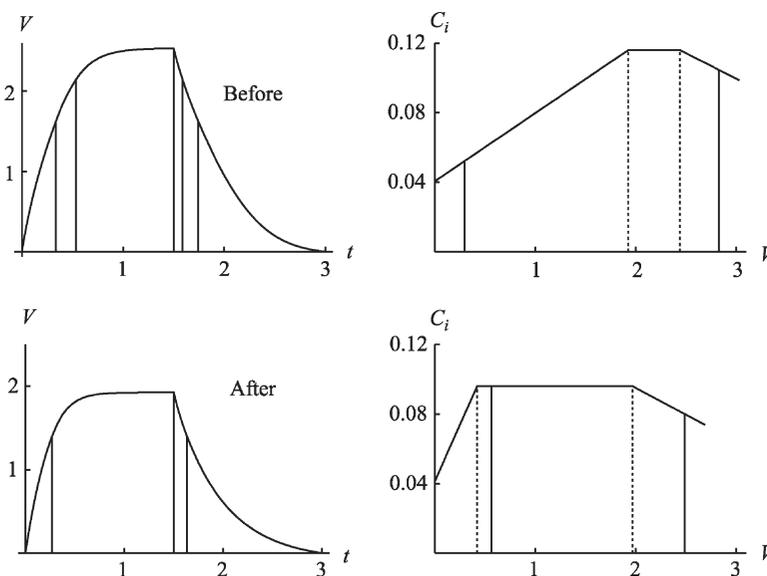


FIGURE 9 Volume and compliance functions before and after recruitment maneuver for patient 2.

TABLE III Tidal Volumes, end-expiratory pressures, mean alveolar pressures, and average volume for 14 patients before and after recruitment maneuver, using data from Svantesson *et al.* (1998)

Patient no	Before recruitment				After recruitment			
	V_T	P_{ex}	P_m	V_{ave}	V_T	P_{ex}	P_m	V_{ave}
1	1.730	5.292	18.155	0.953	1.508	5.644	15.235	0.877
2	2.534	5.708	19.141	1.393	1.925	5.900	16.991	1.095
3	2.104	5.552	18.873	1.148	1.817	5.622	17.333	1.047
4	2.400	6.285	18.800	1.346	2.438	6.775	18.278	1.386
5	2.832	7.364	18.662	1.603	2.462	7.374	16.775	1.415
6	2.456	6.009	19.264	1.344	2.328	6.455	18.410	1.321
7	3.490	7.953	20.501	1.874	2.629	8.290	15.465	1.541
8	3.187	7.518	19.684	1.735	2.438	7.275	16.919	1.422
10	3.591	10.231	19.886	1.986	2.734	8.472	16.206	1.584
11	3.281	9.781	17.637	1.838	3.055	9.079	17.723	1.723
12	2.853	7.152	19.165	1.577	2.308	7.321	16.680	1.352
13	2.820	6.808	19.009	1.570	1.844	6.397	14.673	1.090
14	3.153	7.936	20.067	1.707	2.589	7.726	16.547	1.504
15	2.948	7.418	19.432	1.681	1.944	6.224	16.676	1.113
Average	2.902	7.251	19.186	1.623	2.340	7.106	16.789	1.355

increase, both before and after recruitment. The percentage changes in the key outcome variable before and after recruitment are much smaller at the lower PEEPs. Another aspect of the change with PEEP before and after the recruitment maneuvers is which segments of the compliance function is the ventilation taking place. For the data in Table IV, all three segments of $C_i(V)$ are used for $P_{peep} = 0, 2, 4$, before and after recruitment. For $P_{peep} = 6, 8, 10, 12$, only the second and third segments are used for the after recruitment compliance function. For $P_{peep} = 15$, the second and third segments are used before and after recruitment. This would indicate that following recruitment, the lower inflection point would not be crossed for $P_{peep} \geq 6$ cm H₂O. In this individual after recruitment, ventilation could take place above the lower inflection point at lower PEEP levels and hence, lower mean alveolar pressures, with similar average volumes to those found before recruitment.

In simulations performed for the other patients, there is even more variability. For example, using the compliance data for patient 2, the same PEEP simulations were performed. It was found that for $P_{peep} \geq 4$ cm H₂O after recruitment, the lower inflection point is avoided. At $P_{peep} = 4$, the mean alveolar pressure was lower by 10.3% by the recruitment maneuver. The importance of

a mathematical model is evident in this type of theoretical approach. For the clinician it is a balancing act to choose values for PEEP that lead to sufficient oxygenation levels and non-collapsing alveoli without the imposing high internal pressures.

CLINICAL IMPLICATIONS

Recent experimental and clinical evidence indicates that high pressure mechanical ventilation—at volumes above the upper inflection point—can inflict lung damage. Pressure limiting ventilatory strategies have been shown to lower mortality in ARDS. Ventilation with a pattern in which the system repeatedly traverses the lower inflection point is also observed in experimental models of lung injury, although the current clinical evidence is somewhat less compelling. Accordingly, current ventilatory strategies endeavor to avoid overdistention, while avoiding repetitive cycles of recruitment–derecruitment. In this context, pressure targeted ventilation with high applied PEEP provides a valuable adjunct, for it absolutely restricts the maximal alveolar pressure. Although pressure control has the salutary effect of limiting

TABLE IV Tidal Volumes, total PEEPs, mean alveolar pressures, and average volumes for different levels of applied PEEP using the compliance functions parameters for patient 1 in Svantesson *et al.* (1998)

PEEP	Before recruitment				After recruitment			
	V_T	P_{ex}	P_m	V_{ave}	V_T	P_{ex}	P_m	V_{ave}
0.0	2.066	0.258	16.351	1.134	1.925	0.405	16.114	1.122
2.0	1.935	2.273	17.066	1.063	1.798	2.530	16.108	1.047
4.0	1.800	4.286	17.791	0.990	1.623	4.640	15.728	0.945
6.0	1.660	6.297	18.517	0.915	1.407	6.597	15.050	0.818
8.0	1.517	8.305	19.231	0.837	1.256	8.518	15.503	0.728
10.0	1.371	10.306	19.929	0.757	1.108	10.439	16.146	0.640
12.0	1.222	12.298	20.593	0.675	0.963	12.358	16.945	0.553
15.0	1.005	15.252	21.708	0.555	0.768	15.234	18.504	0.434

alveolar pressures, in choosing this mode of ventilation, the clinician sacrifices control over the level of ventilation i.e. the tidal volume or average lung volume.

Desired outcomes of mechanical ventilation are a minute ventilation ($\dot{V}_E = f V_T$), adequate to protect the systemic pH (via removal of CO_2), and a mean alveolar pressure which is sufficient to maintain lung volume and support adequate oxygenation. Predictions of the three-segment model differ from those of the constant compliance model in a number of clinically relevant respects.

In the constant compliance model, tidal volume diminishes with increasing respiratory frequency; the decline arises from the effects of shortened inspiratory time (less opportunity for alveolar filling) as well as increasing total PEEP (decreased gradient of driving pressure). The three-segment model predicts a smaller dependence of tidal volume on ventilatory frequency. This is potentially important in the clinical setting, as it suggests that increasing respiratory frequency in this pressure-limited mode of ventilation may preserve tidal volume and increase minute ventilation more than expected from the constant compliance case. As the maximum acceptable driving pressure may be limited by the relatively small difference between a high applied PEEP (used to avoid derecruitment) and a lower P_{set} (to avoid overdistension), increased respiratory frequency may be the only mechanism for elevating minute ventilation.

Similarly, in a constant compliance system with airflow obstruction, there is a strong dependence of tidal volume on inspiratory time fraction D , with a clear optimum (Marini and Crooke, 1993). Elevating the inspiratory time fraction above the optimal value leads to a rapid decline in V_T . The dependence of tidal volume on the duty cycle in the three segment model is somewhat less marked, indicating that reasonable increases in duty cycle to increase mean alveolar pressure (vide infra) may not overtly compromise minute ventilation.

Our model does not attempt to address the micro-structural basis for observed nonlinearity of the $P_{\text{elastic}} - V_{\text{curve}}$. Rather, it addresses the effects of a nonlinear macroscopic pressure-volume curve behavior on common clinical outcomes: tidal volume, end-expiratory pressure, mean alveolar pressure, and average lung volume. In this regard, it predicts important consequences arising from the presence of nonlinearity. Although the regional distribution of pressure and tidal volume are also of crucial importance, our data indicate that the presence of upper and lower inflection points alone will significantly affect the macroscopic outcomes most commonly tracked in the clinical setting. The qualitative behaviors are those of importance in this setting, as they suggest the overall responses to common clinical manipulations of ventilator settings. Better knowledge of these effects may be useful in optimizing ventilatory strategies in the clinical setting.

CONCLUSION

In this paper, a mathematical model for pressure controlled ventilation with three-segment compliance function has been presented and used to study the effects of clinician-set inputs on the key ventilatory outcome variables. The model can be used to predict the effects on the outcome variables using recruitment maneuvers.

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